BUSINESS AND DEFAULT CYCLES FOR CREDIT RISK

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SUMMARY

Various economic theories are available to explain the existence of credit and default cycles. There remains empirical ambiguity, however, as to whether these cycles coincide. Recent papers suggest by their empirical research set-up that they do, or at least that defaults and credit spreads tend to co-move with macroeconomic variables. If true, this is important for credit risk management as well as for regulation and systemic risk management. In this paper, we use 1933–1997 US data on real GDP, credit spreads and business failure rates to shed new light on the empirical evidence. We use a multivariate unobserved components framework to disentangle credit and business cycles. We distinguish two types of cycles in the data, corresponding to periods of around 6 and 11–16 years, respectively. Cyclical co-movements between GDP and business failures mainly arise at the longer frequency. At the higher frequency of 6 years, co-cyclicality is less clear-cut. We also show that spreads reveal a positive and negative co-cyclicality with failure rates and GDP, respectively. This pattern disappears, however, if we concentrate on the post World War II period. We comment on the implications of our findings for credit risk management. Copyright © 2005 John Wiley & Sons, Ltd.

1. INTRODUCTION

Credit risk research has gained considerable momentum over the last decade, see for example Caouette *et al.* (1998) and Allen and Saunders (2003) for an overview.[1] Spurred by regulatory developments, different classes of models have been put forward to measure, manage and price credit risk. In this paper we study the dynamic behaviour of two important determinants of credit risk, namely the default rate and the credit spread, in their relation to business cycle developments. We use a multivariate unobserved components approach to disentangle long-term patterns from shorter-term cyclical patterns. We are particularly interested in testing whether cycles in credit risk factors coincide with business cycles. To answer this question, our model explicitly allows for different cyclical movements in credit risk factors and economic activity, as measured by real GDP.

Early credit risk models focus on the prediction of the likelihood to default (credit scoring) using, e.g., Altman's Z-score, logit and probit models, and neural networks, see Altman (1983) and Caouette *et al.* (1998). These models usually emphasize the cross-sectional rather than the time-series dimension of the sample to distinguish 'good' from 'bad' companies. The time-series or dynamic behaviour of credit risk, however, has become increasingly important over the last few years among academics, practitioners and regulators. At least two reasons for this appear important.

First, the market for credit risk has become much more liquid, see for example Patel (2003). Asset backed securities like collateralized bond and loan obligations (CBOs and CLOs), as well as credit derivatives, allow financial institutions to mitigate their credit risk exposure without breaking up client relationships. A second reason for the attention paid to credit risk dynamics lies in the adoption of a portfolio perspective to credit risk, see Gupton *et al.* (1997), Credit Suisse (1997) and Wilson (1997a,b). Making the standard distinction between idiosyncratic and systematic risk, it is the systematic risk that is most important at a portfolio level, see for example Jarrow *et al.* (2003), Frey and McNeil (2001), Lucas *et al.* (2001) and Giesecke and Weber (2003). Systematic credit risk factors are usually thought to correlate with macroeconomic conditions. If, therefore, a link can be established between the macroeconomic environment and systematic credit risk factors, knowledge on the state and direction of macrovariables may help in assessing portfolio credit risk over time.

Given the importance of dynamic credit risk modelling and the controversy over the exact relation of credit risk drivers with the state of the business cycle as mentioned above, we set out in this paper to build a multivariate time-series model for business failure rates, credit spreads and real GDP growth. Empirical models that link default rates to macrovariables can be found in Wilson (1997a,b), Nickell *et al.* (2000), Bangia *et al.* (2002), Kavvathas (2001) and Pesaran *et al.* (2003). The general conclusion of these models is that default probabilities tend to be higher in recession states, see also Allen and Saunders (2003). Empirical evidence linking credit spreads to the business cycle can be found in, for example, Fama and French (1989), Chen (1991) and Stock and Watson (1989). There, the general conclusion is that risk premia on bonds contain a countercyclical component and that credit spreads are good predictors for future business cycle conditions.

Our paper contains the following contributions. First, we build a trivariate model including both default rates and spreads in their relation to economic growth. In this way, we can investigate the claimed lead relationship of credit spreads over growth, the (in)congruence between credit and business cycles, and the dynamics of default rates in one unified framework. Our second contribution lies in the fact that we use an unobserved components model, see Harvey (1989) and Durbin and Koopman (2001). In this way, we are able to disentangle long-term (co)-movements from short-term cyclical movements in a clear and interpretable way. By focusing on the time-series dimension of our series, we also complement the existing literature by considering a long time span of data: 1933–1997. By contrast, papers like Nickell *et al.* (2000) and Bangia *et al.* (2002) focus much more on the cross-sectional dimension to estimate their models, typically using time series of 20 to 25 years for a large number of companies. Our longer time span allows for repeated observations on business cycles and therefore helps to test for the presence and co-variation of cyclical patterns in credit risk factors.

Our empirical findings reveal a rich and diverse view on the dynamic relations between the three series considered. After filtering out the long-term trends from the data, we find two types of cycles for the 1933–1997 period. The first type of cycle has a frequency of around 6 years. There is clear (positive) co-cyclicality between spreads and business failures and (negative) between spreads and GDP. The relation between GDP and business failures is insignificant at this frequency. The second type of cycle has a longer period of around 11 years. For this frequency, there is a clear positive relation between spreads and failures, and a negative relation between GDP on the one hand and spreads and failures on the other hand. Contemporaneous correlations between the innovations for each of the components in our model show the same intuitive pattern.

We check the robustness of our results in three ways. First, we lag GDP and credit spreads, as one may argue that business failures only react with a lag to these variables. The effects remain robust, with the exception that co-cyclicality between GDP and business failures at the 6-year frequency becomes counter-intuitively positive. We also test the robustness of our findings by concentrating on the post World War II period. Interestingly, for this shorter period, co-cyclicality only appears statistically significant between GDP and business failures. The longer cycle now has a period of around 16 years. Again, the co-cyclicality appears economically more important at this lower frequency than at the higher frequency of 6 years. Third, we use quarterly data over the post-war period and corroborate the results for the annual data.

Our results support the findings in, for example, Nickell *et al*. (2000) and Bangia *et al*. (2002). At the same time, however, the double cyclicality found in our analysis for both the long and short data sample indicates that the relation between defaults and GDP may be more complicated than assumed in earlier papers on credit risk. It is also interesting to see that credit spreads appear to contain little predictive information with respect to business failures in the post World War II sample. This appears especially puzzling given the usual timeliness of financial markets' information.

The paper is set up as follows. In Section 2, we discuss the data and our modelling approach. The empirical results are contained in Section 3. Section 4 concludes.

2. DATA AND MODELLING APPROACH

We use three data series in our analysis: real GDP, credit spreads and business failure rates. The first series, real GDP, is taken from the database of the Federal Reserve Bank of St. Louis (FRED). The series contains GDP in chained 1996 dollars. From the same site, we also obtain Moody's yields on Baa corporate bonds and the yield on government bonds with a maturity exceeding 10 years. These are used to construct annual credit spreads, defined as the difference between the two yields. Our third series is from Dun and Bradstreet (1998) and contains US business failure rates per 10,000 companies over the period 1927–1997. After 1997, the series was discontinued. Following the description of Dun and Bradstreet (1998), the numbers indicate businesses that ceased operation after assignment or bankruptcy; ceased operation with losses to creditors after such actions as foreclosure or attachment; voluntarily withdrew leaving unpaid debts; were involved in court actions such as receivership, reorganization or arrangement; or voluntarily compromised with creditors. As such, the business failure rate may be an underestimate of the default rate, because defaulting investment projects within a business may be compensated by well-performing projects within that same business, see also Kwark (2002). In this paper, however, we are not involved so much with the level of the default rate, as with its dynamic behaviour over time and its co-variation with other variables included in the model. Given the difficulty of obtaining reliable default rate statistics from competing sources, we take the business failure rate as a proxy for describing default rate dynamics.[2] Combining all three series, our sample runs

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[2] One additional potential complication is the change in data collection by Dun and Bradstreet after 1984. This increased both the number of businesses and business failures. The failure rate, however, appears relatively unaffected. We tested for possible effects by including a dummy variable for a level break in defaults from 1984 onwards. This variable turned out to be insignificant.
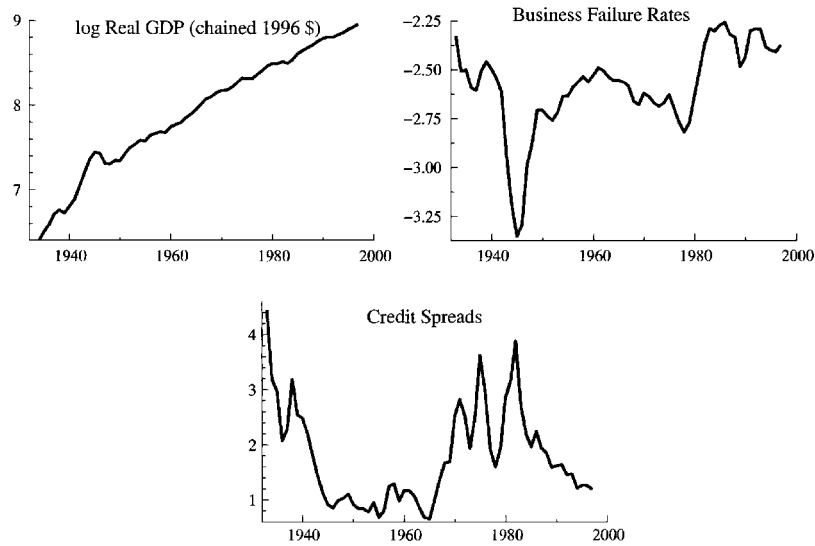
Figure 1. Logarithm of real GDP, Dun and Bradstreet business failure rates and credit spreads (Moody's Baa minus long-term government bonds)

from 1933 up to 1997. The data is presented in Figure 1 for the two sample periods used in this paper.

To describe the dynamic behaviour of the three series as well as their interdependencies, we introduce an unobserved components model, see Harvey (1989) and Durbin and Koopman (2001). Our basic specification is

$$y_t = \mu_t + A\gamma_t + B\psi_t + e_t, \qquad e_t \overset{\text{i.i.d.}}{\sim} \text{N}(0, \Sigma_e), \quad t = 1, \ldots, n \qquad (1)$$

where y_t represents the time-series observation vector as given by

$$y_t = \begin{bmatrix} y_t^R \\ y_t^S \\ y_t^D \end{bmatrix} = \begin{bmatrix} \text{real GDP (GDP)} \\ \text{business failures (DEFLT)} \\ \text{credit spreads (SPRD)} \end{bmatrix}, \quad t = 1, \ldots, n \qquad (2)$$

with $t = 1$ for 1933 and $t = n = 65$ for 1997. The trend component is represented by the vector μ_t and the cycle components by the vectors γ_t (short cycle) and ψ_t (long cycle). The irregular component e_t in (1) is included to allow for measurement noise in the observations.

The trend component μ_t is specified as

$$\mu_t = \mu_{t-1} + \beta_t$$
$$\beta_t = \beta_{t-1} + \eta_t \qquad (3)$$

where η_t is a zero mean normal innovation with variance matrix Σ_η. The η_t's are serially independent and, moreover, independent of the other innovations in the model. The role of μ_t is to filter out the low-frequency or long-term dynamics from the data. Alternatively, we could use the Hodrick–Prescott (HP) filter for this, which is a restricted version of (3). As shown by

Harvey and Jaeger (1993), our current procedure is more flexible. This may be important in our current context, where we have multiple time series. The HP filter is optimized to filter out the low-frequency patterns from GDP-type data. It is not clear *a priori*, however, that this filter is also optimal for non-GDP data like defaults and credit spreads. Therefore, we prefer the inclusion of μ_t over pre-filtering the data using the HP filter.

We can now interpret $y_t - \mu_t$ as the cyclical components in our data. After some preliminary experimentation, a model with two cyclical components appeared empirically the most promising. The cycles correspond to short business cycle type frequencies of around 6 years, and a somewhat longer frequency between 11 and 16 years, respectively. We label the cycles γ_t and ψ_t, respectively. We normalize γ_t to be the cycle with the shorter period. Note that both γ_t and ψ_t are trivariate. In this way we can test whether the cycle in real GDP is the same as that in credit spreads or business failures. This is done by an inspection of the 'cycle loading' matrices A and B. Various specifications for the stationary cycle components can be considered. For example, the cycles can be modelled as an autoregressive process of order 2, in short AR(2), with the polynomial autoregressive coefficients selected in the complex range. To enforce this restriction we can represent the model as a trigonometric process, that is

$$
\begin{pmatrix} \psi_t \\ \psi_t^* \end{pmatrix} = \phi_\psi \left(\begin{bmatrix} \cos \lambda_\psi & \sin \lambda_\psi \\ -\sin \lambda_\psi & \cos \lambda_\psi \end{bmatrix} \otimes I_3 \right) \begin{pmatrix} \psi_{t-1} \\ \psi_{t-1}^* \end{pmatrix} + \begin{pmatrix} \omega_t \\ \omega_t^* \end{pmatrix} \tag{4}
$$

$$
\begin{pmatrix} \omega_t \\ \omega_t^* \end{pmatrix} \overset{\text{i.i.d.}}{\sim} \quad N(0, I_2 \otimes D_\omega)
$$

with frequency λ_ψ and persistence parameter $|\phi_\psi| < 1$. The disturbances ω_t and ω_t^* are serially and mutually uncorrelated and normally distributed, where D_ω is a diagonal 3×3 matrix. A similar specification holds for the short cycle component γ_t. This stochastic cycle specification generates three stationary cyclical processes with a common period of $p = 2\pi/\lambda_\psi$. The factor loading matrices A and B scale the cycles γ_t and ψ_t for each of the individual series. For the identification of D_ω, B is restricted to a lower triangular matrix with unity as diagonal elements. A similar restriction applies to A.

It is well known that lead and lag relationships between macroeconomic time series may exist. To allow for this, we perform several robustness checks of our benchmark results later on in terms of lagging some of the variables in the analysis.

The multivariate unobserved components model (1)–(4) can be put into the state space form

$$
\alpha_t = T\alpha_{t-1} + \nu_t
$$
$$
y_t = Z\alpha_t + \varepsilon_t \tag{5}
$$

where the state vector contains the mean parameters including the unobservables, that is $\alpha_t = (\mu_t, \gamma_t', \gamma_t^{*'}, \psi_t', \psi_t^{*'})'$. The system matrices Z and T are constructed according to the specifications implied by the model. The state disturbance vector ν_t contains the disturbances, e.g., e_t, ω_t, etc. The unknown coefficients of the model can be estimated by numerically maximizing the log-likelihood function of the model for a given set of observations $y_1, \ldots, y_n$. The log-likelihood function can be computed via the Kalman filter; see, for example, Durbin and Koopman (2001) for details of the Kalman filter and associated methods and techniques. Once the parameters are estimated, the unobserved components γ_t and ψ_t can be extracted from the observations using the Kalman filter and the associated smoother. These estimates, together with confidence intervals, can be presented

graphically. Diagnostic statistics and graphs can be obtained as by-products of the Kalman filter and can be used to test the underlying assumptions of the model such as normality and independence of the disturbances. Finally, standard goodness-of-fit statistics can be computed for each equation of the multivariate model. We estimate our model using the software package STAMP, see Koopman *et al.* (2000).

3. EMPIRICAL RESULTS

In an attempt to provide clear evidence on the existence and commonality of credit cycles and business cycles in our data, we consider the decomposition model explained in the previous section. Our benchmark results are presented in the first three columns of Table I.

The diagnostics of the model appear adequate given the limited number of observations. The data show clear evidence of a cyclical pattern. We start our discussion with the short business cycles γ_t. Note that γ_t is trivariate, such that there are three cycles. These cycles have a period of 6.3 years and are all significant as can be seen from the elements of D_γ. The cycles are persistent with a damping factor ϕ_γ of 0.917. Given the period length, it is tempting to label this cycle the typical business cycle. To determine whether there is any co-cyclicality, we look at the load matrix A. There is no evidence of a common short cycle between real GDP and defaults. By contrast, real GDP and credit spreads have a common cycle given the significant loading of -14.5 on the GDP cycle in the credit spread equation. The loading has the intuitive negative sign: if economic activity declines, credit risks and thus credit spreads increase. Credit spreads also share some of the cyclicality in defaults given the significant loading of 6.12 on the default cycle. Again, this loading has the intuitive sign: default activity and credit spreads appear to be positively correlated.

The second set of cycles, ψ_t, has a period of 11.6 years and is also highly persistent with a damping factor of 0.924. Again, all three cycles are statistically significant given the elements of D_ψ. By comparing D_ψ and D_γ we see that ψ_t is economically more important than γ_t for GDP and defaults. For credit spreads, by contrast, both cycles are about equally important. This is also clearly seen in Figure 2, which plots the data and smoothed components for the different series. The load matrix B of ψ_t shows significant co-cyclicality between all series at this longer frequency. The signs are intuitively plausible: positive between defaults and spreads, and negative between GDP and spreads and defaults. The covariance matrices Σ_η and Σ_e (not completely shown in the table) also have the same intuitive signs. Interestingly, though, Σ_e has rank one, such that effectively there is only one irregular component affecting all three series simultaneously. Given the magnitude of the diagonal of Σ_e, it appears that this is the irregular component for the credit spread. The other two variances are negligible compared to the variances of the cyclical components. The matrix for the slope coefficient is full rank, but also shows a large correlation of -0.94 between the GDP and default equation. Therefore, the long-term trend between these two series also appears to be correlated. By contrast, the slope innovation's correlation between GDP and spreads is only -0.41.

The main conclusion following from the discussion of our benchmark results is that there appears co-cyclicality between defaults, credit spreads and GDP. The co-cyclicality is strongest at frequencies of around 12 years rather than at 'typical' business cycle frequencies of 6 years. To test the robustness of these findings, we perform three additional analyses. First, one may argue that default activity only reacts with a lag to economic indicators such as GDP (growth) and credit

Table I. Parameter estimates

The table contains parameter estimates for the model

$$y_t = \mu_t + A\gamma_t + B\psi_t + e_t, \quad e_t \overset{i.i.d.}{\sim} N(0, \Sigma_e)$$

$$\Delta\mu_{t+1} = \beta_t = \beta_{t-1} + \eta_t, \quad \eta_t \overset{i.i.d.}{\sim} N(0, \Sigma_\eta)$$

$$\begin{pmatrix} \gamma_t \\ \gamma_t^* \end{pmatrix} = \phi_\gamma \begin{pmatrix} \cos(\lambda_\gamma)I & \sin(\lambda_\gamma)I \\ -\sin(\lambda_\gamma)I & \cos(\lambda_\gamma)I \end{pmatrix} \begin{pmatrix} \gamma_{t-1} \\ \gamma_{t-1}^* \end{pmatrix} + \begin{pmatrix} \kappa_t \\ \kappa_t^* \end{pmatrix}, \quad (\kappa_t, \kappa_t^*)' \overset{i.i.d.}{\sim} N(0, I_2 \otimes D_\gamma)$$

$$\begin{pmatrix} \psi_t \\ \psi_t^* \end{pmatrix} = \phi_\psi \begin{pmatrix} \cos(\lambda_\psi)I & \sin(\lambda_\psi)I \\ -\sin(\lambda_\psi)I & \cos(\lambda_\psi)I \end{pmatrix} \begin{pmatrix} \psi_{t-1} \\ \psi_{t-1}^* \end{pmatrix} + \begin{pmatrix} \omega_t \\ \omega_t^* \end{pmatrix}, \quad (\omega_t, \omega_t^*)' \overset{i.i.d.}{\sim} N(0, I_2 \otimes D_\psi)$$

with y_t containing real GDP (GDP), Dun and Bradstreet (1998) business failures (DEFLT) and credit spreads (SPRD), respectively. The failure rates are transformed using a probit transformation. The $Q(k)$ statistics have a χ^2 distribution with k degrees of freedom, while the normality test has a $\chi^2(2)$ distribution. Parameter significance is denoted by [a](20%), [b](10%) or [c](5%). Panels labelled lagged are performed on lagged real GDP, business failures, and lagged credit spreads.

	No lags, 1933–1997			Lags, 1933–1997			No lags, 1948–1997			Lags, 1948–1997		
period $(2\pi/\lambda_\gamma)$	6.324[c]			5.630[c]			6.096[c]			5.567[c]		
ϕ_γ	0.917[c]			0.887[c]			0.833[c]			0.870[c]		
variance D_γ	0.0072[b]	0.0117[c]	0.0598[c]	0.0104[c]	0.0104[c]	0.0005[a]	0.0071[c]	0.0123[c]	0.0011	0.0052[c]	0.0115[c]	0.0008[a]
load matrix A	γ_{gdp}	γ_{def}	γ_{spr}	γ_{gdp}	γ_{def}	γ_{spr}	γ_{gdp}	γ_{def}	γ_{spr}	γ_{gdp}	γ_{def}	γ_{spr}
GDP	1	0	0	1	0	0	1	0	0	1	0	0
DEFLT	−0.148	1	0	0.290[b]	1	0	−1.830[c]	1	0	−0.101	1	0
SPRD	−14.5[c]	6.12[c]	1	−27.4[c]	4.20[c]	1	−0.215	−0.013	1	−0.245	−0.005	1
period $(2\pi/\lambda_\psi)$	11.58[c]			10.40[c]			16.36[c]			15.46[c]		
ϕ_ψ	0.924[c]			0.917[c]			0.974[c]			0.931[c]		
variance D_ψ	0.0198[b]	0.0395[c]	0.0610[c]	0.0178[c]	0.0179[c]	0.0	0.0083[b]	0.0140[c]	0.0	0.0088[b]	0.0242[c]	0.0
load matrix B	ψ_{gdp}	ψ_{def}	ψ_{spr}	ψ_{gdp}	ψ_{def}	ψ_{spr}	ψ_{gdp}	ψ_{def}	ψ_{spr}	ψ_{gdp}	ψ_{def}	ψ_{spr}
GDP	1	0	0	1	0	0	1	0	0	1	0	0
DEFLT	−1.16[c]	1	0	−1.77[c]	1	0	−3.298[c]	1	0	−2.235[c]	1	0
SPRD	−1.16[c]	1.88[c]	1	−1.21[c]	6.84[c]	1	−0.110	0.0248	1	−0.0986	0.0340	1
diagonal Σ_e	0.00007	0.00002	0.0277	0.00012	0.00026	0.0222	0.0	0.00014	0.0	0.00013	0.00012	0.000001
diagonal Σ_η	0.00006	0.00037	0.0028	0.00007	0.00066	0.0025	0.000001	0.00001	0.0	0.000002	0.00007	0.0
R_d^2	0.36	0.36	0.17	0.41	0.35	0.25	0.26	0.33	0.26	0.24	0.33	0.30
normality	9.68	8.33	4.61	12.5	9.16	2.27	2.03	2.04	6.40	3.53	0.15	8.40
First-order autocorrelation	0.12	−0.01	0.07	0.16	0.09	0.07	0.12	0.20	−0.01	0.13	−0.10	−0.02
Q(13)	20.6	8.91	5.30	22.5	7.93	5.26	7.20	14.7	9.49	7.25	8.29	8.37
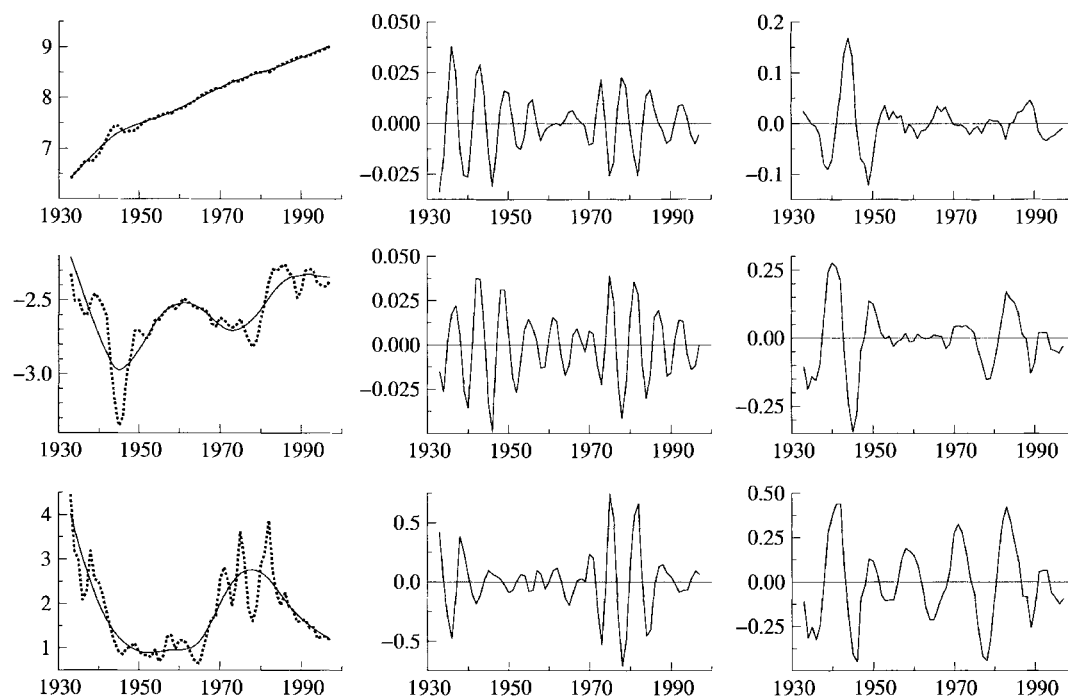
Note: This figure presents the fit (smoothed estimates) of the model estimated in Table I for the sample 1933–1997, variables not lagged. The top row of graphs indicates the real GDP (top-left) indicated by the dotted line, and the trend component (solid line, μ_t). The graphs for business failure rates and credit spreads are the middle and bottom graphs, respectively. The middle column of graphs contains the shorter cyclical component (γ_t) of the three series considered. The last column of graphs contains the longer cyclical component (ψ_t) of the three series considered.

Figure 2. Time series with trend (μ_t), 'business' cycle (γ_t) and longer cycle (ψ_t) components in real GDP, business failure rates and the credit spread

spreads. To test this, we estimate the same model, but with real GDP and spreads lagged 1 year. The results are in the second set of three columns in Table I.

The diagnostics of this model are similar to those for our benchmark model. Also, the results appear to carry over. There are three main differences. First, both the 5.6 and 10.4 cycles have reduced rank as one of the elements of D_γ and D_ψ is estimated to be (almost) zero. Moreover, the magnitude of the elements in D_γ and D_ψ is generally lower in the model with lagged variables than in the model without lags. The cyclical part of the model, therefore, explains less of the dynamics. This is supported by the fact that the variances of the irregular component (see the diagonal of Σ_e) have increased. Finally, the loading on the short GDP cycle in the default equation has turned from negative and insignificant into positive and significant. This finding is counter-intuitive. We come back to it when discussing the results of the quarterly data.

As another important robustness test, we re-estimate the model using only data from the post World War II period 1948–1997. The data and trends are presented in the left-hand column of graphs in Figure 3. By dropping the first 15 years of the sample, the shape of the time series for defaults and credit spreads becomes substantially different. The estimation results are in the third set of columns in Table I. With respect to the benchmark model, there are three main differences.
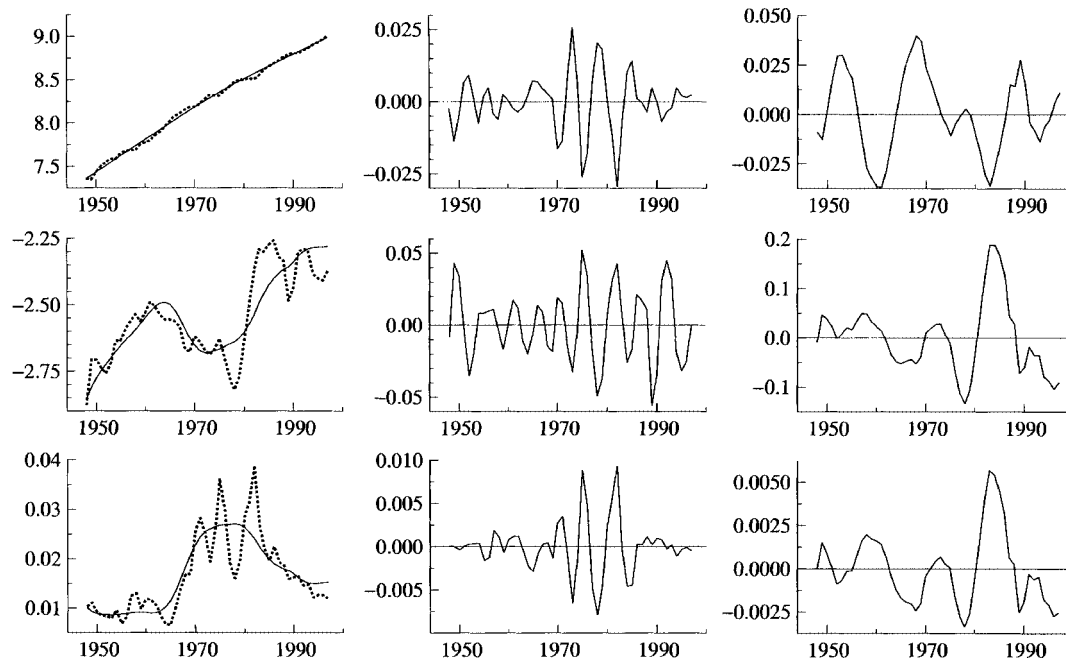
Note: This figure presents the fit (smoothed estimates) of the model estimated in Table I for the sample 1948–1997, variables not lagged. The top row of graphs indicates the real GDP (top-left) indicated by the dotted line, and the trend component (solid line, μ_t). The graphs for business failure rates and credit spreads are the middle and bottom graphs, respectively. The middle column of graphs contains the shorter cyclical component (γ_t) of the three series considered. The last column of graphs contains the longer cyclical component (ψ_t) of the three series considered.

Figure 3. Time series with trend (μ_t), 'business' cycle (γ_t) and longer cycle (ψ_t) components in real GDP, business failure rates and the credit spread

First, the period of the longer cycle has increased from 12 to 16 years. The cycle (ψ_t) has also become slightly more persistent given its decay factor ϕ_ψ of 0.97. Second, as was the case with lagged variables for the 1933–1997 sample, the long cycle has reduced rank. To some extent, this also holds for the short cycle. With respect to the co-cyclicality issue, there is a strong and negative correlation between the GDP and the default cycle. The cyclicality between credit spreads and GDP and defaults, however, has become statistically insignificant. This constitutes an important difference with our previous analysis. This finding is in line with Collin-Dufresne *et al.* (2001), who find that changes in credit spreads are not well explained by systematic factors such as business climate and term structure variables. The results are similar if we lag GDP and spreads by 1 year for the short sample as well, see the last three columns of Table I. In that case, only the correlation between the short GDP and default cycles decreases in magnitude and has a much higher *p*-value.

So far two main results emerge. First, co-cyclicality appears economically more important and empirically more robust between real GDP and defaults at frequencies that are lower than typical business cycle frequencies of 6 years. At 5- to 6-year frequencies, negative co-cyclicality between GDP and defaults is only found if the two variables enter the model contemporaneously. Second, co-cyclicality between credit spreads and the other variables in the model does not appear to be a

robust phenomenon. In particular, for post-war data, cycle loadings for the GDP and default cycles in the credit spread equation are not significant. They do have the correct signs, however, except for the link between the short (6-year) credit spreads and default cycle, which is nearly zero.

To conclude the analysis, we investigate the shift in the correlation between the short cyclical component in GDP and defaults if we lag GDP and credit spreads in the model. To do this, we use quarterly data for 1948–1997. The data are obtained from the same sources as the original annual data. The only problem is caused by the default series, for which we only have annual data. As a rough approximation, we spread the default frequency in each year evenly over the four quarters. Using the quarterly data, we estimated the model without lags. Next, we lag GDP one up to three quarters, and re-estimate the model. The results are given in Table II.[3]

Obviously, given the different type of data the estimation results differ somewhat from those in Table I. The broad picture, however, in terms of signs of cycle loadings, lengths of cycles and damping factors is fairly consistent. The correlation between GDP and default cycles on the one hand, and credit spreads on the other hand is never significant. At the short frequency between 5 and 6 years, the correlation between the GDP cycle and the default cycle is negative and strongest for lags of zero or one quarters. At lag 2, the correlation drops significantly given a decrease in factor loading from 1.27 to 0.82. At a lag of three quarters, the correlation has dropped to zero and has become insignificant. By contrast, the corresponding loading (B) for the long cycle becomes stronger, a phenomenon not found for the annual data. It appears that the lead/lag times between defaults and economic predictors should not be set too high. Lags of up to one quarter appear acceptable, but at longer lags common features between defaults and other variables may be corrupted. This holds in particular for co-cyclicality at higher frequencies.

4. CONCLUSIONS

In this paper we used a multivariate unobserved components approach to describe the dynamic behaviour of credit risk factors in their relation to the real economy. We depart from other approaches in credit risk modelling in that we focus on the time-series behaviour rather than the cross-section dimension of default-related data. Moreover, we model credit spreads and business failure rates jointly with macroeconomic developments. By adopting the unobserved components approach, we were able to disentangle medium and short-term cyclical movements from longer-term developments in credit risk factors. In this way, we could retrace some of the earlier empirical evidence on the relation between credit risk and the macro-economy. For our longest data sample, there appeared to be strong co-cyclicality between spreads and defaults and between spreads and GDP at typical business frequencies of 6 years. At longer frequencies of 11 years, there was also significant co-cyclicality between GDP and defaults. The latter result is robust to a variety of changes in the model specification. The other two effects are not. In particular, looking at more recent, i.e., post-war data, co-cyclicality between credit spreads and the other two series has become statistically insignificant. Moreover, the co-cyclicality between GDP and defaults at typical business cycle frequencies of 6 years is easily corrupted if GDP is lagged by more than one quarter.

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[3] Possibly due to the rough approximation of the quarterly default series from the annual data, the estimation procedure ran into some numerical difficulties. We solved these by fixing the period of the long cyclical component to 16 years, which appears adequate given the estimation results in the last six columns of Table I.

Table II. Parameter estimates

The table contains parameter estimates for the model

$$y_t = \mu_t + A\gamma_t + B\psi_t + e_t, \quad e_t \overset{\text{i.i.d.}}{\sim} N(0, \Sigma_e)$$

$$\Delta\mu_{t+1} = \beta_t = \beta_{t-1} + \eta_t, \quad \eta_t \overset{\text{i.i.d.}}{\sim} N(0, \Sigma_\eta)$$

$$\begin{pmatrix} \gamma_t \\ \gamma_t^* \end{pmatrix} = \phi_\gamma \begin{pmatrix} \cos(\lambda_\gamma)I & \sin(\lambda_\gamma)I \\ -\sin(\lambda_\gamma)I & \cos(\lambda_\gamma)I \end{pmatrix} \begin{pmatrix} \gamma_{t-1} \\ \gamma_{t-1}^* \end{pmatrix} + \begin{pmatrix} \kappa_t \\ \kappa_t^* \end{pmatrix}, \quad (\kappa_t, \kappa_t^*)' \overset{\text{i.i.d.}}{\sim} N(0, I_2 \otimes D_\gamma)$$

$$\begin{pmatrix} \psi_t \\ \psi_t^* \end{pmatrix} = \phi_\psi \begin{pmatrix} \cos(\lambda_\psi)I & \sin(\lambda_\psi)I \\ -\sin(\lambda_\psi)I & \cos(\lambda_\psi)I \end{pmatrix} \begin{pmatrix} \psi_{t-1} \\ \psi_{t-1}^* \end{pmatrix} + \begin{pmatrix} \omega_t \\ \omega_t^* \end{pmatrix}, \quad (\omega_t, \omega_t^*)' \overset{\text{i.i.d.}}{\sim} N(0, I_2 \otimes D_\psi)$$

with y_t containing real GDP (GDP), Dun and Bradstreet (1998) business failures (DEFLT) and credit spreads (SPRD), respectively. The failure rates are transformed using a probit transformation. The sample consists of quarterly observations from 1948 to 1997. Parameter significance is denoted by [a](20%), [b](10%) or [c](5%).

	No lags, 1948–1997			GDP, lag 1			GDP, lag 2			GDP, lag 3		
	GDP	DEFLT	SPRD	GDP	DEFLT	SPRD	GDP	DEFLT	SPRD	GDP	DEFLT	SPRD
period $2\pi/(4\lambda_\gamma)$	5.036[c]			4.932[c]			5.177[c]			5.096[c]		
ϕ_γ	0.938[c]			0.952[c]			0.934[c]			0.922[c]		
variance D_γ	0.00533[c]	0.00113[a]	0.0045[c]	0.0036[c]	0.0009[b]	0.0053[c]	0.0045[c]	0.0	0.0053[c]	0.0062[b]	0.0	0.0078[c]
load matrix A	GDP	DEFLT	SPRD	GDP	DEFLT	SPRD	GDP	DEFLT	SPRD	GDP	DEFLT	SPRD
γ_{gdp}	1	−1.199[c]	−0.199	1	−1.273[c]	−0.195	1	−0.820[c]	−0.080	1	0.024	0.017
γ_{def}	0	1	0.031	0	1	0.015	0	1	0.245	0	1	0.17
γ_{spr}	0	...	1	0	0	1	0	0	1	0	0	1
period $(2\pi/\lambda_\psi)$	16.0			16.0			16.0			16.0		
ϕ_ψ	0.979[c]			0.982[c]			0.979[c]			0.982[c]		
variance D_ψ	0.0139[c]	0.0	0.0038[c]	0.0086[c]	0.0	0.0038[c]	0.0097[c]	0.0	0.0038[c]	0.0114[c]	0.0	0.0038[c]
load matrix B	GDP	DEFLT	SPRD	GDP	DEFLT	SPRD	GDP	DEFLT	SPRD	GDP	DEFLT	SPRD
ψ_{gdp}	1	−1.344[c]	−0.114	1	−1.762[c]	−0.122	1	−1.873[c]	−0.117	1	−2.123[c]	−0.106
ψ_{def}	0	1	0.036	0	1	0.034	0	1	0.041	0	1	0.040
ψ_{spr}	0	0	1	0	0	1	0	0	1	0	0	1

Our results corroborate some of the earlier results in the empirical credit risk literature. They also open up some new possibilities for making default probabilities dependent on the state of the economy. This may prove useful in, for example, a dynamic credit risk management setting, where default scenarios are needed over a variety of economic conditions. An important extension of our current research would be to test whether our results hold up for more recent data. Of particular interest is the lack of correlation between the credit spread and the other variables in our model. The advantage of more recent data is that we may come up with better measurements of defaults and credit spreads using available databases. The obvious drawback, however, will be the relatively short time span available for a proper time-series analysis of the type presented in this paper.

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