## technoteach technocamps

























#### Welcome!

Unit 3 CPD for
Secondary
Education



#### Introductions

Your lecturers for the course will be:



**Daniel North**daniel.north@technocamps.com



Alex Southern
alex.southern@technocamps.com



#### Unit 3

Unit 3 will be 9 weekly sessions, with a 2-week break over the Easter holiday period and a further 5-week break over the May exam period:

#### Unit 3 Term 1:

- 1. 27<sup>th</sup> Feb | Assembly Language & LMC pt.1
- 2. 5<sup>th</sup> Mar | Assembly Language & LMC pt.2
- 3. 12<sup>th</sup> Mar | Number Systems pt.1
- 4. 19<sup>th</sup> Mar | Number Systems pt.2

\*\* EASTER BREAK\*\*



#### Unit 3

Unit 3 will be 9 weekly sessions, with a 2-week break over the Easter holiday period and a further 5-week break over the May exam period:

#### Unit 3 Term 2:

- 7. 9<sup>th</sup> Apr | File Types & Compression
- 8. 16<sup>th</sup> Apr | Boolean Algebra pt.1
- 9. 23<sup>rd</sup> Apr | Boolean Algebra pt.2
  - \*\*HALF TERM AND EXAMS\*\*
- 7. 4<sup>th</sup> Jun | Greenfoot pt.1
- 8. 11<sup>th</sup> Jun | Greenfoot pt.2 \*\*FND OF UNIT\*\*



# Components of Computer Systems





#### **Motherboard**











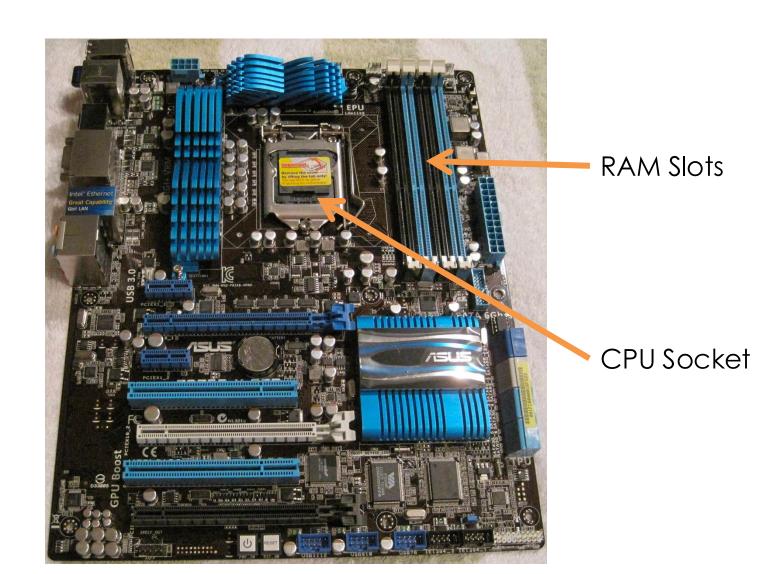
**CPU Socket** 



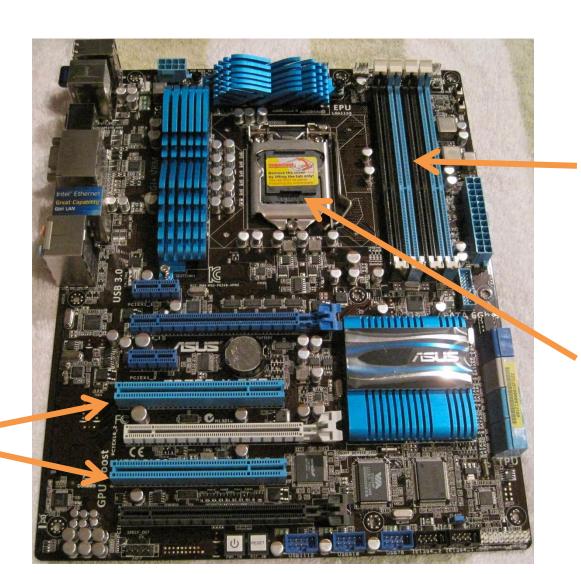


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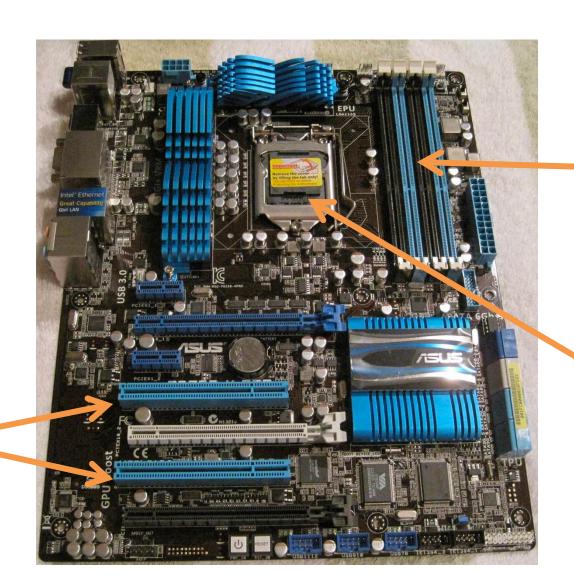




RAM Slots

**CPU Socket** 



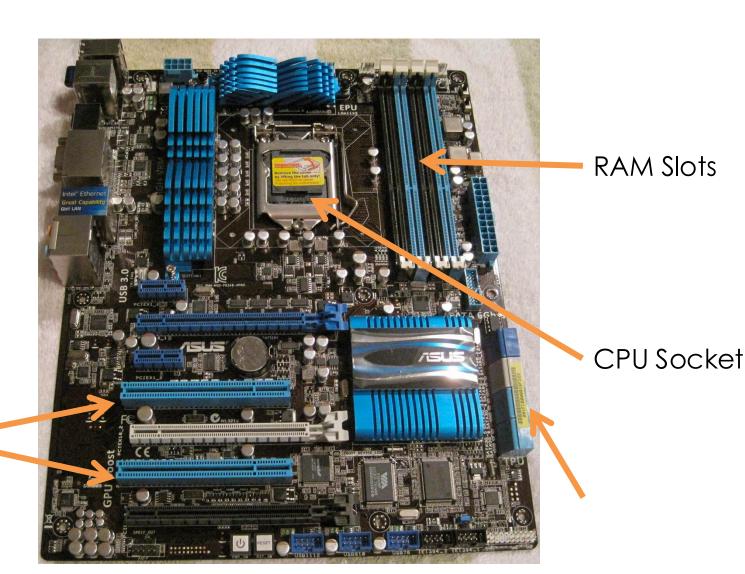


**RAM Slots** 

**CPU Socket** 

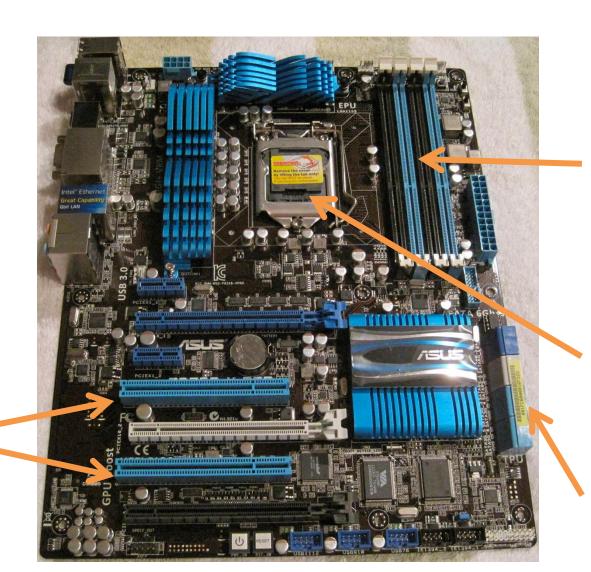
PCI Slots





PCI Slots





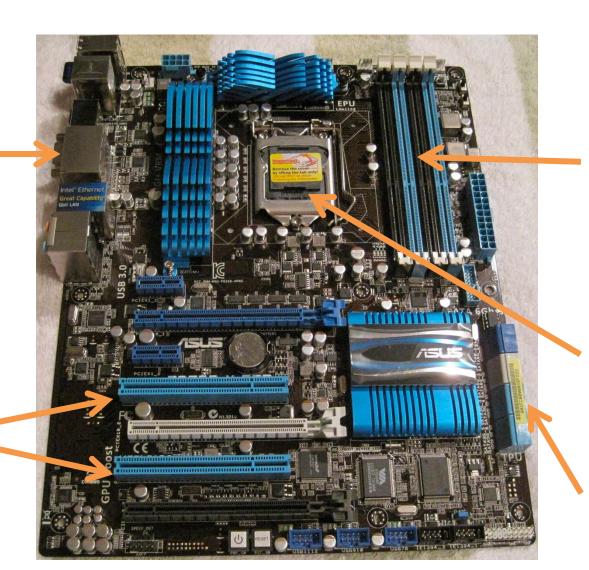
**RAM Slots** 

**CPU Socket** 

PCI Slots

**SATA Port** 





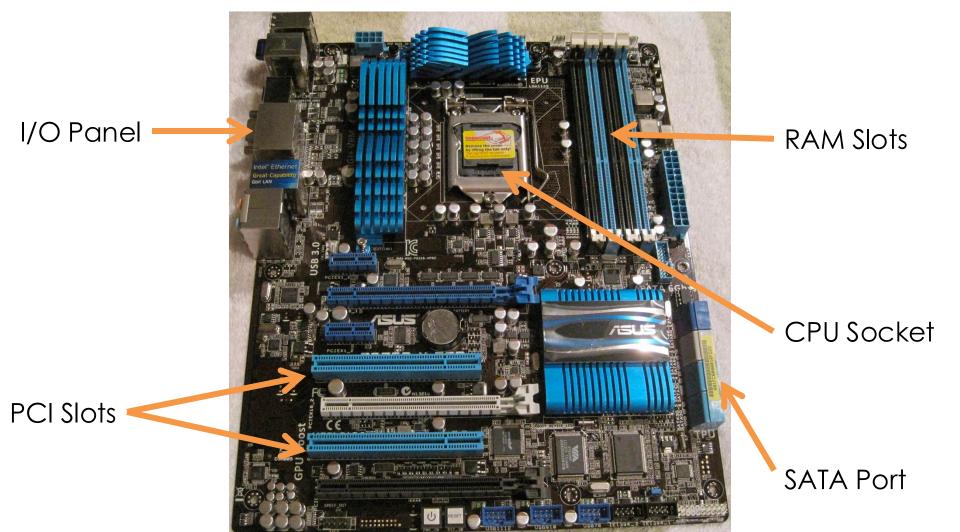
**RAM Slots** 

**CPU Socket** 

PCI Slots

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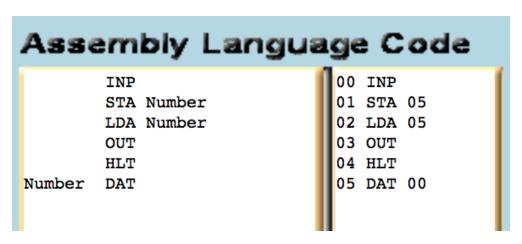






Assembly language is a low-level programming language which uses an assembler to convert a program into machine code which can be run by the computer.

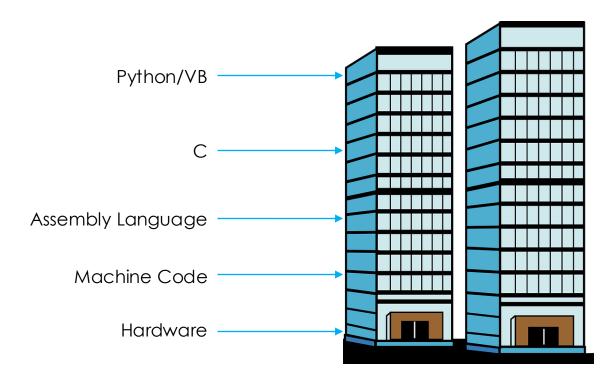
Assembly languages usually use short mnemonics as instructions and each one is specific to the computer architecture and operating system.



Little Man Computer



Assembly languages are considered to be low-level because they are very close to machine languages. They are only one step removed from a computer's machine language.





## Why Assembly?





## Relationship between Assembly Language and Machine Code

A CPU cannot directly read source code. Different CPUs may have different architecture and each different architecture has its own machine language.

This prevents direct source code to machine code translation – we need to use an assembly language to assemble the code which bridges the gap.

For example, a piece of Python code assembled to run on a 64 bit Windows machine will not have the same instruction set as the Python code assembled to run on a 32 bit Linux machine.



#### Python → Assembly

Simple program in Python:

```
def main():
   for i in range(10):
      print(i)
```

This can be compiled into the following assembly:

```
.section _TEXT, _text
.globl _main
_main:
                 $0
        pushq
        pushq
                %rbp
        movq
                %rsp, %rbp
                $0, 8(%rbp)
        movq
main_1_while:
                $10, %rdx
        movq
                8(%rbp), %rax
        movq
                %rdx, %rax
        cmpq
                $0, %rax
        movq
                main_3_less
        jnl
        inca
                 %rax
```

```
main_3_less:
                 $0, %rax
        cmpq
                main_2_break
        jΖ
        pushq
                8(%rbp)
        call
                 print
                 $8, %rsp
        addq
                 $1, %rdx
        movq
                8(%rbp), %rax
        movq
        addq
                %rdx, %rax
                %rax, 8(%rbp)
        movq
                main_1_while
        jmp
main_2_break:
                 $0, %edi
        movl
                 $0x2000001, %eax
        movl
        syscall
```

```
putc:
        pushq
                 %rbp
                 %rsp, %rbp
        movq
                 $0x2000004, %eax
        movl
                 $1, %edi
        movl
                 %rbp, %rsi
        movq
                 $16, %rsi
        addq
                 $1, %rdx
        movq
        syscall
        popq
                 %rbp
        ret
```



If we wrote the same code in **LMC Assembly language**, it would look like this.

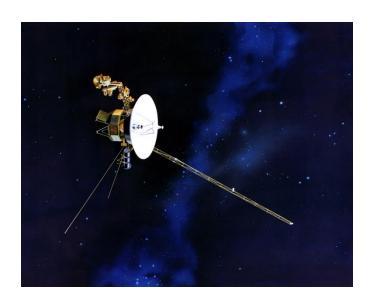
```
loop LDA value // load value
     OUT
               // output value
     ADD one
                // add one to value and store
     STA value
     LDA max // load how many times we need to loop
     SUB value // subtract the current value
     BRP loop // if this is positive keep looping
                // halt
     HLT
value DAT 0
     DAT 9
max
     DAT 1
one
```

We have **10 lines** of LMC Assembly language code instead of the **30** we got from converting Python to Assembly.



## Why Are Assembly Languages Used?

Low-level languages are especially useful when speed of execution is critical or when writing software which interfaces directly with the hardware, e.g. device drivers.





## Why Are Assembly Languages Used?

Example: The Voyager space probe launched in 1977 (now outside our solar system) is programmed using an old assembly language. NASA are struggling to find anyone who still has a working knowledge of the language to keep it going!

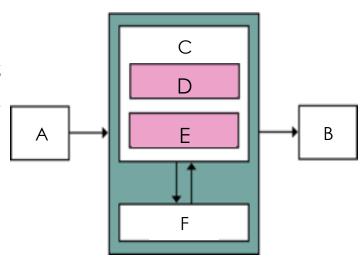








Just like architecture of a building, computer architecture is the way that a computer is designed to function in terms of hardware.

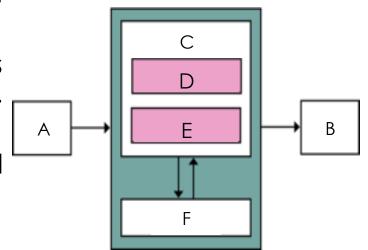




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The most common architecture is known as von Neumann architecture. This architecture is made up of:

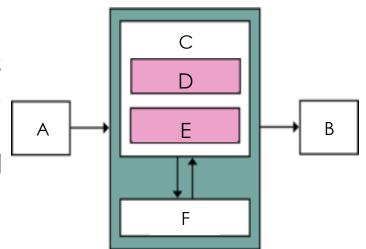
 CPU – Control unit, Arithmetic and Logic unit and registers





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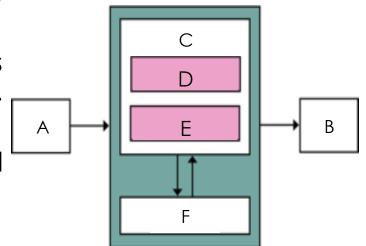
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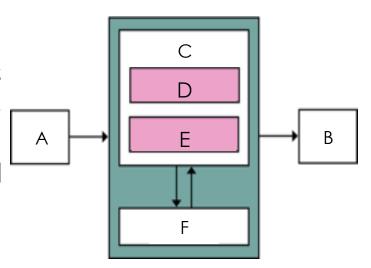
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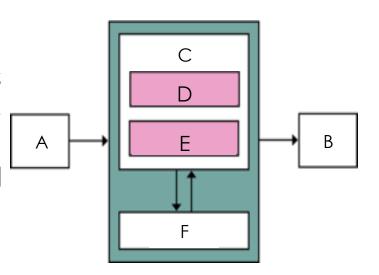
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- Input device Keyboard, mouse
- Output device Monitor, speakers



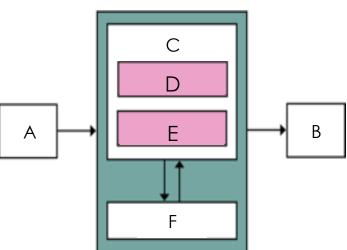


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Activity: von Neumann Architecture



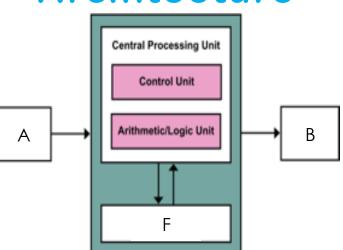


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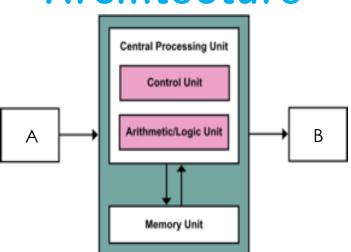


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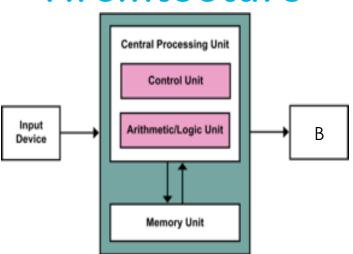
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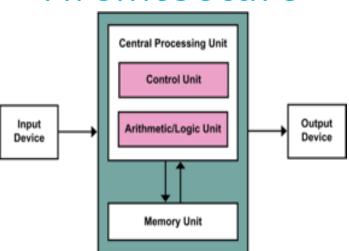
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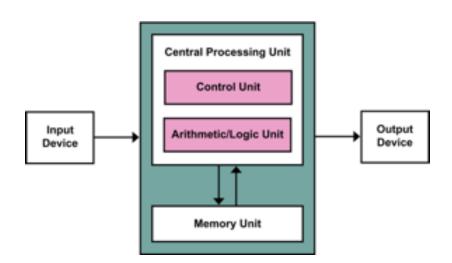
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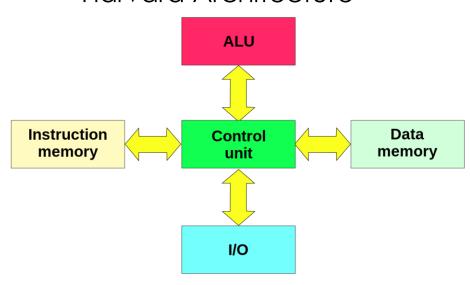


#### von Neumann Architecture



This stores both instructions and data within the same memory addresses and uses the same bus for both.

#### Harvard Architecture



This has separate memory addresses for instructions and data meaning it can run a program and access data simultaneously.



	von Neumann	Harvard
Flexibility		
Speed		
Cost		
Examples		



	von Neumann	Harvard
Flexibility	High level of flexibility as the memory is shared between instructions and data so the amount assigned to each can fluctuate depending on the task.	
Speed		
Cost		
Examples		



	von Neumann	Harvard
Flexibility	High level of flexibility as the memory is shared between instructions and data so the amount assigned to each can fluctuate depending on the task.	Limited flexibility as there is only a certain amount of memory that can be used for data and a certain amount for instructions.
Speed		
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Cost	Simpler control unit design, and development of one bus is cheaper and faster.	Control unit for two buses is more complicated which adds to the development cost.
Examples	Typically used in general purpose computers that will be used for many different purposes.	Typically used in embedded systems that only perform few functions like washing machines, burglar alarms etc.



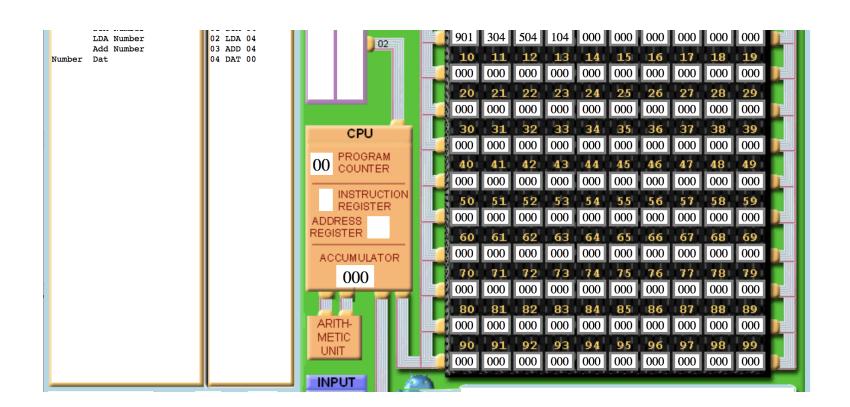
# Little Man Computer (LMC)





# Little Man Computer (LMC)

Little Man Computer (LMC) is a simulator that mimics von Neumann architecture.





# LMC – Fetch-Decode-Execute

Everything in a computer's memory is data.

Although programs may seem different from data, they are treated in exactly the same way: the computer executes a program, instruction by instruction.

These instructions are the 'data' of the fundamental program cycle:

- 1. **fetch** the next instruction
- 2. decode it
- 3. execute it

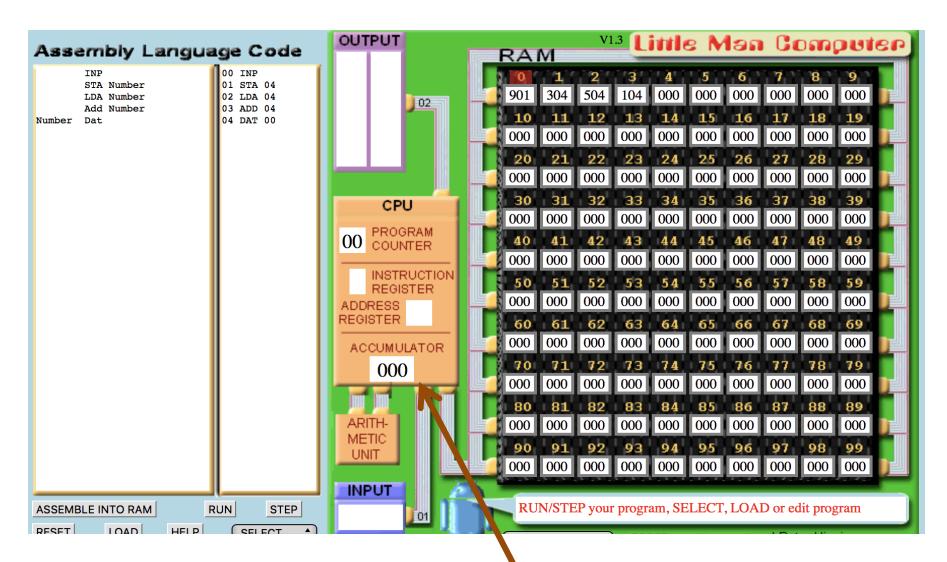
Then the next program cycle starts which will process the next instruction. Even the location of the next instruction is just data.



## The LMC Environment

Accumulator – This is like the active memory of the simulator. The
majority of our instructions will modify the contents of the
Accumulator.





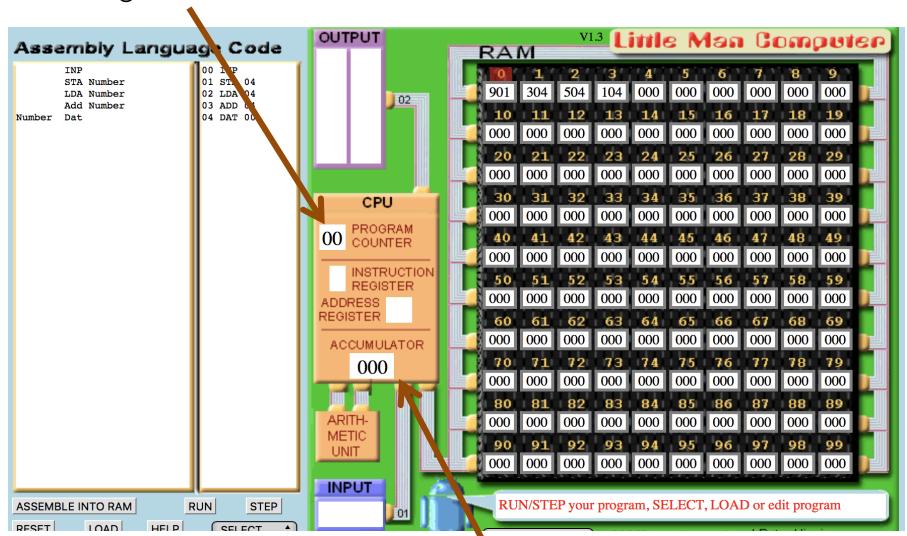


# The LMC Environment

- Accumulator This is like the active memory of the simulator. The majority of our instructions will modify the contents of the Accumulator.
- Program Counter This shows the current memory location that the processor is running.



#### **Program Counter**



Accumulator

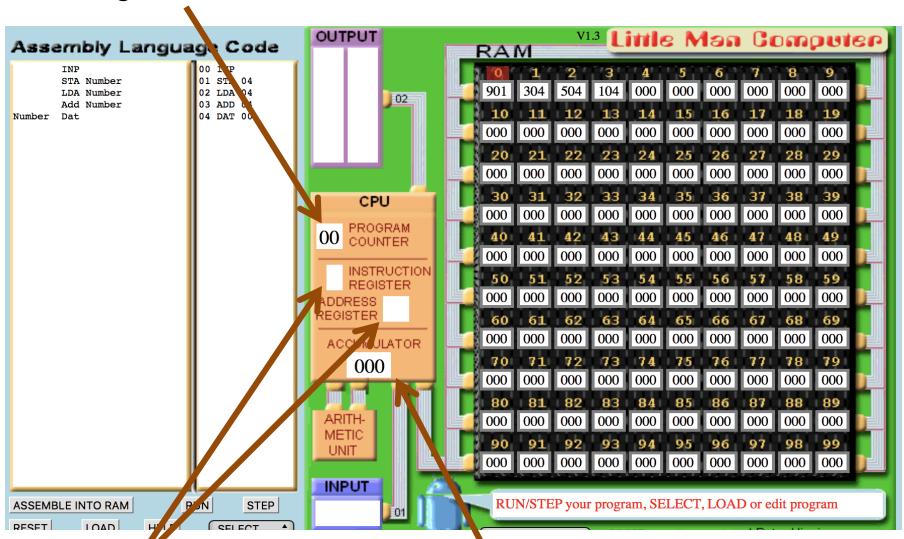


# The LMC Environment

- Accumulator This is like the active memory of the simulator. The majority of our instructions will modify the contents of the Accumulator.
- **Program Counter** This shows the current memory location that the processor is running.
- Instruction and Address register This shows which type of instruction is being used and which memory address it is being used on.



#### Program Counter



Instruction and Address register

Accumulator

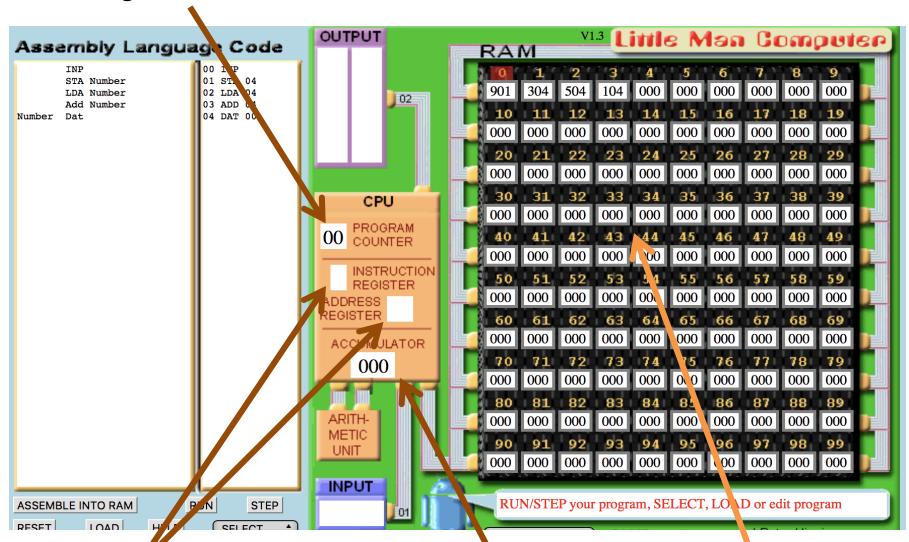


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#### Program Counter



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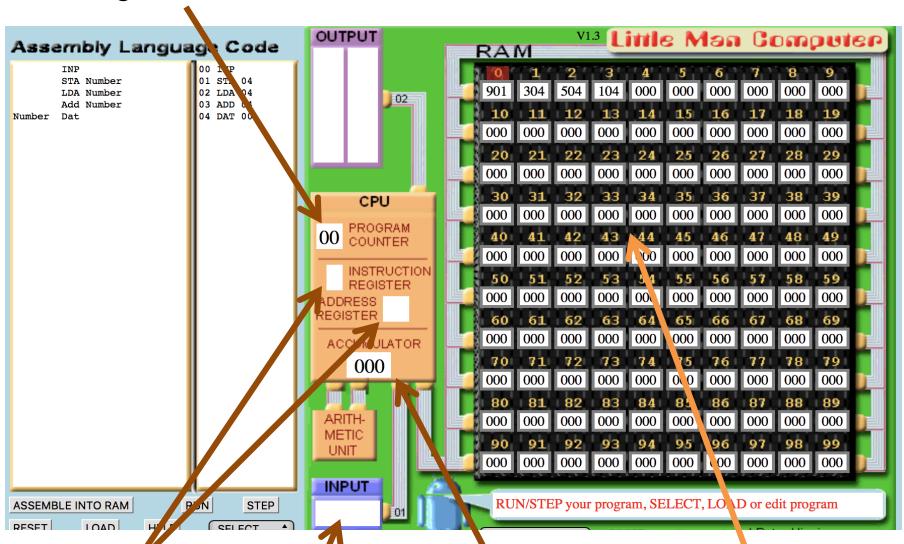


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- **Input Box** This is where user inputs are stored initially before being copied to the Accumulator.



#### Program Counter



Instruction and Address register

Input Box Accumulator

Memory Addresses



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- Input Box This is where user inputs are stored initially before being copied to the Accumulator.
- Output Box This is where a value is copied to from the Accumulator to display to the user.



Program Counter Output Box OUTPUT VI3 Little Man Computer Assembly Language Code RAM6 7 8 9 01 ST. 04 STA Number 000 000 02 LDA 04 LDA Number 03 ADD Add Number Number Dat 04 DAT 00 CPU 000 000 000 000 **PROGRAM** 00 COUNTER 41 42 44 45 46 INSTRUCTION 51 52 53 55 56 57 58 REGISTER 000 00 000 000 DDRESS. EGISTER 61 62 63 67 68 000 000 ACC' MULATOR 0.0 ARITH-METIC UNIT 000 000 INPUT **STEP** RUN/STEP your program, SELECT, LOAD or edit program ASSEMBLE INTO RAM RESET LOAD SELECT

Instruction and Address register

Input Box

Accumulator

Memory Addresses



# LMC Instruction Set





# **Taking Input**

Name: Input
Mnemonic: INP

**Code**: 901

#### **Description:**

The Input instruction copies the value input by the user into the Accumulator.

#### **Next Action:**

After the value has been copied, the Program Counter will move onto the next (sequential) memory location.



# **Providing Output**

Name: Output

**Mnemonic**: OUT **Code**: 902

#### **Description:**

The Output instruction copies the value in the Accumulator into the Output Box.

#### **Next Action:**

After the value has been copied, the Program Counter will move onto the next (sequential) memory location.



# Stopping the Programming

Name: Halt Mnemonic: HLT Code: 000

#### **Description:**

The Halt instruction does not affect any of the memory locations and stops the program.

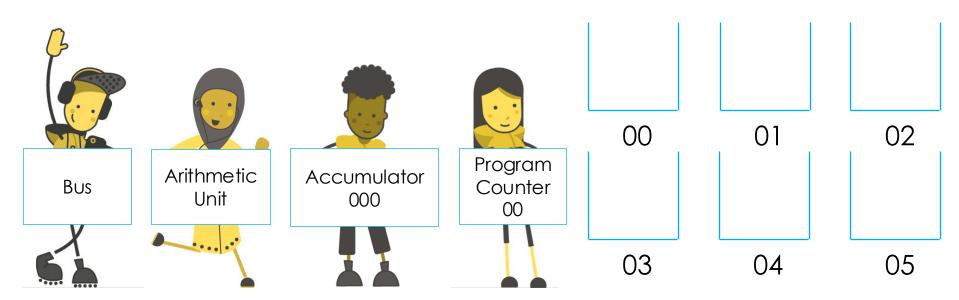
#### **Next Action:**

The execution of the program will stop.



# Activity: Visualising a Program Running

Using a few boxes and a few volunteers we can simulate running an assembly language program in the classroom. The rest of you will need to turn to the list of instructions in your workbooks.



The rest of the class are acting as the control unit, deciding what to do with the instructions and data.



# Here's the Program

Assembly	Language Code
INP	00 INP
OUT	01 OUT
HLT	02 HLT



# **LMC Code Summary**

\_\_\_ INP \_\_ - Input \_\_\_ OUT \_\_ - Output HLT - Halt



# **Storing Data**

Name: Store

**Mnemonic**: STA variable

**Code**: 3 \_ \_

#### **Description:**

The Store instruction will copy the value from the Accumulator and place it in an allocated memory location referred to by the variable name given.

#### **Next Action:**

After the value has been copied, the Program Counter will move onto the next (sequential) memory location.



# **Retrieving Data**

Name: Load

**Mnemonic**: LDA variable

**Code**: 5 \_ \_

#### **Description:**

The Load instruction will copy the value stored at the memory location, given by the variable, into the Accumulator.

#### **Next Action:**

After the value has been loaded into the Accumulator, the Program Counter will move onto the next (sequential) memory location.



#### **Data Memory Locations**

**Name**: Data

**Mnemonic**: variable DAT xxx

**Code**: (the data)

#### **Description:**

The Data instruction will reserve a memory location to store data. This location can be referred to by the given variable name. If you want to give the variable an initial value, replace the xxx with a value, the default is 0.

#### **Next Action:**

After the memory location has been reserved, the Program Counter will move onto the next (sequential) memory location.



# Input & Print a Number

Python Code:

Assembly Language:

num = int (input( ))
print (num)

INP

STA num

LDA num

OUT

HLT

num DAT



# Activity: Running a Program

Assembly Language Code				
INP	00 INP			
STA Number	01 STA 05			
LDA Number	02 LDA 05			
OUT	03 OUT			
HLT	04 HLT			
Number DAT	05 DAT 00			

Program counter	
-----------------	--

Instruction register

Address register

00	01	02	03	04
05	06	07	08	09
10	11	12	13	14
15	16	17	18	19

Accumulator





Create a program which takes in two inputs and outputs them in reverse order.



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We have to output the second input before the first. So we know we are going to have to store the first number at some point.



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**INP** get the first number

**STA** number1 — store it away for later



Create a program which takes in two inputs and outputs them in reverse order.

Next up we need to get the second number.

**INP** — get the first number

**STA** number1 — store it away for later

**INP** get the second number



Create a program which takes in two inputs and outputs them in reverse order.

We need to output the second number before the first. We could store the second number but we don't have to.

**INP** get the first number

**STA** number1 — store it away for later

**INP** get the second number

**OUT** output the second number



Create a program which takes in two inputs and outputs them in reverse order.

Now we need to output the first number. But we can only output the number in the accumulator. So we need to load it first.

**INP** — get the first number

**STA** number1 — store it away for later

**INP** get the second number

**OUT** output the second number

**LDA** number 1 — load the first number from the registry

**OUT** output the first number



# **Activity: Storing and Loading**

1. Create a program which takes and **stores** two inputs from the user and outputs the first input followed by the second input.

2. Create a program which takes and **stores** four inputs from the user and always outputs the third input.

3. Create a program which takes in three inputs and outputs them in reverse order.



#### LMC Code Summary

```
INP
                       // Input
       OUT
                       // Output
       HLT
                       // Halt
       STA
                       // Store
               var
       LDA
                   // Load
               var
                       // Data (Default for xxx is 0)
var
       DAT
               XXX
```

2. Create a program which takes and **stores** four inputs from the user and always outputs the third input.

3. Create a program which takes in three inputs and outputs them in reverse order.



#### Addition

**Name**: Addition

**Mnemonic**: ADD variable

**Code**: 1 \_ \_

#### **Description:**

The Add instruction adds the value stored in the given memory location to the Accumulator.

#### **Next Action:**

After the value has been loaded into the Accumulator, the Program Counter will move onto the next (sequential) memory location.



#### Subtraction

**Name**: Subtraction

**Mnemonic**: SUB variable

**Code**: 2\_\_

#### **Description:**

The Subtraction instruction subtracts the value stored in the given memory location away from the Accumulator.

#### **Next Action:**

After the value has been loaded into the Accumulator, the Program Counter will move onto the next (sequential) memory location.



#### Addition and Subtraction (1)

Using a pen and paper write LMC programs to solve the problems.

- Create a program which takes in and stores two inputs from the user and outputs the sum of them.
- 2. Create a program which takes in three numbers and stores them and then outputs the sum of the first two numbers with the third subtracted.

When you think you are finished, go to your computer and test it.



## Addition and Subtraction (2)

In small groups, try and solve the following problems.

- Create a program which takes in a number, doubles it and outputs the result.
- Create a program which takes a number and multiplies it by eight.

**Challenge** - Create a program which takes in a number and multiplies it by forty.



#### **LMC Code Summary**

```
INP
                     // Input
       OUT
                    // Output
       HLT
                    // Halt
                  // Store
      STA
             var
       LDA
                 // Load
             var
             xxx // Data (Default for xxx is 0)
       DAT
var
             var // Addition
       ADD
                 // Subtraction
       SUB
             var
```



# Go To (Branch Always)

**Name**: Branch Always

**Mnemonic**: BRA variable

**Code**: 6 \_ \_

#### **Description:**

Updates the Program Counter to the memory location referred to by the variable given.

#### **Next Action:**

After the memory location has been loaded into the program counter, that memory location will be executed.



# **Activity: Looping**

 Create a program which allows the user to input numbers indefinitely and outputs each number.

2. Create a program which allows the user to input numbers indefinitely and outputs the running total after each entry.



## Go To (Branch If Zero)

**Name**: Branch If Zero

**Mnemonic**: BRZ variable

**Code**: 7 \_ \_

#### **Description:**

Updates the Program Counter to the memory location referred to by the variable given if the value in the Accumulator is **equal** to zero.

#### **Next Action:**

After the memory location has been loaded into the program counter, that memory location will be executed.



# Go To (Branch If Zero or Positive)

**Name:** Branch If Zero or Positive

**Mnemonic**: BRP variable

**Code**: 8 \_ \_

#### **Description:**

Updates the Program Counter to the memory location referred to by the variable given if the value in the Accumulator is **zero or positive**.

#### **Next Action:**

After the memory location has been loaded into the program counter, that memory location will be executed.



In Little Man Computer we do not have "if statements" like we have in Python for comparisons.

The only way to branch based on a condition is to do a subtraction and then branch based on whether the result is:

- 0 (BRZ)
- 0 or positive (BRP)



```
LDA two
SUB five
BRP outputTwo
LDA five
OUT
HLT
outputTwo LDA two
OUT
HLT
two DAT 2
five DAT 5
```



LDA two

SUB five

BRP outputTwo

LDA five

OUT

HLT

outputTwo LDA two

OUT

HLT

two DAT 2 five DAT 5 Split up into 4 sections of code



```
LDA two
SUB five
BRP outputTwo

LDA five
OUT
HLT

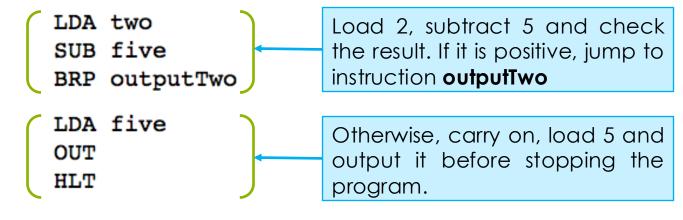
OutputTwo LDA two
OUT
HLT

two DAT 2
```

five

DAT 5





outputTwo LDA two

OUT

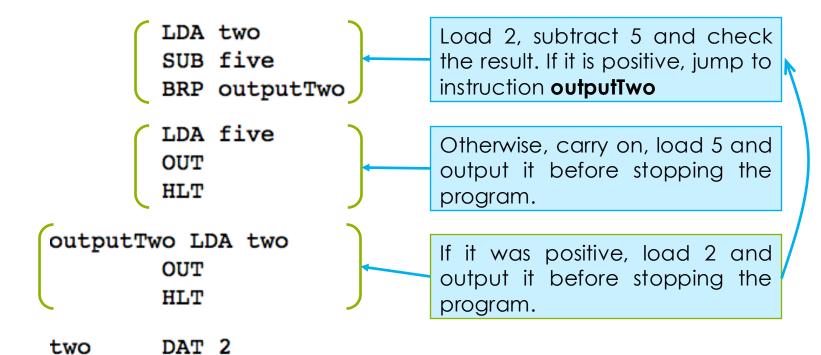
HLT

two DAT 2 five DAT 5



five

DAT 5





# **Activity: Conditional Branching**

- 1. Create a program which allows the user to input two numbers and outputs the smallest number. Hint: if you do a b and the number is positive, then a is bigger than b.
- 2. Create a program which allows the user to repeatedly input two numbers and checks if they're equal. Only output the number if they are equal.
- 3. Create a program that repeatedly takes in inputs and only outputs them if they are zero.
- 4. Similar to 3, create a program which outputs everything except zeroes.

**Challenge** - Create a program which allows the user to input two numbers and outputs the multiplication of the two numbers.



#### **LMC Code Summary**

```
INP
                      // Input
       OUT
                      // Output
                      // Halt
       HLT
       STA
                      // Store
              var
                      // Load
       LDA
              var
                      // Data (Default for xxx is 0)
       DAT
var
              XXX
                      // Addition
       ADD
              var
                      // Subtraction
       SUB
              var
                      // Branch Always
       BRA
              var
                      // Branch If Zero
       BRZ
              var
                      // Branch If Positive
       BRP
              var
```



In order to calculate the equation for a given sequence of numbers we must first look at the difference between them e.g.

Index term: 1 2 3 4 5 ...



In order to calculate the equation for a given sequence of numbers we must first look at the difference between them e.g.

Index term: 1 2 3 4 5 ...

+2



In order to calculate the equation for a given sequence of numbers we must first look at the difference between them e.g.

Index term: 1 2 3 4 5 ...

+2 +2



In order to calculate the equation for a given sequence of numbers we must first look at the difference between them e.g.

Index term: 1 2 3 4 5 ...

+2 +2 +2



In order to calculate the equation for a given sequence of numbers we must first look at the difference between them e.g.

Index term: 1 2 3 4 5 ...

+2 +2 +2 +2



In order to calculate the equation for a given sequence of numbers we must first look at the difference between them e.g.

Index term: 1 2 3 4 5 ...

+2 +2 +2 +2

Number: 3,5,7,9,11...

The difference between each number is +2.

So the number in front of the nth term in our equation must be 2 i.e. **2n** 

The final step is to check if we need to add or subtract from 2n.



In order to calculate the equation for a given sequence of numbers we must first look at the difference between them e.g.

Index term: 1 2 3 4 5 ...

+2 +2 +2 +2

Number: 3,5,7,9,11...

If we try inserting the index term into our nth term equation **2n** does the answer match up correctly?



In order to calculate the equation for a given sequence of numbers we must first look at the difference between them e.g.

Index term: 1 2 3 4 5 ...

+2 +2 +2 +2

Number: 3,5,7,9,11...

If we try inserting the index term into our nth term equation 2n does the answer match up correctly?  $2 \times 1 = 2$ 



## Sequences (Mathematics GCSE)

In order to calculate the equation for a given sequence of numbers we must first look at the difference between them e.g.

Index term: 1 2 3 4 5 ...

+2 +2 +2 +2

Number: 3,5,7,9,11...

If we try inserting the index term into our nth term equation 2n does the answer match up correctly?  $2 \times 1 = 2$ 

What should we add to correct this?



## Sequences (Mathematics GCSE)

In order to calculate the equation for a given sequence of numbers we must first look at the difference between them e.g.

Index term: 1 2 3 4 5 ...

+2 +2 +2 +2

Number: 3,5,7,9,11...

If we try inserting the index term into our nth term equation 2n does the answer match up correctly?  $2 \times 1 = 2$ 

What should we add to correct this? +1



## Sequences (Mathematics GCSE)

In order to calculate the equation for a given sequence of numbers we must first look at the difference between them e.g.

Index term: 1 2 3 4 5 ...

+2 +2 +2 +2

Number: 3,5,7,9,11...

If we try inserting the index term into our nth term equation 2n does the answer match up correctly?  $2 \times 1 = 2$ 

What should we add to correct this? +1

Therefore our equation is: 2n + 1



The first 5 terms of a sequence are:

What is the difference between each term?

What is the equation so far?

Do we need to add/subtract something to get the right values?



The first 5 terms of a sequence are:

What is the difference between each term? +2

What is the equation so far?

Do we need to add/subtract something to get the right values?



The first 5 terms of a sequence are:

What is the difference between each term? +2

What is the equation so far? 2n

Do we need to add/subtract something to get the right values?



The first 5 terms of a sequence are:

What is the difference between each term? +2

What is the equation so far? 2n

Do we need to add/subtract something to get the right values? -5



The first 5 terms of a sequence are:

What is the difference between each term? +2

What is the equation so far? 2n

Do we need to add/subtract something to get the right values? -5

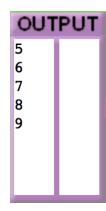


## **Activity: Sequences**

#### For the following sequences:

- a. Write out the nth term equation.
- b. Calculate the 20th term in the sequence
- 1. 7, 8, 9, 10, 11 ...
- 2. 3, 6, 9, 12, 15 ...
- 3. 12, 17, 22, 27, 32 ...
- 4. -6, -2, 2, 6, 10 ...
- 5. 3, -3, -9, -15, -21 ...

- 6. a. Write out the first 5 terms of the sequence given by 3n 7.
  - b. Calculate the 15th term of the sequence.





## **Activity: LMC Example**

Now we are going to implement this nth term equation in LMC to produce the first 5 terms in the sequence: 5, 6, 7, 8, 9.

Using the space in your workbooks discuss with a partner and try to write down the steps you would need to implement it. Think about:

- What is the nth term equation?
- Would you need to use a loop?
- What other variables would you need?
- You will need to be adding or subtracting by 1, how could you implement this?

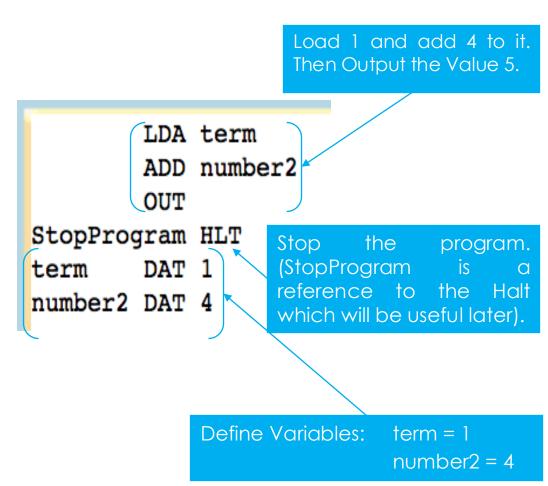


### The First Value

To get the first result we need to load the first index term = 1, add 4 to it and then output it.

We always add 4 in our nth term equation so should store 4 as a variable called number 2.

We also need to define a variable so we know which index term we are inserting into our equation.





## **Looping for More Values**

Now we need to add one to the index term variable before we calculate the next number in our sequence.

To do this we define a variable called one which we add to the index term variable.

We use a loop to repeat the previous calculations and output each new number in the sequence.

LDA term 00 01 ADD number2 02 OUT Loop back to the first Increase the current 03 LDA term line (00) Always. term by one 04 ADD one store it again. 05 STA term BRA 00 06 07 StopProgram HLT 08 DAT 1 term 09 DAT 1 one number2 DAT 4

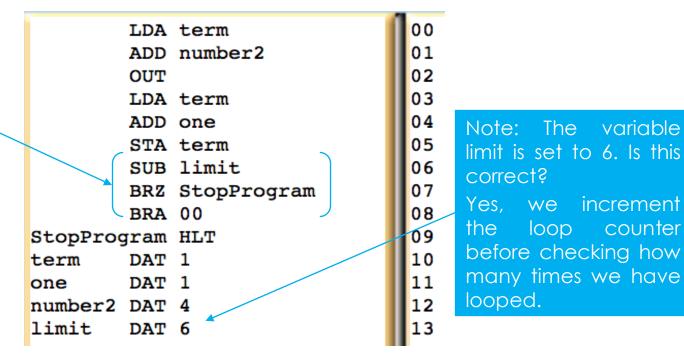


counter

## Only Outputting the First 5 Values

If we want to stop the loop after 5 values have been output we need to compare our term variable to a limit. Once our term reaches the same value as the limit, we halt the program.

Check if the term and limit are the same, if so jump to the HLT instruction.





# Activity: Creating Your Own Sequences

You can use this code as a starting point for creating your own sequences. What would we change to make the sequence n + 8 for example?

In your workbooks, answer the questions and try running the code in LMC to see if you're correct.

n – 7 2n + 4 2n – 6 3n + 8 8n - 3

LDA	term	00
ADD	number2	01
OUT		02
LDA	term	03
ADD	one	04
STA	term	05
SUB	limit	06
BRZ	StopProgram	07
BRA	00	08
StopProgram	HLT	09
term DAT	1	10
one DAT	1	11
number2 DAT	4	12
limit DAT	6	13



## **Activity: Advanced LMC**

- 1. Create a program which takes in inputs and outputs the positive value, i.e. if it's negative, you output the positive, -3 would output 3.
- 2. Create a program which takes an input, outputs that value and then counts down and outputs every value until it reaches 0 (or counts up to 0 if value is negative).
- 3. Create a program which takes two inputs and checks if they have the same sign (both positive or both negative). If they have the same sign output a zero, otherwise output a 1.
- 4. Create a program which takes two inputs and returns the remainder if you divided the first by the second. (Don't worry about negative numbers, but dividing zero by a number and diving a number by zero should be considered.)



## **Activity: Very Advanced LMC**

Create a program which takes in an input and outputs all of the numbers in the Fibonacci sequence up to that input number. The Fibonacci sequence is 1, 1, 2, 3, 5, 8, 13, 21 You can set one variable to 1 at the beginning. No cheating!

Note the Fibonacci sequence is made by adding the previous number to the current one, starting with 1:

1 0+1=1 1+1=2 2+1=3 3+2=5