Source:

1 | Broader vector spaces

- · Doesn't have to be physics vectors
- · maybe it's like matrices
- · or linear maps themselves

2 | The Linear Map 0

A linear map S=0 is a map where $Su=0 \forall u$.

3 | Axler 3.A ex7

Let w = Tv.

3.1 | If
$$v = 0$$
 then

$$Tv = 0$$

By Axler 3.11 (Maps take 0 to 0). Thus, λ can be anything in \mathbb{F} .

3.2 | Otherwise,

 $\frac{1}{n} \in \mathbb{F}$ because the field has multiplicative inverses for all elements except 0.

$$Tv = w = \left(w\frac{1}{v}\right)v$$

Let $\lambda = w \frac{1}{v}$, then

$$\lambda v = w \frac{1}{v} v = w$$

which is in $\mathbb F$ because $w,\frac{1}{v}\in\mathbb F$ and fields are closed under multiplication.

4 | Axler 3.A ex10

The additivity of a linear map T requires T(u+v)=Tu+Tv. Because $U\subset V, U\neq V$

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