Axler 7.B exercise 7 June 1, 2021

Suppose V is a complex inner product space and  $T\in\mathcal{L}(V)$  is a normal operator such that  $T^9=T^8$ . Prove that T is self-adjoint and  $T^2=T$ .

In 7.1, Axler asserts that V is finite-dimensional.

T has a diagonal matrix w.r.t. an orthonormal basis of V.

$$TT^* = T^*T$$

Suppose T is invertible. Then,

$$T^9 = T^8$$

$$T^9T^{-7} = T^8T^{-7}$$

$$T^2 = T$$