Source: [KBhMATH401Limits]

1 | Epsilon Delta Proofs

The secrets of the limit

Formal Definition of a Limit

Definition 1
$$\cdot$$
 Limit Definition $\lim_{x\to a} f(x) = L$ for all $\epsilon>0$, there exists a δ such that $if\ 0<|x-a|<\delta,\ then\ 0<|f(x)-L|<\epsilon$

An Epsilon Delta Proof

Let's prove $\lim_{x\to 2} x^2 = 4$ together!

The crux of the proof is to come up with a value δ that is a function of ϵ assuming that $0 < \epsilon$ that meets $0 < |x - a| < \delta$.

Oh, here's some symbols

Symbol	Definition
\forall	For all
3	There exisits
s.t.	Such that

And so, the formal and pretentious definition of a limit:

$$\forall \epsilon > 0, \exists \delta > 0, \ s.t. \ 0 < |x - a| < \delta \rightarrow |f(x) - L| < \epsilon$$

This needs to go before every Epsilon Delta proof.