## 1 | Exercise 7

Suppose  $T \in \mathcal{L}(V)$  has a diagonal matrix A with respect to some basis of V and that  $\lambda \in \mathbb{F}$ . Prove that  $\lambda$  appears on the diagonal of A precisely dim  $E(\lambda,T)$  times.

## 2 | **Proof**

There must be \$\odim V\$ (non-distinct) eigenvalues on the diagonal.

Any eigenvalue  $\lambda$  must have dim  $E(\lambda,T)$  associated eigenvectors, by definition. ("In other words,  $E(\lambda,T)$  is the set of all eigenvectors of T corresponding to  $\lambda$ , along with the 0 vector").

Therefore,  $\lambda$  appears exactly once for each associated eigenvector, which is precisely dim  $E(\lambda, T)$ .