

$$1 \mid \int \ln x dx$$

$$\begin{aligned}\int \ln x dx &= \int 1 \ln x dx \\ &= x \ln x - \int x \frac{1}{x} dx \\ &= x \ln x - \int 1 dx \\ &= \boxed{x \ln x - x}\end{aligned}$$

$$2 \mid \int \tan^{-1} x dx$$

$$\int \tan^{-1} x dx = x \tan^{-1} x - \int x \frac{1}{x^2 + 1} dx$$