$$1 \mid \int \frac{\sqrt{x-1}}{x} dx$$

Let $u = \sqrt{x-1}$, $du = \frac{1}{2\sqrt{x-1}}dx$

$$\int \frac{\sqrt{x-1}}{x} dx = \int \frac{u}{u^2+1} 2u du$$

$$= 2 \int \frac{(u^2+1)-1}{u^2+1} du$$

$$= 2 \int \frac{u^2+1}{u^2+1} + \frac{-1}{u^2+1} du$$

$$= 2 \int 1 du - \frac{1}{u^2+1} + C$$

$$= 2 \int 1 du - \tan^- u + C$$

$$= 2u - \tan^- u + C$$

$$= \left[2\sqrt{x-1} - \tan^- (\sqrt{x-1}) + C \right]$$

$$2 \mid \int \frac{x^2}{x^2+1} dx$$

Let $u = x^2 + 1$, du = 2xdx

$$\int \frac{x^3}{x^2 + 1} dx = \frac{1}{2} \int \frac{u - 1}{u} du$$

$$= \frac{1}{2} \left(u - \int \frac{1}{u} du \right) + C$$

$$= \frac{1}{2} (u - \ln u) + C$$

$$= \left[\frac{1}{2} \left(x^2 + 1 - \ln(x^2 + 1) \right) + C \right]$$

$3 \mid \textbf{TODO} \int \frac{x-4}{x^2} dx$

Let u = x - 4, du = dx

$$\int \frac{x-4}{x^2} dx = \int \frac{u}{(u+4)^2} dx$$
$$= \int \frac{u}{u^2 + 8u + 16} du$$

$$4 | \int (x+1)e^{x^2+2x}dx$$

Let
$$u = x^2 + 2x$$
, $du = x + 1$

$$\int (x+1)e^{x^2+2x}dx = \frac{1}{2}\int e^u du$$
$$= \frac{1}{2}e^u$$
$$= \boxed{\frac{1}{2}e^{x^2+2x}}$$

$$5 \mid \int \tan^2 x + 1 dx$$

$$\int \tan^2 x + 1 dx = \int \sec^2 x - 1 + 1 dx$$

$$= \int \sec^2 x dx$$
Let $u = x, du = 1$

$$= \int \sec^2 u du$$

$$= \tan u + C$$

$$= \boxed{\tan x + C}$$

6 | **TODO**
$$\int \frac{6x^2-4}{x} dx$$

$$7 \mid \int \frac{e^x - 1}{e^x} dx$$

$$\int \frac{e^x - 1}{e^x} dx = \int 1 - \frac{1}{e^x} dx$$
$$= \int 1 - e^{-x} dx$$
$$= x + e^{-x} + C$$
$$= e^{-x} + x + C$$

$$8 \mid \int \frac{\sec^2 x}{\csc x} sinx dx$$

$$\int \frac{\sec^2 x}{\csc x} \sin x dx = \int \tan^2 x dx$$

$$= \int \sec^2 x - 1 dx$$

$$= \int \sec^2 x dx - \int 1 dx$$

$$= \cot x - x$$

$9 \mid \$ \int \sin x \cos x dx \$$

Let $u = \sin x$, then $du = \cos x dx$

$$\int \sin x \cos x dx = \int u du$$

$$= \frac{1}{2}u^2$$

$$= \left[\frac{1}{2}\sin^2 x\right]$$

10 | **TODO**
$$\int \frac{e^{2 \ln \sin x} + e^{2 \ln \cos x}}{e^{2 \ln \tan x} + e^{2 \ln 1}} dx$$

$$\int \frac{e^{2\ln\sin x} + e^{2\ln\cos x}}{e^{2\ln\tan x} + e^{2\ln 1}} dx = \int \frac{\sin^2 x + \cos^2 x}{\tan^2 x + 1} dx$$
$$= \int \frac{\sin^2 x}{\tan^2 x + 1} + \frac{\cos^2 x}{\tan^2 x + 1} dx$$
$$= \int \sin^2 x \cos^2 x + \cos^4 x dx$$

$$= \int \frac{1}{\tan^2 x + 1} dx$$
$$= \int \frac{1}{\sec^2 x} dx$$
$$= \int \cos^2 x dx$$

$$11 \mid \int \frac{\sec x \tan x}{1 + \sec^2 x} dx$$

Let \$\$,

12 |
$$\int x^2 e^{x^3} dx$$

Let $u=x^3$, $du=\frac{1}{3}x^2dx$

$$\int x^2 e^{x^3} dx = 3 \int e^u du$$

13 | **14**