Axler 6.B #10 May 4, 2021

1 | Problem

Suppose V is a real inner product space and v_1, \ldots, v_m is a linearly independent list of vectors in V. Prove that there exist exactly 2^m orthonormal lists e_1, \ldots, e_m of vectors in V that preserve the prefix spans.

2 | Proof Sketch

In general, during the Gram-Schmidt procedure, both e_j or $-e_j$ preserve orthonormality and prefix span equality. Thus, there are m independant binary choices and thus 2^m possibilities.

But why does the vector space have to be real?

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