

1 | Exercise 7

Suppose $T \in \mathcal{L}(V)$ has a diagonal matrix A with respect to some basis of V and that $\lambda \in \mathbb{F}$. Prove that λ appears on the diagonal of A precisely $\dim E(\lambda, T)$ times.

2 | Proof

Any eigenvalue λ must have $\dim E(\lambda, T)$ associated eigenvectors, by definition. ("In other words, $E(\lambda, T)$ is the set of all eigenvectors of T corresponding to λ , along with the 0 vector"). Therefore, λ appears exactly once for each associated eigenvector, which is precisely $\dim E(\lambda, T)$. \square