

Suppose  $T \in \mathcal{L}(V)$  and  $\lambda \in \mathbb{F}$ . Prove that  $\lambda$  is an eigenvalue of  $T$  iff  $\bar{\lambda}$  is an eigenvalue of  $T^*$ .

Given  $\lambda$  is an eigenvalue of  $T$ , show that  $\bar{\lambda}$  is an eigenvalue of  $T^*$ . This will imply both directions, since  $\lambda = \overline{\bar{\lambda}}$  and  $T = T^{**}$ .

There exists some  $v$  s.t.

$$Tv = \lambda v$$

$$\langle \lambda v, w \rangle = \langle Tv, w \rangle = \langle v, T^*w \rangle$$