1 | Problem

Suppose $T \in \mathcal{L}(V)$. Prove that $T/(\operatorname{null} T)$ is injective if and only if $(\operatorname{null} T) \cap (\operatorname{range} T) = \{0\}$

2 | **Proof**

First, we will rewrite the problem as logical statements for easier manipulation. The left-hand side " $T/(\operatorname{null} T)$ is injective" is equivalent to:

 $T/(\mathsf{null}\,T)$