Source: [KBe2020math530floIndex]

#flo

1 | Polynomials

See KBrefPolynomial

1.1 | 0 polynomial

- Has degree -infty
- · Degrees are usually positive, except for the 0 degree
- "that's too hard, and we're not going to do it here"

1.2 | Identically zero

- Like 0 or $0x^0$
- Most polynomials are sometimes zero, but polynomials that are "identically zero" means that it's always zero (instead of just sometimes zero)

1.3 | $\mathcal{P}_{m}(F)$

- Polynomials with coefficients in F whose highest degree is m
- It can't be "whose degree is exactly m" because otherwise you won't have the identity and it won't be closed under addition (in the case where coefficient sum $a_m + b_m = 0$)

1.3.1 | It's a finite dimensional vector space

 $a_0z^0 + \dots + a_mz^m + b_0z^0 + \dots + b_mz^m = (a_0 + b_0)z^0 + \dots + (a_m + b_m)z^m$

1.4 | **Proof of 2.16**

· Structure: proof by contradiction

2 | Linear Independence

- · "non-trivial" means "simplest possible", which has usually got the most zeros
- See ||KB20math530refLinearIndependence|

2.1 | 2.21 Linear Dependence Lemma 2.21

- it's saying that any linearly independent list has a vector inside that doesn't "contribute anything", and that if you remove it you'l have the same span. Implicitly, maybe through induction?) if you remove a dependent vector enough times then you get a linearly independent list.
- The list (1,1,1),(2,2,2),(3,3,3) is really dependent, but (0),(0),(0) is the most dependent (you have to remove all to get independence).

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3 | Exercise 2.A.1

3.1 | **Lemma**

If vectors v_1, v_2, v_3, v_4 span V, then the list

$$v_1 - v_2, v_2 - v_3, v_3 - v_4, v_4$$

also spans V.

3.2 | **Proof**

We prove the lemma by showing that any vector $v \in V$ can be written in the form $a_1v_1 + a_2v_2 + a_3 + v_3 + a_4v_4$ can also be written as a linear combination of the form

$$b_1(v_1-v_2)+b_2(v_2-v_3)+b_3(v_3-v_4)+b_4v_4$$

If we set

$$b_1 = a_1$$

$$b_2 = a_1 + a_2$$

$$b_3 = a_1 + a_2 + a_3$$

$$b_4 = a_1 + a_2 + a_3 + a_4$$

then the two combinations will be equivalent:

$$a_1(v_1 - v_2) + (a_1 + a_2)(v_2 - v_3) + (a_1 + a_2 + a_3)(v_3 - v_4) + (a_1 + a_2 + a_3 + a_4)v_4$$

$$= a_1v_1 - a_1v_2 + a_1v_2 + a_2v_2 - (a_1 + a_2)v_3 + (a_1 + a_2)v_3 + a_3v_3 - (a_1 + a_2 + a_3)v_4 + (a_1 + a_2 + a_3)v_4$$

4 | **Rock**

And here's a rock for good measure:

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Figure 1: ../Pasted image 20200929184245.png

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