#ret #disorganized #incomplete

1 | **Introduction**

The purpose of this lab is to verify the relation between capacitance, resistance, voltage, and charge time of a simple capacitor circuit. The equation that will be verified is

$$V_{cap} = V_{bat} \left(1 - e^{-\frac{t}{\tau}} \right)$$

where each variable has the following meaning:

Variable	Units	Description
t	Seconds (s)	Time elapsed since charging of the capacitor started. May be represented as $t - t_0$, where t is the current absolute time and t_0 is the absolute start time.
V_{cap}	Volts (V)	Voltage across the capacitor after a given elapsed time
V_{bat}	Volts (V)	Voltage of the battery, assumed to be constant.
τ	Seconds (s)	"Time constant" that scales the equation to the circuit. Equal to the product of the resistance and capacitance of the circuit (RC), and roughly equal to the number of seconds required to charge the capacitor to $\frac{2}{3}$ of V_{bat}.

2 | **Charging Capacitors**

2.1 | **Voltage over Time**

2.2 | **Charge Stored**

3 | **Time Constant with Various Components**

Most of the analysis for data collected as a class was done on the "charge rate constant" (`time/RC`) of each circuit, defined as:

$$\frac{t}{RC}$$

`time/RC` is a unitless scalar that represents how quickly it takes to charge any capacitor for a given voltage. Voltage data was not collected during the experiment, so the voltage is assumed to be constant across trials. If our model of capacitor charge rate is correct, we expect `time/RC` to be constant across trials. The actual data was skewed right:
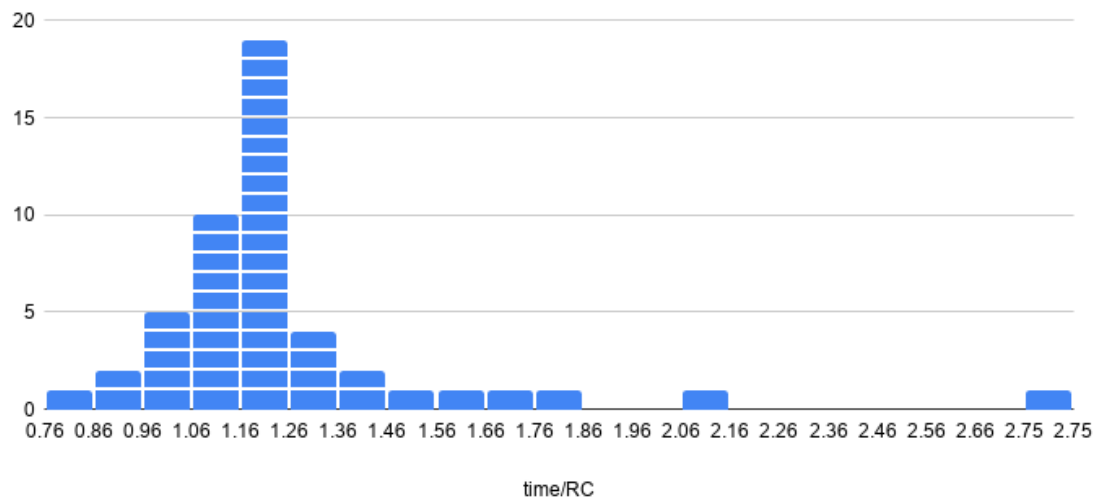
Histogram of time/RC

Figure 1: Histogram of time/RC

By comparing the `time/RC` and different properties of each circuit, reasoning for the outliers may be deduced. The visualization of the histogram is reflected in each of the following charts by the density of points in a column.

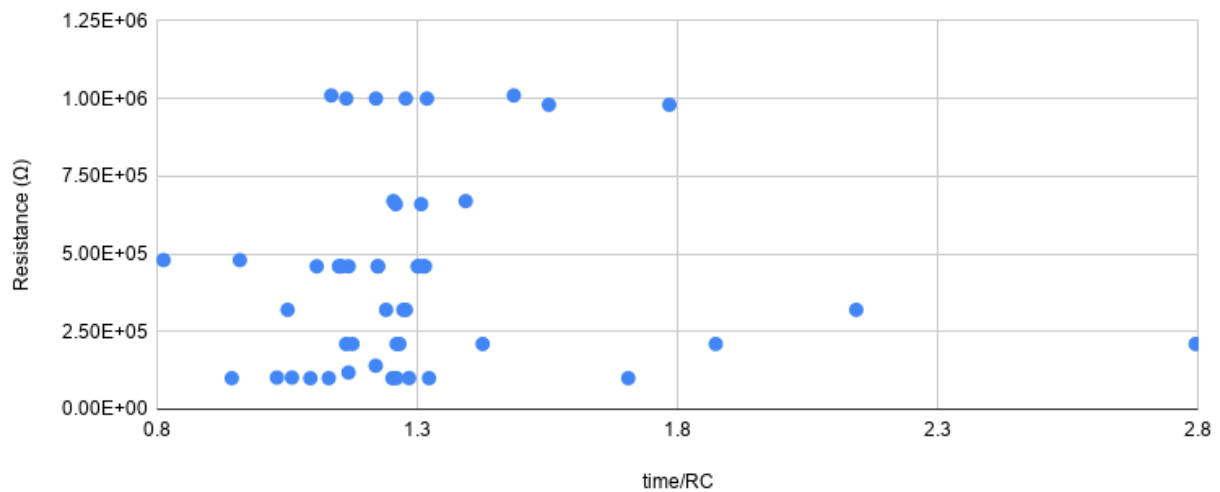First, the `time/RC` values were compared with the resistance of the circuit:

time/RC vs. R (Ω)

Figure 2: time/RC vs Resistance

Although some outliers came from circuits with high resistance, the most skewed ones came from those with least resistance. The same can be said of capacitance:
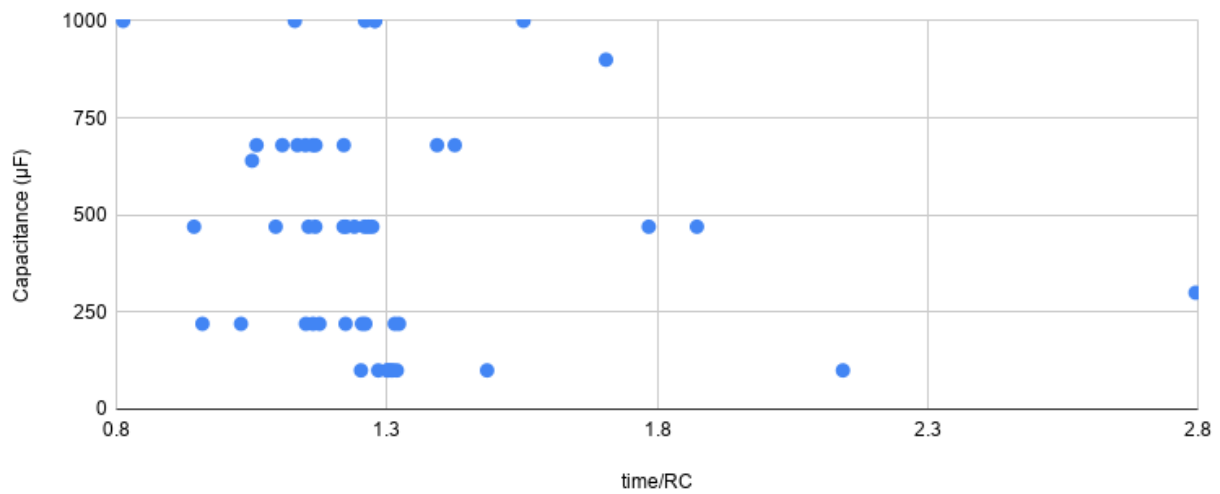
time/RC vs. C (µF)

Figure 3: time/RC vs Capacitance

Finally, the comparison with time taken to charge the capacitor shows the strongest correlation, which is to be expected because according to the model, this value is the product of the previous two trends.
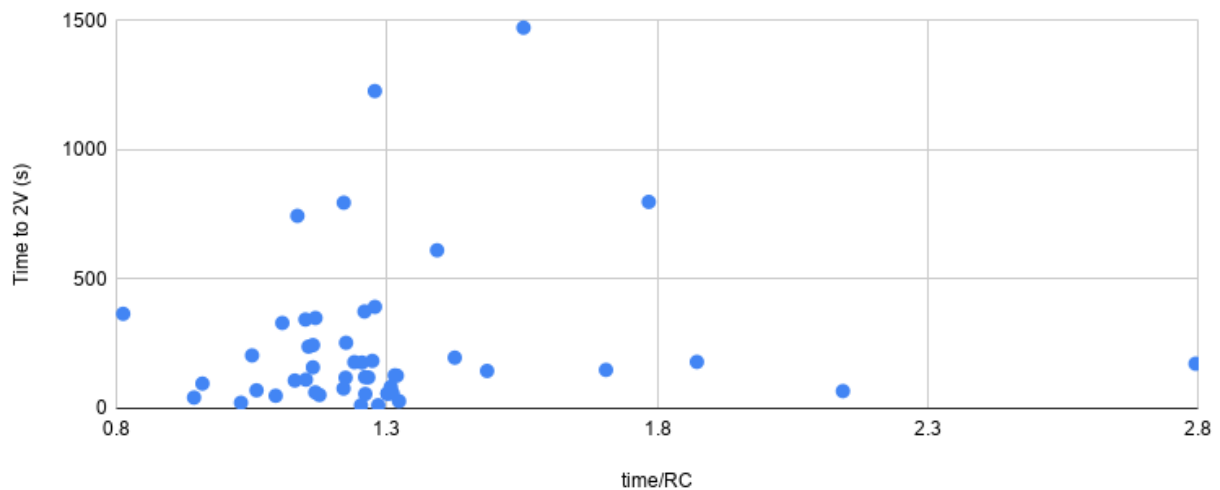
time/RC vs. Time to 2V (s)

Figure 4: time/RC vs Time to Charge

On explanation for the data skew is reaction time: for lower values of τ, the capacitor plateus faster