Source: |KBhMATH401Limits|

## 1 | Epsilon Delta Proofs

The secrets of the limit

## **Formal Definition of a Limit**

Definition 1 
$$\cdot$$
 Limit Definition  $\lim_{x \to a} f(x) = L$  for all  $\epsilon > 0$ , there exists a  $\delta$  such that  $if \ 0 < |x-a| < \delta$ ,  $then \ 0 < |f(x)-L| < \epsilon$ 

## **An Epsilon Delta Proof**

Let's prove  $\lim_{x\to 2} x^2 = 4$  together!

The crux of the proof is to come up with a value  $\delta$  that is a function of  $\epsilon$  assuming that  $0 < \epsilon$  that meets  $0 < |x - a| < \delta$ .

Oh, here's some symbols

Symbol	Definition
A	For all
∃	There ebsits
	Such that