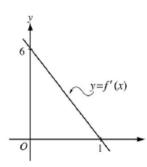
Calculus 2020-2021

Handout 20: Applications of FTC and Net Change Theorem

$$\int f'(x)dx = f(x), \frac{d}{dx} \int f(x)dx = f(x), \int_a^b f'(x)dx = f(b) - f(a)$$

A pizza, heated to a temperature of 350 degrees Fahrenheit (°F) is taken out of an oven and placed in a 75°F room at time t = 0 minutes. The temperature of the pizza is changing at a rate of $-110e^{-0.4t}$ degrees Fahrenheit per minute. To the nearest degree, what is the temperature of the pizza at time t = 5 minutes?

2.



The graph of f', the derivative of f, is the line shown in the figure above. If f(0) = 5, then f(1) =

3.

Let $f(x) = \int_{-2}^{x^2 - 3x} e^{t^2} dt$. At what value of x is f(x) a minimum?

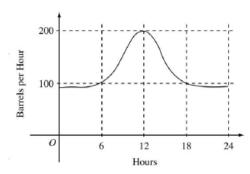
- (A) For no value of x (B) $\frac{1}{2}$ (C) $\frac{3}{2}$ (D) 2 (E) 3

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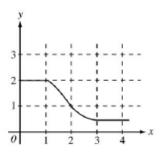
4.



The flow of oil, in barrels per hour, through a pipeline on July 9 is given by the graph shown above. Of the following, which best approximates the total number of barrels of oil that passed through the pipeline that day?

- (A) 500
- (B) 600
- (C) 2,400
- (D) 3,000
- (E) 4,800

5.



The graph of f is shown in the figure above. If $\int_1^3 f(x) dx = 2.3$ and F'(x) = f(x), then F(3) - F(0) =

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6.

The rate at which people enter an amusement park on a given day is modeled by the function E defined by

$$E(t) = \frac{15600}{\left(t^2 - 24t + 160\right)}.$$

The rate at which people leave the same amusement park on the same day is modeled by the function L defined by

$$L(t) = \frac{9890}{\left(t^2 - 38t + 370\right)}.$$

Both E(t) and L(t) are measured in people per hour, and time t is measured in hours after midnight. These functions are valid for $9 \le t \le 23$, the hours during which the park is open. At time t = 9 there are no people in the park.

- (a) How many people have entered the park by 5:00 P.M. (t=17)? Round answer to the nearest whole number.
- (c) Let $H(t) = \int_{9}^{t} (E(x) L(x)) dx$ for $9 \le t \le 23$. The value of H(17) to the nearest whole number is 3725. Find the value of H'(17) and explain the meaning of H(17) and H'(17) in the context of the park.