

Source:

1 | **new schedule today :/**

2 | **Systems of equations, matrix equations, and vectors**

2.1 | **How many solutions x satisfy $Ax = 0$?**

2.2 | **When the answer is "infinitely many" what tools might we have to describe the size of that set?**

2.3 | **How many possible outcomes b are there for the equation $Ax = b$ for any x .**

3 | **in class work! See `./KBe20math530srcNull_space_and_column_space_intro.pdf`**

3.1 | $A = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$

3.1.1 | **How many solutions x satisfy $Ax = 0$?**

The only solution is $x=0$, because $Ax = x$.

3.1.2 | **When the answer is "infinitely many" what tools might we have to describe the size of that set?**

N/A

3.1.3 | **How many possible outcomes b are there for the equation $Ax = b$ for any x .**

There can be infinitely many values of b ..?

3.2 | $A = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}$

3.2.1 | **How many solutions x satisfy $Ax = 0$?**

Infinitely many (anything of the form $\begin{pmatrix} 0 \\ 0 \\ x \end{pmatrix}$)

3.2.2 | **When the answer is "infinitely many" what tools might we have to describe the size of that set?**

A column in the matrix is zero? Maybe the columns are linearly dependent

3.2.3 | How many possible outcomes b are there for the equation $Ax = b$ for any x .

Infinite with dim 2?

$$3.3 \mid A = \begin{pmatrix} 1 & 0 \\ 0 & 1 \\ 0 & 0 \end{pmatrix}$$

3.3.1 | How many solutions x satisfy $Ax = 0$?

Only one value of x makes the product zero.

3.3.2 | When the answer is "infinitely many" what tools might we have to describe the size of that set?

n/a

3.3.3 | How many possible outcomes b are there for the equation $Ax = b$ for any x .

column vector has dimension 3, but the vector space has dim 2

$$3.4 \mid A = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

3.4.1 | How many solutions x satisfy $Ax = 0$?

infinite, same vectors as subproblem 2

3.4.2 | When the answer is "infinitely many" what tools might we have to describe the size of that set?

dimension 2? column vectors in the matrix are linearly dependent.

3.4.3 | How many possible outcomes b are there for the equation $Ax = b$ for any x .

infinite, dim 2 (but each vector is dim 3)

$$3.5 \mid A = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{pmatrix}$$

3.5.1 | How many solutions x satisfy $Ax = 0$?

infinite, vectors of the form $\begin{pmatrix} 0 \\ a \\ -a \end{pmatrix}$ (columns linearly dependent)

3.5.2 | **When the answer is "infinitely many" what tools might we have to describe the size of that set?**

dimension 2 subspace of \mathbb{F}^3

3.5.3 | **How many possible outcomes b are there for the equation $Ax = b$ for any x .**

infinite, dim2 subspace of \mathbb{F}^3

$$3.6 \mid A = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 3 \\ 0 & 0 & 0 \end{pmatrix}$$

3.6.1 | **How many solutions x satisfy $Ax = 0$?**

infinite, vectors of the form $\begin{pmatrix} a \\ b \\ 0 \end{pmatrix}$ (columns linearly dependent)

3.6.2 | **When the answer is "infinitely many" what tools might we have to describe the size of that set?**

dim 1 subspace of \mathbb{F}^3

3.6.3 | **How many possible outcomes b are there for the equation $Ax = b$ for any x .**

see previous