Source: [[KBe2020math530floIndex]]

#flo

1 | Polynomials

- See [[KBrefPolynomial]]

1.1 | 0 polynomial

- Has degree $-infty$
- Degrees are usually positive, except for the 0 degree
- "that's too hard, and we're not going to do it here"

1.2 | Identically zero

- Like 0 or $0x^0$
- Most polynomials are sometimes zero, but polynomials that are "identically zero" means that it's always zero (instead of just sometimes zero)

1.3 | $\mathcal{P}_m(F)$

- Polynomials with coefficients in F whose highest degree is m
- It can't be "whose degree is exactly m" because otherwise you won't have the identity and it won't be closed under addition (in the case where coefficient sum $a_m + b_m = 0$)

1.3.1 | It's a finite dimensional vector space

- $$a_0 z^0 + ... + a_m z^m + b_0 z^0 + ... + b_m z^m = (a_0 + b_0) z^0 + ... + (a_m + b_m) z^m$$

1.4 | Proof of 2.16

- Structure: proof by contradiction

2 | Linear Independence

- "non-trivial" means "simplest possible", which has usually got the most zeros
- See [[KB20math530refLinearIndependence]]

2.1 | 2.21 Linear Dependence Lemma 2.21

- it's saying that any linearly independent list has a vector inside that doesn't "contribute anything", and that if you remove it you'l have the same span. Implicitly, maybe through induction?) if you remove a dependent vector enough times then you get a linearly independent list.
- The list $(1, 1, 1), (2, 2, 2), (3, 3, 3)$ is really dependent, but $(0), (0), (0)$ is the most dependent (you have to remove all to get independence).

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3 | Exercise 2.A.1

3.1 | Lemma

If vectors v_1, v_2, v_3, v_4 span V, then the list

$$v_1 - v_2, v_2 - v_3, v_3 - v_4, v_4$$

also spans V.

3.2 | Proof

We prove the lemma by showing that any vector $v \in V$ can be written in the form $a_1v_1 + a_2v_2 + a_3 + v_3 + a_4v_4$ can also be written as a linear combination of the form

$$b_1(v_1 - v_2) + b_2(v_2 - v_3) + b_3(v_3 - v_4) + b_4v_4$$

If we set

$$\begin{aligned} b_1 &= a_1 \\ b_2 &= a_1 + a_2 \\ b_3 &= a_1 + a_2 + a_3 \\ b_4 &= a_1 + a_2 + a_3 + a_4 \end{aligned}$$

then the two combinations will be equivalent:

$$a_1(v_1 - v_2) + (a_1 + a_2)(v_2 - v_3) + (a_1 + a_2 + a_3)(v_3 - v_4) + (a_1 + a_2 + a_3 + a_4)v_4$$

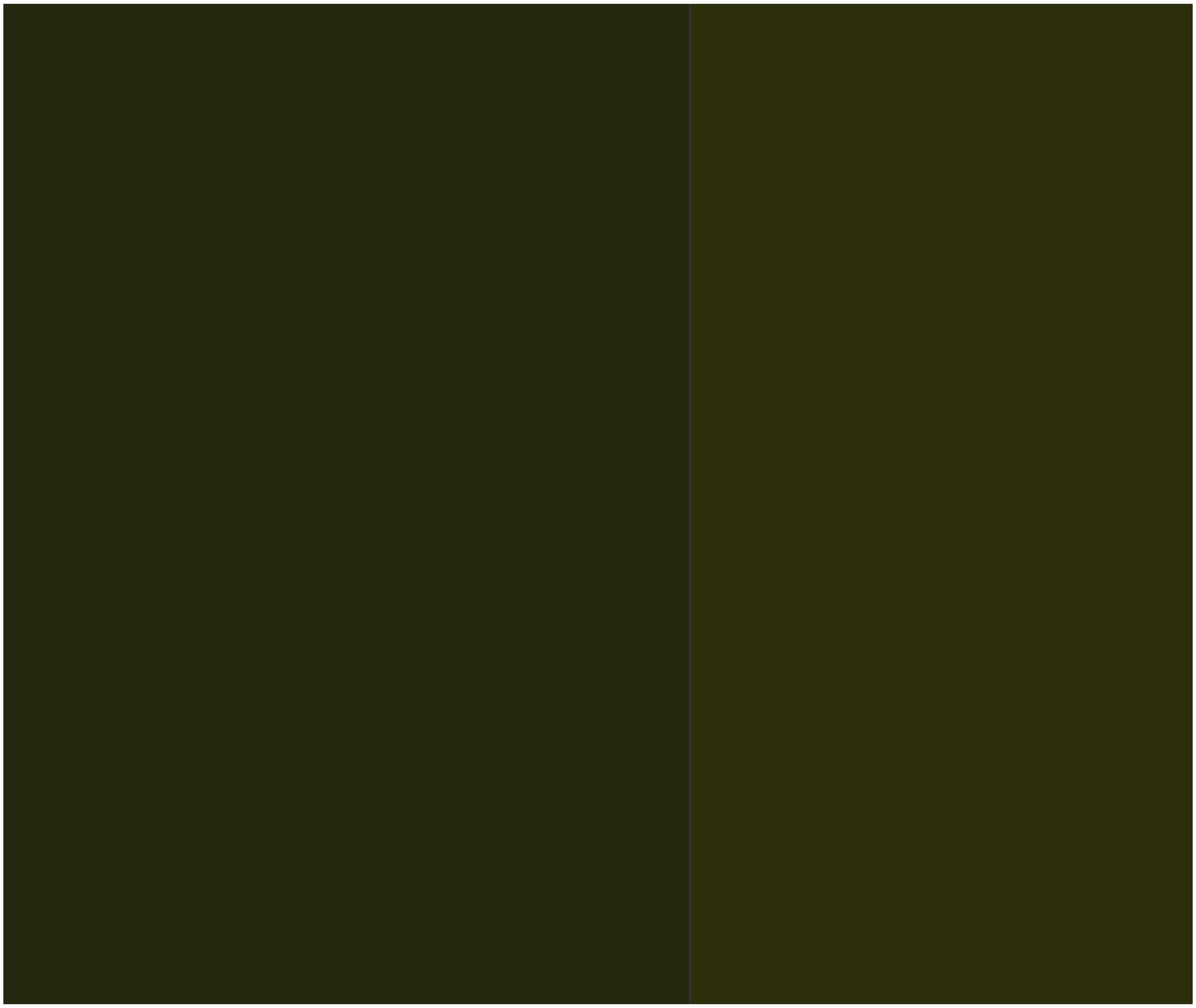
$$= a_1v_1 \cancel{- a_1v_2 + a_1v_2} + a_2v_2 \cancel{- (a_1 + a_2)v_3 + (a_1 + a_2)v_3} + a_3v_3 \cancel{- (a_1 + a_2 + a_3)v_4 + (a_1 + a_2 + a_3)v}$$

$= a_1v_1 + a_2v_2 + a_3v_3 + a_4v_4$

4 | Rock

And here's a rock for good measure:

Look at these colors!



```
BUILDNUMBER_FILE='buildID.txt'

while true; do
    printf "working...                                                   \r"
    echo "\n\n\nLog for attempt at $(date)" >> log.txt
    git pull >> log.txt

    changes="$(git status --porcelain | cut -c4-)"

    if [[ -n "$changes" ]]; then
        #find . -type f -name '*.md' -exec sed -i'' -e 's/\/Users\/houliu\/Documents\/School Work\/2020\-2021\/KnowledgeBase/./g' {} +

        ./compile.sh

        #if make >> log.txt 2>>recent_errors.txt; then
        #    [[ -f $BUILDNUMBER_FILE ]] || echo 0 > $BUILDNUMBER_FILE;
        #    echo $(( $(cat $BUILDNUMBER_FILE) + 1 )) > $BUILDNUMBER_FILE
        #fi
        [[ -f $BUILDNUMBER_FILE ]] || echo 0 > $BUILDNUMBER_FILE;
        echo $(( $(cat $BUILDNUMBER_FILE) + 1 )) > $BUILDNUMBER_FILE

        (git add -A >> log.txt && \
        git reset -- log.txt >> log.txt && \
        git commit -m "b$(cat buildID.txt): $(echo $changes | paste -sd ', ' -) $(printf "\n(\n")automated compilation $(cat buildID.txt))" >> log.txt && \
        git push --quiet) && \
        printf "Snapshotted and commited at $(date)\r" || printf "Sync Failed!!! $(date)"
    else
        printf "Nothing to sync at $(date)                    \r"
    fi

    sleep 30
done
```

Figure 1: ../MISC/IMG_1417.jpg