Source:

1 | Definition

#definition Axler3.2 Linear Map #aka linear transformation A *linear map* from V to W is a function $T:V\to W$ with the following properties:

1.1 | Additivity

$$T(u+v) = Tu + Tv \forall u, v \in V$$

1.2 | Homogenity

$$T(\lambda v) = \lambda(Tv) \forall \lambda \in \mathbb{F}, v \in V$$

2 | Other Notation

2.1 | Set of Maps

#definition Axler3.3 $\mathcal{L}(V, W)$

The set of all linear maps from V to W is denoted $\mathcal{L}(V, W)$.

3 | Examples

3.1 | zero (0)

Zero is a function $0: V \to W$ s.t. $0v = 0 \forall v \in V$. (It takes all vectors in V and maps them to the additive identity of W)

3.2 | identity (*I*)

The identity maps each from one vector space to itself (in the same vector space):

$$I \in \mathcal{L}(V, V), v \in V : Iv = v$$

3.3 | differentiation (D)

$$D \in \mathcal{L}(\mathcal{P}(\mathbb{R}), \mathcal{P}(\mathbb{R})) : Dp = p'$$

Basically stating that for two polynomials $a, b \in \mathcal{P}(\mathbb{R})$, a'+b'=(a+b)' and with a constant $\lambda \in \mathcal{R}$ $(\lambda a)'=\lambda a'$.

- 3.4 | integration
- 3.5 | multiplication by x^2
- 3.6 | backward shift

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