Source: [[KBe2020math530floIndex]]

#flo

1 | Polynomials

- See [[KBrefPolynomial]]

1.1 | 0 polynomial

- Has degree $-\infty$
- Degrees are usually positive, except for the 0 degree
- "that's too hard, and we're not going to do it here"

1.2 | Identically zero

- Like 0 or $0x^0$
- Most polynomials are sometimes zero, but polynomials that are "identically zero" means that it's always zero (instead of just sometimes zero)

1.3 | $\mathcal{P}_m(F)$

- Polynomials with coefficients in F whose highest degree is m
- It can't be "whose degree is exactly m" because otherwise you won't have the identity and it won't be closed under addition (in the case where coefficient sum $a_m + b_m = 0$)

1.3.1 | It's a finite dimensional vector space

- $$a_0z^0 + ... + a_mz^m + b_0z^0 + ... + b_mz^m = (a_0 + b_0)z^0 + ... + (a_m + b_m)z^m$$

1.4 | Proof of 2.16

- Structure: proof by contradiction

2 | Linear Independence

- "non-trivial" means "simplest possible", which has usually got the most zeros
- See [[KB20math530refLinearIndependence]]

2.1 | 2.21 Linear Dependence Lemma 2.21

- it's saying that any linearly independent list has a vector inside that doesn't "contribute anything", and that if you remove it you'l have the same span. Implicitly, maybe through induction?) if you remove a dependent vector enough times then you get a linearly independent list.
- The list $(1, 1, 1), (2, 2, 2), (3, 3, 3)$ is really dependent, but $(0), (0), (0)$ is the most dependent (you have to remove all to get independence).

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3 | **Exercise 2.A.1**

3.1 | **Lemma**

If vectors v_1, v_2, v_3, v_4 span V, then the list

$$v_1 - v_2, v_2 - v_3, v_3 - v_4, v_4$$

also spans V.

then the two combinations will be equivalent:

$$a_1(v_1 - v_2) + (a_1 + a_2)(v_2 - v_3) + (a_1 + a_2 + a_3)(v_3 - v_4) + (a_1 + a_2 + a_3 + a_4)v_4$$

$$= a_1v_1 \cancel{- a_1v_2 + a_1v_2} + a_2v_2 - \cancel{(a_1 + a_2)v_3 + (a_1 + a_2)v_3} + a_3v_3 - \cancel{(a_1 + a_2 + a_3)v_4 + (a_1 + a_2 + a_3)v}$$

$= a_1v_1 + a_2v_2 + a_3v_3 + a_4v_4$

4 | **Rock**

And here's a rock for good measure:

Figure 1: ferrero!

epppic LaTeX
