1 orthogonal def

Two vectors $u, v \in V$ are called *orthogonal* if $\langle u, v \rangle = 0$

2 | results

- 2.1 | orthogonal ~= perpendicular
- 2.2 | Axler 6.12 orthogonality and zero
- 2.2.1 **|0** is orthogonal to every vector in V
- $2.2.2 \mid$ 0 is the only vector in V that is orthogonal to itself
- 2.3 | Axler 6.13 Pythagorean Theorem

Suppose u and v are orthogonal vectors in V. Then

$$||u+v||^2 = ||u||^2 + ||v||^2$$

2.3.1 proof with more algebra written out

$$||u+v||^2 = \langle u+v, u+v \rangle$$

$$= \langle u, u+v \rangle + \langle v, u+v \rangle$$

$$= \langle u, u \rangle + \langle u, v \rangle + \langle v, u \rangle + \langle v, v \rangle$$

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