

**Source:**

## 1 | Definitions

### 1.1 | **DONE** group

A set and binary operation that satisfies Group Properties

- Closed
- Identity
- Inverse
- Associative

### 1.2 | **DONE** field

A set and two binary operations: the primary (addition) and secondary (multiplication) that "mostly" satisfies group properties for both operations, and are **commutative and distributive**. It must be a group under the primary operation and a group under the secondary operation except without a secondary inverse for the primary identity.

### 1.3 | **DONE** non-singular matrices

singular matrix: has no inverse. non-singular matrix: has an inverse aka determinant non zero

## 2 | Connections

### 2.1 | **DONE** connect direct sum and linear independence

the sum of two spaces is direct if their bases are linearly independent

### 2.2 | **TODO** matrices to represent complex numbers

## 3 | Computation

### 3.1 | **DONE** Find the determinant of matrices

$$\begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc$$

### 3.2 | **DONE** compute cross product

$$\begin{pmatrix} a \\ b \\ c \end{pmatrix} \times \begin{pmatrix} d \\ e \\ f \end{pmatrix} = \begin{vmatrix} i & j & k \\ a & b & c \\ d & e & f \end{vmatrix} = i \begin{vmatrix} b & c \\ e & f \end{vmatrix} + j \begin{vmatrix} c & a \\ f & d \end{vmatrix} + k \begin{vmatrix} a & b \\ d & e \end{vmatrix} = bf - ce, cd - fa, ae - bd$$

### 3.3 | **TODO Find equations of lines and planes using cross product and dot product**

## 4 | **Derivations**

### 4.1 | **TODO properties of the determinant**

#### 4.1.1 | **zero when matrix has no inverse (singular)**

#### 4.2 | **DONE inverse of a 2x2 matrix**

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} e & f \\ g & h \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$ae + bg = 1$$

$$ce + dg = 0$$

$$af + bh = 0$$

$$cf + dh = 1$$

Then you do some algebra to get

$$e = \frac{d}{ad - bc}$$

$$g = \frac{-c}{ad - bc}$$

$$f = \frac{-b}{ad - bc}$$

$$h = \frac{a}{ad - bc}$$

### 4.3 | **TODO rotation matrices**

Don't try to algebra it. Use polar coordinates and the angle sum trig identities:

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

## 5 | **review quizzes**

### 5.1 | **DONE first quiz**

#### 5.1.1 | **see "find equations of lines and planes using cross product and dot product"**

#### 5.1.2 | **rotation matrices**

#### 5.1.3 | **cross product**

### 5.2 | **DONE mini take home quiz**

no feedback

### 5.3 | **DONE linear independence quiz**

teacher gave no problems

### 5.4 | **DONE quick linear quiz (linear independence and bases)**

no feedback, I think that quiz was pretty solid..