

Source: [KBhMATH401Limits](#)

## 1 | The Limit Notation

### Single-Sided Limits

Definition 1 · **Right Single-Sided Limit**  $\lim_{x \rightarrow a^+} f(x)$   
"What is  $y$  approaching when  $x$  approaches  $a$  from the right (+)?"

Definition 2 · **Left Single-Sided Limit**  $\lim_{x \rightarrow a^-} f(x)$   
"What is  $y$  approaching when  $x$  approaches  $a$  from the left (-)?"

**Watch!** If both the left and right single-sided limit exists and is the same, the Double-Sided Limit exists.

### Double-sided Limits

Definition 3 · **Left Single-Sided Limit**  $\lim_{x \rightarrow a} f(x)$   
"What is  $y$  approaching when  $x$  approaches  $a$ ?" This exists only if  $\lim_{x \rightarrow a^-} f(x) = \lim_{x \rightarrow a^+} f(x)$

**Vocab!** When the Double-Sided Limit does not exist, it is called *DOES NOT EXIST!*. It is not! undefined