Source:

1 | cube root

1.1 | approximation

$$(1+x)^{\frac{1}{3}} \to \frac{1}{3}(1+x)^{\frac{-2}{3}}$$

at x = 0 is

$$\frac{1}{3}(1+0)^{...} = \frac{1}{3}$$

so the linear approximation is

$$y \approx m(x-0) + f(0) = \frac{1}{3}x + 1$$

1.2 | estimations

value	estimate
0.05	1.016666
-0.25	0.916666

These will be overestimates because the graph is concave down in this reigon.

2 | sin(x)

2.1 | approximation

$$y \approx \frac{d}{dx}\sin x\Big|_{0}(x-0) + \sin 0 = x$$

2.2 | estimates

estimate
-0.1
0.1

The first estimate will be an underestimate because $\sin x$ is concave up in that reigon. The opposite is true for the second estimate.

3 | unknown function (only some points known

3.1 | approximation

$$y \approx \frac{d}{dx}f(x)\Big|_c(x-c) + f(c)$$

 $y \approx 5(x-1) - 4$

3.2 | estimations

plugging in c = 1,

value	estimate
1.2	-3

This will be an underestimate because the second derivative is positive and the graph is thus concave up.

4 | cube error

4.1 | equation

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