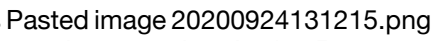


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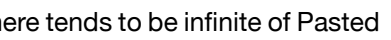
#flo

1 | Span

Smallest/largest containing subspaces

- Spans are not the largest vector space that contains the given vectors 
- The span of that vector is a line. It's a subspace. But it's not the biggest, because there's also \mathbb{R}^2

Spans tend to be infinite

- Usually a span has infinitely many vectors (unless you're in a weird field (modulo) or have the zero span)
- In the span of just one vector, you can multiply by any scalar which there tends to be infinite of 
- The span of that vector is a line. It's a subspace. But it's not the biggest, because there's also \mathbb{R}^2
- It only won't be infinite if your span is the span of $()$ (empty list)

Given a linearly independent set of vectors, would the span equal to the vector space?

- No? It's unclear which vector space is being referred to.

Span of vectors (example 2.6)

- When it's two vectors, you'd expect the span to be a 2d plane unless the vectors are parallel
 - In other words, if they are linear combinations or scalar multiples of one another
 - A linear combination on one other vector is the same as a scalar multiple
 - in 2space they have to not be colinear, in 3space they have to not be coplanar.
 - They have to be linearly independent
- That probably generalizes to higher and lower dimensions

Adding a vector doesn't make the span smaller

- Because you can just do what you had originally and make it's coefficient zero

Size of spans/subspaces

- You can't really just count the number of vectors, because say a line and a plane both have infinite points
- But we still want a plane to be larger than a line and a space to be larger than a plane
- So one way we compare is to say A is larger than B if B is strictly contained within A
- something like "dimensionality", maybe the minimum number of vectors needed for their span to be equal to the space

2 | 2.7 Span is the smallest containing subspace

- First the proof shows that the span is a subspace
- Then, because the span only needs to contain each vector and be a subspace, any subspace containing those vectors will at least contain the span.

3 | Linear Dependence

- When one of the vectors provides no “new information” aka can be constructed by a linear combination of vectors you already had
 - It’s a property of a set of vectors, not just one vector. A single vector is always linearly independent on its own, because there’s nothing else to depend on.
 - The span of the zero vector (0) is linearly dependent on itself, and you already don’t really get anything. So we usually talk about it as a span of no vectors (\emptyset)
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