Source: [KBhMATH401SubIndex]

1 | Derivatives

=> Instantaneous rate of change at a particular point

• Average rate of change = $\frac{\Delta Y}{\Delta X}$

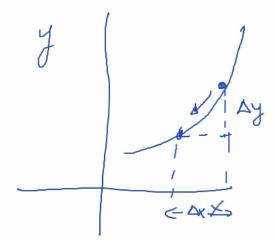


Figure 1: rateofchange.png

• Instantaneous rate of change = $\lim_{\Delta x \to 0} \frac{\Delta Y}{\Delta X}$

Derivative of $f(x) \Rightarrow \frac{dy}{dx}$

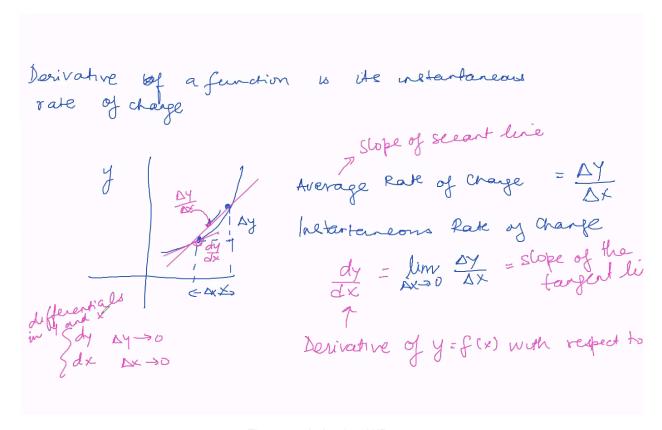


Figure 2: derivativesWB.png

1.1 | Useful Table of Derivatives

| f(x) | f'(x) |
|------------------|-----------------------|
| $\overline{x^2}$ | 2x |
| x^3 | $3x^2$ |
| x^n | nx^{n-1} |
| $\frac{1}{x}$ | $\frac{-1}{x^2}$ |
| \sqrt{x} | $\frac{1}{2\sqrt{x}}$ |
| $\sin(x)$ | $\cos(x)$ |
| $\cos(x)$ | $-\sin(x)$ |
| tan(x) | $1 + \tan^2(x)$ |
| $\cot(x)$ | $-\csc^2(x)$ |
| sec(x) | $\tan(x)\sec(x)$ |
| $\csc(x)$ | $-\cot(x)\csc(x)$ |
| e^x | e^x |
| ln(x) | $\frac{1}{x}$ |
| a^x | $a^x ln(a)$ |
| $log_a(x)$ | $\frac{1}{xln(a)}$ |

| f(x) | f'(x) |
|---------------|---------------------------|
| $f^{-}1(x)$ | $\frac{1}{f'(f^-1(x))}$ |
| $sin^-1(x)$ | $\frac{1}{\sqrt{1-x^2}}$ |
| $\cos^- 1(x)$ | $\frac{-1}{\sqrt{1-x^2}}$ |
| $tan^-1(x)$ | $\frac{1}{1+x^2}$ |