

## 1 | Slicing into Rectangles

The general idea of Riemann sums is to slice a curve into vertical non-overlapping rectangles to approximate the area between the curve and the x-axis. This can be expressed mathematically as a summation given the function  $f(x)$ , the range  $[a, b]$ , and the number of rectangles  $n$ :

$$\sum_{k=1}^n \frac{b-a}{n} f\left(a + k \frac{b-a}{n}\right)$$

This can be written more concisely by defining  $\Delta x = \frac{b-a}{n}$  and  $x_i = a + k\Delta x$ :

$$\sum_{k=1}^n \Delta x f(x_i)$$

These estimates all have the right endpoint of the rectangle touching the curve. You could also use the left endpoint, or use the minimum value one and add a triangle to form a trapezoid.

## 2 | Area Interpretation

## 3 | Upper and Lower Bound

## 4 | the Definite Integral