#### Source:

#### 1 | Broader vector spaces

- · Doesn't have to be physics vectors
- · maybe it's like matrices
- · or linear maps themselves

### 2 | The Linear Map 0

A linear map S = 0 is a map where  $Su = 0 \forall u$ .

## 3 | Axler 3.A ex7

Let w = Tv.

3.1 | If v = 0 then

$$Tv = 0$$

By Axler 3.11 (Maps take 0 to 0). Thus,  $\lambda$  can be anything in  $\mathbb{F}$ .

#### 3.2 | Otherwise,

 $\frac{1}{n} \in \mathbb{F}$  because the field has multiplicative inverses for all elements except 0.

$$Tv = w = \left(w\frac{1}{v}\right)v$$

Let  $\lambda = w \frac{1}{v}$ , then

$$\lambda v = w \frac{1}{v} v = w$$

which is in  $\mathbb{F}$  because  $w, \frac{1}{v} \in \mathbb{F}$  and fields are closed under multiplication.

# 4 | Axler 3.A ex10

The additivity of a linear map T requires T(u+v)=Tu+Tv. Because  $U\subset V, U\neq V$ , there must be some element  $v\in V$  yet  $v\notin U$ .

For some element  $u \in U$ ,

$$Tu + Tv = Su + 0 = Su$$

Yet  $u + v \notin U$  because if it were, then v would be in U.

$$T(u+v) = 0$$

Exr0n · 2020-2021