

1 | Problem

Suppose V is a real inner product space and v_1, \dots, v_m is a linearly independent list of vectors in V . Prove that there exist exactly 2^m orthonormal lists e_1, \dots, e_m of vectors in V that preserve the prefix spans.

2 | Proof Sketch

In general, during the Gram-Schmidt procedure, both e_j or $-e_j$ at each step