## 1 | Export

https://www.overleaf.com/project/606b2fa8be363f9005d8ce03

## 2 | Exercise 7

Suppose  $T \in \mathcal{L}(V)$  has a diagonal matrix A with respect to some basis of V and that  $\lambda \in \mathbb{F}$ . Prove that  $\lambda$  appears on the diagonal of A precisely dim  $E(\lambda, T)$  times.

## 3 | **Proof**

We will show that for each eigenvalue  $\lambda$ , there are at least  $E(\lambda,T)$  occurrences of that eigenvalue and at most  $E(\lambda,T)$  occurrences.

Suppose  $\lambda$  appears on the diagonal m times.

Suppose again that  $\lambda$  is on the diagonal m times. Each of those occurrences corresponds to where the diagonal matrix sends a (linearly independent) basis eigenvector, which implies that the basis of V has at least m eigenvectors corresponding to  $\lambda$ . These m eigenvectors can be extended to a basis of  $E(\lambda,T)$ , implying that  $\dim E(\lambda,T) \geq m$ .

3.1 | TODO Suppose  $\lambda$  is on the diagonal m times. show that there are at most dim E(;I, T) occurances on the diagonal