Axler 6.A exercise 9 April 27, 2021

1 | Axler 6.A exercise 9

Suppose $u,v\in V$ and $\|u\|\leq 1$ and $\|v\|\leq 1$. Prove that

$$\sqrt{1 - \|u\|^2} \sqrt{1 - \|u\|^2} \le 1 - |\langle u, v \rangle|$$

2 | **Proof**

We will prove this by showing that the left hand side is less than or equal to an intermediate term, which is less than or equal to the right hand side.

$$\begin{aligned} |\langle u, v \rangle| &\leq ||u|| ||v|| \\ \Longrightarrow 1 - |\langle u, v \rangle| &\geq 1 - ||u|| ||v|| \end{aligned}$$

Now, the proble

Taproot · 2020-2021 Page 1 of 1