I chose to use Reigon B (bounded by x=0, y=sqrt(x), and x=9) and the semicircle as my cross section. The integral to calculate the volume is the integral of the area of each slice.

$$\int_0^9 \pi r_x^2 dx$$

$$= \int_0^9 \pi \left(\frac{\sqrt{x}}{2}\right)^2 dx$$

$$= \frac{\pi}{4} \int_0^9 x dx$$

$$= \frac{\pi}{8} g^2$$

$$= \boxed{\frac{81\pi}{8}}$$

This value is corroborated to four decimal points using the slice generator, seen here: