1 | orthogonal decomposition

An orthogonal decomposition is a way of writing some vector $v \neq 0 \in V$ as the scaled other vector $u \in V$ plus an orthogonal component

Suppose $u, v \in V$, with $v \neq 0$. Set $c = \frac{\langle u,v \rangle}{\|v\|^2}$ and $w = u - cv$. Then,

$$\langle w, v \rangle = 0 \text{ and } u = cv + w$$

The important algebra is just setting up a system of equations and noticing that orthogonality implies

$$0 =$$