#### Source:

# 1 | Definition

#definition Axler3.2 Linear Map #aka linear transformation A *linear map* from V to W is a function  $T:V\to W$  with the following properties:

### 1.1 | Additivity

$$T(u+v) = Tu + Tv \forall u, v \in V$$

### 1.2 | Homogenity

$$T(\lambda v) = \lambda(Tv) \forall \lambda \in \mathbb{F}, v \in V$$

# 2 | Other Notation

### 2.1 | Set of Maps

#definition Axler3.3  $\mathcal{L}(V, W)$ 

The set of all linear maps from V to W is denoted  $\mathcal{L}(V, W)$ .

# 3 | Examples

## 3.1 | **zero (**0**)**

Zero is a function  $0:V\to W$  s.t.  $0v=0 \forall v\in V$ . (It takes all vectors in V and maps them to the additive identity of W)

# 3.2 | identity (*I*)

The identity maps each from one vector space to itself (in the same vector space):

$$I \in \mathcal{L}(V,V), v \in V: Iv = v$$

# 3.3 | differentiation (D)

$$D \in \mathcal{L}(\mathcal{P}(\mathbb{R}), \mathcal{P}(\mathbb{R})) : Dp = p'$$

Basically stating that for two polynomials  $a, b \in \mathcal{P}(\mathbb{R})$ , a'+b'=(a+b)' and with a constant  $\lambda \in \mathcal{R}$   $(\lambda a)'=\lambda a'$ .

# 3.4 | integration (T)

Exr0n · **2020-2021** Page 1