1 | cooling pizza

Compute

$$\int_0^5 -110e^{-0.4t}dt$$

to the nearest degree.

$$\int -110e^{-0.4t}dt = \frac{-110}{-0.4}e^{-0.4t} = 275e^{-0.4t}$$

Using the net change theorem,

$$\begin{aligned}
\Delta\beta \int_0^5 -110e^{-0.4t}dt &= \int -110e^{-0.4(5)}dt & -\int -110e^{-0.4(0)}dt \\
&= 275e^{-0.4(5)} & -275e^0 \\
&= 37.21720289 & -275 \\
&= 37.21720289 & -275 \\
&= 350 - 237.78279711 & \approx \boxed{112°F}
\end{aligned}$$

2 | definite integral as area under a curve

The area in the triangle is 3 square units, so $5 + 3 = \boxed{8}$

3 | minimum value of $f(x) = \int_{-2}^{x^2-3x} e^{t^2}dt$

$$\begin{aligned}
\frac{d}{dx}f(x) =& e^{(x^2-3x)^2}(2x-3) = 0 \\
&\implies 2x - 3 = 0 \\
&\implies 2x = 3 \\
&\implies \boxed{x = \frac{3}{2}}
\end{aligned}$$

4 | approximate area under the curve graphically

The function looks symmetric about $x = 12$, so I will focus on $[0, 12]$.
On the interval $[0, 6)$ a little under $6 \cdot 100$ barrels of oil flow through.
On the interval $[6, 12)$ a little over $6 \cdot 100 + \frac{1}{2}6 \cdot 100$ barrels flow through, for a total of

$$\approx 2(6 \cdot 100 + 6 \cdot 100 + \frac{1}{2}6 \cdot 100) = 3000$$

barrels of oil.

$\boxed{\text{D}}$

5 | fundamental theorem of calculus but worded confusingly

$F(x)$ is the antiderivative of $f(x)$, so differences of its values are definite integrals. In this case,

$$F(3) - F(0) = \int_0^3 f(x)dx = \int_0^1 f(x)dx + \int_1^3 f(x)dx = 2 + 2.3 = \boxed{4.3}$$

6 | TODO amusement park word problem

$$E(t) = \frac{15600}{t^2 - 24t + 160}$$
$$L(t) = \frac{9890}{t^2 - 38t + 370}$$

valid over the domain $[9, 23]$, and there are zero people in the park at $t = 9$.

6.1 | number of people who have entered the park by some time

$$\int_9^x E(t)dt = \int_9^x \frac{15600}{t^2 - 24t + 160}dx$$
$$= 15600 \ln(t^2 - 24t + 160)(2t - 24)?????$$

I don't know how to integrate this symbolically, and WolframAlpha says it contains an inverse tangent. Thus, I will use a calculator:

$$\int_9^{15} \frac{15600}{t^2 - 24t + 160}dt = 5019.3$$