Source:

1 | find taylor series

1.1
$$|y = \cos(x)|$$

$$P_n(x) = f(0) + \frac{d}{dx}f(0)x + \frac{\frac{d^2}{d^2x}f(0)}{2!}x^2 + \frac{\frac{d^3}{d^3x}f(0)}{3!}x^3 + \cdots$$

$$= \cos(0) - \sin(0)x + \frac{-\cos(0)}{2!}x^2 + \frac{\sin(0)}{3!}x^3 + \cdots$$

$$= 1 -0x - \frac{1}{2!}x^2 + \frac{0}{3!}x^3 + \cdots$$

$$= 1 - \frac{1}{2!}x^2 + \frac{1}{4!}x^4 + \cdots$$

$$= \sum_{k=0}^{\infty} \frac{(-1)^k}{(2k)!}x^{2k}$$

1.2 |
$$y = e^x$$

$$P_n(x) = f(0) + \frac{d}{dx}f(0)x + \frac{\frac{d^2}{d^2x}f(0)}{2!}x^2 + \frac{\frac{d^3}{d^3x}f(0)}{3!}x^3 + \cdots$$

$$= e^0 + e^0x + \frac{e^0}{2!}x^2 + \frac{e^0}{3!}x^3 + \cdots$$

$$= 1 + x + \frac{1}{2!}x^2 + \frac{1}{3!}x^3 + \cdots$$

$$= \sum_{l=0}^{\infty} \frac{1}{k!}x^k$$

1.3 **| TODO**
$$y = \sqrt{x}$$

2 | prove approximations

2.1
$$\left| \frac{1}{1-x} \right| = 1 + x + x^2 + x^3 + \cdots$$

Proof by geometric series

$$2.2 \mid \frac{1}{1+x} = 1 - x + x^2 - x^3 + \cdots$$

Plug -x for x in the previous equation.

2.3
$$\left| \frac{1}{1+x^2} \right| = 1 - x^2 + x^4 - x^6 + \cdots$$

Plug x^2 for x in the previous equation.

3 | more finding of polynomial

$$3.1 \mid TODO \$ y = In (1+x)\$$$

3.2 | **TODO**
$$y = \tan^- x$$

3.3 | **DONE**
$$y = (1+x)^k$$

$$P_n(x) = f(0) + \frac{d}{dx}f(0)x + \frac{\frac{d^2}{d^2x}f(0)}{2!}x^2 + \frac{\frac{d^3}{d^3x}f(0)}{3!}x^3 + \cdots$$

$$= k(1)^k + k(k-1)(1)^{k-1}x + \frac{k(k-1)(k-2)(1)^{k-2}}{2!}x^2 + \frac{k(k-1)(k-2)(k-3)(1)^{k-3}}{3!}x^3 + \cdots$$

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