Integration By Parts April 20, 2021

 $1 \mid \int \ln x dx$

$$\int \ln x dx = \int 1 \ln x dx$$

$$= x \ln x - \int x \frac{1}{x} dx$$

$$= x \ln x - \int 1 dx$$

$$= x \ln x - \int 1 dx$$

 $2 \mid \int \tan^- x dx$

$$\int \tan^{-} x dx = x \tan^{-} x - \int x \frac{1}{x^{2} + 1} dx$$

$$= x \tan^{-} x - \frac{1}{2} \int \frac{du}{u}$$

$$= x \tan^{-} x \frac{1}{2} \ln u + C \qquad = x \tan^{-} x \frac{1}{2} \ln(x^{2} + 1) + C$$

 $3 \mid \int x \sec^2 x dx$

$$\int x \sec^2 x dx = x \tan x - \int \tan x dx$$
$$= x \tan x + \ln|\cos x| + C$$

 $4 \mid \int x^2 e^{5x} dx$

$$\begin{split} \int x^2 e^{5x} dx &= x^2 \frac{1}{5} e^{5x} - \int 2x \frac{1}{5} e^{5x} dx \\ &= x^2 \frac{1}{5} e^{5x} - 2x \frac{1}{25} e^{5x} + \int 2 \frac{1}{25} e^{5x} dx \\ &= \frac{1}{5} e^{5x} (x^2 - \frac{2}{5} x + \frac{2}{25}) + C \end{split}$$

 $5 \mid \int x^2 \cos x dx = f(x) - \int 2x \sin x dx$

 $\mathsf{Find}\; f(x)$

$$f(x) = x^2 \sin x$$

 $6 \mid \int x \cos x dx$

$$\int x \cos x dx = x \sin x - \int \sin x dx$$
$$= x \sin x + \cos x + C$$

Taproot · 2020-2021 Page 1 of 2

Integration By Parts April 20, 2021

$$7 \mid \int x^2 \sin x dx$$

$$\int x^2 \sin x dx = -x \cos x - \int -\cos x dx$$
$$= -x \cos x - \sin x dx$$

Taproot · 2020-2021 Page 2 of 2