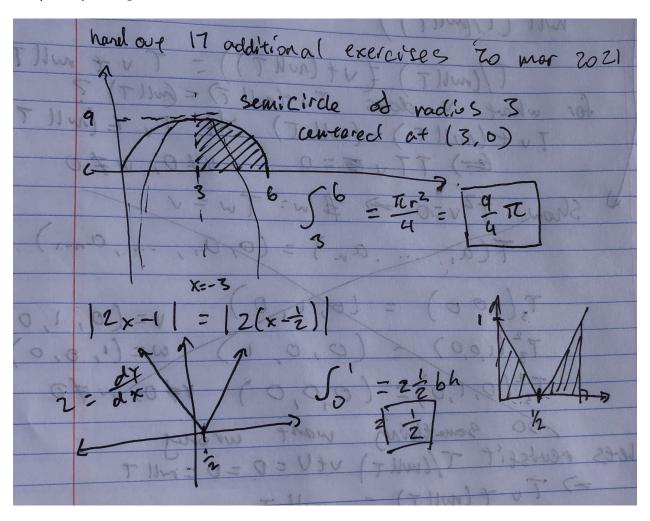
## 1 | Exercises

## 1.1 | interpreting in terms of area



## 1.3 | subtracting integrals

I expect

$$\int_{1}^{2} f(x)dx = \int_{1}^{5} f(x)dx - \int_{2}^{5} f(x)dx = -3 - 4 = -7$$

In fact, I expect

$$\int_{a}^{b} f(x)dx + \int_{b}^{c} f(x)dx = \int_{a}^{c} f(x)dx$$

1.4 | show 
$$\int_a^b x^2 dx = \frac{b^3 - a^3}{3}$$

(see attached pages)

Exr0n · 2020-2021 Page 1 of 3

Keep in mind

$$\sum_{k=1}^{n} af(x) = a \sum_{k=1}^{n} f(x)$$
$$\sum_{k=1}^{n} (a + f(x)) = an + \sum_{k=1}^{n} f(x)$$

$$\sum_{k=1}^{n} (a + f(x)) = an + \sum_{k=1}^{n} f(x)$$

Exr0n · 2020-2021 Page 2 of 3

$$\begin{split} \int_{a}^{b} x^{2} dx &= \lim_{n \to \infty} \sum_{k=1}^{n} \left( \frac{b-a}{n} \left( a + k \frac{b-a}{n} \right)^{2} \right) \\ &= \lim_{n \to \infty} \frac{b-a}{n} \sum_{k=1}^{n} \left( a + k \frac{b-a}{n} \right)^{2} \\ &= \lim_{n \to \infty} \frac{b-a}{n} \sum_{k=1}^{n} \left( a^{2} + \left( k \frac{b-a}{n} \right)^{2} + 2ak \frac{b-a}{n} \right) \\ &= \lim_{n \to \infty} \frac{b-a}{n} \sum_{k=1}^{n} a^{2} + \sum_{k=1}^{n} \left( k \frac{b-a}{n} \right)^{2} + \sum_{k=1}^{n} 2ak \frac{b-a}{n} \\ &= \lim_{n \to \infty} \frac{b-a}{n} \left( a^{2}n + \sum_{k=1}^{n} k^{2} \left( \frac{b-a}{n} \right)^{2} + 2a \frac{b-a}{n} \sum_{k=1}^{n} k \right) \\ &= \lim_{n \to \infty} \frac{b-a}{n} \left( a^{2}n + \left( \frac{b-a}{n} \right)^{2} \sum_{k=1}^{n} k^{2} + 2a \frac{b-a}{n} \sum_{k=1}^{n} k \right) \\ &= \lim_{n \to \infty} \frac{b-a}{n} \left( a^{2}n + \left( \frac{b-a}{n} \right)^{2} \frac{n(n+1)(2n+1)}{6} + 2a \frac{b-a}{n} \frac{n(n+1)}{2} \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \left( \frac{b-a}{n} \right)^{2} \frac{(n+1)(2n+1)}{6} + 2a \frac{b-a}{n} \frac{n(n+1)}{2} \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \left( \frac{b-a}{n} \right)^{2} \left( n \frac{(2n+1)}{6} + \frac{(2n+1)}{6} \right) + ak \frac{b-a}{n} (n+1) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{n^{2}} \left( n \frac{(2n+1)}{6} + \frac{(2n+1)}{6} \right) + ak \frac{b-a}{n} (n+1) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{n^{2}} \left( n \frac{(2n+1)}{6} + \frac{(2n+1)}{6} \right) + a(b-a) + a \frac{b-a}{n} \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{n^{2}} \left( n \frac{(2n+1)}{6} + a(b-a) \right) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{n^{2}} \left( n \frac{(2n+1)}{6} + a(b-a) \right) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{n^{2}} \left( n \frac{(2n+1)}{6} + a(b-a) \right) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{3} \left( 2(n+1) + a(b-a) \right) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{3} \left( 2(n+1) + a(b-a) \right) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{3} \left( 2(n+1) + a(b-a) \right) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{3} \left( 2(n+1) + a(b-a) \right) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{3} \left( 2(n+1) + a(b-a) \right) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{3} \left( 2(n+1) + a(b-a) \right) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{3} \left( 2(n+1) + a(b-a) \right) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{3} \left( 2(n+1) + a(b-a) \right) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a^{2} + \frac{(b-a)^{2}}{3} \left( 2(n+1) + a(b-a) \right) \right) \\ &= \lim_{n \to \infty} (b-a) \left( a$$

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Exr0n · 2020-2021 Page 3 of 3

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