#### Source:

# 1 | eigenvalues

eigenvalue: multiplied by a scalar? a subspace that, when put through a linear map, only gets scaled.

$$Tv = \lambda v$$

Where  $v \neq 0$ . (we ignore it because its no fun to send zero to zero, and bc the span is empty).

**T must be an operator!** Otherwise the matrix sizes don't work out when subtracting  $\lambda I$ .

where v is the eigenvector and  $\lambda$  is the eigenvalue. The equation is often rewritten as:

$$Tv - \lambda v = 0Tv - \lambda Iv = 0(T - \lambda I)v = 0$$

now this can be factored and roots can be found. also it's an operator.

#### 1.1 | Axler 5.6 equivalent conditions

Only when V is finite dimensional!

1.1.1  $|T - \lambda I|$  is not injective, because both v, 0 are in the null space.

1.1.2  $|T - \lambda I|$  is also not surjective or invertible bc finite dim operator.

## 2 | an example

Given the matrix  $\begin{pmatrix} 3 & 1 \\ 0 & 2 \end{pmatrix}$ , find the eigenvalues and eigenvectors.

Now that we have that other formulation, we can just subtract  $\lambda I$  from T to get

$$\begin{pmatrix} 3 - \lambda & 1 \\ 0 & 2 - lambda \end{pmatrix}$$

Then, we just need to find whether it is non-invertible aka singular aka determinant.

# 3 | depends on

## 3.1 | finding roots is helpful

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