

Please sketch the graph of the functions in each problem.

1. Suppose a company produces a circular plate to repair the skull after brain surgery. The area of such a plate must be 16π square millimeters.
 - a. What is the necessary radius for the plate? (recall the area of a circle)

$$4$$

- b. Suppose the plate still works with an error in area of 0.04π square millimeters. What is the maximum error in radius that will guarantee the area is in error of at most 0.04π square millimeters? (Round to nearest 6th decimal place)

$$\begin{aligned}
 & y = \sqrt{\frac{x}{\pi}} \\
 & |x - 8| < 1 \\
 & \sqrt{\frac{x+8}{\pi}} \\
 & \sqrt{\frac{16.04\pi}{\pi}} = \sqrt{16.04} \approx 4.004997 \\
 & \quad \quad \quad 3.994997 \\
 & \text{+error} = 0.004997 \\
 & \text{-error} = 0.005003
 \end{aligned}$$

2. Suppose we need to manufacture a ball bearing of volume 36π cubic inches (recall: the volume of a sphere is $V = (4/3)\pi r^3$). Note that the volume of the ball is a function of radius. If the volume of our ball bearing can be in error at most 0.4π , what is the maximum permissible error in radius?

$$\begin{aligned}
 & V = \frac{4}{3}\pi r^3 \\
 & \quad \quad \quad 36.4\pi \\
 & r = \sqrt[3]{\frac{3}{4} \cdot 35.6} \approx 0.01115
 \end{aligned}$$

3. Suppose a toilet paper company needs to make hollow cylinders (that is, without a top or bottom) with surface area 12π square centimeters. Suppose the radius must remain a constant 3 square centimeters but the surface area of the cylinder can be of error at most 0.2π square centimeters. What is the maximum permissible error in height?

$$\begin{aligned}
 & A = C * L = 2\pi r * L \\
 & 6\pi L = 12.2\pi \\
 & L = 0.0333
 \end{aligned}$$