1 | Axler6.53 orthogonal projection, P_U def

Suppose U is a finite-dimensional subspace of V. The *orthogonal projection* of V onto U is the operator $P_U \in \mathcal{L}(V)$ defined as follows:
For $v \in V$, write $v = u + w$, where $u \in U$ and $w \in U^{\perp}$. Then $P_U v = u$.

In other words, $P_U \in \mathcal{L}(V)$ takes v to the component of v that is in U.

1.1 | Results

1.1.1 | Axler6.54 calculating $P_U v$

$$P_U v = \frac{\langle v, x \rangle}{\|x\|^2} x$$

Because orthogonal decompositions and stuff

1.1.2 | Axler6.55 properties

Suppose U is a finite-dimensional subspace of V and $v \in V$. Then,

1. $P_U \in \mathcal{L}(V)$