Source: [KBe2020math530floIndex]

## 1 | #exercise 2.A.17

- All polynomials have (x+2) as a factor, and therefore can be written in the form  $(x+2)f_j(x)$  where  $f_j(x)$  has degree at most m-1.
- Because the  $z^0, z^1, ..., z^{m-1}$  is a spanning list of  $P_m 1(F)$ , the spanning list of  $P_{m-1}(F)$  is of length m.
- The original list had m+1 elements, so by Axler 2.23 the list cannot be linearly independent.
- We can therefore find a non-trivial combination that equals zero, and can thus find a non-trivial combination of the original list by multiplying each vector by (x-2).

## 2 | Elementary Matrices

#incomplete

## 2.1 | Things you can do

- · Multiply a row by a nonzero scalar
- · Add two rows

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