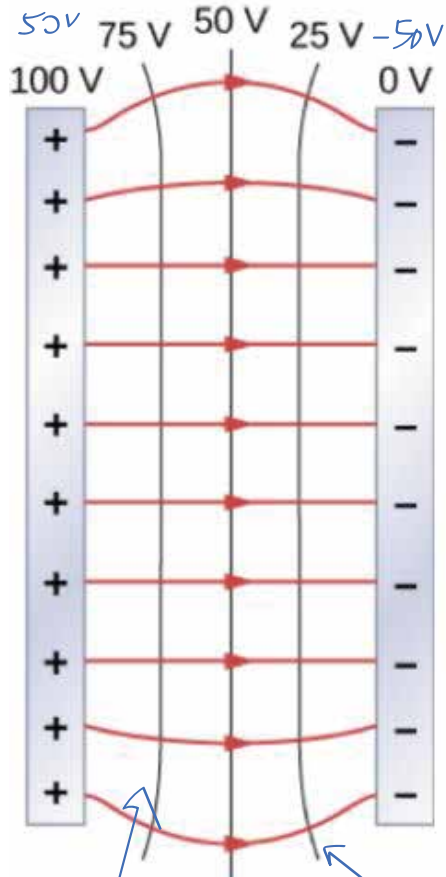


one plate
0V

Relationship Between Voltage and Electric Field



You can easily show that the units of electric field can be written as N/C (Newtons per Coulomb) or V/m (volts per meter).

$$V = \frac{J}{C} = \frac{Nm}{C}$$

$$\frac{V}{m} = \frac{J}{m \cdot C} = \frac{Nm}{C \cdot m} = \frac{N}{C}$$

If \mathbf{E} is uniform between two points along an \mathbf{E} field line:

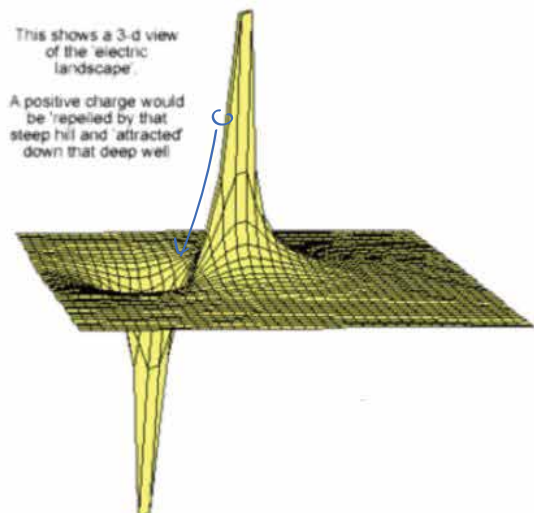
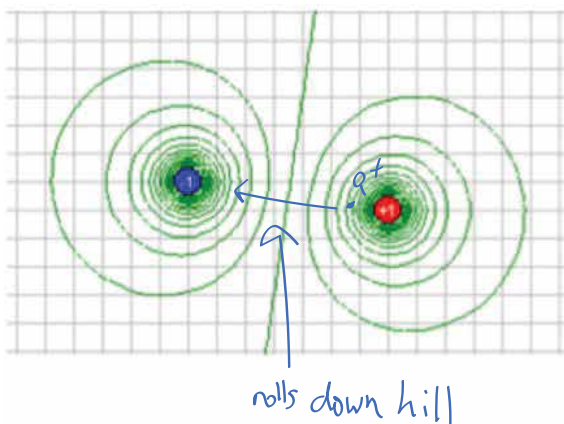
$$\Delta KE = q \vec{E} \cdot \vec{d}$$

$$= \vec{F} \cdot \vec{d} = \Delta PE$$

You have probably seen this before as: Change in potential energy equals force multiplied by distance, if force is constant, and distance is measured in the direction of the force.

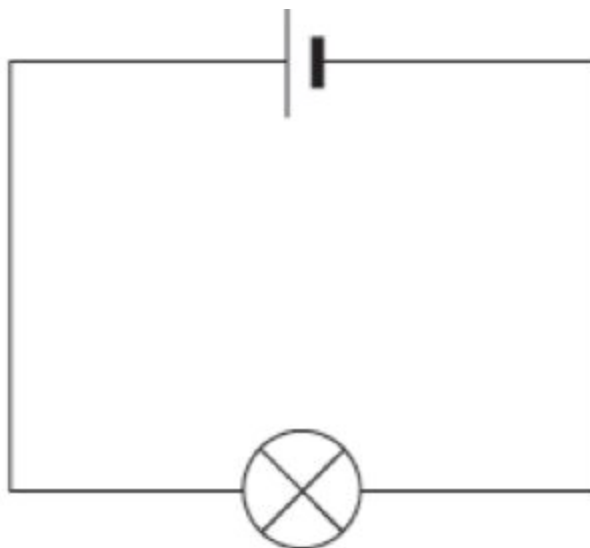
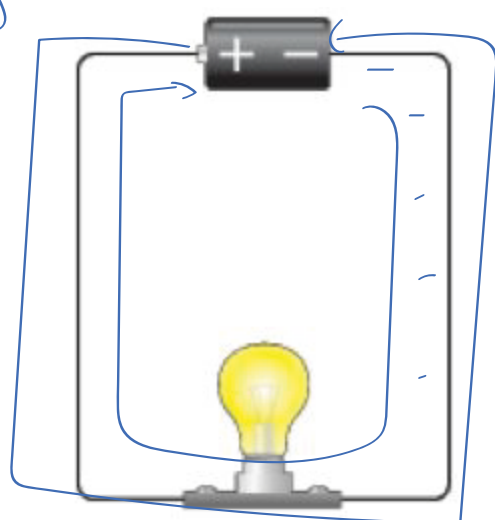
$$\Delta KE = \vec{F} \cdot \vec{d}$$

uniform
equipot lines



convention: show positive flow

The voltage difference between, for example, two ends of a battery, can cause charges to flow. In the picture below, in which direction are charged things moving?



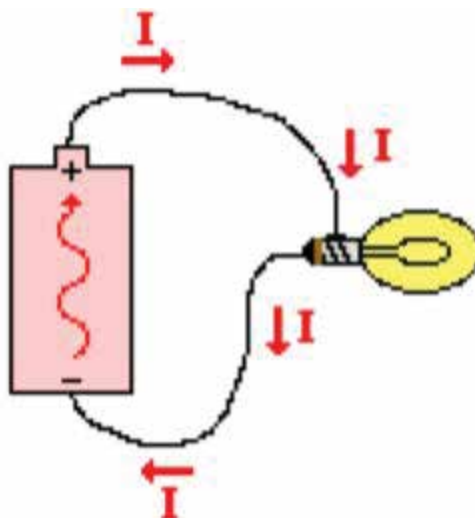
By convention, we take current to be the movement of positive charges.

One Ampere or Amp of current = 1 Coulomb / Second

unit = A

Current is usually represented with the variable I .

Current in the external circuit goes from the positive to the negative terminal of the battery.



How much current flows?

The amount of current flowing through a circuit element depends on the difference in voltage across the item, and the item's resistance.

$$I = \frac{\Delta V}{R} \quad \text{or} \quad \Delta V = IR$$

OHM'S LAW

Resistance is measured in units of Ohms using the symbol Ω .

Resistance depends on
Material
L Length
A Cross-sectional area

$$R = \frac{L\rho}{A}$$

0.0063 m
↑
 $A = 0.25^2 \pi$
 $L = 1.3 \text{ m} = 0.03302 \text{ m}$
 $\rho = 5.5 \times 10^{-5}$

$$R = 0.029 \Omega$$

31:22

Resistivities and Temperature Coefficients of Resistivity for Various Materials

$\rho \leftarrow$ greek letter "rho"

Material	Resistivity ^a ($\Omega \cdot \text{m}$)	Temperature Coefficient ^b $\alpha [(\text{°C})^{-1}]$
Silver	1.59×10^{-8}	3.8×10^{-3}
Copper	1.7×10^{-8}	3.9×10^{-3}
Gold	2.44×10^{-8}	3.4×10^{-3}
Aluminum	2.82×10^{-8}	3.9×10^{-3}
Tungsten	5.6×10^{-8}	4.5×10^{-3}
Iron	10×10^{-8}	5.0×10^{-3}
Platinum	11×10^{-8}	3.92×10^{-3}
Lead	22×10^{-8}	3.9×10^{-3}
Nichrome ^c	1.00×10^{-6}	0.4×10^{-3}
Carbon	3.5×10^{-5}	-0.5×10^{-3}
Germanium	0.46	-48×10^{-3}
Silicon ^d	2.3×10^3	-75×10^{-3}
Glass	10^{10} to 10^{14}	
Hard rubber	$\sim 10^{13}$	
Sulfur	10^{15}	
Quartz (fused)	75×10^{16}	

^a All values at 20°C. All elements in this table are assumed to be free of impurities.

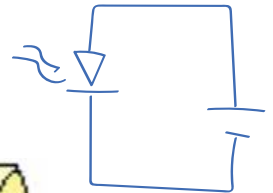
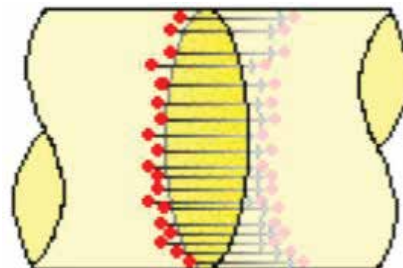
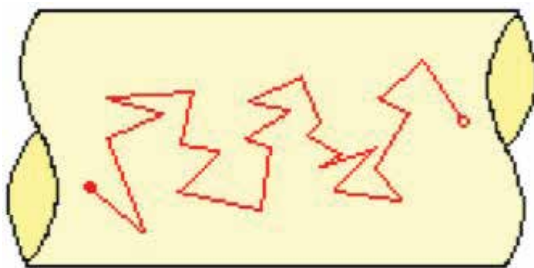
^b See Section 27.4.

^c A nickel–chromium alloy commonly used in heating elements. The resistivity of Nichrome varies with composition and ranges between 1.00×10^{-6} and $1.50 \times 10^{-6} \Omega \cdot \text{m}$.

^d The resistivity of silicon is very sensitive to purity. The value can be changed by several orders of magnitude when it is doped with other atoms.

Dispelling a Common Misconception: Although the electric field in a circuit is set up at the speed of light, current itself flows slowly, and individual electrons move slowly.

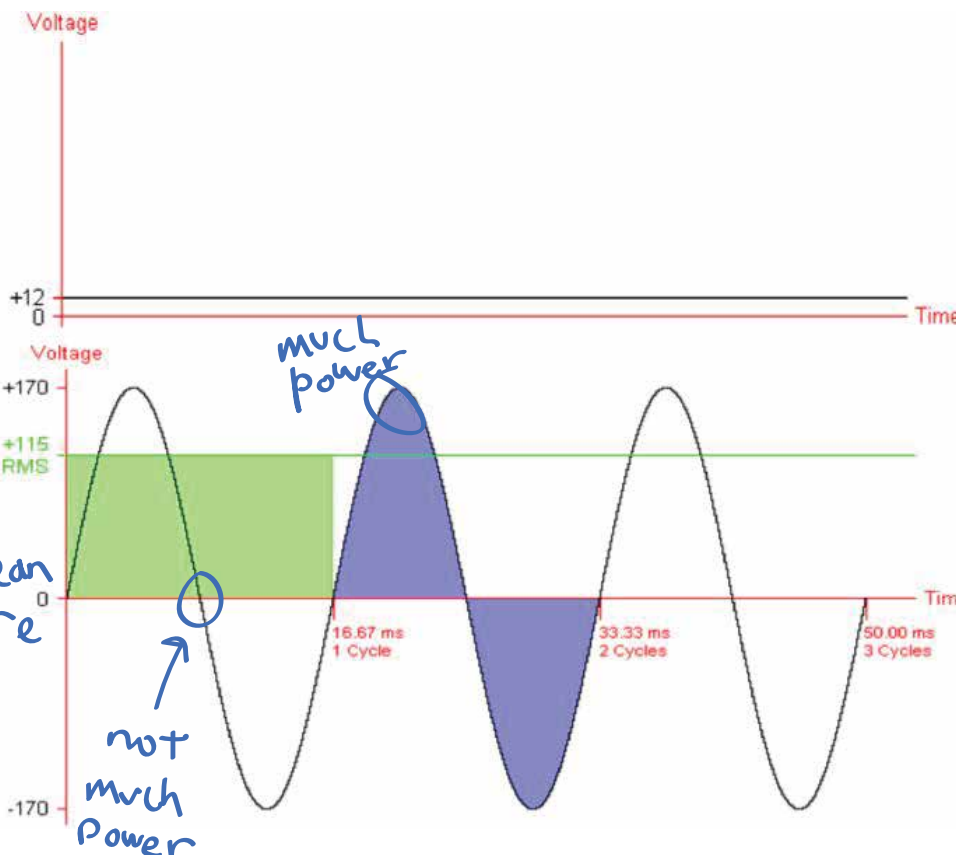
Typical path of an Electron



**Electrons slow,
but field is speed of light**

A high current results from many charge carriers passing through a cross section of wire in a circuit.

AC/DC



Kirchoff's Laws

1. The sum of all voltage changes around a closed loop in a circuit must equal zero.

KVL

2. The sum of all currents entering a point on the circuit (a *node*) equals the sum of all currents leaving the node.

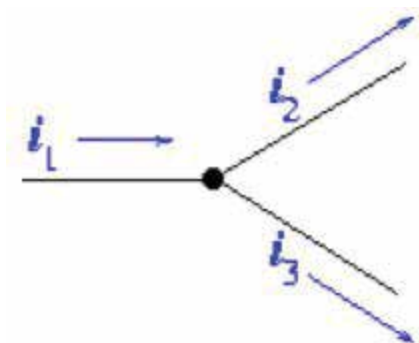
KCL

$$\sum I_{\text{node}} = 0$$

1.



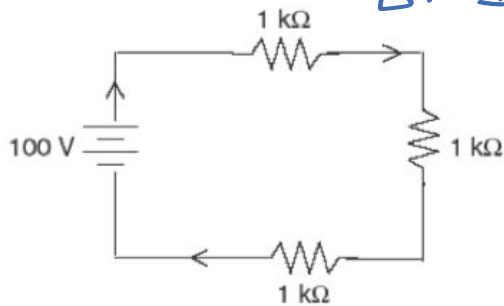
2.



$$i_1 = i_2 + i_3$$

Two Ways of Arranging Circuit Components: Series and Parallel

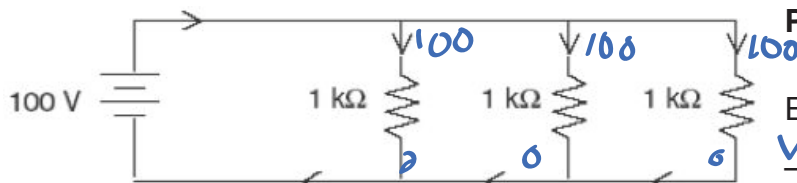
$$\Delta V = IR \quad I = \frac{\Delta V}{R} = \frac{100V}{3k\Omega} \text{ perfect wires}$$



Series

Each component has the same current.
Voltage across each can differ,
depending on its resistance.

$$I_1 = \frac{\Delta V}{R} = \frac{100V}{1k\Omega}$$



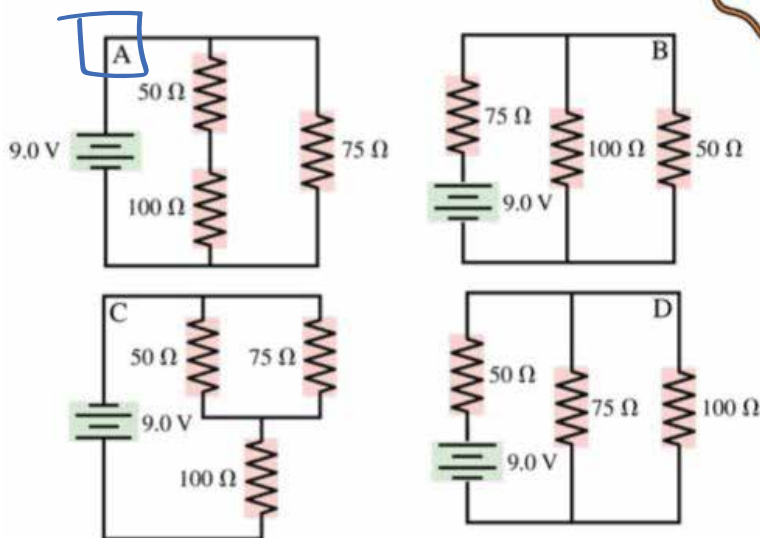
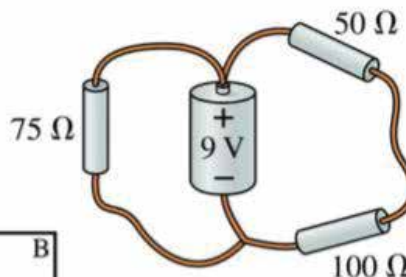
Parallel

Each component has the same voltage across it.
Current through each can

differ, depending on its resistance.
 $I_{\text{tot}} = I_1 + I_2 + I_3 = \frac{300V}{k\Omega} = 0.3A$

QuickCheck 23.5

- Which is the correct circuit diagram for the circuit shown?



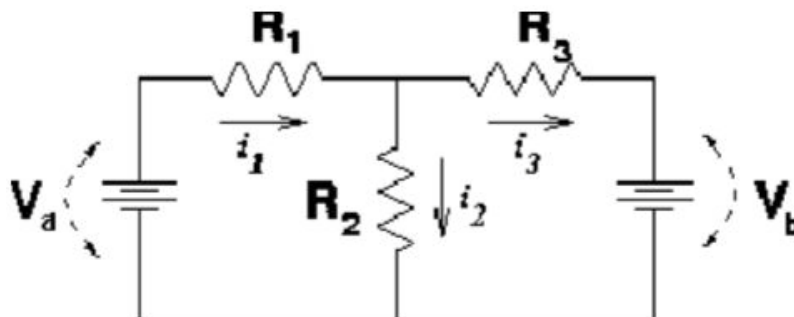
Applying Kirchoff's Laws

1. What single resistor would offer the same resistance as R_1 and R_2 in series?

2. What single resistor would offer the same resistance as R_1 and R_2 in parallel?

3. One resistor in series w/ two parallel resistors

4. A more complicated circuit: $V_a = 9V$, $V_b = 3V$, $R_1 = 10\ \Omega$, $R_2 = 20\ \Omega$, $R_3 = 50\ \Omega$



Frequently-Used Equations in Analyzing Circuits

$$I = \frac{\Delta V}{R} \quad \Delta V = IR$$

Resistors in series

$$R_{eq} = R_1 + R_2 + \dots$$

Resistors in parallel

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \dots$$

For two parallel resistors, this simplifies to

$$R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$$