Source:

1 | sum of a vector and a subspace def

1.1 | for $v \in V$ and $U \subset V$, $v + U = \{v + u : u \in U\}$ (aka shift everything by v)

2 | affine subset, parallel def

2.1 | an affine subset of V is a subset of V that is "shifted" by a vector in V

2.2 | all affine subsets from a subspace are said to be parallel to that subspace

3 | quotient space def

3.1 | A quotient space V/U where $U \subset V$ is the set of affine subsets parallel to U (all shifts)

3.2 | result

3.2.1 | two affine subsets parallel to U are equal or disjoint (Axler3.85)

1. intuition
   (a) if they are 'parallel', then they must be equal (inf intersection) or disjoint (zero intersection)

3.2.2 | the quotient space is a vector space

3.2.3 | quotient map, π def

1. The quotient map $\pi : V \to V/U$ is defined by $\pi(v) = v + U \forall v$