

**Source:****1 | find taylor series**1.1 |  $y = \cos(x)$ 

$$\begin{aligned}
P_n(x) &= f(0) + \frac{d}{dx}f(0)x + \frac{\frac{d^2}{d^2x}f(0)}{2!}x^2 + \frac{\frac{d^3}{d^3x}f(0)}{3!}x^3 + \dots \\
&= \cos(0) - \sin(0)x + \frac{-\cos(0)}{2!}x^2 + \frac{\sin(0)}{3!}x^3 + \dots \\
&= 1 - 0x - \frac{1}{2!}x^2 + \frac{0}{3!}x^3 + \dots \\
&= 1 - \frac{1}{2!}x^2 + \frac{1}{4!}x^4 + \dots \\
&= \sum_{k=0}^{\infty} \frac{(-1)^k}{(2k)!} x^{2k}
\end{aligned}$$

1.2 |  $y = e^x$ 

$$\begin{aligned}
P_n(x) &= f(0) + \frac{d}{dx}f(0)x + \frac{\frac{d^2}{d^2x}f(0)}{2!}x^2 + \frac{\frac{d^3}{d^3x}f(0)}{3!}x^3 + \dots \\
&= e^0 + e^0x + \frac{e^0}{2!}x^2 + \frac{e^0}{3!}x^3 + \dots \\
&= 1 + x + \frac{1}{2!}x^2 + \frac{1}{3!}x^3 + \dots \\
&= \sum_{k=0}^{\infty} \frac{1}{k!} x^k
\end{aligned}$$

1.3 | **TODO**  $y = \sqrt{x}$ **2 | prove approximations**2.1 |  $\frac{1}{1-x} = 1 + x + x^2 + x^3 + \dots$ 

Proof by geometric series

2.2 |  $\frac{1}{1+x} = 1 - x + x^2 - x^3 + \dots$ Plug  $-x$  for  $x$  in the previous equation.2.3 |  $\frac{1}{1+x^2} = 1 - x^2 + x^4 - x^6 + \dots$ Plug  $x^2$  for  $x$  in the previous equation.

### 3 | more finding of polynomial

3.1 | **TODO**  $y = \ln(1+x)$

3.2 | **TODO**  $y = \tan^{-1} x$

3.3 | **TODO**  $y = (1-x)^k$