

$$1 \mid \int \frac{\sqrt{x-1}}{x} dx$$

Let $u = \sqrt{x-1}$, $du = 1$

$$\int \frac{\sqrt{x-1}}{x} dx$$

$$2 \mid \mathbf{2}$$

$$3 \mid \mathbf{3}$$

$$4 \mid \mathbf{4}$$

$$5 \mid \mathbf{5}$$

$$6 \mid \int \tan^2 x + 1 dx$$

$$\begin{aligned} \int \tan^2 x + 1 dx &= \int \sec^2 x - 1 + 1 dx \\ &= \int \sec^2 x dx \end{aligned}$$

Let $u = x$, $du = 1$

$$\begin{aligned} &= \int \sec^2 u du \\ &= \tan u + C \\ &= \boxed{\tan x + C} \end{aligned}$$

$$7 \mid \mathbf{7}$$

$$8 \mid \mathbf{8}$$

$$9 \mid \int \frac{\sec^2 x}{\csc x} \sin x dx$$

$$\begin{aligned} \int \frac{\sec^2 x}{\csc x} \sin x dx &= \int \tan^2 x dx \\ &= \int \sec^2 x - 1 dx \\ &= \int \sec^2 x dx - \int 1 dx \\ &= \tan x - x \end{aligned}$$

10 | **10**

11 | **11**

12 | **12**

13 | **13**

14 | **14**