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Source:

1 | linear approximations

1.1 | cube root

1.1.1 | approximation

$$(1+x)^{\frac{1}{3}} \to \frac{1}{3}(1+x)^{\frac{-2}{3}}$$

at x = 0 is

$$\frac{1}{3}(1+0)^{...} = \frac{1}{3}$$

so the linear approximation is

$$y \approx m(x-0) + f(0) = \frac{1}{3}x + 1$$

1.1.2 | estimations

value	estimate
0.05	1.016666
-0.25	0.916666

These will be overestimates because the graph is concave down in this reigon.

1.2 | sin(x)

1.2.1 | approximation

$$y \approx \frac{d}{dx}\sin x\Big|_{0}(x-0) + \sin 0 = x$$

1.2.2 | estimates

value	estimate
-0.1	-0.1
0.1	0.1

The first estimate will be an underestimate because $\sin x$ is concave up in that reigon. The opposite is true for the second estimate.

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1.3 unknown function (only some points known

1.3.1 | approximation

$$y \approx \frac{d}{dx} f(x) \Big|_{c} (x - c) + f(c)$$

plugging in c = 1,

$$y \approx 5(x-1) - 4$$

1.3.2 | estimations

value	estimate
1.2	-3

This will be an underestimate because the second derivative is positive and the graph is thus concave up.

2 | differentials

For a function y=f(x), dy and dx are differentials and the relationship is dy=f'(x)dx. For a

2.1 | cube error

2.1.1 | differential

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