

$$(a-bi)(a+bi) = i$$

$$a(a+bi) + b i (a+bi)$$

$$a^2 + abi + abi - (bi)^2$$

$$a^2 - b^2 + 2abi = i$$

$$a^2 + 2abi - b^2 - i = 0$$

$$a = \frac{-2bi \pm \sqrt{-4b^2 + 4(b^2 + i)}}{2}$$

$$a = -bi + a + bi \quad \text{ca}$$

or

$$a = -bi - a - bi$$

$$= -a - 2bi$$

$$\Rightarrow 2a = -2bi$$

$$a = -bi$$

$$\pm \sqrt{4(-b^2 + b^2 + i)}$$

$$\frac{-2bi \pm 2\sqrt{i}}{2}$$

$$a = -bi \pm \sqrt{i}$$

$$= -bi \pm (a+bi)$$

$$a^2 - b^2 = 0, \quad 2ab = 1$$

there's the geometric one

$$(a+b)(a-b) = 0$$

$$ab = \frac{1}{2}$$

$$\downarrow \quad \downarrow$$

$$a+b=0 \quad a-b=0$$

$$a=b$$

$$a^2 = \frac{1}{2}$$

$$a = \frac{\sqrt{2}}{2}, b = \frac{\sqrt{2}}{2}$$

$$a=b \rightarrow (a)^2 = \frac{1}{2}, a^2 = -\frac{1}{2} \quad a = \frac{i}{\sqrt{2}} = \frac{\sqrt{2}i}{2}$$

$$a = \pm \frac{i}{\sqrt{2}} = \pm \frac{\sqrt{2}i}{2}$$

$$a^2 = -ab$$

$$-a^2 = ab = \frac{1}{2}$$

$$\text{so } a = \frac{\sqrt{2}i}{2}, b = -\frac{\sqrt{2}i}{2}$$

$$\text{or } a = -\frac{\sqrt{2}i}{2}, b = \frac{\sqrt{2}i}{2}$$

??? are there?