

The dot product is a projection of a vector onto a column space. (It's kind of like the closest vector to the out-of-range one that is in range). We can find this vector for the column space of A by taking $A^T b$. Thus, when we see this

$$AA^T x$$

we are somehow 'projecting' x on to range A .