Source:

- 1 | sum of a vector and a subspace def
- 1.1 | for $v \in V$ and $U \subset V$, $v + U = \{v + u : u \in U\}$ (aka shift everything by v)
- 2 | affine subset, parallel def
- 2.1 | an affine subset of V is a subset of V that is "shifted" by a vector in V
- 2.2 | all affine subsets from a subspace are said to be parallel to that subspace
- 3 | quotient space def
- 3.1 | A quotient space V/U where $U \subset V$ is the set of affine subsets parallel to U (all shifts)
- 3.2 | result
- 3.2.1 | two affine subsets parallel to U are equal or disjoint (Axler3.85)
 - 1. intuition
 - (a) if they are 'parallel', then they must be equal (inf intersection) or disjoint (zero intersection)
- 3.2.2 the quotient space is a vector space
- 3.2.3 | quotient map, π def
 - 1. The quotient map $\pi: V \to V/U$ is defined by $\pi(v) = v + U \forall v$
 - 2. basically it gives a quotient space from a vector (syntactic sugar)
- 3.2.4 dimension of a quotient space
 - 1. dimV/U = dimV dimU

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