#### Source:

### 1 | Definitions

#### 1.1 | DONE group

A set and binary operation that satisfies Group Properties

- Closed
- Identity
- Inverse
- · Associative

#### 1.2 | DONE field

A set and two binary operations: the primary (addition) and secondary (multiplication) that "mostly" satisfies group properties for both operations, and are **commutative and distributive**. It must be a group under the primary operation and a group under the secondary operation except without a secondary inverse for the primary indentity.

#### 1.3 | DONE non-singular matrices

singular matrix: has no inverse. non-singular matrix: has an inverse aka determinant non zero

# 2 | Connections

#### 2.1 | DONE connect direct sum and linear independence

the sum of two spaces is direct if their basises are linearly independent

# 2.2 | TODO matrices to represent complex numbers

The negative one matrix is  $\begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$  and we want the square root of that. It turns out that  $\begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$  satisfies this, and in fact, any complex number a+bi can be represented as  $\begin{bmatrix} a & -b \\ b & a \end{bmatrix}$ .

# 3 | Computation

#### 3.1 | DONE Find the determinant of matrices

$$\begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc$$

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#### 3.2 | DONE compute cross product

$$\begin{pmatrix} a \\ b \\ c \end{pmatrix} \times \begin{pmatrix} d \\ e \\ f \end{pmatrix} = \begin{vmatrix} i & j & k \\ a & b & c \\ d & e & f \end{vmatrix} = i \begin{vmatrix} b & c \\ e & f \end{vmatrix} + j \begin{vmatrix} c & a \\ f & d \end{vmatrix} + k \begin{vmatrix} a & b \\ d & e \end{vmatrix} = bf - ce, cd - fa, ae - bd$$

#### 3.3 | TODO Find equations of lines and planes using cross product and dot product

### 4 | **Derivations**

- 4.1 | DONE properties of the determinant
- 4.1.1 | zero when matrix has no inverse (singular)
- 4.1.2 | det = -1 for rotation matrices?
- 4.2 | DONE inverse of a 2x2 matrix

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} e & f \\ g & h \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$
$$ae + bg = 1$$
$$ce + dg = 0$$
$$af + bh = 0$$
$$cf + dh = 1$$

Then you do some algebra to get

$$e = \frac{d}{ad - bc}$$
$$g = \frac{-c}{ad - bc}$$
$$f = \frac{-b}{ad - bc}$$
$$h = \frac{a}{ad - bc}$$

# 4.3 | DONE rotation matrices

Don't try to algebra it. Use polar coordinates and the angle sum trig identities:

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$
$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

anyways, you get 
$$\begin{bmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{bmatrix}.$$

# 5 | review quizzes

- 5.1 | **DONE first quiz**
- 5.1.1 |see "find equations of lines and planes using cross product and dot product"
- 5.1.2 | rotation matrices
- 5.1.3 | cross product
- 5.2 | DONE mini take home quiz

no feedback

### 5.3 | DONE linear independence quiz

teacher gave no problems

## 5.4 | DONE quick linear quiz (linear independence and bases)

no feedback, I think that quiz was pretty solid..

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