

**Source:**

## 1 | **Broader vector spaces**

- Doesn't have to be physics vectors
- maybe it's like matrices
- or linear maps themselves

## 2 | **Axler 3.A ex7**

If  $v = 0$  then

$$Tv = 0$$

By Axler 3.11 (Maps take 0 to 0). Thus,  $\lambda$  can be anything in  $\mathbb{F}$ . Otherwise,

$$Tv = w = \left(w \frac{1}{v}\right) v = \lambda v$$
$$w \frac{1}{v} = \lambda \in \mathbb{F}$$

which is in  $\mathbb{F}$  because  $w, \frac{1}{v} \in \mathbb{F}$  and fields are closed under multiplication.