

## 1 | Axler5.22 matrix of an operator, $\mathcal{M}(T)$ def

Suppose  $T \in \mathcal{L}(V)$  and  $v_1, \dots, v_n$  is a basis of  $V$ . The *matrix of  $T$*  wrt this basis is the  $n$ -by- $n$  matrix

$$\mathcal{M}(T) = \begin{pmatrix} A_{1,1} & \cdots & A_{1,n} \\ \vdots & \ddots & \vdots \\ A_{n,1} & \cdots & A_{n,n} \end{pmatrix}$$

whose entries  $A_{j,k}$  are defined by

$$Tv_k = A_{1,k}v_1 + \cdots + A_{n,k}v_n$$

Specify a basis with  $\mathcal{M}(T, (v_1, \dots, v_n))$

### 1.1 | intuition

#### 1.1.1 | each column is where the map takes a basis vector