Source: KBMATH401ComputingLimits

## 1 | Solving Limits with Elimination

With solving limits via elimination, we are tipically analyzing a rational function that needs factoring of a term out of the polynomials on the top and/or the bottom to get out of the indeterminate form  $(\frac{0}{0})$ .

- Try factoring both the top and bottom
  - $(x \pm 1)$
  - $(x \pm 2)$
- · Rationalize all of the square roots

Tip for picking factors

Tip! If you plug in a value to an expression, and out pops 0, that value is a zero of the expression. It is helpful like this

Factor:  $(x^6-1)$ 

As you could see, plugging x=1 yields 0, meaning that (x-1) is a **zero** of  $(x^6-1)$ , and hence would be able to be factored out.

To factor it out, either do synthetic division or long division.

Let's do a problem solve for  $\lim_{x\to 2} \frac{(x^2-4)}{(x-2)}$ 

- 1. First, notice the fact this function will have a hole at x=2. This is especially important because after we simplify we will loose this hole.
- 2. Ok, now let's simply.  $\frac{(x^2-4)}{(x-2)} = \frac{(x+2)(\cancel{(x-2)})}{\cancel{(x-2)}} = (x+2)$ 3. Great! So, we know that this function behaves linearly with simply a hole at 2.
- 4. Doing the double-sided limits...
  - Evaluating  $\lim_{x\to 2^+}$ , the value will be 4 because 2+2=4.
  - Evaluating

Here's another one!  $\lim_{x\to 0} \frac{\sqrt{x+4}-2}{x}$ 

- 1. First, notice that if we are going to solve this problem, we have to divide the top thing  $(\sqrt{x+4}-2)$  by
- 2. The only thing we could do here is rationalize the top by multiplying the whole faction by a fancy one  $\frac{\sqrt{x+4}+2}{\sqrt{x+4}+2}.$
- 3. This results in  $\frac{x+4-4}{x\times(\sqrt{x+4}+2)}$ , which simplifies to  $\frac{\cancel{\#}}{\cancel{\#}\times(\sqrt{x+4}+2)}$
- 4. Plugging in x = 0, you get  $\frac{1}{4}$ .

If there is no factors, you got yourself a vertical asymtote. Refer to #missing #disorganized for solution!