

Source: [\[\[KBPHYS360MasterIndex\]\]](#)

## 1 | Problem 1

### 1.1 | (1a)

$$PE = -W$$

$$W = \int_{R_e}^{\infty} F(r) dr$$

We know that the force applied to a point mass  $m$  by the gravitational field of the earth (with mass  $M_e$ ) with distance  $x$  is modeled by

$$F(r) = \frac{GmM_e}{r^2}$$

. Therefore, our work integral can be modified to be

$$\begin{aligned} W &= \int_{R_e}^{\infty} \frac{GmM_e}{r^2} dr \\ &= GmM_e \int_{R_e}^{\infty} \frac{1}{r^2} dr \\ &= GmM_e \left[ -\frac{1}{r} \right]_{R_e}^{\infty} \\ &= -\frac{GmM_e}{R_e} \\ PE &= \frac{GmM_e}{R_e} \end{aligned}$$

### 1.2 | (1b)

$$\begin{aligned} KE &= \frac{1}{2}mv^2 \\ KE &= PE \\ \frac{1}{2}mv^2 &= \frac{GmM_e}{R_e} \\ v &= \sqrt{\frac{2GM_e}{R_e}} \end{aligned}$$

### 1.3 | (1c)

$$\begin{aligned} v &= \sqrt{\frac{2GM_e}{R_e}} \\ &= \sqrt{\frac{2 \cdot 6.674 \cdot 10^{-11} \cdot 5.97210^{24}}{6,371^2}} \\ &= \end{aligned}$$

## 2 | Problem 2

$$\begin{aligned}\sum_{i=1}^n \vec{F}_{net,i} &= \left(\sum_{i=1}^n m_i\right) \ddot{\vec{r}}_{CM} \\ \sum_{i=1}^n m_i \ddot{\vec{r}}_i &= \left(\sum_{i=1}^n m_i\right) \ddot{\vec{r}}_{CM} \\ \int \int \sum_{i=1}^n m_i \ddot{\vec{r}}_i dt dt &= \int \int \left(\sum_{i=1}^n m_i\right) \ddot{\vec{r}}_{CM} dt dt \\ \int \sum_{i=1}^n m_i \dot{\vec{r}}_i dt + C_1 &= \int \left(\sum_{i=1}^n m_i\right) \dot{\vec{r}}_{CM} dt + C_1 \\ \sum_{i=1}^n m_i \vec{r}_i + C_1 t + C_2 &= \left(\sum_{i=1}^n m_i\right) \vec{r}_{CM} + C_1 t + C_2\end{aligned}$$

Both constants are the same constant on both sides of the equation so they will cancel out.

The sum of all mass is just  $M$ .

$$\vec{r}_{CM} = \frac{1}{M} \sum_{i=1}^n m_i \vec{r}_i$$

## 3 | Problem 3

Any force within a system will have an opposite force applied as well (Newton's 3rd law). Therefore, forces within a system will cancel out and will have no effect on the center of mass.

## 4 | Problem 4

$$\begin{aligned}\vec{v} &= \frac{< 1, 4, 1 > + 2 < 3, 2, 6 > + 3 < 2, 5, 3 > + 4 < 2, 4, 6 >}{1 + 2 + 3 + 4} \\ &= < -0.7, 2.3, 2.8 >\end{aligned}$$

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