1 | **Review Sheet**

1.1 | **Problem 1**

1.1.1 | (e)

$$f(x) = x(x^2+2) - \sin(x^4 - x^{90}) + e^{\sin(x)} + \ln\cos(x^2)$$
$$f'(x) = 3x^2 + 2 - (4x^3 - 90x^{89})\cos(x^4 - x^90) + \cos(x)e^{\sin(x)} + -\frac{2x\sin(x^2)}{\cos(x^2)}$$

1.1.2 | (f)

$$y = \frac{x^5 + x^{25}}{\sin(x)} + x^5\sin(x) + x^3\sin(x)e^{5x}$$
$$\frac{d}{dx}[y] = \frac{\sin(x)(5x^4 + 25x^{24}) - \cos(x)(x^4 + x^25)}{\sin^2(x)} + (5x^4\sin(x) + x^5\cos(x)) + ((3x^2\sin(x) + x^3\cos(x))e^{5x} + 5x^4\sin(x)e^{5x})$$

1.2 | **Problem 4**

1.2.1 | (a)

$$\begin{aligned}
V &= 24.0 L mol^{-1} \\
V(t) &= 24t \\
R(t) &= \sqrt[3]{\frac{3}{4}V(t)} \\
&= \sqrt[3]{18t} \\
t &= 3 \\
V(3) &= 72L \\
R(3) &= 3\sqrt[3]{2} * 10cm \qquad\qquad = 30\sqrt[3]{2}cm \\
V'(t) &= 24 \\
R'(t) &= \frac{18}{\sqrt[3]{18t}^2} \\
V'(3) &= 24Ls^{-1} \\
R'(3) &= \frac{18}{\sqrt[3]{18(3)}^2} \\
&= \frac{18}{6\sqrt[3]{2}} * 10cms^{-1} \quad = \frac{30}{\sqrt[3]{2}}cms^{-1}
\end{aligned}$$

1.2.2 | (b)

Assuming that the question is asking how much time would have passed when the radius is 3m:

$$\begin{aligned} 3m &= 30 * 10cm \\ R(t) &= 30 \\ \sqrt[3]{18t} &= 30 \\ 18t &= 30^3 \\ t &= \frac{30^3}{18} \\ &= 1500 \end{aligned}$$

1.3 | **Problem 5**

1.3.1 | (e)

$$\begin{aligned} &\int (4y - y^2 + 4y^3 + 1)^{-2/3}(12y^2 - 2y + 4)\, dy \\ &\qquad = 3\int \frac{1}{3}(4y - y^2 + 4y^3 + 1)^{-2/3}(12y^2 - 2y + 4)\, dy \\ &\qquad = 3(4y - 4^2 + 4y^3 + 1)^{1/3} + C \end{aligned}$$

1.3.2 | (f)

$$\int 2x\cos(x)\, dx =$$