

1 | Let  $F(x) = \int_0^x f(t)dt$

1.1 | complete the table

x	0	1	2	3	4
$F(x)$	0	$\frac{4}{3}$	$\frac{8}{3}$	$\frac{4}{3}$	0

1.2 | sketch the function



2 |  $G(x) = \int_2^x f(t)dt$

2.1 | complete the table

x	0	1	2	3	4
G(x)	$-\frac{8}{3}$	$-\frac{4}{3}$	0	$-\frac{4}{3}$	$-\frac{8}{3}$

## 2.2 | sketch the function



## 3 | 3

## 3.1 | complete the table

x	0	1	2	3	4
H(x)	0	$\frac{4}{3}$	$\frac{8}{3}$	$\frac{4}{3}$	0

## 3.2 | sketch the function

same as 1b

## 4 | complete the table

	$F(x)$	$G(x)$	$H(x)$
maximum	$4x+2$		
minimum	$4x$		
increases	$4x, 4x+2$		
decreases	$4x-2, 4x$		

The other columns are the same, because  $H(x) = F(x)$  and  $G(x) = H(x) - \frac{8}{3}$ .

## 5 | why does it work over the entire domain?

The argument for each cell is the same: it should work across the domain because those are the points where the derivative of  $F(x)$  (which is  $f(x)$ ) is zero and function is periodic.

$F(x)$  increases when  $f(x)$  is positive.

## 6 | family of functions

Changing the 'zero point' of the derivative just shifts the graph up and down, by up to the range of the function.

## 7 | sketching more functions

$$7.1 \mid F_1(x) = \int_x^0 f(t)dt$$

$F(x)$  but reflected across the x-axis (negated)

$$7.2 \mid F_2(x) = \int_0^x f(-t)dt$$

$f$  is an odd function so  $f(-t) = -f(t)$  so  $F_2 = F_1$

$$7.3 \mid F_3(x) = \int_0^{2x} f(t)dt$$