

# Weaknesses of Monoalphabetic Ciphers

## Vigenère Cipher

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As early as the 9th century, the great weakness of monoalphabetic ciphers (Caesar cipher) was recognized in the Islamic world. The distribution of letters follows a specific but constant pattern in every language. As explained in the last section, the letter 'e' is by far the most common letter in the English language.

To demonstrate that this applies to any given (longer) texts, the text of the Book of Revelations from the King James Bible was analyzed. The resulting distribution of letters was plotted against the distribution from the table. The result is shown in the figure below.

```
1 import string
2 import pandas as pd
3 import matplotlib.pyplot as plt
4 import numpy as np
5
6 def file_reader(path : str) -> str:
7
8     with open(path, mode='r', encoding='utf-8') as f:
9         text = f.read()
10
11     return text
12
13 def text_cleaning(text : str) -> str:
14     clean = text.upper() \
15         .replace('Ä', 'AE') \
16         .replace('Ö', 'OE') \
17         .replace('Ü', 'UE') \
18         .replace('ß', 'SS') \
19         .replace(' ', '') \
20
21     cleaned_text = ''
22
23     for c in clean:
24         if c.isalpha():
```

```

25         cleaned_text += c
26
27     return cleaned_text
28
29 def file_writer(path : str, text : str) -> None:
30     i = 0
31     grouped_text = ""
32     for c in text:
33         i += 1
34         if i % 50 == 0:
35             grouped_text += c + "\n"
36         elif i % 5 == 0:
37             grouped_text += c + " "
38         else:
39             grouped_text += c
40
41     with open(path, mode='w', encoding='utf-8') as f:
42         f.write(grouped_text)
43
44 revelation = file_reader('revelation.txt')
45 cleaned_revelation = text_cleaning(revelation)
46 file_writer('cleaned_revelation.txt', cleaned_revelation)
47
48 def letter_frequency(text: str) -> dict:
49     frequency = {}
50     total_letters = 0
51
52     for char in text:
53         if char not in frequency:
54             frequency[char] = 1
55         else:
56             frequency[char] += 1
57         total_letters += 1
58
59     for key, value in frequency.items():
60         frequency[key] = (value / total_letters) * 100
61
62
63     return frequency
64
65 frequency_revelation = letter_frequency(cleaned_revelation)
66
67
68 standard_frequency = {
69     'E': 12.02,

```

```

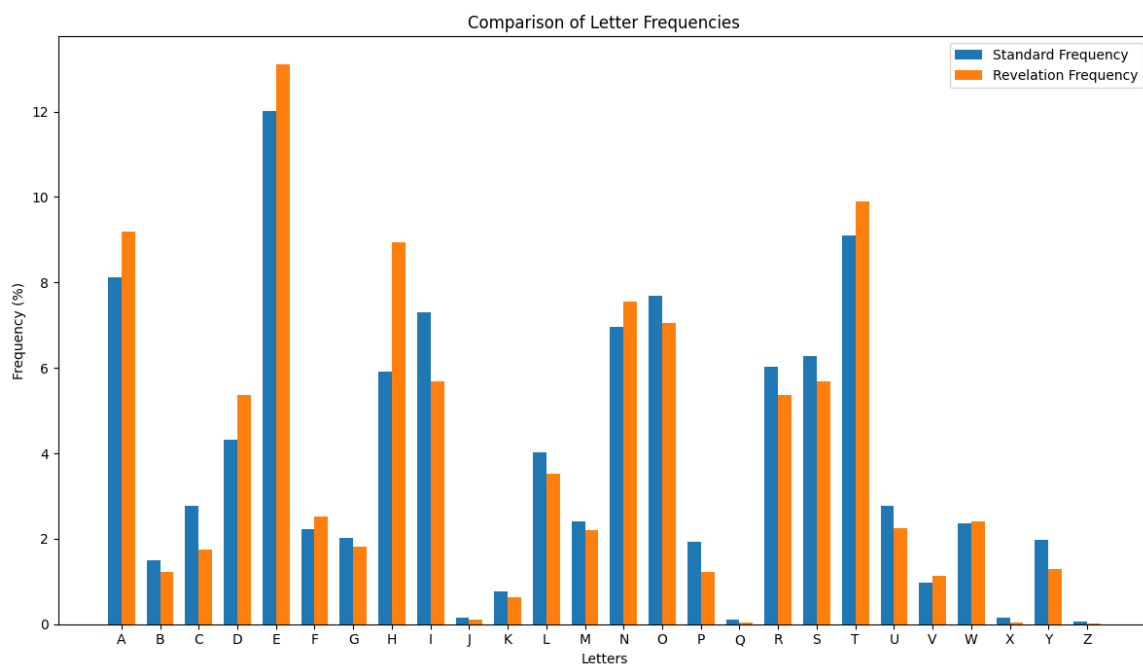
70     'T': 9.10,
71     'A': 8.12,
72     'O': 7.68,
73     'I': 7.31,
74     'N': 6.95,
75     'S': 6.28,
76     'R': 6.02,
77     'H': 5.92,
78     'D': 4.32,
79     'L': 4.03,
80     'C': 2.78,
81     'U': 2.76,
82     'M': 2.41,
83     'W': 2.36,
84     'F': 2.23,
85     'G': 2.02,
86     'Y': 1.97,
87     'P': 1.93,
88     'B': 1.49,
89     'V': 0.98,
90     'K': 0.77,
91     'J': 0.15,
92     'X': 0.15,
93     'Q': 0.10,
94     'Z': 0.07
95 }
96
97 df = pd.DataFrame.from_dict([standard_frequency, frequency_revelation])
98 df.index = ['Standard Frequency', 'Revelation Frequency']
99 dft = df.T
100 dft = dft.sort_index()
101 dft['Standard Frequency'] = dft['Standard Frequency'].astype(float)
102 dft['Revelation Frequency'] = dft['Revelation Frequency'].astype(float)
103
104 # --- Erstellen Sie das Side-by-Side-Balkendiagramm ---
105 # Legen Sie die Breite der Balken fest
106 bar_width = 0.35
107
108 # Verwenden Sie den Index des transponierten DataFrames (dft)
109 x = np.arange(len(dft.index))
110
111 fig, ax = plt.subplots(figsize=(12, 7))
112
113 # Zeichnen Sie die Balken für die beiden Spalten aus dft
114 ax.bar(x - bar_width/2, dft['Standard Frequency'], bar_width, label='Standard Frequency')

```

```

115 ax.bar(x + bar_width/2, dft['Revelation Frequency'], bar_width, label='Revelation Frequency')
116
117 ax.set_xticks(x)
118 ax.set_xticklabels(dft.index)
119
120 ax.set_xlabel('Letters')
121 ax.set_ylabel('Frequency (%)')
122 ax.set_title('Comparison of Letter Frequencies')
123 ax.legend()
124 plt.tight_layout()
125
126 plt.show()

```



The graphic shows that for a text length of 57,891 letters, the distribution in a literary text is almost identical to the general frequency distribution in the English language.

The following graphic shows what happens to the distribution of letters when the same text is encrypted with a Caesar cipher.

```

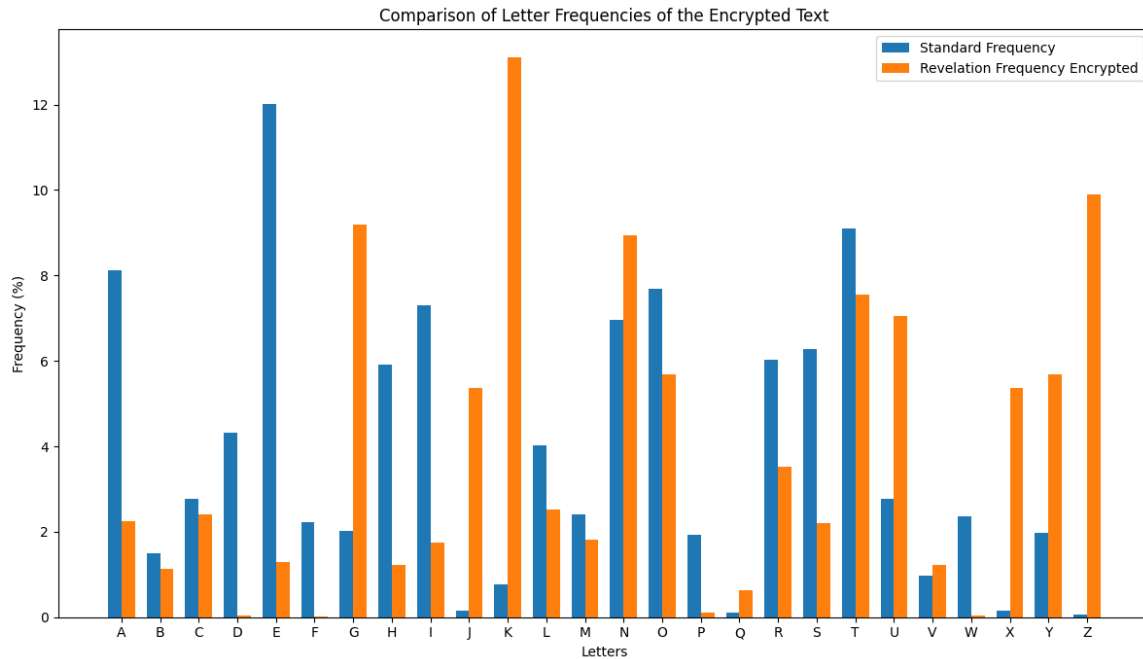
1 def caesar(text : str, shift : int, encrypt=True) -> str:
2     text = text.upper()
3     result = ""
4
5     if encrypt:
6         for char in text:
7             shifted = (ord(char) - ord('A') + shift) % 26 + ord('A')

```

```

8         result += chr(shifted)
9     else:
10         for char in text:
11             shifted = (ord(char) - ord('A') - shift) % 26 + ord('A')
12             result += chr(shifted)
13
14     return result
15
16
17 ciphered_revelation = caesar(cleaned_revelation, 6, encrypt=True)
18 frequency_encyrpyted_revelation = letter_frequency(ciphered_revelation)
19 dft['Revelation Frequency Encrypted'] = pd.Series(frequency_encyrpyted_revelation)
20
21 # --- Erstellen Sie das Side-by-Side-Balkendiagramm ---
22 # Legen Sie die Breite der Balken fest
23 bar_width = 0.35
24
25 # Verwenden Sie den Index des transponierten DataFrames (dft)
26 x = np.arange(len(dft.index))
27
28 fig, ax = plt.subplots(figsize=(12, 7))
29
30 # Zeichnen Sie die Balken für die beiden Spalten aus dft
31 ax.bar(x - bar_width/2, dft['Standard Frequency'], bar_width, label='Standard Frequency')
32 ax.bar(x + bar_width/2, dft['Revelation Frequency Encrypted'], bar_width, label='Revelation')
33
34 ax.set_xticks(x)
35 ax.set_xticklabels(dft.index)
36
37 ax.set_xlabel('Letters')
38 ax.set_ylabel('Frequency (%)')
39 ax.set_title('Comparison of Letter Frequencies of the Encrypted Text')
40 ax.legend()
41 plt.tight_layout()
42
43 plt.show()

```



It is clearly visible that the distribution follows the same pattern - shifted by six positions. This analysis allows the decryption of the text without having to try all possible key alphabets.

## Vigenère Chiffre

The Vigenère Cipher is a polyalphabetic cipher. The method is named after Blaise de Vigenère (1523 - 1596). Polyalphabetic means that not one shift is used for encryption, but - changing after each letter - several shifts are used.

To achieve this, a so-called Vigenère square is used as shown below.

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
A	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
B	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A
C	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B
D	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C
E	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D
F	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E
G	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F
H	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
I	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H
J	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I
K	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J
L	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K
M	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L
N	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M
O	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
P	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Q	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
R	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
S	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
T	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
U	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
V	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U
W	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V
X	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W
Y	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
Z	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y

To encrypt a plaintext, the Vigenère method requires a keyword. The keyword should be as long as possible. The following example is intended to show how the Vigenère method works. The plaintext to be encrypted is 'Cryptology is amazing' and the key is 'Buelrain'. As an aid, text and key are presented in a table.

```
cryptologyisamazing
buelrainbuelrainbue
```

The key is repeated without spaces until the letter sequence of the key is as long as the letter sequence to be encrypted.

Next the letter to be encrypted is searched in the header of the Vigenère square. This identifies the column with the shifted alphabet. The encrypted letter is obtained by searching

in the column with the row headers the letter of the key located under the letter to be encrypted. The intersection of the row with the previously found column corresponds to the encrypted letter.

cryptologyisamazing  
buelrainbuelrainbue

DLCAKOTBHSMJHR

On a computer, the Vigenère cipher can be implemented by using modular arithmetic. To do this, each letter is assigned a numerical value according to the pattern  $a = 0, b = 1, \dots, z = 25$ . The encryption is then performed according to the 'formula'  $C_i = (P_i + K_i) \bmod 26$  where the letters  $C$  stand for the ciphertext,  $P$  for the plaintext and  $K$  for the key. The index  $i$  stands for the  $i$ -th letter in the text sequence.

The example above can be illustrated as follows.

c	r	y	p	t	o	l	o	g	i	e	s	a	m	a	z	i	n	g
02	17	24	15	19	14	11	14	06	08	04	18	00	12	00	25	08	13	06
b	u	e	l	r	a	i	n	b	u	e	l	r	a	i	n	b	u	e
01	20	04	11	17	00	08	13	01	20	04	11	17	00	08	13	01	20	04
03	37	28	26	36	14	19	27	07	28	08	29	17	12	08	38	09	33	10
03	11	02	00	10	14	19	01	07	02	08	19	09	19	00	02	01	07	17
D	L	C	A	K	O	T	B	H	C	I	T	J	T	A	C	B	H	R

For decryption, the same formula can be used, but with a minus instead of a plus ( $P_i = (C_i - K_i + 26) \bmod 26$ ). The addition of 26 in the brackets is used to avoid negative numbers.

How the Vigenère cipher affects the distribution of letters can be seen in the graphic below.

```

1 def vigenere_chiffre(text: str, key: str, encrypt=True) -> str:
2     """
3     Implementiert die Vigenère-Verschlüsselung für einen gegebenen Klartext und
4     Schlüssel.
5
6     Args:
7         klartext (str): Der zu verschlüsselnde Text schluessel (str): Das
8         Schlüsselwort für die Verschlüsselung
9
10    Returns:
11        str: Der verschlüsselte Text

```



```

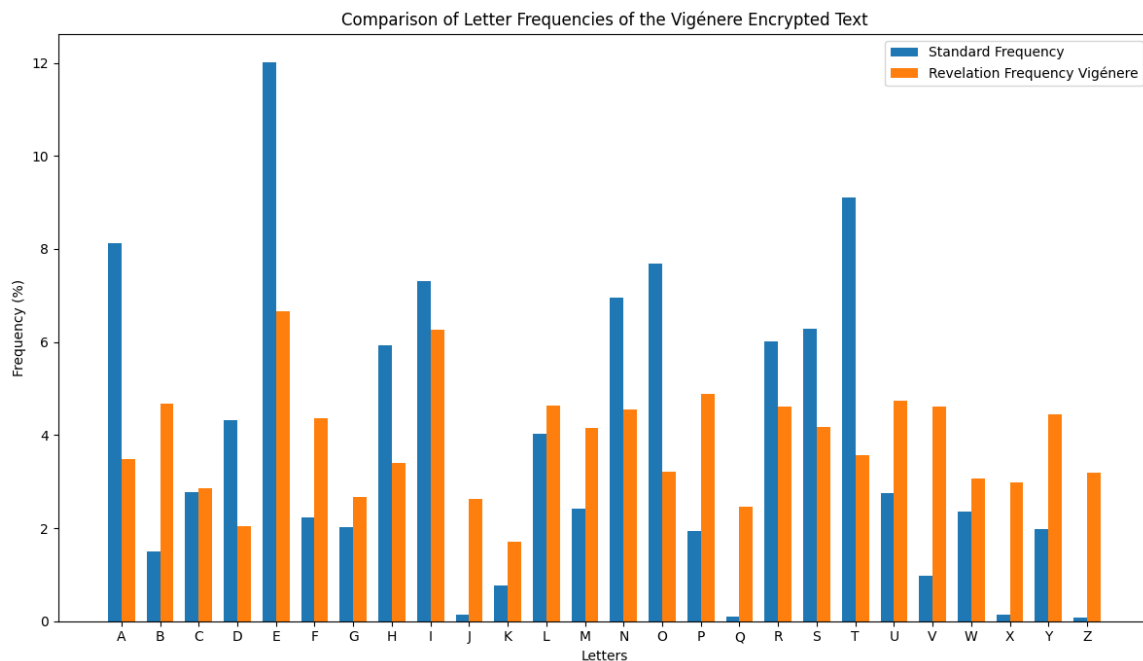
12     """
13
14     # initialisiere den resultierenden Text
15     resulting_text = ''
16
17     # bestimme die Schlüssellänge für die anschließende Modulo-Operation
18     key_length = len(key)
19
20     # iteriere über den Eingabetext unter gleichzeitiger Erfassung des Index
21     for i, char in enumerate(text):
22         # berechne den Zahlwert des Buchstabens aus der ascii Tabelle
23         char_no = ord(char) - 97
24         key_no = ord(key[i % key_length]) - 97
25
26         if encrypt == True:
27             # berechne den Zahlwert des verschlüsselten Buchstabens
28             ciph_no = (char_no + key_no) % 26
29         else:
30             # berechne den Zahlwert des entschlüsselten Buchstabens
31             ciph_no = (char_no + (26 - key_no)) % 26
32
33         # übernehme das Zeichen aufgrund seines Zahlwertes aus der ascii Tabelle
34         ciph = chr(ciph_no + 97)
35
36         # füge den Buchstaben am resultierenden Text an
37         resulting_text += ciph
38     return resulting_text
39
40 revelation_vigenere = vigenere_chiffre(cleaned_revelation.lower(), 'buelrain', encrypt=True)
41
42 revelation_vigenere_frequency = letter_frequency(revelation_vigenere.upper())
43 dft['Revelation Frequency Vigenere'] = pd.Series(revelation_vigenere_frequency)
44
45 # --- Erstellen Sie das Side-by-Side-Balkendiagramm ---
46 # Legen Sie die Breite der Balken fest
47 bar_width = 0.35
48
49 # Verwenden Sie den Index des transponierten DataFrames (dft)
50 x = np.arange(len(dft.index))
51
52 fig, ax = plt.subplots(figsize=(12, 7))
53
54 # Zeichnen Sie die Balken für die beiden Spalten aus dft
55 ax.bar(x - bar_width/2, dft['Standard Frequency'], bar_width, label='Standard Frequency')
56 ax.bar(x + bar_width/2, dft['Revelation Frequency Vigenere'], bar_width, label='Revelation

```

```

57
58 ax.set_xticks(x)
59 ax.set_xticklabels(dft.index)
60
61 ax.set_xlabel('Letters')
62 ax.set_ylabel('Frequency (%)')
63 ax.set_title('Comparison of Letter Frequencies of the Vigenère Encrypted Text')
64 ax.legend()
65 plt.tight_layout()
66
67 plt.show()

```



It is quite obvious that the distribution of letters in a polyalphabetically encrypted text is significantly different from that in normal text. The Vigenère cipher was therefore considered 'la chiffre indéchiffrable' for about 300 years.

However, a special case of the Vigenère cipher is actually not decipherable. This is the case when the key is longer than the plaintext. This is called the "One-Time Pad".