50.040 Natural Language Processing (Summer 2022) Homework 2

Due 1st July 2022, 5PM

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Introduction

Constituency parsing aims to extract a constituency-based parse tree from a sentence that represents its syntactic structure according to a phrase structure grammar. A typical constituency parse tree is shown below:



S is a distinguished start symbol, node labels such as NP(noun phrase), VP(verb phrase) are non-terminal symbols, leaf labels such as "a", "banana" are terminal symbols.

In this homework, we will implement a constituency parser based on probabilistic context-free grammars (PCFGs) and evaluate its performance.

Dataset

We will be using a version of the "Penn Treebank" released in NLTK corpora to induce PCFGs and evaluate our algorithm. The preprocessing code has been provided, do not make any changes to the text and code unless you are requested to do so. Run the code we provide to load the training and test sets as Python lists, it will take ~1 minute. Since we will not tune hyper-parameters in this homework, there will be no need for a development set.

PCFGs

A probabilistic context-free grammar consists of:

- A context-free grammar $G = (N, \Sigma, S, R)$ where N is a finite set of non-terminal symbols, Σ is a finite set of terminal symbols, R is a finite set of rules (e.g., $NP \to NP PP$), $S \in N$ is the start symbol.
- One parameter $q(A \to \beta)$ for each rule $A \to \beta$ in R. Since the grammar is in Chomsky normal form, there are only two types of rules: $A \to B$ C and $A \to \alpha$, where $A, B, C \in N$, $\alpha \in \Sigma$.

We can estimate the parameter $q(A \rightarrow \beta)$ using maximum likelihood estimation:

$$q_{MLE}(A \to \beta) = \frac{count(A \to \beta)}{count(A)}$$

where $count(A \to \beta)$ refers to the number of occurrences of the rule $A \to \beta$ in all the parse trees in the training set, and count(A) refers to the number of occurrences of the non-terminal symbol A.

In [1]:

```
import copy
from collections import Counter
from nltk.tree import Tree
from nltk import Nonterminal
from nltk.corpus import LazyCorpusLoader, BracketParseCorpusReader
from collections import defaultdict
import time
```

```
In [2]:
```

```
st = time.time()
```

In [3]:

```
import nltk
nltk.download('treebank')
!pip install svgling
```

```
[nltk_data] Downloading package treebank to /Users/skylee/nltk_data...
```

[nltk data] Package treebank is already up-to-date!

Requirement already satisfied: svgling in /Users/skylee/.pyenv/versions/3.8.10/lib/python3.8/site-packages (0.3.1)

Requirement already satisfied: svgwrite in /Users/skylee/.pyenv/vers ions/3.8.10/lib/python3.8/site-packages (from svgling) (1.4.2)

WARNING: You are using pip version 21.1.1; however, version 22.1.2 is available.

You should consider upgrading via the '/Users/skylee/.pyenv/version s/3.8.10/bin/python3.8 -m pip install --upgrade pip' command.

In [4]:

```
def set leave lower(tree string):
    if isinstance(tree string, Tree):
        tree = tree string
    else:
        tree = Tree.fromstring(tree string)
    for idx, _ in enumerate(tree.leaves()):
        tree location = tree.leaf treeposition(idx)
        non terminal = tree[tree location[:-1]]
        non terminal[0] = non terminal[0].lower()
    return tree
def get train test data():
    Load training and test set from nltk corpora
    train num = 3900
    test index = range(10)
    treebank = LazyCorpusLoader('treebank/combined', BracketParseCorpusReader, r
'wsj .*\.mrg')
    cnf train = treebank.parsed sents()[:train num]
    cnf test = [treebank.parsed sents()[i+train num] for i in test index]
    #Convert to Chomsky norm form, remove auxiliary labels
    cnf train = [convert2cnf(t) for t in cnf train]
    cnf test = [convert2cnf(t) for t in cnf test]
    return cnf train, cnf test
def convert2cnf(original tree):
    Chomsky norm form
    tree = copy.deepcopy(original tree)
    #Remove cases like NP->DT, VP->NP
    tree.collapse unary(collapsePOS=True, collapseRoot=True)
    #Convert to Chomsky
    tree.chomsky_normal_form()
    tree = set leave lower(tree)
    return tree
```

In [5]:

```
### GET TRAIN/TEST DATA
cnf_train, cnf_test = get_train_test_data()
```

```
In [6]:
```

```
cnf train[0].pprint()
(S
  (NP-SBJ
    (NP (NNP pierre) (NNP vinken))
    (NP-SBJ | <, -ADJP-, >
      (,,)
      (NP-SBJ | <ADJP-,>
        (ADJP (NP (CD 61) (NNS years)) (JJ old))
         (, ,))))
  (S | < VP - . >
    (VP
      (MD will)
      (VP
        (VB join)
         (VP | <NP-PP-CLR-NP-TMP>
           (NP (DT the) (NN board))
           (VP | < PP-CLR-NP-TMP>
             (PP-CLR
               (IN as)
               (NP
                 (DT a)
                 (NP | <JJ-NN> (JJ nonexecutive) (NN director))))
             (NP-TMP (NNP nov.) (CD 29))))))
    (. .)))
```

Question 1

To better understand PCFG, let's consider the first parse tree in the training data "cnf train" as an example. Run the code we have provided for you and then write down the roles of .productions(), .rhs(), .lhs(), .leaves() in the ipynb notebook.

Out[8]:

```
In [7]:
rules = cnf train[0].productions()
print(rules, type(rules[0]))
[S -> NP-SBJ S| < VP-.>, NP-SBJ -> NP NP-SBJ| <, -ADJP-,>, NP -> NNP NN
P, NNP -> 'pierre', NNP -> 'vinken', NP-SBJ |<,-ADJP-,> -> , NP-SBJ |<
ADJP-,>, , -> ',', NP-SBJ | < ADJP-,> -> ADJP ,, ADJP -> NP JJ, NP -> C
D NNS, CD -> '61', NNS -> 'years', JJ -> 'old', , -> ',', S | <VP-.> -
> VP ., VP -> MD VP, MD -> 'will', VP -> VB VP|<NP-PP-CLR-NP-TMP>, V
B -> 'join', VP|<NP-PP-CLR-NP-TMP> -> NP VP|<PP-CLR-NP-TMP>, NP -> D
T NN, DT -> 'the', NN -> 'board', VP | < PP-CLR-NP-TMP> -> PP-CLR NP-TM
P, PP-CLR -> IN NP, IN -> 'as', NP -> DT NP | <JJ-NN>, DT -> 'a', NP | <
JJ-NN> -> JJ NN, JJ -> 'nonexecutive', NN -> 'director', NP-TMP -> N
NP CD, NNP -> 'nov.', CD -> '29', . -> '.'] <class 'nltk.grammar.Pro
duction'>
In [8]:
rules[0].rhs(), type(rules[0].rhs()[0])
```

((NP-SBJ, S|<VP-.>), nltk.grammar.Nonterminal)

```
In [9]:
    rules[10].rhs(), type(rules[10].rhs()[0])
Out[9]:
    (('61',), str)
In [10]:
    rules[0].lhs(), type(rules[0].lhs())
Out[10]:
    (S, nltk.grammar.Nonterminal)
In [11]:
    print(cnf_train[0].leaves())
['pierre', 'vinken', ',', '61', 'years', 'old', ',', 'will', 'join', 'the', 'board', 'as', 'a', 'nonexecutive', 'director', 'nov.', '29', '.']
```

ANSWER HERE

- .productions(): It returns a grammar production where each of them maps a single symbol on the "left hand side" to a sequence of symbols on the "right hand side"
- .rhs(): It returns the right-hand side of a production(it's children nodes)
- .lhs(): It returns the left-hand side of a production (it's parent node)
- .leaves(): It returns the leaves of the tree when joined from the whole sentence, the order reflects the order of leaves in the tree hierarchical structure

Question 2

To count the number of unique rules, nonterminals and terminals, please implement functions **collect_rules**, **collect nonterminals**, **collect terminals**

In [12]:

```
def collect rules(train data):
    Collect the rules that appear in data.
        train data: list[Tree] --- list of Tree objects
    return:
        rules: list[nltk.grammar.Production] --- list of rules (Production objec
ts)
        rules counts: Counter object --- a dictionary that maps one rule (nltk.N
onterminal) to its number of
                                          occurences (int) in train data.
    111
    rules = list()
    rules counts = Counter()
    ### YOUR CODE HERE
    for train in train data:
        for rule in train.productions():
            rules.append(rule)
            rules counts[rule] += 1
    ### YOUR CODE HERE
    return rules, rules counts
def collect nonterminals(rules):
    collect nonterminals that appear in the rules
    params:
        rules: list[nltk.grammar.Production] --- list of rules (Production objec
ts)
    return:
        nonterminals: set(nltk.Nonterminal) --- set of nonterminals
    ### YOUR CODE HERE
    nonterminals = list()
    for rule in rules:
        nonterminals.append(rule.lhs())
        for r in rule.rhs():
            if type(r) == str:
                continue
            else:
                nonterminals.append(r)
    nonterminals = set(nonterminals)
    ### END OF YOUR CODE
    return nonterminals
def collect terminals(rules):
    collect terminals that appear in the rules
        rules: list[nltk.grammar.Production] --- list of rules (Production objec
ts)
    return:
        terminals: set of strings --- set of terminals
```

```
In [13]:
```

```
train_rules, train_rules_counts = collect_rules(cnf_train)
nonterminals = collect_nonterminals(train_rules)
terminals = collect_terminals(train_rules)
```

In [14]:

```
len(train_rules), len(set(train_rules)), len(terminals), len(nonterminals)
Out[14]:
(196646, 31656, 11367, 7869)
In [15]:
print(train_rules_counts.most_common(5))
```

```
[(, -> ',', 4876), (DT -> 'the', 4726), (. -> '.', 3814), (PP -> IN NP, 3273), (S | < VP -.> -> VP ., 3003)]
```

Question 3

Implement the function **build_pcfg** which builds a dictionary that stores the terminal rules and nonterminal rules.

In [16]:

```
def build pcfg(rules counts):
    Build a dictionary that stores the terminal rules and nonterminal rules.
        rules counts: Counter object --- a dictionary that maps one rule to its
number of occurences in train data.
    return:
        rules dict: dict(dict(dict)) --- a dictionary has a form like:
                    rules dict = { 'terminals':{ 'NP':{ 'the':1000, 'an':500}, 'AD
J':{'nice':500,'good':100}},
                                   'nonterminals':{'S':{'NP@VP':1000},'NP':{'NP@N
P':540}}}
    When building "rules_dict", you need to use "lhs()", "rhs()" funtion and con
vert Nonterminal to str.
    **All the keys in the dictionary are of type str**.
    '@' is used as a special symbol to split left and right nonterminal strings.
    ### YOUR CODE HERE
    rules dict = dict()
    rules dict['terminals'] = defaultdict(dict)
    rules dict['nonterminals'] = defaultdict(dict)
    for rule in rules counts:
        temp = []
        rhs = rule.rhs()
        lhs = str(rule.lhs())
        if len(rhs) == 1:
            if type(rhs[0]) == str:
                rules dict['terminals'][lhs][rhs[0]] = rules counts[rule]
        else:
            for r in rhs:
                temp.append(str(r))
            at str = '@'.join(temp)
            rules dict['nonterminals'][lhs][at str] = rules counts[rule]
    ### END OF YOUR CODE
    return rules dict
```

```
In [17]:
```

```
train_rules_dict = build_pcfg(train_rules_counts)
```

Question 4

Count and find all the terminal symbols in "cnf_test" that never appeared in the PCFG we built.

In [18]:

```
unseen_symbols = []
for i in cnf_test:
    test_rules, test_rules_counts = collect_rules([i])
    test_terminals = collect_terminals(test_rules)
    for t in test_terminals:
        if t not in terminals:
            unseen_symbols.append(t)

print(f"count of unseen symbols: {len(unseen_symbols)}")
print(f"terminal symbols that never appeared in PCFG:\n{unseen_symbols}")
```

```
count of unseen symbols: 19
terminal symbols that never appeared in PCFG:
['constitutional-law', 'kurland', 'tribe', 'laurence', 'professors',
'procedure', 'scuttle', 'procedure', 'implicitly', 'kennedy', 'spect
rum', 'kurland', 'tribe', 'professors', 'professors', 'authorizes',
'partial', 'lawmaking', 'shared']
```

Question 5

We can use smoothing techniques to handle these cases. A simple smoothing method is as follows. We first create a new "unknown" terminal symbol unk.

Next, for each original non-terminal symbol $A \in N$, we add one new rule $A \to unk$ to the original PCFG.

The smoothed probabilities for all rules can then be estimated as:

$$q_{smooth}(A \to \beta) = \frac{count(A \to \beta)}{count(A) + 1}$$
$$q_{smooth}(A \to unk) = \frac{1}{count(A) + 1}$$

where |V| is the count of unique terminal symbols.

Implement the function smooth rules prob which returns the smoothed rule probabilities

In [19]:

```
def smooth rules prob(rules counts):
    params:
        rules counts: dict(dict(dict)) --- a dictionary has a form like:
                      rules counts = { 'terminals':{ 'NP':{ 'the':1000, 'an':500},
 'ADJ':{'nice':500,'good':100}},
                                       'nonterminals':{'S':{'NP@VP':1000},'NP':
{'NP@NP':540}}}
    return:
        rules prob: dict(dict(dict)) --- a dictionary that has a form like:
                               rules prob = {'terminals':{'NP':{'the':0.6,'an':
0.3, '<unk>':0.1},
                                                            'ADJ':{'nice':0.6,'goo
d':0.3,'<unk>':0.1},
                                                            'S':{'<unk>':0.01}}}
                                              'nonterminals':{'S':{'NP@VP':0.99}}
    rules_prob = copy.deepcopy(rules counts)
    unk = ' < unk > '
    ### YOUR CODE HERE
    for dicts in rules prob['terminals'].values():
        summ = 0
        for count in dicts.values():
            summ += count
        for word, count in dicts.items():
            dicts[word] = count / (summ + 1)
        dicts[unk] = 1 / (summ + 1)
    for key, dicts in rules prob['nonterminals'].items():
        summ = 0
        for count in dicts.values():
            summ += count
        for word, count in dicts.items():
            dicts[word] = count / (summ + 1)
        if key not in rules prob['terminals']:
            rules prob['terminals'][key] = {unk:(1/(summ+1))}
    ### END OF YOUR CODE
    return rules prob
```

In [20]:

```
s_rules_prob = smooth_rules_prob(train_rules_dict)
terminals.add('<unk>')
```

```
In [21]:

print(s_rules_prob['nonterminals']['S']['NP-SBJ@S|<VP-.>'])
print(s_rules_prob['nonterminals']['NP-SBJ-1@S|<VP-.>'])
print(s_rules_prob['nonterminals']['NP']['NNP@NNP'])
print(s_rules_prob['terminals']['NP'])

0.1300172371337109
0.025240088648116228
0.039506305917861376
{'<unk>': 5.389673385792821e-05}

In [22]:
len(terminals)

Out[22]:
```

Question 6

Estimate the probability of the first parse tree in the testing data "cnf_test" by using "s_rules_prob".

```
In [23]:
```

```
probability = 1
try:
    for rule in cnf_test[0].productions():
        lhs = rule.lhs()
        rhs = rule.rhs()
        if len(rhs) == 1: #terminal
            probability *= s_rules_prob['terminals'][lhs][rhs[0]]
        else:
            child = str(rhs[0]) + '@' + str(rhs[1])
            probability *= s_rules_prob['nonterminals'][lhs][child]
except KeyError: # nonterminal not found = (prob -> 0)
        probability = 0

print("Probability of the first parse tree in cnf_test is:", probability)
```

Probability of the first parse tree in cnf_test is: 0

CKY Algorithm

Similar to the Viterbi algorithm, the CKY algorithm is a dynamic-programming algorithm. Given a PCFG $G=(N,\ \Sigma,\ S,\ R,\ q)$, we can use the CKY algorithm described in class to find the highest scoring parse tree for a sentence.

First, let us complete the *CKY* function from scratch using only Python built-in functions and the Numpy package.

The output should be two dictionaries π and bp, which store the optimal probability and backpointer information respectively.

Given a sentence $w_0, w_1, \ldots, w_{n-1}, \pi(i, k, X), bp(i, k, X)$ refer to the highest score and backpointer for the (partial) parse tree that has the root X (a non-terminal symbol) and covers the word span w_i, \ldots, w_{k-1} , where $0 \le i < k \le n$. Note that a backpointer includes both the best grammar rule chosen and the best split point.



Question 7

Implement **CKY** function and run the test code to check your implementation.

In [24]:

```
def CKY(sent, rules prob):
    111
    params:
        sent: list[str] --- a list of strings
        rules prob: dict(dict(dict)) --- a dictionary that has a form like:
                                            rules prob = {'terminals':{'NP':{'th
e':0.6, 'an':0.3, '<unk>':0.1},
                                                                        'ADJ':{'ni
ce':0.6, 'good':0.3, '<unk>':0.1},
                                                                        'S':{'<unk
>':0.01}}}
                                                           'nonterminals':{'S':{'N
P@VP':0.99}}
   return:
        score: dict(dict) --- score[(i,i+span)][root] represents the highest sco
re for the parse (sub)tree that has the root "root"
                          across words w_i, w_{i+1},..., w_{i+span-1}.
        back: dict(dict) --- back[(i,i+span)][root] = (split , left child, right
child); split: int;
                         left child: str; right child: str.
    111
    score = defaultdict(dict)
    back = defaultdict(dict)
    sent len = len(sent)
    ### YOUR CODE HERE
    for i in range(0, sent len):
        term = sent[i]
        for A, dicts in rules prob['terminals'].items():
            if term in dicts:
                score[(i, i+1)][A] = dicts[term]
                back[(i, i+1)][A] = (-1, term, '')
    for span in range(2, sent len + 1):
        for begin in range(0, sent_len - span + 1):
            end = begin + span
            for split in range(begin + 1, end):
                for A in rules prob['nonterminals'].keys():
                    for key in rules prob['nonterminals'][A].keys():
                        B = \text{key.split('0')[0]}
                        C = \text{key.split('@')[1]}
                        if (B in score[(begin, split)].keys()) and (C in score[(
split, end)].keys()):
                            updated score = rules prob['nonterminals'][A][key] *
                                             score[(begin, split)][B] *\
                                             score[(split, end)][C]
                             if (A not in score[(begin, end)]) or (updated score
> score[(begin, end)][A]):
                                 score[(begin, end)][A] = updated_score
                                back[(begin, end)][A] = (split, B, C)
    ### END OF YOUR CODE
    return score, back
```

Question 8

Implement **build tree** function to reconstruct the parse tree.

In [25]:

```
def build tree(back, root):
    Build the tree recursively.
    params:
        back: dict() --- back[(i,i+span)][X] = (split , left child, right chil
d); split:int; left child: str; right child: str.
        root: tuple() --- (begin, end, nonterminal symbol), e.g., (0, 10, 'S
    return:
        tree: nltk.tree.Tree
    begin = root[0]
    end = root[1]
    root label = root[2]
    ### YOUR CODE HERE
    split, left node, right node = back[(begin, end)][root label]
    if right_node != '':
        left_tree = build_tree(back, (begin, split, left_node))
        right tree = build tree(back, (split, end, right node))
        tree = nltk.tree.Tree(root label, [left tree, right tree])
    else:
        tree = nltk.tree.Tree(root label, [left node])
    ### END OF YOUR CODE
    return tree
```

Question 9 & 10

- Use CKY function to compute the max probability for the sentence of the first parse tree in the testing data "cnf_test".
- Generate and display the parse tree of the sentence.

In [26]:

```
test_rules, test_rules_counts = collect_rules(cnf_test)
test_nonterminals = collect_nonterminals(test_rules)
test_terminals = collect_terminals(test_rules)

test_rules_dict = build_pcfg(test_rules_counts)

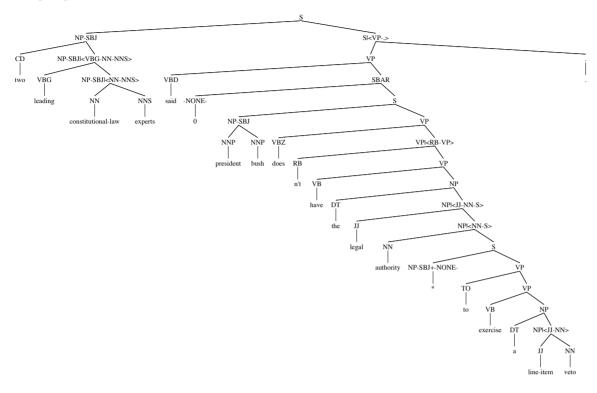
test_rules_prob = smooth_rules_prob(test_rules_dict)
test_terminals.add('<unk>')

test_sent = cnf_test[0].leaves()
test_score, test_back = CKY(test_sent, test_rules_prob)
```

```
In [27]:
```

```
test_tree = build_tree(test_back, (0, len(test_sent), 'S'))
test_tree
```

Out[27]:



Question 11

Run the remaining code to test your model on test data "cnf_test".

In [28]:

```
def set leave index(tree):
    Label the leaves of the tree with indexes
        tree: original tree, nltk.tree.Tree
    Return:
        tree: preprocessed tree, nltk.tree.Tree
    for idx, in enumerate(tree.leaves()):
        tree location = tree.leaf treeposition(idx)
        non terminal = tree[tree location[:-1]]
        non terminal[0] = non terminal[0] + " " + str(idx)
    return tree
def get nonterminal bracket(tree):
    Obtain the constituent brackets of a tree
        tree: tree, nltk.tree.Tree
    Return:
        nonterminal brackets: constituent brackets, set
    nonterminal brackets = set()
    for tr in tree.subtrees():
        label = tr.label()
        #print(tr.leaves())
        if len(tr.leaves()) == 0:
            continue
        start = tr.leaves()[0].split('_')[-1]
        end = tr.leaves()[-1].split('_')[-1]
        if start != end:
            nonterminal brackets.add(label+'-('+start+':'+end+')')
    return nonterminal brackets
def word2lower(w, terminals):
    Map an unknow word to "unk"
    return w.lower() if w in terminals else '<unk>'
```

In [29]:

```
correct count = 0
pred_count = 0
gold count = 0
for i, t in enumerate(cnf test):
   #Protect the original tree
   t = copy.deepcopy(t)
   sent = t.leaves()
   #Map the unknow words to "unk"
   sent = [word2lower(w.lower(), terminals) for w in sent]
   #CKY algorithm
   score, back = CKY(sent, s rules prob)
   candidate tree = build tree(back, (0, len(sent), 'S')) #, nonterminals)
   #Extract constituents from the gold tree and predicted tree
   pred_tree = set_leave_index(candidate tree)
   pred brackets = get nonterminal bracket(pred tree)
    #Count correct constituents
   pred count += len(pred brackets)
   gold tree = set leave index(t)
   gold brackets = get nonterminal bracket(gold tree)
   gold count += len(gold brackets)
   current_correct_num = len(pred_brackets.intersection(gold brackets))
   correct count += current correct num
   print('#'*20)
   print('Test Tree:', i+1)
   print('Constituent number in the predicted tree:', len(pred brackets))
   print('Constituent number in the gold tree:', len(gold brackets))
   print('Correct constituent number:', current correct num)
recall = correct count/gold count
precision = correct count/pred count
f1 = 2*recall*precision/(recall+precision)
```

```
######################
Test Tree: 1
Constituent number in the predicted tree: 20
Constituent number in the gold tree: 20
Correct constituent number: 14
######################
Test Tree: 2
Constituent number in the predicted tree: 54
Constituent number in the gold tree: 54
Correct constituent number: 30
#####################
Test Tree: 3
Constituent number in the predicted tree: 30
Constituent number in the gold tree: 30
Correct constituent number: 23
######################
Test Tree: 4
Constituent number in the predicted tree: 17
Constituent number in the gold tree: 17
Correct constituent number: 16
######################
Test Tree: 5
Constituent number in the predicted tree: 32
Constituent number in the gold tree: 32
Correct constituent number: 26
#####################
Test Tree: 6
Constituent number in the predicted tree: 40
Constituent number in the gold tree: 40
Correct constituent number: 18
######################
Test Tree: 7
Constituent number in the predicted tree: 22
Constituent number in the gold tree: 22
Correct constituent number: 7
######################
Test Tree: 8
Constituent number in the predicted tree: 18
Constituent number in the gold tree: 18
Correct constituent number: 6
#####################
Test Tree: 9
Constituent number in the predicted tree: 28
Constituent number in the gold tree: 28
Correct constituent number: 16
######################
Test Tree: 10
Constituent number in the predicted tree: 40
Constituent number in the gold tree: 40
Correct constituent number: 8
In [30]:
print('Overall precision: {:.3f}, recall: {:.3f}, f1: {:.3f}'.format(precision,
recall, f1))
Overall precision: 0.545, recall: 0.545, f1: 0.545
```