

Sheet1

logical cannibals: determine a particular cannibal(C) always lies or tells the truth; ask that cannibal exactly one question

A) Why asking "Are you a liar?" is not helpful?

B) Is it possible to live? If no, prove one question not enough. If yes, the question.

"Are you either deceitful or truthful?": must be one of two given.

(D | T) XOR?

D T

n y no can only be a liar, yes can only be truthful

Are you a liar?

y indeterminate = true from liar or false from truthful

n could be either true or false

4. encounter two knights or knaves, A and B. determine, if possible, what A and B are, if as below..

If you cannot determine what these two people are, can you draw any conclusions?

A: One reference for every two inputs?

A) A says "At least one of us is a knave", B says nothing

B) A says "The two of us are both knights", B says "A is a knave"

C) A says "I am a knave or B is a knight", B says nothing

D) Both A and B say "I am a knight"

E) A says "We both are knaves", B says nothing

A	B	C	D	E
a b	a b	a b	a b	a b
0 0	0 0	0 0	0 0	0 0
0 1	0 1	0 1	0 1	0 1
1 0	1 0	1 0	1 0	1 0
1 1	1 1	1 1	1 1	1 1

5. 50 senators: given. How many honest and dishonest senators do you have in the senate?

Given: $t=50$ $(h | d) \ \&\& \text{ (at least one honest) } \ \&\& \text{ (at least 1 of 2 dishonest)}$

(i) each either honest or dishonest $t=d+h$ $(h | d) = \text{binary choice}$

(ii) at least one honest $h \geq 1$ $(\text{at least one honest}) = h \geq 1$

(iii) in any two, at least one dishonest $(\text{at least 1 of 2 dishonest}) = h < 2$

Each given must be satisfied individually.

The only way to guarantee (iii) is to never have more than one honest senator.

solve for h; $1 \leq h < 2 = 1$

solve for d; $t-h = 50-1 = 49$