

# (E) Use the Force (1/2)

E1.

- a. you must go
- b. I think this one is strong with the force
- c. please don't forget to pick up milk before coming home tonight

E2.

- a. [ Use < [ force Luke ] the > ]
- b. < Luke < [ the force ] Use > > MORE POSSIBLE
- c. < Luke < force < the Use > > MORE POSSIBLE
- d. NOT POSSIBLE
- e. < [ the < Luke force > ] Use >

E3. 24 (4!)

E4. 22

This can be done by enumeration or by noting that all permutations of 3 items are Yoda-isms and that placing two adjacent sequential items (i.e. the permutation contains e.g. 23 or 32) yields a sequence of 3 items after the first rule application; there are only 2 permutations of 4 items that don't place two adjacent sequential items (2413 and 3142).

E5.

- a. Permutations: 12 Yoda-isms: 12

Since  $4! = 24$  (from above) and each sequence has a twin (where the first "do" can stand in for the second) we can divide by 2. Any sequence is identical to the one where 1 and 3 are swapped; it can be seen that the two non-Yoda-ism cases are equivalent to Yoda-ism cases so all are Yoda-isms.

- b. Permutations: 120 Yoda-isms: 90

$5! = 120$  Note that any sequence of 4 items in either of the 2 bad-4 patterns (call them a and b) will result in a fail, regardless of where the 5th item is placed. So 52413, 25413....24135. But let the sequence "1235" map to "1234" and then its permutation, "2513" is non-Yoda-ism no matter where the 4 is placed. 5 sets of 4 items x 5 configurations of those 4 (i.e. where to place the 5th) x 2 patterns = 50. But some of those 50 are duplicates. Note:

2413 3142

2513 3152

2514 4152

3514 4153

3524 4253

(the sequence of 4 items in configurations a and b). Each vertical pair contains 2 duplicates. E.g. 2413 and 2513 both yield 25413 and 24513. That's 4 pairs x 2 duplicates x 2 configurations = 16 duplicates. And there are 4 "twins" between configurations a and b; each yields a single duplicate:

2413 - 4153 (24153)

2513 - 4253 (42513)

3524 - 3152 (31524)

3514 - 3142 (35142)

Note 2514 and 4152 are not twins, so  $50 - 16 - 4 = 30$ , which are the non-Yoda-ism permutations.

$$120 - 30 = 90$$



## (E) Use the Force (2/2)

c. Permutations: 60      Yoda-isms: 52

$5!/2 = 60$  per above. From the above table note that any sequence of 4 containing both 3 and 4 will have identical patterns that are Yoda-isms (e.g. 2413 = 2314, which is a Yoda-ism, no matter where the 5 is placed). That leaves 2513 and 3152 (2514/4152 are redundant to them). That's  $5 \times 2 = 10$  cases, but of those 10 the placement of the 4 on either side of the 3 are identical, so eliminate 2.  $60 - 10 - 2 = 52$ .

