

Problem 1

a.

```
1 C = 'C UYGHARMZ IUWMPRWIR GAIR YVRMP MBHMZWMPUM C VMMXWPE YV PYR VCZ 2
2 F = {}
3 for i in range(ord('A'),ord('Z')+1):
4     F[chr(i)] = 0
5 for letter in C:
6     if letter != ' ':
7         F[letter] += 1
8 F = dict(sorted(F.items()))
9 for alphabet in F.keys():
10    print(f'{alphabet} : {F[alphabet]}')
```

PROBLEMS 8 OUTPUT DEBUG CONSOLE TERMINAL PORTS Code + - [] [X] ...

```
A : 2
B : 2
C : 12
D : 6
E : 4
F : 0
G : 5
H : 3
I : 4
J : 0
K : 2
L : 1
M : 19
N : 5
O : 1
P : 12
Q : 2
R : 9
S : 3
T : 1
U : 6
V : 7
W : 9
X : 6
Y : 12
Z : 9
```

b.

Table 3: Ciphertext to plaintext mapping

Ciphertext	A	B	C	D	E	F	G	H	I	J	K	L	M
	0	1	2	3	4	5	6	7	8	9	10	11	12
Plaintext	U	X	A	D	G	J	M	P	S	V	Y	B	E
	20	23	0	3	6	9	12	15	18	21	24	1	4
Ciphertext	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
	13	14	15	16	17	18	19	20	21	22	23	24	25
Plaintext	H	K	N	V	T	W	Z	C	F	I	L	O	R
	7	10	13	21	19	22	25	2	5	8	11	14	17

c.

$$C = 9P + 2 \pmod{30}$$

d.

$$a = 9, b = 2$$

e.

Key size is **26!**

Yes, it is approximately equal to 2^{88} .

Problem 2

a.

$$\Phi(30) * 30 = 8 * 30 = \mathbf{240}$$

b.

$$a = 1: a^{(-1)} = 1, \text{ since } 1 * 1 \equiv 1 \pmod{30}$$

$$a = 7: a^{(-1)} = 13, \text{ since } 7 * 13 \equiv 91 \equiv 1 \pmod{30}$$

$$a = 11: a^{(-1)} = 11, \text{ since } 11 * 11 \equiv 121 \equiv 1 \pmod{30}$$

$$a = 13: a^{(-1)} = 7, \text{ since } 13 * 7 \equiv 91 \equiv 1 \pmod{30}$$

$$a = 17: a^{(-1)} = 23, \text{ since } 17 * 23 \equiv 391 \equiv 1 \pmod{30}$$

$$a = 19: a^{(-1)} = 19, \text{ since } 19 * 19 \equiv 361 \equiv 1 \pmod{30}$$

$$a = 23: a^{(-1)} = 17, \text{ since } 23 * 17 \equiv 391 \equiv 1 \pmod{30}$$

$$a = 29: a^{(-1)} = 29, \text{ since } 29 * 29 \equiv 841 \equiv 1 \pmod{30}$$

c.

$$8 = 4a + b \pmod{30}$$

$$26 = 10a + b \pmod{30}$$

$$7 = 27a + b \pmod{30}$$

Trial-and-error : **a = 13, b = 16**

d.

$$13 * 7 = 1 \pmod{30}$$

$$y = 13x + 16 \pmod{30}$$

$$\Leftrightarrow x = (y - 16)/13 \pmod{30}$$

$$\Leftrightarrow x = 7(y - 16) \pmod{30}$$

$$\Leftrightarrow x = 7y - 112 \pmod{30}$$

$$\Leftrightarrow x = 7y + 8 \pmod{30}$$

$$\mathbf{c = 7, d = 8}$$