

## Homework 6

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10:10 PM

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## Problem 1

$$1. \text{err}_{\text{Gser}} = \Pr(\text{label} = x, \text{Gser} \neq x) \\ = 1/k \cdot (k-1/k) = k-1/k^2$$

$$2. \text{err}_{\text{Zavulon}} = \sum \Pr(\text{label} = x, \text{Zavulon} \neq x) \\ = \sum_i^k w_i (1 - w_i) = \sum_i^k w_i - w_i^2 \\ = 1 - \sum_i^k w_i^2$$

## Problem 2

$$1. \begin{array}{ll} x=1,4 & Y=1 \\ x=2,3 & Y=0 \end{array} \quad \begin{array}{ll} h(x)=1, & x=2,3,4 \\ h(x)=0, & x=1 \end{array}$$

$$\text{err}_{D_1} h(x) = 3/4$$

$$2. h_4(x) = 1 \text{ if } x > 4 \text{ and } 0 \text{ o.w.}$$

$$\begin{array}{ll} x=1,4 & Y=1 \\ x=2,3 & Y=0 \end{array} \quad \begin{array}{ll} h(x)=1 & x=4 \\ h(x)=0 & x=1,2,3 \end{array}$$

$$\text{err}_{D_1} h_4(x) = 1/4$$

We do have a non-zero bias when the concept class is  $C$  and the data distribution  $D_1$ .

$$\begin{aligned}
 3. \text{err}_{D_2} h(x) &= \sum \Pr(Y=0, h(x)=1, x=i) + \\
 &\quad \sum \Pr(Y=1, h(x)=0, x=i) \\
 &= (8/10)(1)(1/4) + (7/10)(1)(1/4) + (6/10)(1)(1/4) \\
 &\quad + (1/10)(1)(1/4) = 22/40 \quad \text{err}_{D_2} h(x) = 22/40
 \end{aligned}$$

$h_4(x) = 1$  if  $x > 4$  and 0 o.w.

$$\begin{aligned}
 \text{err}_{D_2} h_4(x) &= \sum \Pr(Y=1, h(x)=0, x=i) \\
 &= (1/10)(1)(1/4) + (2/10)(1)(1/4) \\
 &\quad + (3/10)(1)(1/4) + (4/10)(1)(1/4) = 10/40
 \end{aligned}$$

$$\text{err}_{D_2} h_4(x) = 10/40$$

We have a non-zero bias when the concept class is  $C$  and distribution  $D_2$ .

### Problem 3

	Train error	Test error
3	.136	.64
7	.204	.47
10	.556	.23
15	.458	.4033
20	.186	.1567

Words	Train	Test
1	remember	remember
2	lack	france
3	france	lack
4	universite	html
5	monday	linguist
6	editor	title
7	otherwise	england
8	ling	clearly
9	marker	universite
10	linguist	reach