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В пособии излагаются основные понятия и определения теории параллельных вычислений. Рассматриваются основные принципы построения программ на языке «Си» для многоядерных и многопроцессорных вычислительных комплексов с общей памятью. Предлагается набор заданий для проведения лабораторных и практических занятий.

Учебное пособие предназначено для студентов, обучающихся по магистерским программам направления «09.04.04 – Программная инженерия», «09.04.01 – Информатика и вычислительная техника», и может быть использовано выпускниками (бакалаврами и магистрантами) при написании выпускных квалификационных работ, связанных с проектированием и исследованием многоядерных и многопроцессорных вычислительных комплексов.



Университет ИТМО – ведущий вуз России в области информационных и фотонных технологий, один из немногих российских вузов, получивших в 2009 году статус национального исследовательского университета. С 2013 года Университет ИТМО – участник программы повышения конкурентоспособности российских университетов среди ведущих мировых научно-образовательных центров, известной как проект «5 в 100». Цель Университета ИТМО – становление исследовательского университета мирового уровня, предпринимательского по типу, ориентированного на интернационализацию всех направлений деятельности.

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## Introduction

Currently, most microprocessors are multi-core. This applies not only to desktop computers, but also to mobile phones and tablets (so far, only embedded computing systems are an exception). To fully realize the potential of a multi-core system, a programmer needs to use special methods of parallel programming, which are becoming increasingly popular in industrial programming. However, parallel programming methods are significantly more difficult to master than traditional sequential program writing methods.

The purpose of this study book is to describe practical tasks (laboratory work) that can be used to consolidate the theoretical knowledge gained as part of a lecture course on parallel programming technologies. In addition, the book summarizes the basic principles of parallel programming.

While programming multi-threaded applications, you have to resolve conflicts that arise when simultaneously accessing the shared memory of several threads. The following three conceptually different approaches are currently used to synchronize simultaneous access to shared memory:

1. **Explicit use of blocking primitives** (mutexes, semaphores, condition variables). This approach historically appeared first and is now the most common and supported in most programming languages. The disadvantage of this method is a rather high entry threshold, since the programmer is required to manage blocking primitives in the "manual mode", tracking conflict situations when accessing shared memory.
2. **Software Transactional Memory (STM)**. This method is easier to learn and use than the previous one, however it still has limited support in compilers, and it will also be able to fully manifest itself with the wider distribution of processors with hardware support for STM.
3. **Non-blocking algorithms** (lockless, lock-free, wait-free algorithms). This method implies a complete rejection of the use of blocking primitives with the help of complex algorithmic tricks. Moreover, for the correct functioning of the non-blocking algorithm, it is required that the processor supports special atomic (conflict-free) operations of the form "compare and exchange" (cmpxchg, "compare and swap"). Currently, most processors have this type of operation as part of the instruction system (with rare exceptions, for example: "SPARC 32").

The methodological manual proposed is devoted to the first of the listed methods, since he received the greatest coverage in literature and the greatest

application in industrial programming. Two other methods may be the subject of in-depth training courses on parallel computing.

# 1 Theoretical Foundations of Parallel Computing

## 1.1 History of parallel computing

Conversation about the development of parallel computing is usually begun with the history of the development of supercomputers. However, the world's first supercomputer CDC6600, created in 1963, had only one central processor, so it can hardly be considered a full-fledged SMP system.

The third-ever CDC8600 supercomputer was designed to use four processors with shared memory, which suggests the first use of SMP, but the CDC8600 was never released since its development was discontinued in 1972.

Only in 1983 was it possible to create a working supercomputer (Cray X-MP), which used two central processors that used shared memory. It is worth noting that a little earlier (in 1980) the first Russian multiprocessor computer Elbrus-1 appeared, however, it was significantly inferior in performance to supercomputers of that time.

Already in 1994 it was possible to freely buy a desktop computer with two processors, when ASUS released its first motherboard with two sockets - connectors for installing processors.

The next step in the development of SMP-systems was the emergence of multi-core processors. The first multi-core processor for mass use was POWER4, released by IBM in 2001. But the truly widespread multi-core architecture received only in 2005, when AMD and Intel released their first dual-core processors.

The figure 1 shows how much CPU with a different number of cores occupied when creating supercomputers at different times (according to the materials of the site (<http://top500.org>)). Закрашенные области помечены цифрами 1, 2, 4, 6, 8, 10, 12, 16 для обозначения количества ядер. Ширина области по вертикали равна относительной частоте использования процессоров соответствующего типа в рассматриваемом году.



*Рис. 1: Frequency of using processors with different number of cores when creating supercomputers*

As you can see, the active use of dual-core processors in supercomputers began already in 2002, and by about 2005 completely disappeared, whereas in desktop computers their use was only just beginning in 2005. Based on this, you can make a simple forecast of the prevalence of multi-core "desktop" processors by the desired year, if we assume that they in general outline repeat the development of multi-core architectures of supercomputers.

## 1.2 Terms and Definitions

**Parallel computing** – A method of organizing calculations in which the program is a set of interacting modules that work simultaneously. Typically, the concept of concurrency may include:

1. **Instruction level parallelism** - one processor core can execute several instructions simultaneously. For example, this technology is implemented in Intel Pentium 4 processors.
2. **Hypertreading** - one processor core is designed so that it can do the work of two threads at once. Implemented in the Intel Core i7 series processors. When performing laboratory work, it is important to disable this in the BIOS (if the processor is compatible with this technology), since it significantly affects the performance of parallel acceleration and efficiency.
3. **Multi core programming** - a method for solving computational problems with simultaneous execution of program parts on different physical computing cores. All cores have shared memory banks, as they are located on the same computer. It includes the case of a multi-core processor architecture and a multi-processor architecture of a system in which there are several processors, since in both cases the program runs on several cores of one or many processors, but on one physical computer.
4. **Distributed computing** - a way to solve time-consuming computing problems using several computers, most often combined into a parallel computing system. Different parts of the program can run on different computers.

Usually the last two concepts are physically implemented using architectures. *SMP* и *MMP*. More details about these architectures can be found in the next section.



It is important to see difference between the concepts of parallel computing and parallel technologies. Let analyze the following concepts, which, although they are parallel technologies (at the core or internuclear interaction level), however, are not parallel calculations, but often textbf by mistake are assigned to them:

- *Pipeline data processing (superscalarity)* represents the simultaneous processing by the processor of several instructions, in which at one time for each of the instructions a different execution step is performed. For example, if any processor can simultaneously receive, decode, and execute an instruction, then when it receives the first instruction, it can decode the second and execute the third (figure ??). This way of organizing calculations is not parallel computing, because the instructions are still executed sequentially, and only one core is involved.

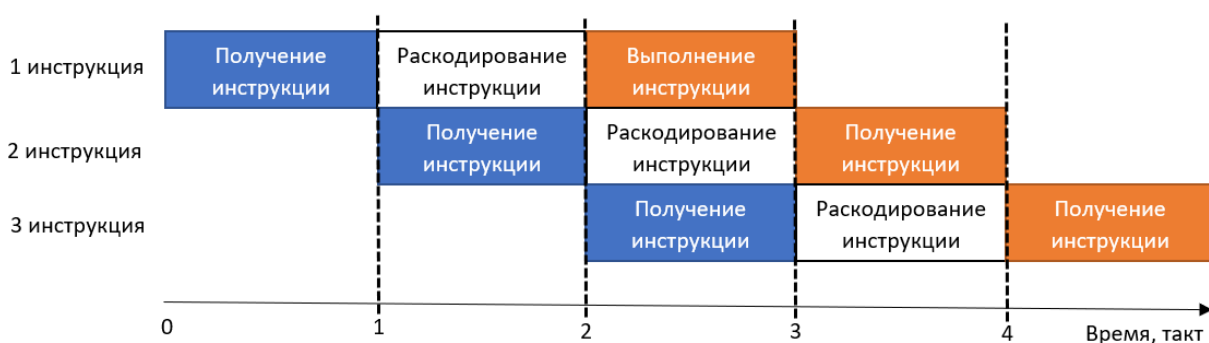


Рис. 2: Instruction pipelining

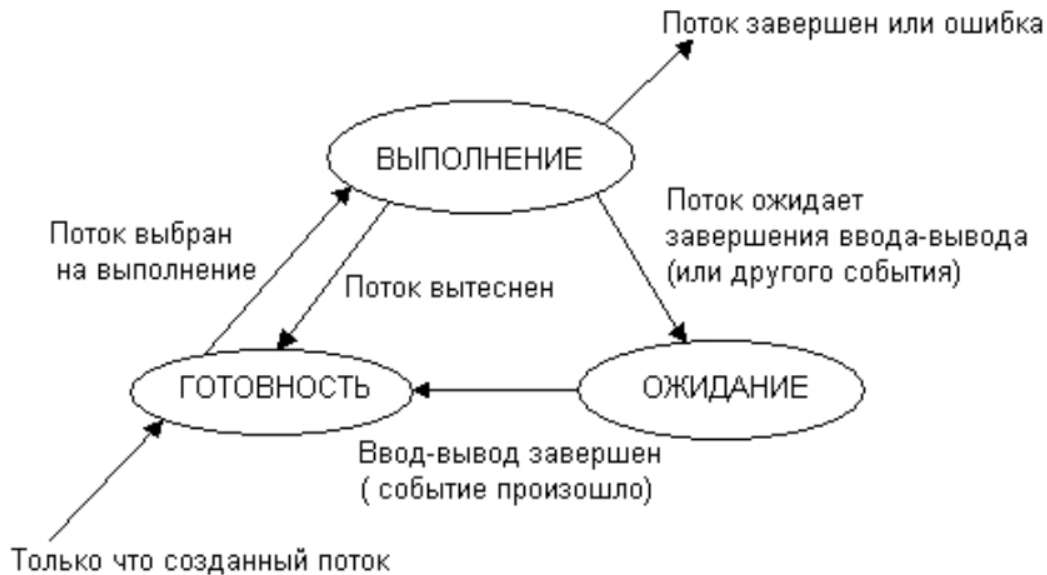
- *SIMD-extensions (MMX, SSE)* provide concurrency at the data level. For example, a processor can simultaneously multiply 4 numbers instead of one using the SSE instruction. However, the command flow still remains single, i.e. one program instruction is executed in a period of time, which is not the case of parallel computing.
- *Preemptive Multitasking* organized by the operating system. Several processes are in the execution queue and the OS decides how to manage the processor time between them. If the first thread is given a higher priority than the second, then the OS will allocate more time to execute the first thread, only one thread will be executed at a time, therefore, preemptive multitasking is also not included in the concept of parallel computing.

Various parallelization technologies are used to organize parallel computing:

- **Process** - the most heavyweight mechanism used for parallelization. Each process has its own independent address space, so data synchronization between processes is long and complicated. May include several threads of execution.
- **Thread** It runs independently of other threads, but has a common address space with other threads in the same process. At this level, data synchronization mechanisms are used (will be discussed later).
- **Fiber** - lightweight thread of execution. Like threads, fiber has a common address space, however, it uses joint multitasking instead of preemptive one. The OS does not switch the context from one thread to another, instead, the main thread itself allocates time for the child fiber to work, or is blocked logically (that is, the programmer controls the fiber life cycle). Also, all fibers work on one core, unlike threads, which can work on different kernels.

For a better understanding of threads, we will schematically consider its life cycle. Figure 3 shows that the flow can be in three states - readiness, expectation and fulfillment. After creating the stream, it is in a ready state. Then, the OS decides to change its state (clarifying multitasking). For fiber, the life cycle is the same, but the programmer or synchronization mechanisms control the transitions between them.

Different standards of programming languages can add new states to the life cycle of threads, for example, blocking a thread, interrupting a thread, and others, but the general scheme of work remains the same.



*Рис. 3: Thread lifecycle*

Among programmers there are concepts of **thread-safe** и **reentrant** functions, however, they may have different meanings in different communities. Definitions are written from various sources in table 1.

*Таблица 1: Definitions of thread-safe and reentrant functions*

| Источник определения | Thread-safe  | Reentrant   |
|----------------------|--|---|
| Qt                   | Внутри функции обращение ко всем общим переменным осуществляется строго последовательно, а не параллельно (Thread-safe является reentrant, но не наоборот) | При вызове функции одновременно несколькими потоками гарантируется правильная работа, только если потоки не используют общие данные |
| Linux                | Функция показывает правильные результаты, даже если вызвана несколькими тредами одновременно   | Функция показывает правильные результаты, даже если повторно вызвана изнутри себя   |
| POSIX                | ?  | Функция показывает правильные результаты, даже если вызвана несколькими тредами одновременно  |

Consider examples of functions that fit the definition of the Linux

community.

```
1  int t;
2  void swap(int *x, int *y) {
3      t = *x;
4      *x = *y;
5      // hardware interrupt
6      *y = t;
7  }
8  void interrupt_handler() {
9      int x = 1, y = 2;
10     swap(&x, &y);
11 }
```

This function is not thread safe, not reentrant, because all threads calling it will use the common variable `t`. If you call the function inside itself, then the value of `t` is overwritten and the parent function will not work correctly. Let's try to fix these errors by declaring a variable of type `t` `__threadint`.

```
1  __threadint t;
2  void swap(int *x, int *y) {
3      t = *x;
4      *x = *y;
5      // hardware interrupt
6      *y = t;
7  }
8  void interrupt_handler() {
9      int x = 1, y = 2;
10     swap(&x, &y);
11 }
```

Now the compiler will create a copy of the variable for each thread `t` and the function will become thread safe, however, it is still not reentrant for the same reason. We will save the value of the global variable `t` at the beginning of the function and restore it at the end.

```
1  int t;
2  void swap(int *x, int *y) {
3      int s;
4      s = t; // save global variable
5      t = *x;
6      *x = *y;
7      // hardware interrupt
8      *y = t;
9      t = s; // restore global variable
10 }
11 void interrupt_handler() {
12     int x = 1, y = 2;
13     swap(&x, &y);
14 }
```

The new function is reentrant, but again non thread-safe. Finally, we give an example of a standard and proper implementation of swap(), which is thread safe and reentrant:

```
1 void swap(int *x, int *y) {  
2     int t = *x;  
3     *x = *y;  
4     // hardware interrupt  
5     *y = t;  
6 }  
7 void interrupt_handler() {  
8     int x = 1, y = 2;  
9     swap(&x, &y);  
10 }
```

### 1.3 Classification of parallel systems (architectures)

By physical architecture, parallel systems can be divided into 2 types:

1. **SMP** (Shared Memory Parallelism, Symmetric MultiProcessor system) – multiprocessing, multicore, GPGPU.
2. **MPP** (Massively Parallel Processing) – cluster systems, GRID (distributed computing).

Next, we consider these two architectures in more detail.

**SMP** - architecture of multiprocessor systems in which two or more identical processors of comparable performance are connected in the same way to the shared memory (and peripheral devices) and perform the same functions (why, in fact, the system is called symmetrical). SMP systems are also called tightly coupled multiprocessors, since in this class of systems processors are closely connected to each other via a common bus and have equal access to all resources of the computing system (memory and input-output devices) and are controlled by all one copy of the operating system. In this architecture, all processors are located on the same physical machine, so they have common memory banks. There are two types of connecting processors to shared memory:

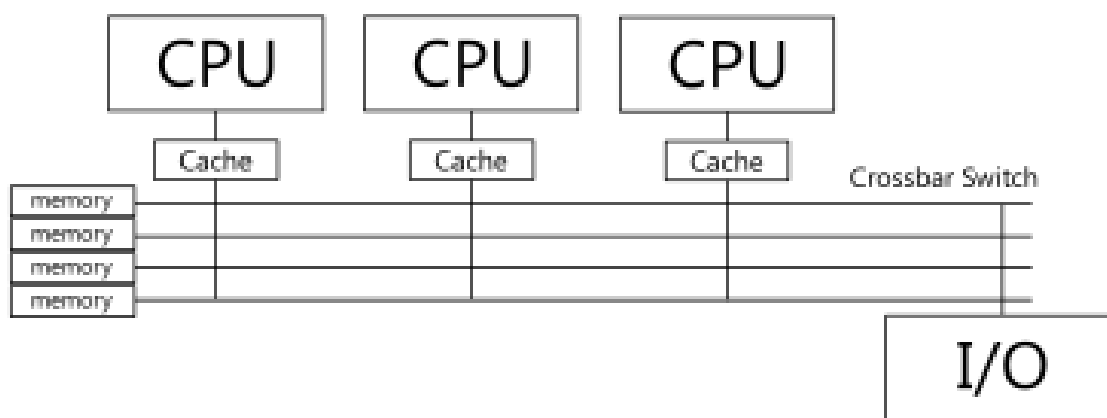
- The connection on the system bus is shown in the figure. 4. In this case, only one processor can access memory at any given moment, which imposes a significant limitation on the number of processors supported in such systems. The more processors, the greater the load on the shared bus, the longer each processor must wait until the bus is free to access the memory. A decrease in the overall

performance of such a system with an increase in the number of processors occurs very quickly, therefore, usually in such systems the number of processors does not exceed 2-4. An example of SMP machines with this method of connecting processors is any entry-level multiprocessor server.



*Puc. 4: SMP architecture. Processor connection via system bus*

- The crossbar switch is shown in the figure. 5. With this connection, the entire shared memory is divided into memory banks, each memory bank has its own bus, and the processors are connected to all buses, having access to any of the memory banks through them. Such a connection is technologically more complex, but it allows processors to access shared memory at the same time. This allows you to increase the number of processors in the system to 8-16 without a noticeable decrease in overall performance.



*Рис. 5: SMP architecture. Processor connection via dial-up connection*

The advantages of this approach are the high speed of data exchange between processors and the relative simplicity of software development. However, there may be problems with the scalability of the system (if there are only 2 sockets on the motherboard, you can't put 3 processors anymore).

**MMP** - architecture of multiprocessor systems, in which the memory between the processors is physically divided. On such systems, distributed computing is performed. The system is built from separate nodes containing a processor, a local memory bank, communication processors or network adapters, sometimes hard drives and other input-output devices. Access to the memory bank of this node is available only to processors from the same node. The nodes are connected by special communication channels (figure 6).



*Рис. 6: MMP Architecture*

The advantages of this approach are its good scalability (if necessary, to increase system performance it is enough to simply add more nodes). However,

the speed of interprocessor exchange is significantly reduced, since memory banks are now physically separated. Also, the cost of the software that distributes the calculations is very high.

In parallel programs, the developer often faces the problem of synchronization between threads. As a rule, problems arise when accessing memory and at the same time executing some critical sections of code - critical sections.

**Critical area** is the section of the program, which must be executed with the exclusive right of access to shared data referenced in this program. A process preparing to enter a critical area may be delayed if any other process is in progress at that time in a similar critical area.

This section will discuss in detail thread synchronization mechanisms at the program level.

The following methods are available for solving thread synchronization problems:

- **Atomic operations** are operations that are performed in their entirety or not at all. For example, a transaction to a database is an atomic operation. When two threads try to increment the same memory cell out of sync, the value can increase by 2, or maybe 1, depending on the behavior of the threads, since the increment operation is at least 3 assembler instructions. To avoid this, it is worth declaring the data type atomic (if there is one in this programming language / library). A special case of atomic operations is read-modify-write operations: compare-and-swap, test-and-set, fetch-and-add. The problem of the implementation of atomic operations will be raised in more detail in the section.

#### *1.6 Atomic operations in a multithreaded program.*

- **Semaphore** - an object that limits the number of threads that can enter this area of code. Typically, this number is set when the semaphore is initialized. Then, when capturing a semaphore by a thread, the number of threads that captured the semaphore is checked. If the maximum number of threads is reached, then the thread will wait until some of the threads that entered the code area release it. Often the use of semaphores is unjustified, since the overhead of creating and maintaining a semaphore is large. You should also avoid the "semaphore leak" a situation in which the thread does not exit the semaphore when the code area completes execution if the programmer forgot to free the resource.
- **Reader/writer semaphore** gives the threads *only* read or write permissions,



and while writing data to one thread, the rest of the threads do not have access to the resource. However, in such semaphores there may be a problem *resource starvation*, in which while streams will read data, other streams will not be able to write data for a long period of time or vice versa. A particular solution to this problem with equal priority of threads can be sequential access of threads in the queue to access and write.

- **Mutex** is a special case of a semaphore, in which only one thread can capture a given area of code. If the mutex serves several critical sections, only one thread can be in any of the critical sections. It is often used in the organization of critical section management, since it is "lighter" than the classical semaphore (it is enough to store one boolean variable instead of a counter), but unlike it, it is assumed that the same stream will capture and release the mutex. It should be noted that in the C++11, in addition to the standard mutex, there are various modifications of it: *recursive\_mutex* - mutex that allow re-entry into the critical section by the same stream. *timed\_mutex* - mutex with capture timer, and *recursive\_timed\_mutex*, combining the advantages of both versions.
- **Spinlock** is a lock in which a thread in a loop waits for a resource to free. It is not always the optimal solution, since the waiting thread works while waiting. Inside the code section, thread interruptions must be avoided to avoid deadlock.
- **Seqlock** - synchronization mechanism designed to quickly record a variable in multiple threads. The Linux kernel works as follows: the thread waits until the critical section is released (spinlock); when entering the section, the counter increments, the stream does its work. When exiting a section, the flow checks the counter value. If the counter value has not changed, it means that no one has written data at the moment and the stream exits the critical section, otherwise it reads the value of the variable again.
- **Knuth-Bendix completion algorithm** - One of the solutions to synchronization problems is the Knuth-Bendix algorithm from the course of discrete mathematics. With it, you can go from a sequential program to a cascading one. However, this algorithm does not work for all programs; sometimes it can go into an infinite loop or fail.

- **Barrier** - a part of code in which the state of threads is synchronized. For example, if a function in the main thread requires all child threads to finish their work, you can put a barrier in front of it. Then it will wait for the completion of the child threads, after which all threads will continue to work. An example of a barrier implementation may be a critical section, the code of which is allowed to be executed only by the last thread that requested execution. The rest of the threads should expect it. To do this, you need to know how many threads should come to the barrier.
- **Non-blocking algorithms.** It is often useful not to use standard locking techniques, but to make the algorithm non-blocking. In this case, the programmer must independently guarantee that critical sections of the code will not be executed simultaneously and the integrity of the shared memory. Another advantage of such algorithms is the safe handling of interrupts. Other synchronization technologies are often used to implement such algorithms: read-modify-write, CAS (see section 1.6) and etc.
- **RCU (read-copy-update)** - is an algorithm that allows threads to efficiently read data, leaving the data updated at the end of the algorithm, while guaranteeing relevant data. Only one thread can write data, but multiple threads can read data at once. This is achieved, for example, by atomic pointer substitution (CAS). Old versions of the data are stored for past hits, as long as they have at least one pointer. There are newer tools for replacing the pointer: a separate deadlock for writers or the membarrier mechanism used in recent versions of Linux. RCU can be useful in organizing data structures without explicit locks.
- **Monitor** - An object encapsulating a mutex and utility variables to provide secure access to a method or variable by multiple threads. The monitor characterizes that at one moment only one thread can execute any of its methods. For example, if we have a class (in C++ terms) Account with add methods \_money(), sub\_money(), it makes sense to make it a monitor so that there are no conflicts when conducting operations with the account.

However, it is not necessary to organize parallel computations using synchronization or locks. Some technologies offer an alternative approach to parallel computing:

- **Program Transactional Memory** - a memory model in which operations performed on memory cells are atomic. Advantages of use: ease of use (enclosing code blocks in a transaction block), lack of locks, however, if used incorrectly, performance may drop, as well as the inability to use operations that cannot be undone inside a transaction block. In the compiler, GCC is supported since version 4.7 as follows:
  1. `__transaction_atomic { ... }` — an indication that the code block is a transaction;
  2. `__transaction_relaxed { ... }` — an indication that the unsafe code inside the block does not lead to side effects;
  3. `__transaction_cancel` — explicit transaction cancellation;
  4. `attribute((transaction_safe))` — indication of a transaction-safe function;
  5. `attribute((transaction_pure))` — indication of function without side effects.
- **Actor model** - a mathematical model of parallel computing, in which the program is an actor objects that interact with each other and can create new actors, send and send messages to each other. The parallelism of computations within one actor is assumed. Each actor has an address to which you can send a message. Each actor works in a separate thread. The actor model is used to organize email, some SOAP web services, and etc.

Despite the large number of synchronization methods, it is most often necessary to proceed from the problem being solved. For example, if we want to make a general incremental integer variable for several threads, it makes no sense to create a mutex or semaphore, it is more optimal to make the variable atomic. Always consider the overhead of creating locks and development time.

## 1.4 Automatic parallelization of programs

Parallel computing is a rather complicated manual process, so it seems obvious that it needs to be automated using a compiler. Such attempts are made, however, the efficiency of auto-parallelization is not yet sufficient, because good indicators of parallel acceleration are achieved only for a limited set of simple for-cycles in which there are no data dependencies between iterations and the number of iterations cannot change after the start of the cycle. But even

if the two indicated conditions are satisfied in a certain for-cycle, but it has a complex non-obvious structure, then its parallelization will not be performed. Types of automatic parallelization:

- *Fully automatic:* participation of the programmer is not required, all actions are performed by the compiler.
- *Semi-automatic:* programmer gives instructions to the compiler in the form of special keys that allow you to adjust some aspects of parallelization.

Weaknesses of automatic parallelization:

- erroneous change in program logic
- speed reduction instead of increase.
- lack of manual parallelization flexibility.
- only cycles are efficiently parallelized.
- inability to parallelize programs with a complex algorithm of work.

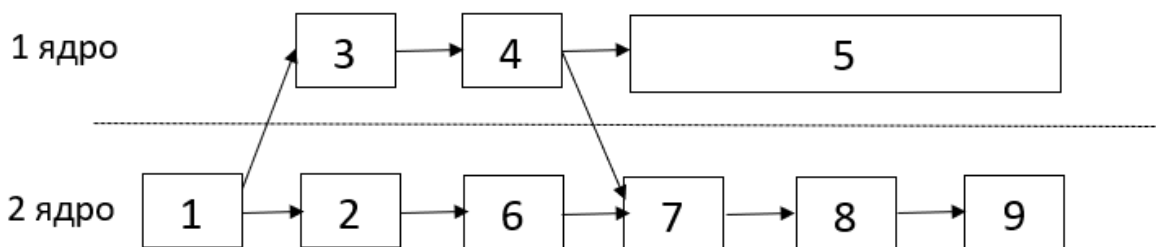
Here are examples of how the c-program in the src.c file can be automatically parallelized using some popular compilers:

- Compiler GNU Compiler Collection: `gcc -O3 -floop-parallelize-all -ftree-parallelize-loops=K -fdump-tree-parloops-details src.c`. In this case, the programmer can choose the value of the parameter K, which is recommended to be set equal to the number of cores (processors). Features of the auto-parallelization implementation in gcc are dedicated to an independent project:  
<https://gcc.gnu.org/wiki/AutoParInGCC>.
- Intel compiler: `icc -c -parallel -par-report file.cc`
- Oracle compiler: `solarisstudio -cc -O3 -xautopar -xloopinfo src.c`

## 1.5 The main approaches to parallelization

In practice, there are a large number of parallel computing patterns. However, all these patterns basically use three basic approaches to parallelization:

- **Data parallelization:** The programmer finds in the program an array of data whose elements the program sequentially processes in some function. Then the programmer tries to break this data array into blocks that can be processed in function independently of each other. Then the programmer starts several threads at once, each of which executes function, but at the same time processes data blocks different from other flows in this function.
- **Instruction parallelization:** The programmer finds in the program sequentially called functions, the process of which does not affect each other (such functions do not change common global variables, and the results of one are not used by the other). Then the programmer starts these functions in parallel threads.
- **Parallelization of information flows:** A program is a set of functions that can be performed, and several functions can expect the result of the previous ones. In this case, each core performs the function for which the data is already ready. Consider this method as an example of an abstract dual-core processor, as the most difficult to understand. The structural algorithm shown in the figure 7 consists of 9 functions, some of which use the result of the previous function in their work. We assume that function 3 uses the result of the function 1, and function 7 uses the result of functions 4 and 6, etc., and also function 5 is executed in time approximately as much as functions 7, 8, and 9 combined. Then, on a dual-core machine, this parallelization method will be the optimal solution.



*Рис. 7: An example of the operation of a structural algorithm on a dual-core processor*

The three methods described are easier to understand by analogy from everyday life. Let two students in the construction team be given the task of sweeping the street and painting the fence. If students decide to use data

parallelization, he will first sweep the street together, and then paint the fence together. If they decide to use parallelization according to the instructions, then one student will completely sweep the street, and the other will paint the entire fence at this time. This situation cannot be parallelized over the information flows, since these two actions are in no way dependent on each other. If we assume that they both need tools for work, then one of them must first go after them, and then both of them will begin to do their work.

In more cases, the decision to use the method is obvious due to the internal features of the parallelized program. The choice of method is determined by which one loads flows more evenly. Ideally, all threads should finish the work allocated to them approximately at the same time in order to optimally load the kernels (processors) and so that the threads that have finished their work do not stand idle while waiting for the completion of work by neighboring threads.

## **1.6 Atomic operations in a multithreaded program**

The main problem with parallel computing is the need to resolve conflicts while accessing the shared memory of several threads. To solve this problem, they usually try to streamline the access of streams to shared data using special tools - synchronization primitives. However, the question arises whether there are such atomic operations, the execution of which by several threads simultaneously does not require synchronization of actions, because these operations would be performed by the processor in one fell swoop, or, as they say, atomically (i.e., no other operation can push the previous atomic operation out of the processor before it is completed).

Almost all assembler instructions are such operations, since at a low level they use only those operations that are present in the processor command system, which means that they can be performed atomically (uninterruptedly). However, when compiling a C program, C language commands are usually translated into several assembler instructions. In this regard, the question arises about the possible existence of C-commands that are compiled into one assembler instruction. Such commands could not be "protected" by synchronization primitives (mutexes) in parallel computing.

However, there are very few such operations, and some of them can behave both atomically and non-atomically depending on the hardware platform for which the C program is compiled. Consider the simplest increment command of an integer variable (int type) in C: `w++`. You can easily verify (for example, using the gcc compiler's `S` key) that this command will be translated into three assembler instructions (take from memory, increase, put back):

```

1  movl  w, %ecx
2  addl  $1, %ecx
3  movl  %ecx, w

```

This means that it is not safe to perform the increment operation of a variable in several threads at the same time, because when executing assembler instruction 2, the thread can be interrupted and the processor transferred to another thread, which will receive an incorrect value of the underreduced variable.

It is logical to assume that assignment operations should not have the described problem. Indeed, in Assembler there is a separate instruction for writing the value of a variable to the specified address. Unfortunately, this assumption is not completely true: when assigning a variable of type char, this operation will be performed by a single assembler instruction. However, with other data types this cannot be said for sure. The general rule of thumb can be roughly stated as follows: "the atomicity of the assignment operation is guaranteed only for operations with data whose bit capacity does not exceed the processor bit capacity "

For example, when assigning an int variable to a 32-bit processor, one assembler instruction will be generated. However, when compiling the same operation on a 16-bit computer, two assembler instructions will be generated to write the low and high bits independently.

The formulated rule works with the assignment of variables and expressions, however, it cannot always be satisfied with the assignment of constants. Consider an example of C-code in which a 64-bit variable s (type uint64\_t) is assigned a large number, obviously exceeding the 32-bit value:

```

1  uint64_t s;
2  s = 99999999999999L;

```

This code will be translated into the following assembler code on a 64-bit processor:

```

1  movabsq $99999999999999, %rsi
2  movq  %rsi, s

```

As you can see, the assignment operation was translated into two assembler instructions, which makes it impossible to safely parallelize such an operation.

This rule applies not only to the assignment operation, but also to the operation of reading a variable from memory, so any of these operations in a thread-safe environment will have to be protected by mutexes or critical sections.

A special case of atomic data changes is structure changes. To do this, we need to use a CAS operation with a pointer to this structure. Performing such an operation, the processor will create a second data structure with the specified fields and compare it with the old version of the structure. If the value of at least one field has changed, then it will atomically replace the pointer. There is overhead in this: even a simple change of one field of the structure requires the creation of a full copy of the structure, then to replace the pointer.

## 1.7 Lock-free data structures

In multi-threaded programs, problems with thread collaboration usually occur when accessing shared resources. In addition to the blocking approach using synchronization primitives, they also use the non-blocking approach. To avoid race conditions, you can use special non-blocking data structures. This approach is based on the use of atomic variables and lock-free or wait-free objects.

A shared object is called a lock-free object if it guarantees that some thread completes the operation on the object in a finite number of steps, regardless of the results of other threads.

An object is wait-free if each thread completes an operation on an object in a finite number of steps.

The question may arise: why are non-blocking data structures needed, if synchronization primitives can be used to access the usual data structure. Lock-free structures have several advantages over blocking data structures. So, in terms of bandwidth, they exceed blocking ones by 1.5–3 times, however, both blocking and non-blocking queues have poor scalability with respect to the number of threads. In terms of the delay of elements in the queue, non-blocking queues also have better characteristics, but their advantage is quite small. Also, the use of synchronization primitives can lead to deadlock, and errors can also occur associated with forgetting to capture or release primitives.

Lock-free data structures do not contain locks and remain in a consistent state regardless of the number of threads accessing it at the same time. Such data structures can be organized using RMW - read, modify and write operations that occur atomically.

An example of RMW operation is CAS. In the C++ library, there are two options for implementing this operation: weak and strong (figure ??). Weak version may return false in case when the read value was equal to the expected one. Strong always returns the correct value.



```

bool
compare_exchange_weak(_Tp& __e, _Tp __i, memory_order __s,
                      memory_order __f) noexcept

bool
compare_exchange_strong(_Tp& __e, _Tp __i, memory_order __s,
                       memory_order __f) noexcept

```

*Puc. 8: Signatures of CAS operations in the C++ library*

An alternative to CAS operations is a pair of LL/SC operations in ARM processors. The load-link operation loads a value from memory, and store-conditional sets a new value, but only if the memory area has not changed. To implement LL/SC operations, we had to change the cache structure so that a LINK flag is added to each cache line. The flag is set during LL operation and is reset during SC or cache line preemption. LL/SC operations are not subject to the ABA problem, however, false sharing may occur due to hardware implementation. In modern processors, the cache line length is 64 - 128 bytes, therefore, several variables can be in the same cache line. When working with multiple variables on the same line, LL/SC operations will have a common LINK flag, which can lead to incorrect operation. In order to avoid this problem, one should place one variable in a line.

```

1 struct data {
2     atomic_int nShared1;
3     /* padding for cache line = 64 - sizeof(atomic_int) = 60 byte */
4     char _padding1[60];
5     atomic_int nShared2;
6     /* padding for cache line=60 byte */
7     char _padding2[60];
8 };

```

CAS operation can be quite easily implemented using LL / SC operations:

```

1 bool CAS(int *pAddr, int nExpected, int nNew) {
2     if (LL(pAddr) == nExpected)
3         return SC(pAddr, nNew);
4     return false;
5 }

```

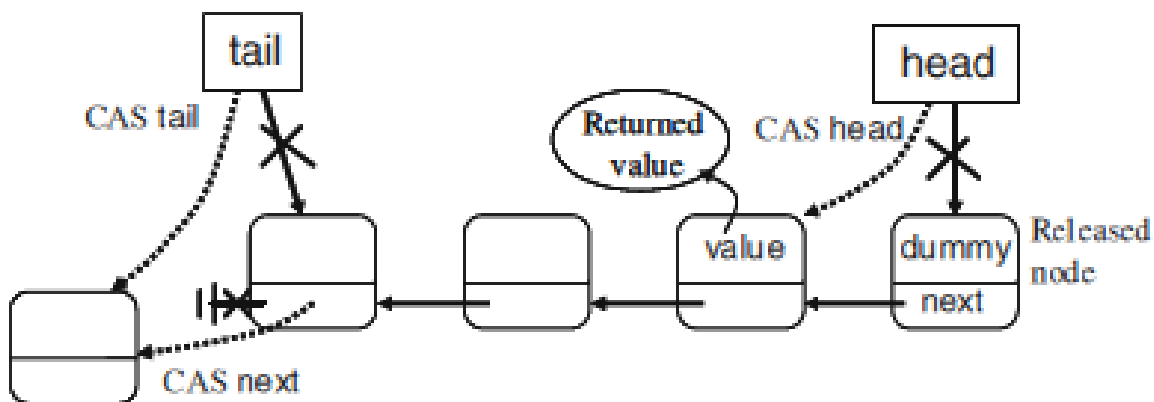
It is also important to understand that lock-free algorithms are sensitive to reordering machine instructions in their code. To avoid this, memory barriers are used. The memory barrier X\_Y ensures that all X-operations before the barrier are executed before the Y-operations after the barrier begin to be executed. In theory, there are 4 types of barriers - LoadLoad, LoadStore, StoreLoad,

StoreStore, but not all of them are implemented in all architectures. There are 4 processor memory models:

- **Relaxed model** – reordering of any memory access instructions is possible, even depending on the data (DEC Alpha).
- **Weak model** – reordering of any read and write instructions is possible, except for those that have data dependencies (ARM, PowerPC, Intel Itanium).
- **Strong model** – only reordering read to write is possible (x86).
- **Sequential consistency model** – any reordering is prohibited.

There are various lock-free data structures: queues (with strict and weakened order), stack, linked lists, hash tables. In C++, data structure data can be used by connecting various libraries. For example, Boost contains the implementation of the queue and stack, and Libcds contains all of the above.

An example of a lock-free data structure is the Michael-Scott queue. This queue is implemented on the basis of a singly linked list and two pointers, one of which points to the head of the list (dummy node), and the other to the tail (рисунк 9).



*Рис. 9: Michael-Scott queue*

Consider the simplified queue code from the libcds library. Below is the enqueue function - adding to the queue. First, the passed value is put in node. Then we try to put it in the tail of the line. After receiving the current tail, the pointer advances until it reaches the actual tail. Then the value is put at the end of the queue and the value of the inserted element is assigned to the tail.

```

1  bool enqueue (value_type& val) {
2
3      node_type * pNew = node_traits::to_node_ptr(val);
4      node_type * t = m_pTail;
5
6      while (true) {
7          //продвижение хвоста
8          node_type * pNext = t->m_pNext.load();
9          if (pNext != nullptr) {
10             m_pTail.compare_exchange_weak(t, pNext);
11             continue;
12         }
13
14         //фактическая вставка нового элемента
15         node_type * tmp = nullptr;
16         if (t->m_pNext.compare_exchange_strong(tmp, pNew))
17             break;
18     }
19
20     //попытка продвинуть хвост
21     //в случае неудачи это сделает позже другой поток
22     m_pTail.compare_exchange_strong(t, pNew);
23
24     return true;
25 }

```

In order to get an element from the queue (dequeue function), so that the queue is not empty, and also that the tail and voices are advanced. The code is below.

```

1 value_type * dequeue() {
2
3     node_type * pNext;
4     node_type * h;
5
6     while (true) {
7         h = m_pHead;
8         pNext = h->m_pNext;
9
10        // кто-то успел изменить связь между головой и следующим узлом
11        if (m_pHead.load() != h)
12            continue;
13
14        //очередь пуста, голова всегда dummy node
15        if (pNext == nullptr)
16            return nullptr;
17
18        //хвост оказался не продвинут, пытаемся продвинуть
19        node_type * t = m_pTail.load();
20        if (h == t) {
21            m_pTail.compare_exchange_strong(t, pNext);
22            continue;
23        }
24
25        //продвигаем голову
26        if (m_pHead.compare_exchange_strong(h, pNext))
27            break;
28    }
29
30    return pNext;
31 }

```

## 2 Показатели эффективности параллельной программы

### 2.1 Parallel Acceleration and Parallel Efficiency

To evaluate the effectiveness of a parallel program, the performance indicators of this program are compared when it is run on several identical computing systems, which differ only in the number of central processors (or cores). In practice, several independent hardware platforms are rarely used for this purpose because it is quite difficult to ensure their full identity in all respects. Instead, measurements are performed on a single multiprocessor (multi-core) computing system, in which the number of processors (cores) involved in the calculations is artificially limited. This is usually achieved in one of the following ways:

- Setting the affinity of processors (cores).
- Virtualization of processors (cores).
- Controlling the number of threads of execution.

**Affinity setting.** By affinity (processor affinity/pinning) is meant the instruction to the operating system to run the specified thread/process on an explicitly specified processor (core). Affinity can be established either using a special system call from within the parallel program itself, or in some way from outside the parallel program (for example, using the Task Manager or using the start command with the / AFFINITY key in MS OS Windows, or the "taskset " command on Linux). The disadvantages of this method are:

- The need to modify the parallel program under study when using a system call from the program itself..
- Inability to control affinity at the thread level, as usually, the OS allows affinity to be set only for processes when affinity is set by means external to the parallel program.

**Virtualization of processors (cores).** When creating a virtual computer in most specialized programs (for example, VMWare, VirtualBox) it is possible to "highlight " the created virtual machine not all the processors (kernels) present in the host system, but only a part of them. This can be used to simulate a test environment with a given number of cores (processors). For example, figure 10 shows that for a custom virtual machine, of the eight available physical (and logical) processors, only three are available.



*Рис. 10: Choosing the Number of Virtual Processors in Oracle VirtualBox*

The disadvantage of this approach is the virtualization overhead, which in an unpredictable way can affect the results of experimental measurements of parallel program performance. The advantage of virtualization (in comparison with controlled affinity) is a more natural behavior of the tested program when using available processors, because The OS does not give hard instructions that certain threads should always be “ tied ” to predefined processors (cores) - this feature allows you to more accurately reproduce the scenario of potential "live" use of the program under test, which increases the reliability of the obtained performance measurements .

**Thread management.** Quite often, the number of threads created during the work of a program is not set in the form of a rigidly fixed value. On the contrary, it is a flexibly configurable quantity  $p$ , the choice of the value of which allows optimal use of the computing resources of the hardware platform on which the program runs. This allows the program to "adapt" to the number of processors (cores) that are available on a particular computer.

This feature of a parallel program can be used to experimentally measure its performance indicators, for which a parallel program is started at  $p = 1, 2, \dots, n$ , where  $n$  – is the number of available processors (cores) on the multiprocessor hardware platform used for testing. The described approach allows you to artificially limit the number of processors (cores) used in the

program, because at any time, a parallel program can be executed no more than  $p$  calculators. By analyzing the measurements of the program speed obtained for various  $p$ , it is possible to calculate the values of some indicators of parallelization efficiency (see below).

**Parallel speedup.** In contrast to the concept of the value of acceleration used in physics as an increase in speed per unit time, in programming, parallel acceleration is understood to be a dimensionless quantity that reflects the increase in the speed of parallel program execution on a given number of processors compared to a single-processor system, i.e.

$$S(p) = \frac{V(p)}{V(1)}, \quad (1)$$

where  $V(p)$  is the average speed of program execution on  $p$  processors (cores), expressed in arbitrary units of work per second (W/s). Examples of W/S can be the number of summed matrix elements, the number of image points processed by the filter, the number of bytes written to the file, etc.

It is believed that the value of  $S(p)$  can never exceed  $p$ , which on the intuitive level sounds plausible, because with an increase in the number of employees, for example, four times it is not possible to get the job done five times faster. However, as we consider below, in experiments, super-linear parallel acceleration may well be observed with an increase in the number of processors. Of course, such a result most often means an experimenter's mistake, however, there are situations where this result can be explained by the fact that with an increase in the number of processors, their computing resource not only multiplies, but also the volume of the first-level cache increases, which allows some tasks significantly increase the percentage of cache hits and, as a result, reduce the time to solve the problem.

**Parallel efficiency.** Although the value of parallel acceleration is dimensionless, its analysis is not always possible without information on the value of  $p$ . For example, suppose in some experiment that  $S(p) = 10$ . Without knowing the value of  $p$ , we can only say that with parallel execution the program began to work 10 times faster. However, if at the same time  $p = 1000$ , this acceleration cannot be considered a good achievement, since in other conditions, it was possible to achieve an almost 1000-fold increase in the speed of work and not spend such impressive resources on a poorly parallelized task. On the contrary, with a value of  $p = 11$ , one could consider the value  $S(p) = 10$  to be quite acceptable.

This problem led to the need to determine another indicator of the effectiveness of a parallel program, which would allow us to obtain some estimate of the parallelization efficiency taking into account the number of

processors (cores). This quantity is **parallel efficiency**

$$E(p) = \frac{S(p)}{p} = \frac{V(p)}{p \cdot V(1)} \quad (2)$$

Average program execution speed  $V(p)$  can be measured by the following two *nonequivalent* methods

- **Amdal Method:** calculate  $V(p)$ , fixing the amount of work performed (we change the execution time of the program for various).
- **Gustavson-Barsis Method:** calculate  $V(p)$ , fixing the time of the test program (we changes the amount of work done for different  $p$ ).

Let us consider in more detail each of these methods in the next two sections.

## 2.2 Amdal Method

When evaluating the efficiency of parallelization of a program that performs a fixed amount of work, the speed of execution can be expressed as follows:  $V(p)|_{w=const} = \frac{w}{t(p)}$ , where  $w$  is the total amount of W/s contained in the program in question,  $t(p)$  – runtime  $w$  using  $p$  processors. Then the expression for parallel acceleration will take the form:

$$S(p)|_{w=const} = \frac{V(p)}{V(1)} = \frac{w}{t(p)} = \frac{w}{t(1)} = \frac{t(1)}{t(p)}. \quad (3)$$

We write the time  $t(1)$  as follows:

$$t(1) = t(1) + (k \cdot t(1) - k \cdot t(1)) = k \cdot t(1) + (1 - k) \cdot t(1), \quad (4)$$

where  $k \in [0, 1)$  - is the coefficient of parallelism of the program, by which we define the fraction of the time during which perfectly parallelized code is executed inside the program. Such code can be executed exactly  $p$  times faster if the number of processors is increased by  $p$  times. Note that the coefficient  $k$  is never equal to one, because any program always has unparallelized code that must be executed sequentially on one processor (core), even if there are several of them available. If for some program  $k = 0$ , then when you run this program on any number of processors  $p$ , it will be executed in the same time.

Considering that in Amdal's method the amount of work remains unchanged for any  $p$  (since  $w = const$ ), we can guarantee that the value of  $k$  does not change in the experiments, therefore we can write:

$$t(p) = \frac{k \cdot t(1)}{p} + (1 - k) \cdot t(1), \quad (5)$$



where the first term gives the runtime of the parallelized ideally parallelized code by  $p$  times, and the second term gives the runtime of the unparallelized code, which does not change for any  $p$ . Substituting the formula (5) in (3), we get the expression

$$S(p)|_{w=const} = \frac{t(1)}{t(p)} = \frac{t(1)}{\frac{k \cdot t(1)}{p} + (1 - k) \cdot t(1)} = \frac{1}{\frac{k}{p} + 1 - k},$$

which we rewrite in the form

$$S(p)|_{w=const} = S_A(p) = \left( \frac{k}{p} + 1 - k \right)^{-1} \quad (6)$$

better known as **Amdahl's Law** - after the name of the American scientist Gene Amdal, who proposed this expression in 1967. Until now, this law is fundamental in the specialized literature on parallel computing, because allows you to get a theoretical upper limit for the speed of execution of a given program during parallelization.

The graph of parallel acceleration versus the number of cores is shown in the figure. 11:

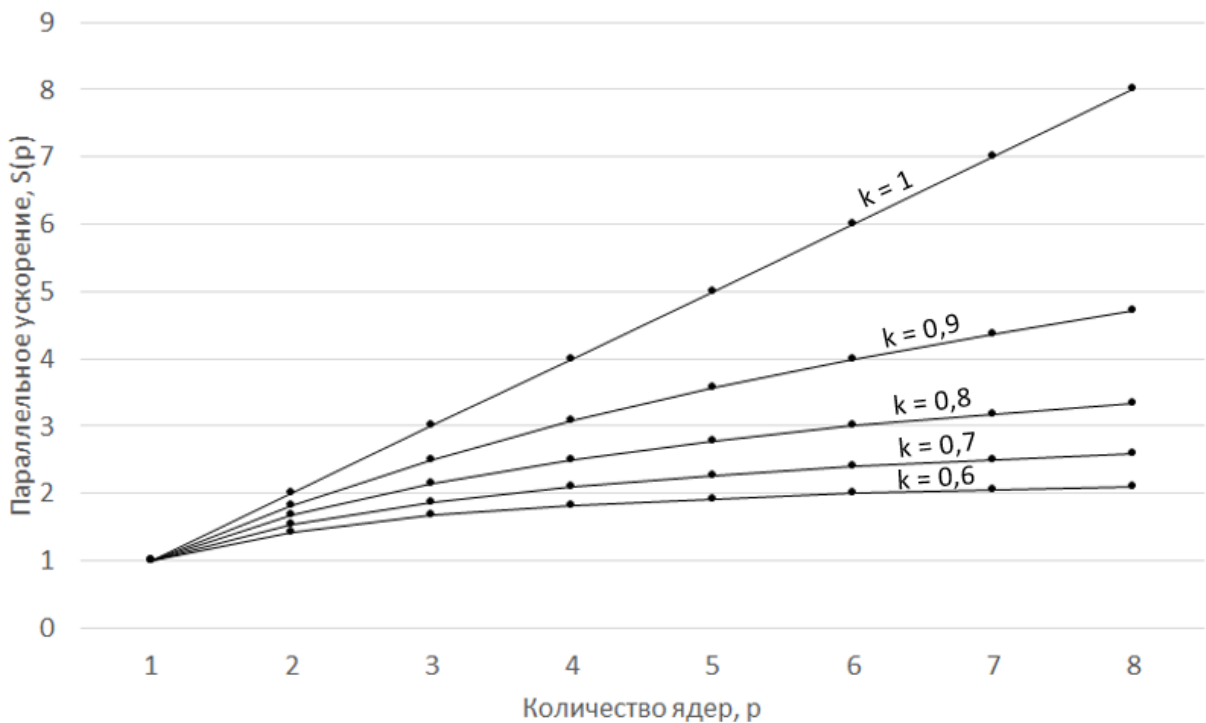


Рис. 11: A graph of the parallel acceleration on the number of cores in Amdal

Note that the expression for calculating parallel efficiency using the Amdahl method can be obtained by combining the formulas (2) и (6), а именно:

$$E_A(p) = (k + p - p \cdot k)^{-1} \quad (7)$$

An important assumption of Amdahl's law is the idealization of the physical meaning of the quantity  $k$ . It consists in the assumption that a perfectly parallelized code will give a linear increase in speed when  $p$  changes from 0 to  $+\infty$ . When solving real problems, it is necessary to limit this interval from above to some finite positive value  $p_{max}$  or to exclude from this interval all values that are not multiples of a certain quantity that usually sets the dimension of the problem.

For example, the code of a program that performs convolutional coding independently for five equal-sized files can give linear acceleration when  $p$  changes from 1 to 5, but even with  $p = 6$  it will most likely show a zero increase in the speed of the task (in comparison with solution for  $p = 5$ ). This is because convolutional coding, also known as convolutional coding, is fundamentally un-parallelizable when coding the selected data block.

### 2.3 Gustavson-Barsis Method

When evaluating the efficiency of parallelization of a certain program running a fixed time, the speed of execution can be expressed as follows:  $V(p)|_{t=const} = \frac{w(p)}{t}$ , where  $w(p) - t$  is the total amount of work that the program manages to complete during  $t$  when using  $p$  processors. Then the expression (1) for parallel acceleration will take the form:

$$S(p)|_{t=const} = \frac{V(p)}{V(1)} = \frac{w(p)}{t} : \frac{w(1)}{t} = \frac{w(p)}{w(1)}. \quad (8)$$

We write the amount of work  $w(1)$  as follows:

$$w(1) = w(1) + (k \cdot w(1) - k \cdot w(1)) = k \cdot w(1) + (1 - k) \cdot w(1), \quad (9)$$

where  $k \in [0, 1)$  – is the parallelism coefficient of the program. Then the first term can be considered the amount of work that perfectly parallelizes, and the second - the amount of work that fails to parallelize when adding processors (cores).

When using  $p$  processors, the amount of work done  $w(p)$  will obviously become larger, while it will consist of two terms:

- number of unparallelled work  $(1 - k) \cdot w(1)$ , which does not change compared to the formula (9).

- amount of parallel work, the volume of which will increase by  $p$  times in comparison with the formula (??), because  $p$  processors will be used instead of one.

Given the above, we obtain the following expression for  $w(p)$ :

$$w(p) = p \cdot k \cdot w(1) + (1 - k) \cdot w(1), \text{ then given the formulas (8) we get: } \frac{w(p)}{w(1)} = \frac{p \cdot k \cdot w(1) + (1 - k) \cdot w(1)}{w(1)}, \text{ that allows you to record:}$$

$$S(p)|_{t=const} = S_{GB}(p) = p \cdot k + 1 - k \quad (10)$$

The above expression is called **Gustavson-Barsis law**, which John Gustavson and Edwin Barsis formulated in 1988.

## 2.4 Modification of Amdal's law (according to Prof. Bukhanovsky)

In real computing systems, the OS spends resources on creating and deleting new threads. The time spent on these operations is not taken into account in Amdal's law. Parallel acceleration of  $S(p)$  depends on the number of cores and the proportion of parallelized operations, but does not depend on the number of the latter. We derive a formula in which the number of operations for which it is necessary to create a stream will be considered.

Let  $N$  be the number of parallelized operations,  $M$  be the number of non-parallelizable operations,  $t_c$  be the execution time of one operation,  $p$  be the number of calculators (cores),  $T_i$  be the program execution time using  $i$  parallel threads on  $i$  calculators,  $\alpha$  is a certain scaling factor that encapsulates the amount of time required to create, delete a stream, and other overhead operations. According to the formula (3),  $S(p) = \frac{T_1}{T_p}$ .

First we find  $T_1$ . Since this code is linearly executed, the time spent on its execution will be equal to the number of operations times the time it takes to execute one operation:  $T_1 = t_c(N + M)$ .

The execution time of the parallel  $T_p$  program includes the time to create the stream:  $t_c \alpha (p - 1)N$  need to create  $(p - 1)$  new threads, since the main thread has already been created and for each spend some time  $\alpha$ ),  $\frac{t_c N}{p}$  parallel code running time on all cores:  $t_c M$ . Total, dividing  $T_1$  на  $T_p$ , we get the formula of Amdahl's law according to prof. Bukhanovsky:

$$S(p, N) = \frac{T_1}{T_p} = \frac{N + M}{\alpha(p - 1)N + \frac{N}{p} + M} \quad (11)$$

From the formula (11) we can see that with an increase in the number of cores after a certain limit  $S(p, N)$  will not grow as in Amdal's law, since time will

be spent a lot of time creating new flows. On the image 12 it is clearly seen that  $S(p, N)$  decreases with a large number of flows and becomes noticeably smaller  $S(p)$  than Amdal even with a small value  $\alpha$ .

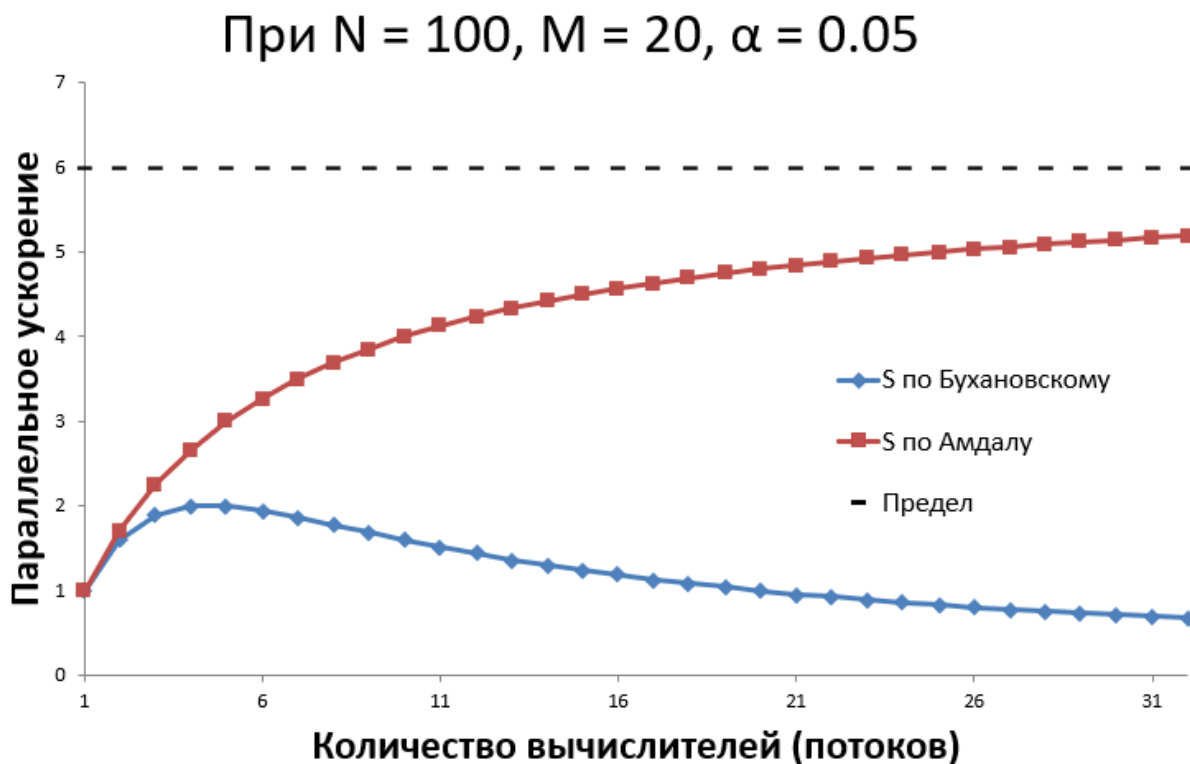


Рис. 12: Graph of parallel acceleration versus number of threads

## 2.5 Measuring the runtime of parallel programs

**Time measuring tools.** Measuring the runtime of a program in C is not a difficult problem, however, in parallel programming, a number of specific difficulties arise in performing this operation. Not all functions suitable for measuring the running time of a sequential program are suitable for measuring the running time of a multithreaded program.

For example, if you use the `ctime` or `localtime` functions in a single-threaded program to measure the operating time of a section of code, they will successfully cope with the task. However, after parallelizing this part of the code, it is possible that hard-to-identify problems arise with incorrect time measurement, because both of these functions have an internal static variable, which, when trying to change it simultaneously by several threads, can take an unpredictable value.

In order to solve the described problem, some C-compilers (for example, `gcc`) implemented thread-safe, re-entrant versions of these functions: `ctime_r`

`_r` and `localtime_r`. Unfortunately, these functions are not available in all compilers. For example, in the Visual Studio compiler, a similar problem was solved using functions with completely different names and APIs: `GetTickCount`, `GetLocalTime`, `GetSystemTime`. For completeness, we list some other gcc functions that also allow you to measure time: `time`, `getrusage`, `gmtime`, `gettimeofday`.

Another standard C-function clock also cannot be used to measure the execution time of multithreaded programs. However, the reason for this is not the lack of reenterability, but the features of the way this function calculates the elapsed time: `clock` returns the number of processor ticks that were executed when the program was running in total with all its threads. Obviously, this amount remains almost unchanged when the program executes with a different number of threads ("almost", since the overhead costs of creating, deleting and managing threads are proposed to be considered insignificant in order to simplify the presentation).

As a result, it turned out that a satisfactory *cross-platform* solution for thread-safe time measurement with high accuracy (up to microseconds) by means of pure C language does not exist yet. However, the problem can be solved using third-party libraries, choosing those that have an implementation on the target platforms.

The OpenMP system, which is implemented in the vast majority of modern compilers for all modern operating systems, stands out among such libraries. OpenMP has two functions for measuring time: `omp_get_wtime` и `omp_get_wtick`, which can be used in C-programs, if you include the `omp.h` header file and specify the necessary key during compilation (for example, in gcc this is the key `"-fopenmp"`).

**Time measurement error.** Another interesting point in measuring the running time of a parallel program is the method by which the researcher excludes various random errors from measurements that inevitably arise during an experiment in a running operating system, which can start the update or optimization process without notifying the user. The generally accepted is the way in which the researcher conducts not one, but immediately  $N$  experiments with a parallel program, without changing the initial data. It turns out  $N$  time measurements, which in the general case will be different due to various random factors affecting the experiment. Further, one of the following methods is most often used:

1. *The calculation of the confidence interval:* consider all  $N$  measurements is calculated confidence interval, e.g., using Student's method.
2. *Search for the minimum measurement:* among  $N$  measurements, the smallest is chosen and it is used as the final result.

The first method gives the correct result only if the measurement errors are distributed according to the normal law. This is most often the case, therefore, the application of the method is justified and allows you to get additional information about the possible use of the tested program in living conditions of a running OS.

The second method does not impose requirements on the form of the law of distribution of measurement errors, and this compares favorably with the previous one. In addition, for large N, the choice of the minimum metering will make it possible to exclude from the experiment all the background influences of the operating system and to obtain as a result an accurate measurement of the operating time of the program under ideal conditions.

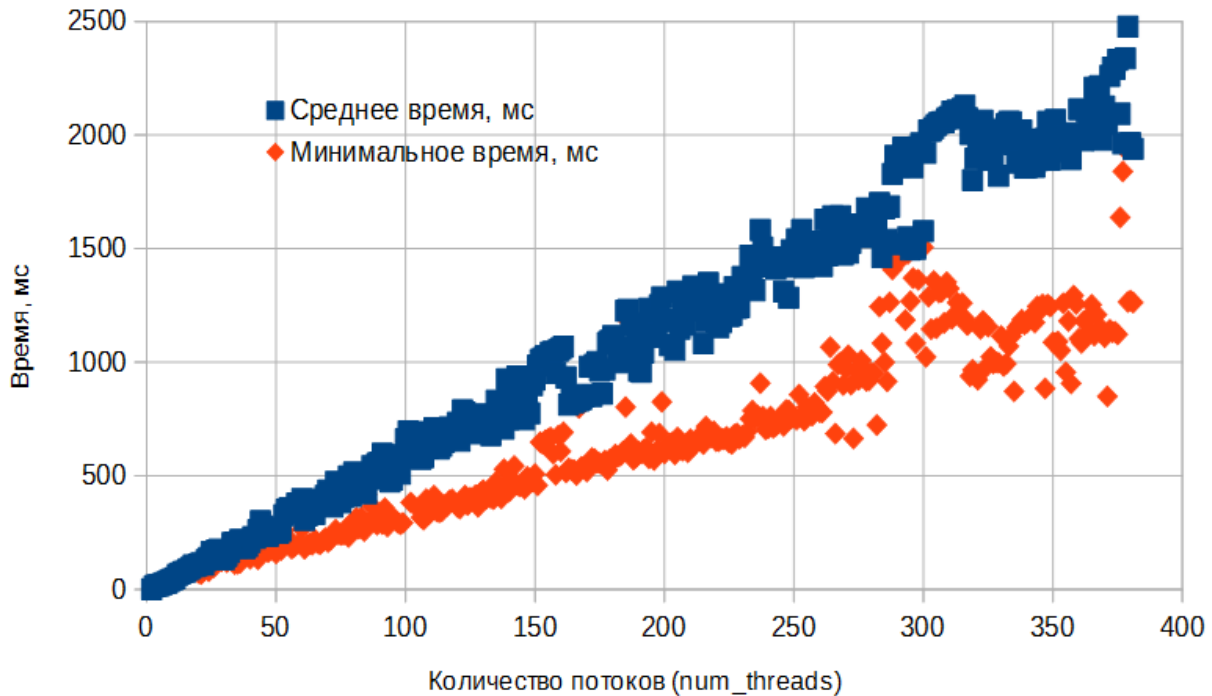
**Practical example.** Let us compare by example the methods described above to get rid of the error of experimental time measurements. We will measure the OpenMP overhead for creating and deleting threads as follows:

```
1  for (i = 1; i < 382; i++) {
2      omp_set_num_threads(i);
3      double T1 = omp_get_wtime();
4      #pragma omp parallel // parallel section start
5      #pragma omp master
6      s++; // parallel section end
7      double T2 = omp_get_wtime();
8      print_delta(T1, T2);
9  }
```

In line 3, we instruct OpenMP that when entering the parallel area located further in the program, *i* threads are created. If you do not give this indication, OpenMP will create the number of threads by the number of calculators available in the system (cores or logical processors). In line 4, we start the parallel program area, OpenMP creates *i* threads. In line 5, we give instructions to execute the following simple instruction in only one thread (the rest of the threads will not do any work. This is necessary so that only the costs of creating / deleting threads fall in the measured time of work, and all other costs would be lost against their background. The parallel area ends in line 6. OpenMP deletes the *i* number of threads from the memory. A more detailed description of the OpenMP commands used can be found in section 3.3 "*OpenMP Technology*" of this book.

Experiments with this program were conducted on a computer with an Intel Core i5 processor (4 logical processors) with 8 gigabytes of RAM in the Debian Wheezy operating system. Empirically, it was revealed that the operating system used on an accessible hardware platform cannot create more than 381 threads in the OpenMP program (this explains the value in line 1).

A total of  $N = 100$  experiments were carried out, the results of which were processed by each of the two described methods. The results are shown in the figure. 13.



*Рис. 13: OpenMP overhead measurement results for thread creation and deletion*

The measured value ( $T2 - T1$ ) in milliseconds is plotted along the ordinate axis, and the values of variable  $i$ , which indicate the number of created flows, are plotted on the abscissa axis. The upper graph, consisting of blue squares, shows the average value ( $T2 - T1$ ) for the 100 experiments performed. The confidence interval is not shown, as it would clutter the graph without adding informativeness, but the width of the confidence interval with a confidence level of 90 % approximately corresponds to the vertical spread of the squares of the upper graph for neighboring values of  $i$ .

The lower graph, consisting of rhombs, represents the minimum of 100 measurements ( $T2 - T1$ ) for the values of  $i$  indicated on the x-axis. We see that even a large number of experiments was not enough for the lower graph to have a smooth continuous structure without noticeable fluctuations.

## **3 Practical Aspects of Parallel Programming**

### **3.1 Debugging Parallel Programs**

Parallel program debugging tools are built into most popular integrated development environments (IDEs), for example: Visual Studio, Eclipse CDT, Intel Parallel Studio, etc. These tools include convenient visualization of timing diagrams of thread execution, automatic search for suspicious program sections in which data races and deadlocks can be observed.

Despite the effectiveness of existing debugging tools, there are significant difficulties when working in a debugger with a parallel program, because for its correct functioning, the debugger adds additional instructions to the machine code of the source parallel program that change the timing diagram of thread execution in relation to each other. This can lead to situations when during the testing of the program in the debugger there are no data races and deadlocks that will fully appear when the Release version of the program is launched.

Also, during debugging of a multi-threaded program, it should be borne in mind that its behavior (both during regular operation and during debugging) can significantly differ when using a single-core and multi-core processor. When several threads are launched on a single-core machine, they will be executed in time-sharing mode, i.e. sequentially. This means that in this case many problems with shared access to memory and ensuring coherence of caches inherent in multi-core systems will not be observed. In addition, when debugging a program on a single-core system, a programmer can use implicit techniques to ensure the sequence of operations.

For example, a programmer may incorrectly assume that when executing a high-priority thread, a low-priority thread cannot take over the processor. This assumption is correct only in a single-core system, because in the presence of several cores and a small number of high-priority threads, a situation may well be observed when a low-priority thread takes possession of one of the cores, while the high-priority thread is operating on the neighboring core.

### **3.2 Memory Managers for Parallel Programs**

When calling malloc / free functions in a single-threaded program, there are no problems even with a rather high call intensity of one of them. However, in parallel programs, these functions can become a bottleneck because when they are used simultaneously from several threads, a shared resource (memory management manager) is blocked, which can lead to a significant degradation in the speed of a multithreaded program.



Despite the formal thread safety of standard memory functions, they can become thread-inefficient when the memory of several threads running in parallel is very intensive.

To solve this problem, there are a number of third-party programs called the "Memory Management Manager (MUP)" (Memory Allocator), both paid and free, open source. Each of them has its own advantages and disadvantages, which should be considered when choosing. We list the most common MUPs with links to official sites:

- tcmalloc: <http://goog-perftools.sourceforge.net/doc/tcmalloc.html>
- ptmalloc: <http://www.malloc.de/malloc/ptmalloc3-current.tar.gz>
- dmalloc: <http://dmalloc.com/>
- HOARD: <http://www.hoard.org/>
- nedmalloc: <http://www.nedprod.com/programs/portable/nedmalloc/>
- jemalloc: <http://jemalloc.net/>
- mimalloc: <https://github.com/microsoft/mimalloc>

The listed MUPs are designed in such a way that they can 'silently' replace the standard MUP libraries of the C language C for the parallel program. This means that the choice of a particular MUP does not affect the source code of the program, so the general practice of using third-party MUPs is as follows: parallel program it is initially created using the libc MUP, then the profiling of the running program is performed, then when a bottleneck is detected in the malloc / free functions, a decision is made to replace the standard MUP with one of the listed.

### 3.3 OpenMP Technology

**Brief description of the technology.** The first version of the OpenMP standard appeared in 1997 with the support of the largest IT companies in the world (Intel, IBM, AMD, HP, Nvidia, etc.). The aim of the new standard was to offer a cross-platform parallelization tool that would be higher-level than the flow control APIs offered by the operating system. OpenMP is currently standardized for three programming languages: C, C ++ and Fortran.

**Compiler support** The vast majority of existing modern C / C ++ compilers support OpenMP version 2.0 (for example, both gcc and Visual Studio). However, only a few compilers support the newer version of OpenMP 4.0, therefore, when setting forth the material, the OpenMP 2.0 technology will be used as the "common denominator".

OpenMP defines a set of directives to the preprocessor, which instructs the compiler to replace the source code that follows them with a parallel version using tools available to the compiler, for example, POSIX Threads on Linux or Windows Threads on Microsoft operating systems. For correct translation of directives, you must specify a special key during compilation, the value of which depends on the compiler (examples are given in the table 2).

*Таблица 2:* Compiler keys to run OpenMP

| Compiler name                | Compiler Key OpenMP |
|------------------------------|---------------------|
| Gcc                          | -fopenmp            |
| icc (Intel C/C++ compiler)   | -openmp             |
| Sun C/C++ compiler           | -xopenmp            |
| Visual Studio C/C++ compiler | /openmp             |
| PGI (Nvidia C/C++ compiler)  | -mp                 |

In addition to preprocessor directives, OpenMP defines a set of library functions. To call them in the source code, you need to include the OpenMP header file:

```
1 #include <omp.h>
```

**Distinctive features.** Among other parallelization technologies, OpenMP stands out for the following important and characteristics:

- Incremental parallelization.
- Backward compatibility.
- High level of abstractions.
- Low coefficient of transformation.
- Support by the largest IT giants.

- Auto scaling.

*Incremental parallelization.* OpenMP allows you to parallelize a sequential program using small iteration-edits, each of which will increase the parallelism coefficient of the program. This feature is unique because most other technologies suggest a significant change in the structure of the parallelized program at the first stage of the parallelization process, i.e. The first workable parallel version of the program appears after a long process of debugging and programming of new components, which are inevitably added during parallelization. OpenMP does not have this lack.

*Backward compatibility.* Most software technologies evolve with backward compatibility when a newer version of the program supports the functionality of old files. The term *forward compatibility* has the opposite meaning: files created in the new version program remain functional when using the old version of the program. In the case of OpenMP, this means that the parallelized program will be correctly compiled in single-threaded mode even on an old compiler that does not support OpenMP. It is important to note that direct compatibility is ensured if, during parallelization, library functions of OpenMP are not used, and only preprocessor directives are present. If you have library functions, to ensure backward compatibility, you will need to write stub functions in the "omp.h" file (some compilers can generate these stubs using a special key).

*High level of abstractions.* A single preprocessor OpenMP directive after processing by the compiler leads to a significant transformation of the source program with the addition of a large number of new logic, which is responsible for determining the number of processors available in the system, for starting and destroying threads, for distributing work between threads, etc. OpenMP takes care of all these operations; in return, the programmer receives a set of very high-level parallelization tools. High-level languages have a traditional drawback: in OpenMP there is no way to change some internal details of working with streams (for example, you cannot set the affinity of streams or reduce the overhead of creating / deleting streams).

*Low parallel transformation ratio (PTR).* When parallelizing an existing sequential program, we need to make a fairly large number of changes to it. Let PTR be the ratio of the lines of the new program code that was added as a result of parallelization to the total number of lines of code in the program. In OpenMP, the CBT is usually significantly lower than most other parallelization technologies. This is due to the high level of abstraction of the OpenMP language (see the previous paragraph).

*Support by the largest IT giants.* Already during the development of

OpenMP, it was supported by the largest players in the IT world. This ensured not only the high quality of standard development, but also the availability of off-the-shelf implementations of the standard in popular compilers. Despite the past twenty years, OpenMP has not lost its adherents and support for the latest versions with a fairly low delay appears in compilers. For example, with the current version of the OpenMP 4.5 standard, the most popular compilers already support OpenMP 4.0. The only exception is Microsoft. Their compiler for several versions invariably only supports OpenMP 2.0.

*Auto scaling.* Low-level parallelization technologies (POSIX Threads, OpenCL) offer the programmer to manually control the number of threads created when performing parallel work. This provides the ability to flexibly manage and configure the process of creating threads depending on the number of processors (cores) available to the system, but it requires a large amount of non-automated work from the programmer. In OpenMP, scaling is controlled automatically, i.e. OpenMP itself asks the number of available processors from the operating system and selects the number of threads to create. But if necessary, OpenMP leaves the ability to set the required number of threads manually.

**Examples of OpenMP programs.** Consider the simplest examples of running parallel programs below, starting with the traditional programming example "Hello, World ":

```
1  #pragma omp parallel
2  printf("Hello, world!");
```

The result of the work will be displayed several times in the console message. The number of messages is determined by the number of logical processors available to the system (for example, when using HyperThreading technology with two cores, the number of logical processors will be four).

The pragma directive extends to the next executable block. In this case, it is a call to the printf function, but one could enclose an arbitrary number of operations in curly braces to expand the executable block:

```
1  int i = 1;
2  #pragma omp parallel
3  {
4      printf("Hello, world!");
5      #pragma omp atomic
6      i++;
7  }
```

In this program, a block of operations enclosed in braces is executed at the same time on several cores. At the same time, in line 5, the processor is

instructed to perform the operation "i ++ " atomically, i.e. not in parallel, but sequentially by each of the threads.

On the one hand, this leads to the fact that the increment operation ceases to be parallelized, which reduces the speed of multi-core execution. On the other hand, the atomic directive is necessary in this case, because otherwise, a difficultly detectable problem with data race could arise, which manifests itself in a conflict when writing data to a common memory area simultaneously by several threads in the variable i. Note that the atomic directive can only be used for single-line simple assignment commands.

To isolate more complex compound commands with the possible invocation of user and system functions, you should use the critical directive, which allows (unlike the atomic directive) the ability to expand its scope to a block of operations enclosed in curly braces, with each critical section having the name, allowing you to group different critical sections by this name to prevent the appearance of a single critical section distributed throughout the program:

```
1  int i = 1;
2  #pragma omp parallel
3  {
4      printf("Hello, world!");
5      #pragma omp critical
6      {
7          i++;
8          printf("i=%d\n", i);
9      }
10 }
```

In this case, the printf function on line 4 is executed by all threads in parallel, which can lead to mixing of the output characters. On the contrary, the printf function in line 8 is executed by threads strictly in turn, which prevents possible conflicts between them, but slows down program execution due to the artificial limitation of the parallelism coefficient.

An example of parallelizing a program containing a sequential call to the functions run\_function1 and run\_function2, which are independent of each other (i.e. do not use common data and the results of one do not affect the results of the other) and therefore allow convenient *instruction parallelization* in pure form:

```
1  #pragma omp parallel sections
2  {
3      #pragma omp section
4      run_function1();
5      #pragma omp section
6      run_function2();
7  }
```

Consider an example of loop parallelization using OpenMP. Suppose that in each cell of a one-dimensional array you need to write the index of this cell raised to the sixth power:

```
1 int i; int a[10];
2 #pragma omp parallel for
3 for (i = 0; i < 10; ++i) {
4     a[i] = i*i*i*i*i*i;
5 }
```

Let the specified program run on a dual-core processor. Then the first processor calculates the values from a [0] to a [4], the second processor calculates the values from a [5] to a [9]. Apparently, when writing to the array, the processor does not interfere with each other, because work with different parts of the array. Let's try to optimize the previous option, reducing the number of multiplication operations for raising to the sixth power:

```
1 int i, tmp;
2 #pragma omp parallel for
3 for (i = 0; i < 10; ++i) {
4     tmp = i*i*i;      /* attempt to optimize */
5     a[i] = tmp*tmp;    /* error */
6 }
```

In this case, the program will work correctly only if there is one processor (core). If there are several cores, the state of the data race will be observed while writing a new value to the tmp variable (line 4) by several threads, as a result, the array will be filled incorrectly. For example, suppose that the first thread performing iteration  $i = 2$  wrote the number 8 in tmp. Now, when calculating a [2], the thread will try to write the number  $8 * 8$ , however, if the second thread working with the iteration  $i = 7$  has time to wedge before line 5, then the tmp value turns into  $7 * 7 * 7$ , and the value of a [2] calculated by the first stream turns into  $7^6$ , instead of the 64 ones. Lets correct the error as follows:

```
1 int i, tmp;
2 #pragma omp parallel for private(tmp)
3 for (i = 0; i < 10; ++i) {
4     tmp = i*i*i;
5     a[i] = tmp*tmp;
6 }
```

A new element has appeared in the directive to the preprocessor: private. This element sets a comma-separated list of local (private) variables for each

stream. In this case, there is only one such variable: `tmp`. Another equivalent way to correct the error is to transfer the declaration of the variable `"int tmp"` inside the parallel region, which forces OpenMP to consider this variable local for each stream. The question may arise, why `i` was not added to the list of local variables. The answer is not obvious: by default, OpenMP considers the parallelized loop variable local.

Any variable declared inside the parallel region is considered local in OpenMP, so such variables do not need to be specified in the list. Any variable declared outside this area is global (in our case, the global variable is a pointer to the array `a`). But if you need to explicitly indicate the globality of the variable, next to the `private` command, use the `shared(x, ...)` command, where `x` defines the list of global variables.

Consider an example in which you need to calculate the amount and for further execution to form an array of elements of the following series:  $\{1^i, 2^i, 3^i, 4^i, 5^i\}$  for various values  $i$ , eg:  $i = 1, 2, 3$ . Below is a solution to the problem, but intentionally make a mistake in it:

```

1  int i, j, sum[3], tmp[5];
2  #pragma omp parallel for private(tmp)                      /* ошибка!!
   */
3  for (i = 0; i < 3; ++i) {
4      for (j = 1; j <= 5; ++j) {
5          tmp[j] = pow(j, i);
6          /* ошибка!! */
7          sum[i] = calculate_sum(tmp, 5);
8      }

```

In line 2, the parallel rsection starts, but the programmer forgets to indicate that the variables `j` and the `tmp` array must be local for each thread. Indeed, in line 4 there is an increment of the variable `j` common for the threads, which is executed by all threads simultaneously. In this situation, threads can interfere with each other by overwriting the value of `j`. We fix both errors as follows:

```

1  int i, j, sum[3];
2  #pragma omp parallel for private(j) // OK
3  for (i = 0; i < 3; ++i) {
4      int tmp[5];
5      for (j = 1; j <= 5; ++j) {
6          tmp[j] = pow(j, i);          // OK
7          sum[i] = calculate_sum(tmp, 5);
8      }
9  }

```

We see that now the variable *j* is explicitly defined as local (private). If we use the *tmp* array, the solution will be different - it can fit inside the parallel section (i.e. each stream will have its own instance of the *tmp* array independent of the others). Why can't we just specify the *tmp* variable in the list of the private command, as was done for *j*? The answer is related to the specifics of the C language: the *tmp* variable is a pointer that does not change during the operation of the loop, but the contents of the memory pointed to by *tmp* change. This means that specifying *tmp* as a private variable would not solve the problem with data racing, because all streams would receive the same *tmp* address and interfere with each other, writing new values to this address.

Let's consider one more error typical for parallel computing. The following program calculates the sum of numbers from 1 to 100:

```
1  int i, sum = 0;
2  #pragma omp parallel for
3  for (i = 0; i < 100; ++i) /* error */
4      sum += i;
```

The *sum* variable is global, so when you try to write a new value to it, the threads will interfere with each other. To fix the error, we have to use the local amount for each thread, and then we need to add all these local amounts:

```
1  int i, sum = 0, sum_private = 0;
2  #pragma omp parallel private (sum_private)
3  {
4      sum_private = 0;          /* repeated initialization! */
5      #pragma omp for
6      for (i = 0; i < 100; ++i)
7          sum_private += i;
8      #pragma omp atomic
9      sum += sum_private;
10 }
```

We see the beginning of the parallel area on line 2 - at this point OpenMP creates several threads. In line 6, new threads are not created (because the *parallel* keyword is missing), but the threads entering the loop divide iterations among themselves, and do not complete each iteration as a whole. In line 8, the thread calculating its partial amount tries to add this amount to the total amount. This has to be done using the *atomic* directive, which ensures that threads will not interfere with each other when overwriting *sum*.

Another difficult point is the reinitialization of the variable *sum\_private* on line 4: this is necessary because OpenMP does not initialize local variables, even if there are global variables with identical names. This solution is designed to reduce the overhead of copying variables.



The described approach is working, but it is almost never used in practice, because the OpenMP standard for a whole class of similar tasks offers a higher-level and simpler solution. It consists in using the *reduction* command:

```
1 int i, sum = 0;
2 #pragma omp parallel for reduction (+:sum)
3 for (i = 0; i < 100; ++i)
4     sum += i;
```

The *reduction* command marks the listed variables as local, and at the end of the parallel region, all local variables are combined (aggregated) into one global variable with the same name using the specified operation. In our case, the operation is the amount. But OpenMP allows the use of " \* ", " - ", " / " instead of the sign " + ". It is important that reduction, among other things, does not initialize the variables with the values of the original global variables, but with the most appropriate values of the aggregation logic: for example, when summing, the variable is initialized to zero, and when multiplying, it is initialized to one.

When parallelizing a cycle, iterations may turn out to be unequal in the amount of work performed among themselves. This can lead to the fact that one thread will cope with the selected part of iterations much faster than the second thread and will be idle. To solve this problem, OpenMP offers four different ways to distribute iterations over threads.

- *Default method*: iterations are divided by the number of parts equal to the number of threads; each thread then performs its part and cannot take someone else's work.
- *Static distribution*: iterations are divided into parts of the size specified by users; then, before starting work, each thread receives a fixed number of parts and performs only them without the ability to switch to others.
- *Dynamic distribution*: iterations are divided into parts of the size specified by users; then the cycle starts immediately and each thread receives a new part of iterations as the work on the previous one is completed.
- *Guided distribution*: the compiler divides the iterations into the number of parts equal to twice the number of threads; then the cycle starts immediately and each thread receives a new part of iterations as the work on the previous one is completed, while the size of the newly

issued part decreases compared to the previous time, but cannot become less than the constant value specified by the user.

The user parameter mentioned in each method is called `chunk_size`. Each of these methods has its own field of application in which it can provide maximum parallel acceleration. Note that the dynamic and guided modes, despite their logical nature, also have their drawbacks: they require significant overhead during the cycle compared to static. It is also important to understand that when choosing the number of `chunk_size` it is necessary to take into account the features of the caching mechanism.

Consider an example of a static iteration distribution:

```
1 int i; double sum = 0;
2 #pragma omp parallel for reduction (+:sum) schedule(static,1)
3 for (i = 1; i < 100; ++i)
4     sum += 1.0/i;
```

With three cores, OpenMP will create three threads. The first thread will get iterations  $i = 1, 4, 7, \dots, 97$  the second – iterations  $i = 2, 5, 8, \dots, 98$ , the third -  $i = 3, 6, 9, \dots, 99$ . Note that choosing a small value for the parameter `chunk_size = 1` in this case does not have any negative effects. However, if  $i$  were used as an index when accessing the array, the proposed partitioning would lead to memory access not sequentially by sequential addresses, but sparse with step 3, which would degrade cache hit performance when using caching.

Lets consider another example:

```
1 double result1, result2, result3;
2 #pragma omp parallel num_threads(3)
3 {
4     #pragma omp for reduction (+:result1) nowait
5     for (i = 0; i < 100; ++i) result1 += i;
6     #pragma omp sections
7     {
8         #pragma omp section
9         result2 = calculate_pi();
10        #pragma omp section
11        result3 = calculate_e();
12    }
13 }
14 use_results(result1, result2, result3);
```

Here is an example of how you can tell OpenMP the number of threads to create using the `num_threads` option (line 2), without focusing on the actually available number of cores (processors) on the computer. Next, the

three created streams share 100 iterations among themselves in a way that is already familiar to us. However, the `nowait` option allows the first thread to cope with work not to wait for the others, but to proceed to the next work after the cycle. Behind a cycle in parallel, two functions are performed (lines 9 and 11). Each of the functions is enclosed in a section, which must have the parent element sections. As a result, the first thread freed up after the loop will calculate the function on line 9. The second freed thread will calculate the function on line 11. The third thread will not get work beyond its share of iterations in the first loop. OpenMP's general requirement for parallelized loops is their *canonicity*. A for loop is called *canonical* if you can calculate the number of upcoming iterations in advance at its start. This is possible if the following conditions are met simultaneously:

- there are no break and return operations inside the loop;
- there is no goto operation inside the loop leading outside the loop;
- the loop variable (iterator) does not change inside the loop;

In this case, the record of the cycle should have the form "for (i = A; i < B; i += C)", where the numbers A, B, C should not change during the operation of the cycle. The second parameter of the loop can use not only the sign "<", but also ">", "> =", "<=". The third parameter of the loop can not only increment, but also decrement the loop variable (a short form of the entry "i ++" is allowed).

If iteration  $k$  affects the results of iteration  $m$ , then the cycle cannot be parallelized, because it is impossible to predict in advance the order of completion of iterations by multiple threads. The responsibility for detecting such conflicts lies with the programmer. For example, OpenMP will not detect the interdependence of iterations and compile the following program:

```
1  #pragma omp parallel for num_threads(2)
2  for(i = 1; i < 20; i++)
3      a[i] = 2*a[i - 1];
```

In this program stream 0 most likely will not have time to fill in the element  $a[9]$  by the time when stream 1 will calculate the value  $a[10] = 2 * a[9]$ .

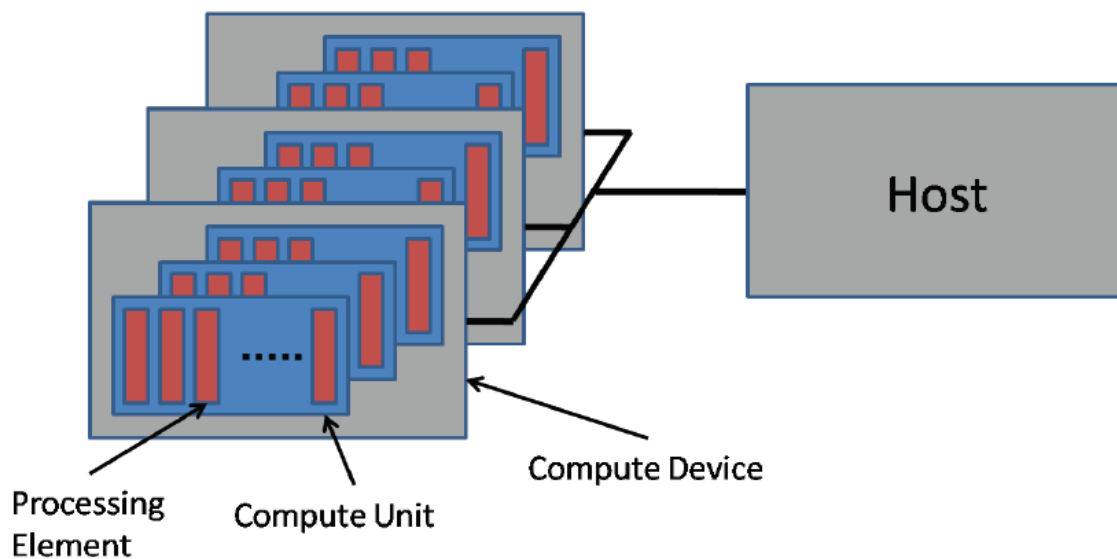
### 3.4 OpenCL Technology

**Brief description of the technology.** OpenCL is a framework for writing computer programs related to parallel computing on various graphic and central

processors, as well as FPGA. OpenCL includes a programming language that is based on the C99 programming language standard, and an application programming interface. OpenCL provides concurrency at the instruction level and data level and is an implementation of the GPGPU technique. OpenCL is a fully open standard, its use is not subject to licensing fees. Using this technology, heterogeneous parallel computing can be performed (distribute tasks between different devices).

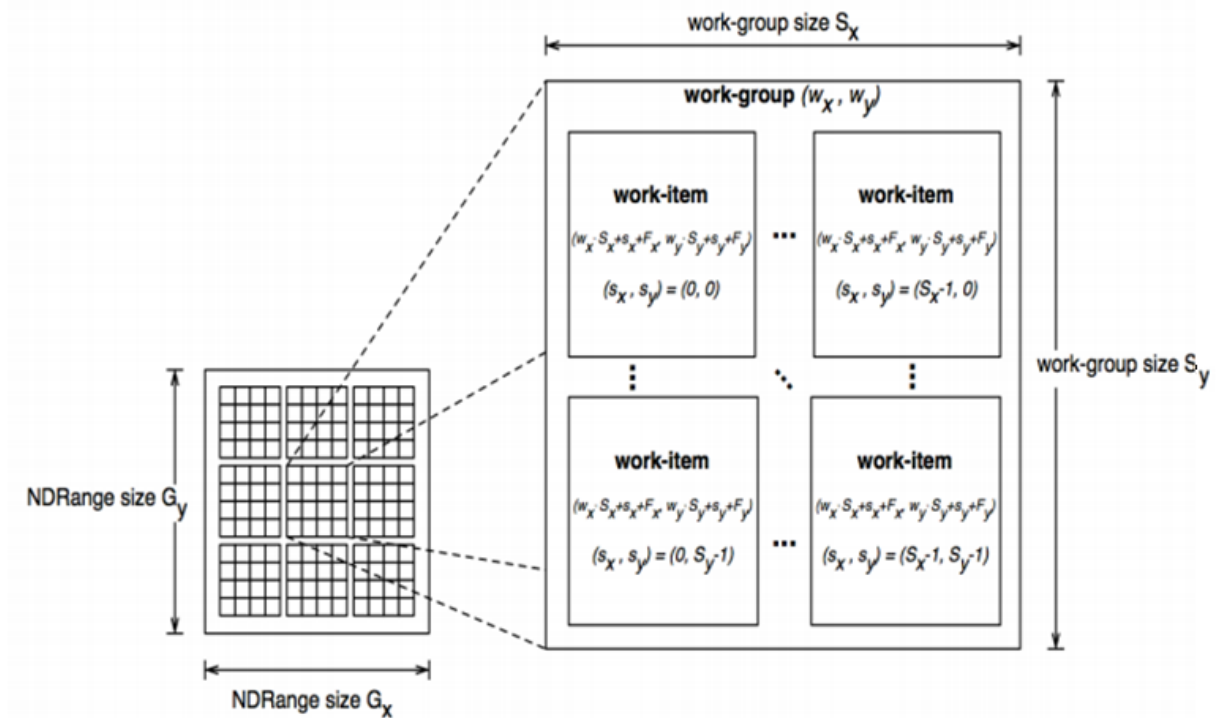
As we already know, it is possible to parallelize a program by tasks between a small number of productive cores (processors of modern PCs) or by data between thousands of simple slow cores (computing cores of modern GPUs). It is for problems solved using data parallelization that OpenCL is used.

**OpenCL Technology Architecture** OpenCL divides two types of devices: *host*, which controls the common logic, and *device*, which perform the calculations. The *host* is usually the central processor, while the *device* is the GPU and other devices. *Device* divided into compute modules *compute units*, which in turn consist of processing elements (*processing elements*) (figure 14). Direct calculations are performed in the processing elements of the device.



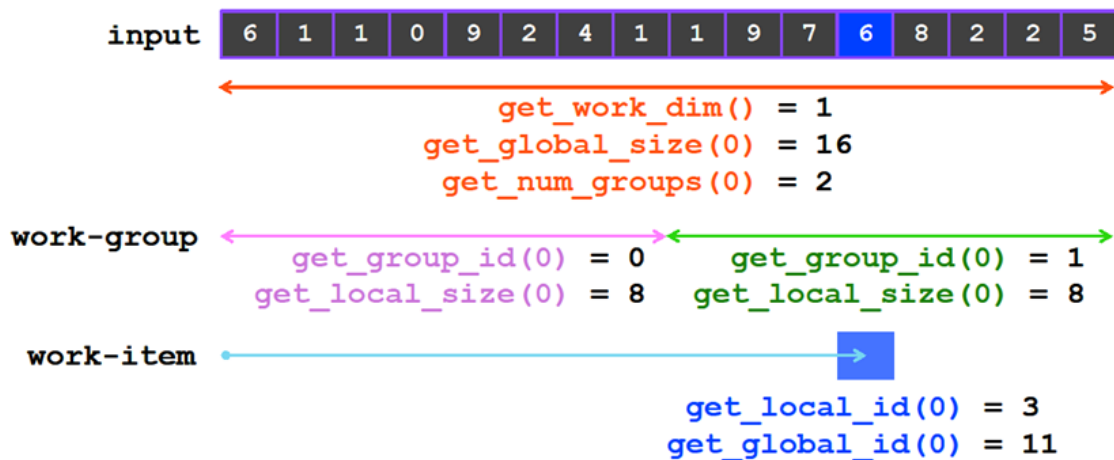
*Puc. 14: OpenCL Architecture*

Physically *computer unit* is *work-group*, which consists of *cells work-item*, which perform the calculations (figure 15).



Puc. 15: OpenCL Architecture - the structure of work-group element

Commands in OpenCL form a queue. *Host* routes commands to devices. These teams queue up similar teams. You can implement a queue in order and without compliance. ID functions *work-group* and *work-item* are shown on figure 16.



Puc. 16: OpenCL. Work with work-group u work-item

**Types of memory in OpenCL devices.** To interact with data, the programmer can use different levels of memory. On the figure 17 it we can

see that the following types of memory exist:

- Private memory. The fastest of all kinds. Exclusive for every item of work.
- Local memory. It can be used by the compiler with a large number of local variables in any function. In terms of speed characteristics, local memory is much slower than register memory. Access from work items in one work-group.
- Constant memory. Fast enough of the available GPUs. It is possible to write data from the host, but at the same time, it is only possible to read data within the entire GPU. Dynamic allocation, unlike global memory, is not supported in constant memory.
- Global memory. The slowest type of memory available from the GPU. Global variables can be selected using the specifier, as well as dynamically. The global memory is mainly used to store large amounts of data received on the device from the host's. In algorithms requiring high performance, the number of operations with global memory must be minimized.



*Puc. 17: Types of memory in OpenCL devices*

The programmer must explicitly give copies between different memory.

An OpenCL program may include the following sequence of actions:

1. **Platform choice:** `clGetPlatformIDs`, `clGetPlatformInfo`
2. **Device choice:** `clGetDeviceIDs`, `clGetDeviceInfo`
3. **Creating Computational Context:** `clCreateContextFromType`
4. **Create a command queue:** `clCreateCommandQueueWithProperties`
5. **Buffer Allocation:** `clCreateBuffer`
6. **Creating a program object:** `clCreateProgramWithSource`
7. **Code compilation:** `clBuildProgram`
8. **Kernel Creation:** `clCreateKernel`
9. **Working with Work-Group:** `clGetKernelWorkGroupInfo`

10. **Kernel execution:** clEnqueueNDRangeKernel

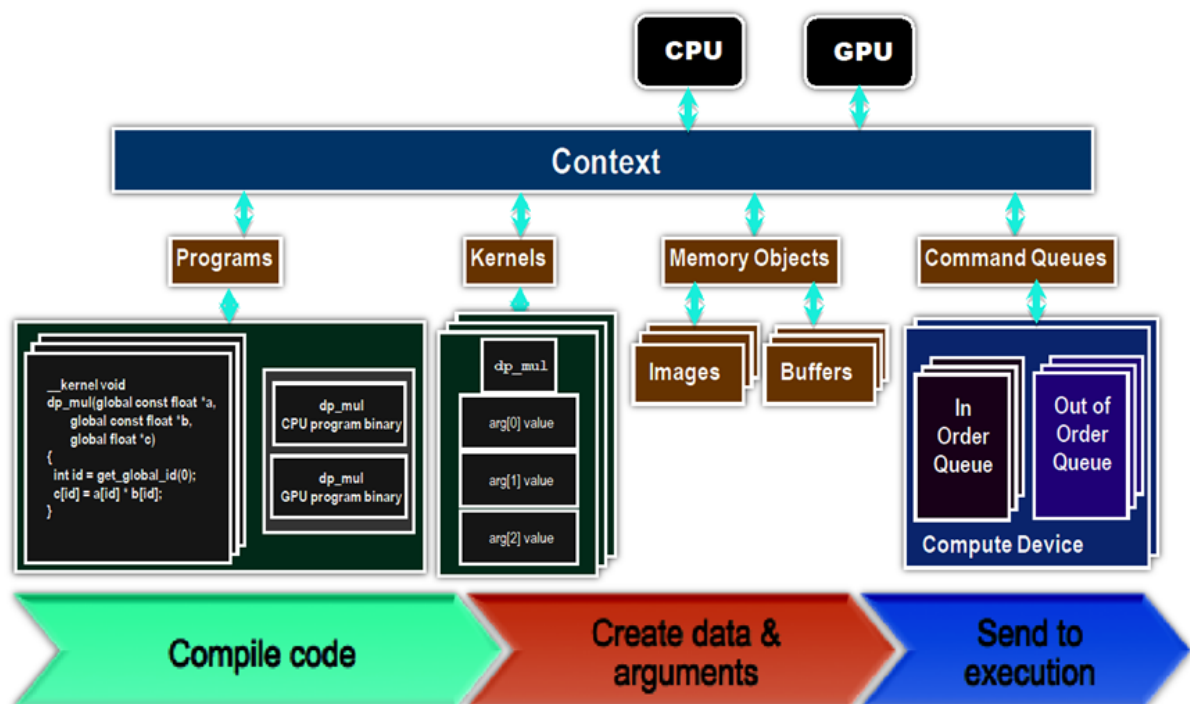
11. **Kernel Pending:** clWaitForEvents

12. **Profiling:** clGetEventProfilingInfo

Next, we consider some of these actions in more detail.

**Platform, device, and context selection.** (*Context*) is required to manage OpenCL objects and resources. All OpenCL resources are context bound. The following data is associated with the context. (figure 18):

- devices
- object objects
- kernel
- memory objects
- command queues.



*Puc. 18: OpenCL Architecture - Context*

It is possible to obtain information about the platform and the computing core using special functions, then to create a context:



- *clGetPlatformInfo()* - contains information about the platform on which the program runs
- *clGetDeviceDs()* - contains information about connected devices
- *clGetDeviceInfo()* - contains information about this device: its type, compatibility, etc.

Context can be created using the function *clCreateContext()*. Here is an example of its creation:

```

/*1*/    //Get the platform ID
/*2*/    cl_platform_id platform;
/*3*/    clGetPlatformIDs(1, &platform, NULL);
/*4*/
/*5*/    //Get the first GPU device associated with the platform
/*6*/    cl_device_id device;
/*7*/    clGetDeviceIDs(platform, CL_DEVICE_TYPE_GPU, 1, &device, NULL);
/*8*/
/*9*/    //Create an OpenCL context for the GPU device
/*10*/    cl_context context;
/*11*/    context = clCreateContext(NULL, 1, &device, NULL, NULL, NULL);

```

*Puc. 19: OpenCL Architecture - Creating a context*

In line 3 we get the platform ID, in line 7 the ID of the first GPU on this platform, in line 11 we create a context for this device. You can read more about the arguments accepted by these functions in the documentation. There is also a function *clCreateContextFromType()* to create the context associated with devices of a particular type.

**Kernel.** A kernel is a function that is part of a program and runs in parallel on a device. The kernel is an analog of a stream function. The part running on the device consists of a set of cores declared with a qualifier **\_\_kernel**. Kernel compilation can be performed at runtime using API functions. Work within the same work group is performed simultaneously by all work items.

When writing the kernel, you can use the following qualifiers for variables:

- **\_\_global** or **global** – data in global memory.
- **\_\_constant** or **constant** – data in constant memory.
- **\_\_local** or **local** – data in local memory.
- **\_\_private** or **private** – data in private memory.

- `__read_only` и `__write_only` – access mode qualifiers.

We can compile kernel code using functions `clCreateProgramWithSource()`, `clBuildProgram()` и `clCreateKernel()`. An example of compiling and running a program to multiply two arrays is given in figure 20.

```
// Build program object and set up kernel arguments
const char* source = "__kernel void dp_mul(__global const float *a, \n"
                    "                    __global const float *b, \n"
                    "                    __global float *c, \n"
                    "                    int N) \n"
                    "{ \n"
                    "    int id = get_global_id (0); \n"
                    "    if (id < N) \n"
                    "        c[id] = a[id] * b[id]; \n"
                    "} \n";

cl_program program = clCreateProgramWithSource(context, 1, &source, NULL, NULL);
clBuildProgram(program, 0, NULL, NULL, NULL, NULL);
cl_kernel kernel = clCreateKernel(program, "dp_mul", NULL);
clSetKernelArg(kernel, 0, sizeof(cl_mem), (void*)&d_buffer);
clSetKernelArg(kernel, 1, sizeof(int), (void*)&N);

// Set number of work-items in a work-group
size_t localWorkSize = 256;
int numWorkGroups = (N + localWorkSize - 1) / localWorkSize; // round up
size_t globalWorkSize = numWorkGroups * localWorkSize; // must be evenly divisible by localWorkSize
clEnqueueNDRangeKernel(cmd_queue, kernel, 1, NULL, &globalWorkSize, &localWorkSize, 0, NULL, NULL);
```

NDRange

*Рис. 20: OpenCL - compiling and running the kernel*

You can read more about other features of OpenCL technology in official documentation.

1. OpenCL – official site: <http://www.khronos.org/opencv/>
2. Intel OpenCL: <http://software.intel.com/en-us/articles/intel-opencv-sdk/>
3. NVIDIA OpenCL: [http://www.nvidia.ru/object/cuda\\_opencv\\_new\\_ru.html](http://www.nvidia.ru/object/cuda_opencv_new_ru.html)
4. AMD OpenCL: <http://www.amd.com/us/products/technologies/stream-technology/opencv/Pages/opencv.aspx>

### 3.5 Errors in multithreaded applications

In addition to the errors common to a programmer, there are a number of errors specific to parallel computing. These errors are caused by the following features of parallel programs:

- **Thread synchronization.** The programmer must ensure the correct sequence of operations performed by different flows. In the general case, it is impossible to say exactly in what sequence the flow commands will be executed, since the operating system may suspend the flow at any time.
- **Thread interaction.** Also, the programmer should not allow conflicts when accessing memory areas common to threads.
- **Load balancing.** If in a parallelized program one of the threads does 99 % of the work, then even on a 64-core system parallel acceleration is unlikely to exceed 1.01.
- **Scalability.** In the ideal case, a parallel program should equally well parallel the work performed on any available number of processors. However, this is not easy to achieve and this often leads to hard-to-detect errors.

Further, we consider in more detail the following incomplete list of typical errors that occur in parallel programs regardless of the parallelization technology used:

- Loss of precision in floating point operations.
- Deadlocks
- Race conditions.
- ABA problems.
- Inversion of priorities.
- Starvation.
- False Sharing.

**Loss of accuracy** If a parallel program is used for floating-point operations when working with variables located in the threads common memory, then

each time the program is launched, a different result of material calculations may be obtained. This is because when several threads work at the same time, it is impossible to accurately predict in what order the operating system will provide the processor with these threads, because at any time, any thread can be temporarily suspended at the discretion of the OS. This in turn leads to an indefinite sequence of floating-point operations, the result of which, as you know, may depend on the order.

Consider an example illustrating the above:

```
1  int i;  
2  float s = 0;  
3  #pragma omp parallel for reduction (+:s) num_threads(8)  
4  for (i = 1; i < 1000000; ++i) {  
5      s += 1.0/i;  
6  }  
7  printf("s=%f\n", s);
```

The variable `s` sums up the results of real calculations with eight threads. The result is `s = 14.393189`. However, if only one thread executes the same program (for this you need to set the parameter `num_threads` to 1 in line 3), the result will be different: `s = 14.357357`. The difference between the two values is approximately 0.25 %.

It turns out that a parallel program can give different results when launched on different platforms. This should be taken into account when verifying parallel programs using their single-threaded unparallelized analogues.

**Deadlocks.** One of the commonly used synchronization primitives is a mutex, which allows several threads to consistently and sequentially execute critical areas of code located inside parallel sections of code. Critical sections slow down the program, because at each moment of time, only one thread can be inside the critical section. Using mutexes, for example, `omp` functions are implemented `_set_lock` and `omp_unset_lock` in OpenMP. When these functions frame a certain section of code, you can make a critical section from it, the entrance to which is controlled by a conditional program lock. In complex programs can use several locks. This can lead to the fact that two threads, capturing several locks, stop the execution of each other without any possibility to exit the state of waiting for each other. This situation is called deadlock.

The simplest example of deadlock is the operation of two threads, the first of which captures lock 1, then lock 2, and the second first captures lock 2, then lock 1. As a result, deadlock occurs if the operations are performed in the following order:

- thread1 captured lock 1;

- thread2 captured lock 2;
- thread1 endlessly waits for release of lock 2;
- thread2 endlessly waits for release of lock 1.

One of the unpleasant aspects of the described situation is that far from always mutual blocking occurs when debugging a program, when it could be easily detected and fixed, because the probability of overlapping events in the right way can be very small. As a result, a program that is running and delivered to the customer may “freeze” at random times for allegedly unknown reasons. Consider an example of an artificially implemented deadlock in which you can calculate the likelihood of its occurrence upon repeated startup.

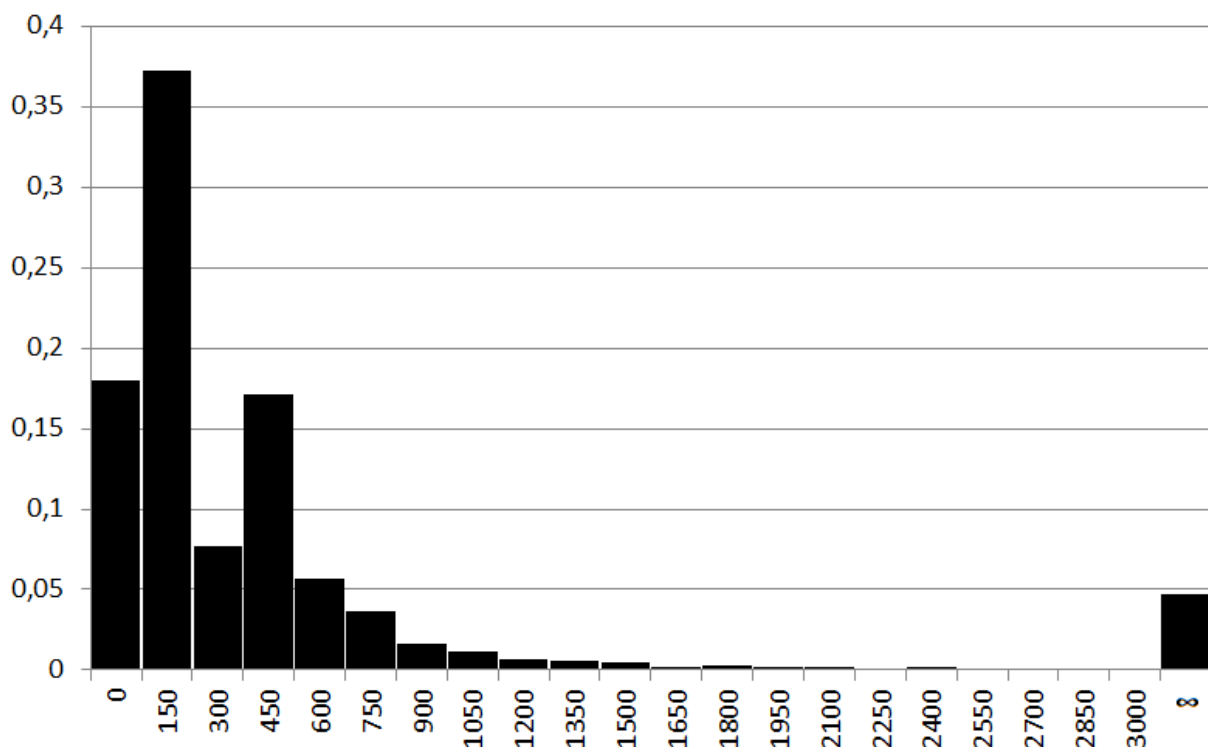
In the program below, in line 7, a stream is created that captures castle1, castle2 in an infinite loop and increments the variable s, freeing both locks after that. In line 13, a stream is created, which also infinitely increments s, but captures the locks in a different order: castle2, castle1. Line 19 creates a thread that monitors the state of s, polling this variable every 10 ms. If the last thread detects that the variable s has stopped changing, it prints a message about the deadlock and the program terminates.

```

1  int old_s, s = 0;
2  omp_lock_t lock1, lock2;
3  omp_init_lock(&lock1);
4  omp_init_lock(&lock2);
5  #pragma omp parallel sections
6  {
7      #pragma omp section
8      for (;;) {
9          omp_set_lock(&lock1);    omp_set_lock(&lock2);
10         s++;
11         omp_unset_lock(&lock2);    omp_unset_lock(&lock1);
12     }
13     #pragma omp section
14     for (;;) {
15         omp_set_lock(&lock2);    omp_set_lock(&lock1);
16         s++;
17         omp_unset_lock(&lock1);    omp_unset_lock(&lock2);
18     }
19     #pragma omp section
20     {
21         for(old_s = !s; old_s != s; old_s = s)
22             usleep(10000);
23         printf("Deadlock with s=%i\n", s);
24         omp_destroy_lock(&lock1);    omp_destroy_lock(&lock2);
25         exit(0);
26     }
27 }
```

The experiments with the above program were carried out on a computer with an Intel Core i5 processor (4 logical processors) with 8 gigabytes of RAM in the Debian Wheezy operating system. The program was run 10,000 times, and 10,000 values of the variable  $s$  were obtained at the time the deadlock occurred. The results of these measurements are shown in the figure. 21 in the form of a histogram of the distribution density  $s$ .

In the above figure, the right borders of the columns are marked on the abscissa. The last column contains all hits from 3000 to infinity. The average value of  $s$  in the described case turned out to be 2445, i.e. two threads manage to capture and release the locks in an obviously wrong dangerous order without a deadlock approximately 1222.5 times.



*Puc. 21: Histogram of the distribution of the number of starts of parallel programs before deadlock occurs*

To correct the described error, you need to make the lock capture order the same in all threads. It is sometimes advised throughout the program to establish some general rule for locking locks, for example, you can lock locks in alphabetical order.

In addition to the described situation with the wrong order of capture of mutexes, there are other reasons for deadlocks. For example, the reacquisition of the mutex (lock). An incorrectly written program may try to re-capture the lock it has already captured, without first releasing it. In this case, a repeated

attempt to capture completely stops the flow. If the program logic requires re-capture of the mutex (for example, to organize recursion), you should use a special subspecies of locks: recursive mutexes.

**Race conditions** - an error in a parallel program in which the result of the calculation depends on the order in which the code is executed (it may be different each time the parallel program is launched). For example, consider the following situation. One thread changes the value of a global variable. At this time, the second thread prints this value. If the second thread prints the value before the first one changes it, the program will execute correctly, however, if the code is executed later, the new value assigned in the first thread will be displayed.

```
1  int a = 0;
2  #pragma omp parallel num_threads(2) shared(a)
3  {
4      if (omp_get_thread_num() == 0) //first thread
5          a = 2; //changes global variable value
6      else { //second thread
7          printf("%d",a); //print var value: 0 or 2?
8      }
9  }
```

This problem can happen even in programs in which multi-threaded programming is not used explicitly, but some shared resources are used. For example, if a program copies text from an input field to the clipboard and then text is immediately inserted into another field, then if it runs on a computer alone, it will always work correctly. However, if a program that also uses the clipboard runs at the same time, it can overwrite the value of the clipboard, even if the copy and paste commands are located strictly one after another. Using shared resources, even for a very short time, can cause errors.

Such a manifestation was called the "heisenbug " or "floating error ". To avoid this situation, it is necessary to block the recording of the new variable value in the first thread until the second thread finishes work. For example, in OpenMP technology, this problem can be solved as follows (save the old value in another variable):

```

1  int a = 0;
2  int old_a = a;
3  #pragma omp parallel num_threads(2) shared(a)
4  {
5      if (omp_get_thread_num() == 0) //first thread
6          a = 2; //changes global variable value
7      else { //second thread
8          printf("%d",old_a); //print old variable value
9      }
10 }

```

**ABA problem** - the problem is that the thread reading the same value twice “thinks” that the data has not changed. For example, the first thread assigned a variable the value *A*. The second thread assigned it the value *B*, and then again *A*. When the first thread reads this variable again, it is equal to *A*, and it “thinks” that nothing has changed. A more practical example from programming: an address is stored in a variable that points to the beginning of the array. The second thread frees memory for the new array with the free function and creates it with the malloc function, which allocated memory in the same place, since this memory area is already free. When the first thread compares the values of the pointer to the array before and after, it sees that they are equal and decides that the array has not changed, although new data is already stored in its place. To solve this problem, you can store a sign that the array has been modified.

**Priority inversion.** Imagine a situation where there are 3 threads with priorities: high, medium and low, and threads with high and low priority capture the general mutex. Let the low priority thread capture the mutex and begin execution, but the medium priority thread interrupt it. Now, if a thread with a high priority intercepts a priority and starts executing, it will wait for the mutex to be freed, but a thread with a low priority cannot release it, since a thread with a medium priority has replaced it. This problem is solved by assigning all threads the same priority for the duration of the mutex retention.

**Starvation** occurs when a thread with a low priority is in a ready state for a long time and is idle. Such starvation is caused by a lack of processor time, there is also a starvation caused by the inability to work with data (ban on reading and / or writing). In modern operating systems, this problem is solved as follows: even if the thread has a very low priority, it is still called for execution after a certain amount of time. In your programs, you should intelligently divide tasks between threads so that a thread performing a more important and long task has a higher priority.

**False sharing** - situation that arises with systems that support memory (cache) coherence, in which extra (unnecessary programs at this point) operations are performed to transfer data between streams. *Memory (Caches) Coherence*



- a memory property in which when changing the value of a memory cell by one process, these changes become visible in other processes. Large resources are spent on organizing such memory, since each time the value changes in one thread, the others need to be notified. Consider the following example:

```
1  struct str {
2      char a;
3      char b;
4  };
5  int n = 10000;
6  struct str array[n];
7
8  void fprint_a()
9  {
10     for (int i = 0; i < n; ++i)
11         str[i].a = 'a';
12 }
13
14 void fprint_b()
15 {
16     for (int i = 0; i < n; ++i)
17         str[i].b = 'b';
18 }
```

If you run the functions `fprint_a` and `fprint_b` in two different threads, then due to the constant synchronization of memory between the threads, the program will run slowly, since `a` and `b` are on the same cache line (usually 64 bytes). It would be more reasonable to parallelize each loop between threads (for example, using the preprocessor directive `#pragma omp parallel for` in OpenMP).

## 4 Лабораторная работа №1. «Автоматическое распараллеливание программ»

### 4.1 Порядок выполнения работы

1. На компьютере с многоядерным процессором установить ОС Linux и компилятор GCC версии не ниже 4.7.2. При невозможности установить Linux или отсутствии компьютера с многоядерным процессором можно выполнять лабораторную работу на виртуальной машине.
2. На языке Си написать консольную программу lab1.c, решающую задачу, указанную в п.IV (см. ниже). В программе нельзя использовать библиотечные функции сортировки, выполнения матричных операций и расчёта статистических величин. В программе нельзя использовать библиотечные функции, отсутствующие в стандартных заголовочных файлах stdio.h, stdlib.h, math.h, sys/time.h. Задача должна решаться 50 раз с разными начальными значениями генератора случайных чисел (ГСЧ). Структура программы примерно следующая:

```
1  #include <stdio.h>
2  #include <stdlib.h>
3  #include <sys/time.h>
4  int main(int argc, char* argv[])
5  {
6      int i, N;
7      struct timeval T1, T2;
8      long delta_ms;
9      N = atoi(argv[1]); /* N равен первому параметру командной строки */
10     gettimeofday(&T1, NULL); /* запомнить текущее время T1 */
11     for (i=0; i<50; i++) /* 50 экспериментов */
12     {
13         srand(i); /* инициализировать начальное значение ГСЧ */
14         /* Заполнить массив исходных данных размером N */
15         /* Решить поставленную задачу, заполнить массив с результатами
16         */
17         /* Отсортировать массив с результатами указанным методом */
18         gettimeofday(&T2, NULL); /* запомнить текущее время T2 */
19         delta_ms = 1000*(T2.tv_sec - T1.tv_sec) + (T2.tv_usec - T1.tv_usec)
20         /1000;
21         printf("\nN=%d. Milliseconds passed: %ld\n", N, delta_ms); /* T2 -
22         T1 */
23         return 0;
24     }
```

3. Скомпилировать написанную программу без использования авто-

матического распараллеливания с помощью следующей команды:  
`/home/user/gcc -O3 -Wall -Werror -o lab1-seq lab1.c`

4. Скомпилировать написанную программу, используя встроенное в gcc средство автоматического распараллеливания Graphite с помощью следующей команды `"/home/user/gcc -O3 -Wall -Werror -floop-parallelize-all -ftree-parallelize-loops=K lab1.c -o lab1-par-K"` (переменной K поочерёдно присвоить хотя бы 4 различных целых значений, выбор обосновать).
5. В результате получится одна нераспараллеленная программа и четыре или более распараллеленных.
6. Закрыть все работающие в операционной системе прикладные программы (включая Winamp, uTorrent, браузеры и Skype), чтобы они не влияли на результаты последующих экспериментов.
7. Запускать файл `lab1-seq` из командной строки, увеличивая значения N до значения N1, при котором время выполнения превысит 0.01 с. Подобным образом найти значение  $N=N2$ , при котором время выполнения превысит 2 с.
8. Используя найденные значения N1 и N2, выполнить следующие эксперименты (для автоматизации проведения экспериментов рекомендуется написать скрипт):
  - запускать `lab1-seq` для значений  $N = N1, N1 + \Delta, N1 + 2\Delta, N1 + 3\Delta, \dots, N2$  и записывать получающиеся значения времени `delta_ms(N)` в функцию `seq(N)`;
  - запускать `lab1-par-K` для значений  $N = N1, N1 + \Delta, N1 + 2\Delta, N1 + 3\Delta, \dots, N2$  и записывать получающиеся значения времени `delta_ms(N)` в функцию `par - K(N)`;
  - значение  $\Delta$  выбрать так:  $\Delta = (N2 - N1)/10$ .
9. Написать отчёт о проделанной работе.
10. Подготовиться к устным вопросам на защите.
11. Найти вычислительную сложность алгоритма до и после распараллеливания, сравнить полученные результаты.

12. **Необязательное задание №1 (для получения оценки «четыре» и «пять»).** Провести аналогичные описанным эксперименты, используя вместо gcc компилятор Solaris Studio (или любой другой на своё усмотрение). При компиляции следует использовать следующие опции для автоматического распараллеливания: `«solarisstudio -cc -O3 -xautopar -xloopinfo lab1.c»`.
13. **Необязательное задание №2 (для получения оценки «пять»).** Это задание выполняется только после выполнения предыдущего пункта. Провести аналогичные описанным эксперименты, используя вместо gcc компилятор Intel ICC (или любой другой на своё усмотрение). В ICC следует при компиляции использовать следующие опции для автоматического распараллеливания: `«icc -parallel -par-report -par-threshold K -o lab1-icc-par-K lab1.c»`.
- Если ключ `«-par-report»` не работает в вашей версии компилятора, то желательно использовать более актуальный ключ `«-qopt-report-phase=par»`.

## 4.2 Состав отчета

1. Титульный лист с названием вуза, ФИО студента и названием работы.
2. Содержание отчета (с указанием номера страниц и т.п.).
3. Описание решаемой задачи (взять из п.I и п.IV).
4. Краткая характеристика использованного для проведения экспериментов процессора, операционной системы и компилятора GCC (официальное название, номер версии/модели, разрядность, количество ядер, ёмкость ОЗУ и т.п.).
5. Полный текст программы lab1.c в виде отдельного файла.
6. Таблицы значений и графики функций  $seq(N)$ ,  $par-K(N)$  с указанием величины параллельного ускорения.
7. Подробные выводы с анализом приведённых графиков и полученных результатов.
8. Отчёт предоставляется на бумажном носителе или на флешке.

### 4.3 Подготовка к защите

1. Уметь объяснить каждую строку программы, представленной в отчёте.
2. Знать о назначении и основных особенностях GCC, а также о назначении всех использованных в работе ключей компиляции GCC.
3. Знать материал лекции №1.
4. Взять с собой все нужные файлы для демонстрации работы программы.

### 4.4 Варианты заданий

Вариант задания выбирается в соответствии с приведёнными ниже описанием этапов, учитывая, что число  $A = \Phi * И * О$ , где  $\Phi$ ,  $И$ ,  $О$  означают количество букв в фамилии, имени и отчестве студента. Номер варианта в соответствующих таблицах выбирается по формуле  $X = 1 + ((A \bmod 47) \bmod B)$ , где  $B$  – количество элементов в соответствующей таблице, а операция  $\bmod$  означает остаток от деления. Например, при  $A = 476$  и  $B = 5$ , получим  $X = 1 + ((470+6) \bmod 47) \bmod 5 = 1 + (6 \bmod 5) = 2$ . Порядок вычислений должен быть следующим:

1. **Этап Generate.** Сформировать массив  $M1$  размерностью  $N$ , заполнив его с помощью функции `rand_r` (нельзя использовать `rand`) случайными вещественными числами, имеющими равномерный закон распределения в диапазоне от 1 до  $A$  (включительно). Аналогично сформировать массив  $M2$  размерностью  $N/2$  со случайными вещественными числами в диапазоне от  $A$  до  $10*A$ .
2. **Этап Map.** В массиве  $M1$  к каждому элементу применить операцию из таблицы:

| Номер<br>варианта | Операция   |
|-------------------|--|
| 1                 | Гиперболический синус с последующим возведением в квадрат            |
| 2                 | Гиперболический косинус с последующим увеличением на 1               |
| 3                 | Гиперболический тангенс с последующим уменьшением на 1               |
| 4                 | Гиперболический котангенс<br>корня числа                             |
| 5                 | Деление на Пи с последующим возведением в третью степень             |
| 6                 | Кубический корень после деления<br>на число e                        |
| 7                 | Экспонента квадратного корня<br>(т.е. $M1[i] = \exp(\sqrt{M1[i]})$ ) |

Затем в массиве M2 каждый элемент поочерёдно сложить с предыдущим (для этого вам понадобится копия массива M2, из которого нужно будет брать операнды), а к результату сложения применить операцию из таблицы (считать, что для начального элемента массива предыдущий элемент равен нулю):

| Номер<br>варианта | Операция  |
|-------------------|---|
| 1                 | Модуль синуса (т.е. $M2[i] =  \sin(M2[i] + M2[i-1]) $ ) |
| 2                 | Модуль косинуса   |
| 3                 | Модуль тангенса   |
| 4                 | Модуль котангенса                                       |
| 5                 | Натуральный логарифм модуля тангенса                    |
| 6                 | Десятичный логарифм, возведенный в степень e            |
| 7                 | Кубический корень после умножения на число Пи           |
| 8                 | Квадратный корень после умножения на e                  |

3. **Этап Merge.** В массивах M1 и M2 ко всем элементам с одинаковыми индексами попарно применить операцию из таблицы (результат записать в M2):

| Номер варианта | Операция   |
|----------------|--|
| 1              | Возведение в степень (т.е. $M2[i] = M1[i]^{M2[i]}$ ) |
| 2              | Деление (т.е. $M2[i] = M1[i]/M2[i]$ )                |
| 3              | Умножение  |
| 4              | Выбор большего (т.е. $M2[i] = \max(M1[i], M2[i]))$ ) |
| 5              | Выбор меньшего                                       |
| 6              | Модуль разности                                      |

4. **Этап Sort.** Полученный массив необходимо отсортировать методом, указанным в таблице (для этого нельзя использовать библиотечные функции; можно взять реализацию в виде свободно доступного исходного кода):

| Номер варианта | Операция  |
|----------------|---|
| 1              | Сортировка выбором (Selection sort).                  |
| 2              | Сортировка расчёской (Comb sort).                     |
| 3              | Пирамидальная сортировка (сортировка кучи, Heapsort). |
| 4              | Глупая сортировка (Stupid sort).                      |
| 5              | Гномья сортировка (Gnome sort).                       |
| 6              | Сортировка вставками (Insertion sort).                |
| 7              | Сортировка выбором (Selection sort).                  |

5. **Этап Reduce.** Рассчитать сумму синусов тех элементов массива  $M2$ , которые при делении на минимальный ненулевой элемент массива  $M2$  дают чётное число (при определении чётности учитывать только целую часть числа). Результатом работы программы по окончании пятого этапа должно стать одно число  $X$ , которое следует использовать для верификации программы после внесения в неё изменений (например, до и после распараллеливания итоговое число  $X$  не должно измениться в пределах погрешности). Значение числа  $X$  следует привести в отчёте для различных значений  $N$ .

## 5 Лабораторная работа №2. «Исследование эффективности параллельных библиотек для С-программ»

### 5.1 Порядок выполнения работы

1. В исходном коде программы, полученной в результате выполнения лабораторной работы №1, нужно на этапах Map и Merge все циклы с вызовами математических функций заменить их векторными аналогами из библиотеки «AMD Framewave» (<http://framewave.sourceforge.net>). При выборе конкретной Framewave-функции необходимо убедиться, что она помечена как MT (Multi-Threaded), т.е. распараллеленная. Полный перечень доступных функций находится по ссылке: [http://framewave.sourceforge.net/Manual/fw\\_section\\_060.html#fw\\_section\\_060](http://framewave.sourceforge.net/Manual/fw_section_060.html#fw_section_060). Например, Framewave-функция min в списке поддерживаемых технологий имеет только SSE2, но не MT.

*Примечание:* выбор библиотеки Framewave не является обязательным, можно использовать любую другую параллельную библиотеку, если в ней нужные функции распараллелены, так, например, можно использовать ATLAS (для этой библиотеки необходимо выключить троттлинг и энергосбережение, а также разобраться с механизмом изменения числа потоков) или Intel Integrated Performance Primitives.

2. Добавить в начало программы вызов Framewave-функции SetNumThreads(M) для установки количества создаваемых параллельной библиотекой потоков, задействуемых при выполнении распараллеленных Framewave-функций. Нужно число M следует устанавливать из параметра командной строки (argv) для удобства автоматизации экспериментов.
3. Скомпилировать программу, не применяя опции автоматического распараллеливания, использованные в лабораторной работе №1. Провести эксперименты с полученной программой для тех же значений  $N_1$  и  $N_2$ , которые использовались в лабораторной работе №1, при  $M = 1, 2, \dots, K$ , где  $K$  – количество процессоров (ядер) на экспериментальном стенде.
4. Сравнить полученные результаты с результатами лабораторной работы №1: на графиках показать, как изменилось время выполне-



ния программы, параллельное ускорение и параллельная эффективность.

5. Написать отчёт о проделанной работе.
6. Подготовиться к устным вопросам на защите.
7. **Необязательное задание №1** (для получения оценки «четыре» и «пять»). Исследовать параллельное ускорение для различных значений  $M > K$ , т.е. оценить накладные расходы при создании чрезмерного большого количества потоков. Для иллюстрации того, что программа действительно распараллелилась, привести график загрузки процессора (ядер) во время выполнения программы при  $N = N_2$  для всех использованных  $M$ . Для получения графика можно как написать скрипт, так и просто сделать скриншот диспетчера задач, указав на скриншоте моменты начала и окончания эксперимента (в отчёте нужно привести текст скрипта или название использованного диспетчера).
8. **Необязательное задание №2** (для получения оценки «пять»). Это задание выполняется только после выполнения предыдущего пункта. Используя закон Амдала, рассчитать коэффициент распараллеливания для всех экспериментов и привести его на графиках. Прокомментировать полученные результаты.

## 5.2 Состав отчета

1. Титульный лист с названием вуза, ФИО студентов и названием работы.
2. Содержание отчета (с указанием номера страниц и т.п.).
3. Краткая характеристика использованного для проведения экспериментов процессора, операционной системы и компилятора (официальное название, номер версии/модели, разрядность, количество ядер, ёмкость ОЗУ и т.п.).
4. Описание особенностей конфигурации использованной параллельной библиотеки, включая описание последовательности шагов, принятых для установки библиотеки, и использованных опций компиляции.

5. Полный текст полученной параллельной программы, а также текст всех скриптов, использованных для компилирования программы и проведения экспериментов.
6. Графики функций времени выполнения использованных программ, а также графики параллельного ускорения и параллельной эффективности для разных  $N$  и  $M$  (допускается совмещать несколько графиков в одной системе координат).
7. Подробные выводы с анализом приведённых графиков и полученных результатов. Отчёт предоставляется на бумажном носителе или на флешке.

### **5.3 Подготовка к защите**

1. Уметь объяснить каждую строку программы, представленной в отчёте.
2. Знать о назначении всех использованных в работе ключей компиляции.
3. Знать материал лекции №2.
4. Взять с собой все нужные файлы для демонстрации работы программы.

## 6 Лабораторная работа №3. «Распараллеливание циклов с помощью технологии OpenMP»

### 6.1 Порядок выполнения работы

1. Добавить во все for-циклы в программе из ЛР №1 следующую директиву OpenMP:  
”#pragma omp parallel for default(none) private(...) shared(...)”. Наличие всех перечисленных параметров в указанной директиве является обязательным.
2. Проверить все for-циклы на внутренние зависимости по данным между итерациями. Если зависимости обнаружались, использовать для защиты критических секций директиву ”#pragma omp critical” или ”#pragma omp atomic” (если операция атомарна), или параметр reduction (предпочтительнее) или вообще отказаться от распараллеливания цикла (свой выбор необходимо обосновать).
3. Убедиться, что получившаяся программа обладает свойством прямой совместимости с компиляторами, не поддерживающими OpenMP (для проверки этого можно скомпилировать программу без опции ”-fopenmp”, в результате не должно быть сообщений об ошибках, а программа должна корректно работать).
4. Провести эксперименты, измеряя параллельное ускорение. Привести сравнение графиков параллельного ускорения с ЛР №1 и ЛР №2.
5. Провести эксперименты, добавив параметр ”schedule” и варьируя в экспериментах тип расписания. Исследование нужно провести для всех возможных расписаний: static, dynamic, guided. Способ варьирования параметра chunk\_size выбрать самостоятельно (но должно быть не менее 5 точек варьирования). Привести сравнение параллельного ускорения при различных расписаниях с результатами п.4.
6. Выбрать из рассмотренных в п.4 и п.5 наилучший вариант при различных  $N$ . Сформулировать условия, при которых наилучшие результаты получились бы при использовании других типов расписания.

7. Найти вычислительную сложность алгоритма до и после распараллеливания, сравнить полученные результаты.
8. Написать отчёт о проделанной работе.
9. Подготовиться к устным вопросам на защите.
10. **Необязательное задание №1** (для получения оценки «четыре» и «пять»). Для иллюстрации того, что программа действительно распараллелилась, привести график загрузки процессора (ядер) от времени при выполнении программы при  $N = N_1$  для лучшего варианта распараллеливания. Для получения графика можно как написать скрипт так и просто сделать скриншот диспетчера задач, указав на скриншоте моменты начала и окончания эксперимента (в отчёте нужно привести текст скрипта или название использованного диспетчера). Недостаточно привести однократное моментальное измерение загрузки утилитой htop, т.к. требуется привести график изменения загрузки за всё время выполнения программы.
11. **Необязательное задание №2** (для получения оценки «пять»). Построить график параллельного ускорения для точек  $N < N_1$  и найти значения  $N$ , при которых накладные расходы на распараллеливание превышают выигрыш от распараллеливания (независимо для различных типов расписания).

## 6.2 Состав отчета

1. Титульный лист с названием вуза, ФИО студентов и названием работы.
2. Содержание отчета (с указанием номера страниц и т.п.).
3. Краткое описание решаемой задачи.
4. Характеристика использованного для проведения экспериментов процессора, операционной системы и компилятора GCC (точное название, номер версии/модели, разрядность, количество ядер и т.п.).
5. Полный текст программы с использованием параметра schedule.
6. Подробные выводы с анализом каждого из приведённых графиков.

7. Отчёт предоставляется в бумажном или электронном виде вместе с полным текстом программы. По требованию преподавателя нужно быть готовыми скомпилировать и запустить этот файл на компьютере в учебной аудитории (или своём ноутбуке).

### **6.3 Подготовка к защите**

1. Уметь объяснить каждую строку программы, представленной в отчёте.
2. Уметь объяснить выводы, полученные в результате работы.
3. Знать назначение каждой директивы OpenMP, использованной в программе.
4. Повторить материал лекции №3, прочитать главу про OpenMP в методическом пособии
5. Прочитать материал о директиве `#pragma_omp_for` в книге Антонова «Параллельное программирование с использованием технологии OpenMP: Учебное пособие», знать ответы на вопросы в конце соответствующей главы.

## 7 Лабораторная работа №4. «Метод доверительных интервалов при измерении времени выполнения параллельной OpenMP-программы»

### 7.1 Порядок выполнения работы

1. В программе, полученной в результате выполнения ЛР-3, так изменить этап Generate, чтобы генерируемый набор случайных чисел не зависел от количества потоков, выполняющих программу. Например, на каждой итерации  $i$  перед вызовом `rand_r` можно вызывать функцию `srand(f(i))`, где  $f$  – произвольно выбранная функция. Можно придумать и использовать любой другой способ.
2. Заменить вызовы функции `gettimeofday` на `omp_get_wtime`.
3. Распараллелить вычисления на этапе Sort, для чего выполнить сортировку в два этапа:
  - Отсортировать первую и вторую половину массива в двух независимых нитях (можно использовать OpenMP-директиву "parallel sections");
  - Объединить отсортированные половины в единый массив.
4. Написать функцию, которая один раз в секунду выводит в консоль сообщение о текущем проценте завершения работы программы. Указанную функцию необходимо запустить в отдельном потоке, параллельно работающем с основным вычислительным циклом.
5. Обеспечить прямую совместимость (forward compatibility) написанной параллельной программы. Для этого все вызываемые функции вида «`omp_*`» можно условно переопределить в препроцессорных директивах, например, так:

```
1 #ifdef _OPENMP
2     #include "omp.h"
3 #else
4     int omp_get_num_procs() { return 1; }
5 #endif
```

6. Провести эксперименты, варьируя  $N$  от  $\min(\frac{N_x}{2}, N_1)$  до  $N_2$ , где значения  $N_1$  и  $N_2$  взять из ЛР-1, а  $N_x$  – это такое значение  $N$ ,

при котором накладные расходы на распараллеливание превышают выигрыш от распараллеливания. Написать отчёт о проделанной работе. Подготовиться к устным вопросам на защите.

7. **Необязательное задание на «четвёрку» и «пятёрку».** Уменьшить количество итераций основного цикла с 100 до 10 и провести эксперименты, измеряя время выполнения следующими методами:

- Использование минимального из десяти полученных замеров;
- Расчёт по десяти измерениям доверительного интервала с уровнем доверия 95%.

Привести графики параллельного ускорения для обоих методов в одной системе координат, при этом нижнюю и верхнюю границу доверительного интервала следует привести двумя независимыми графиками.

8. **Необязательное задание на «пятёрку»:** в п.3 задания на этапе Sort выполнить параллельную сортировку не двух частей массива, а  $k$  частей в  $k$  нитях (тредах), где  $k$  – это количество процессоров (ядер) в системе, которое становится известным только на этапе выполнения программы с помощью команды «`k = omp_get_num_procs()`».

## 7.2 Состав отчета

1. Титульный лист с названием вуза, ФИО студентов и названием работы.
2. Содержание отчета (с указанием номера страниц и т.п.).
3. Краткое описание решаемой задачи.
4. Характеристика использованного для проведения экспериментов процессора, операционной системы и компилятора GCC (точное название, номер версии/модели, разрядность, количество ядер и т.п.).
5. Полный текст программы и использованных в процессе работы скриптов и инструментов с указанием параметров запуска.
6. Подробные выводы с анализом каждого из приведённых графиков.

Отчёт предоставляется в бумажном или электронном виде вместе с полным текстом программы. По требованию преподавателя нужно быть готовыми скомпилировать и запустить этот файл на компьютере в учебной аудитории (или своём ноутбуке).

### **7.3 Подготовка к защите**

1. Уметь объяснить каждую строку программы, представленной в отчёте.
2. Уметь объяснить выводы, полученные в результате работы.
3. Знать назначение каждой директивы OpenMP, использованной в программе.
4. Повторить материал лекции №4, прочитать главу про OpenMP в методическом пособии.
5. Знать ответы на вопросы из разделов «Задание» книги Антонова «Параллельное программирование с использованием технологии OpenMP: Учебное пособие» (см. страницы 12, 28, 35, 54).



## 8 Лабораторная работа №5. «Параллельное программирование с использованием стандарта POSIX Threads»

### 8.1 Порядок выполнения работы

1. Взять в качестве исходной OpenMP-программу из ЛР-5, в которой распараллелены все этапы вычисления. Убедиться, что в этой программе корректно реализован одновременный доступ к общей переменной, используемой для вывода в консоль процента завершения программы.
2. Изменить исходную программу так, чтобы вместо OpenMP-директив применялся стандарт «POSIX Threads»:
  - для получения оценки «3» достаточно изменить только один этап (Generate, Map, Merge, Sort), который является узким местом (bottle neck), а также функцию вывода в консоль процента завершения программы;
  - для получения оценки «4» и «5» необходимо изменить всю программу, но допускается в качестве расписания циклов использовать «schedule static»;
  - для получения оценки «5» необходимо хотя бы один цикл распараллелить, реализовав вручную расписание «schedule dynamic» или «schedule guided».
3. Провести эксперименты и по результатам выполнить сравнение работы двух параллельных программ («OpenMP» и «POSIX Threads»), которое должно описывать следующие аспекты работы обеих программ (для различных  $N$ ):
  - полное время решения задачи;
  - параллельное ускорение;
  - доля времени, проводимого на каждом этапе вычисления («нормированная диаграмма с областями и накоплением»);
  - количество строк кода, добавленных при распараллеливании, а также грубая оценка времени, потраченного на распараллеливание (накладные расходы программиста);
  - остальные аспекты, которые вы выяснили самостоятельно (**Обязательный пункт**);

## **8.2 Состав отчета**

1. Титульный лист с названием вуза, ФИО студентов и названием работы. Содержание отчета (с указанием номера страниц и т.п.).
2. Содержание отчета (с указанием номера страниц и т.п.).
3. Краткое описание решаемой задачи.
4. Характеристика использованного для проведения экспериментов процессора, операционной системы и компилятора GCC (точное название, номер версии/модели, разрядность, количество ядер и т.п.).
5. Полный текст программ («OpenMP» и «POSIX Threads») и использованных в процессе работы скриптов, и инструментов с указанием параметров запуска.
6. Подробные выводы с анализом каждого из приведённых графиков.

Отчёт предоставляется в бумажном или электронном виде вместе с полным текстом программы. По требованию преподавателя нужно быть готовыми скомпилировать и запустить этот файл на компьютере в учебной аудитории (или своём ноутбуке).

## **8.3 Подготовка к защите**

1. Уметь объяснить каждую строку программы, представленной в отчёте.
2. Уметь объяснить выводы, полученные в результате работы.
3. Подготовиться к ответам на вопросы по материалам лекции №5.

## **9 Лабораторная работа №6. «Изучение технологии OpenCL»**

### **9.1 Порядок выполнения работы**

1. Вам необходимо реализовать один (для оценки 3) или два (для оценки 4) этапа вашей программы из предыдущих лабораторных работ. При этом вычисления можно проводить как на CPU, так и на GPU (на своё усмотрение, но GPU предпочтительнее).
2. **Дополнительное задание (оценка 5).**
  - Выполнение заданий для оценки 3 и 4.
  - Расчёт доверительного интервала.
  - Посчитать время 2 способами: с помощью profiling и с помощью обычного замера (как в предыдущих заданиях).
  - Оценить накладные расходы.
  - \* Необязательное задание для магистрантов с большим количеством свободного времени: Проводить вычисления совместно на GPU и CPU (т.е. итерации в некоторой обоснованной пропорции делятся между GPU и CPU, и параллельно на них выполняются).
3. При желании данную лабораторную работу можно написать на CUDA.

### **9.2 Состав отчета**

1. Титульный лист с названием вуза, ФИО студентов и названием работы. Содержание отчета (с указанием номера страниц и т.п.).
2. Краткое описание решаемой задачи.
3. Характеристика использованного для проведения экспериментов процессора, операционной системы и компилятора GCC (точное название, номер версии/модели, разрядность, количество ядер и т.п.).
4. Полный текст распараллеленной программы (для п.2 и п.3).
5. Подробные выводы.

Отчёт предоставляется в бумажном или электронном виде вместе с полным текстом программы. По требованию преподавателя нужно быть готовыми скомпилировать и запустить этот файл на компьютере в учебной аудитории (или своём ноутбуке).

### **9.3 Подготовка к защите**

1. Уметь объяснить каждую строку программы, представленной в отчёте. Уметь объяснить выводы, полученные в результате работы.
2. Прочитать раздел методички 3.4 *Технология OpenCL*.
3. Изучить материал лекции по технологии OpenCL.

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