$$\theta_{PI} = \frac{\sum_{i=1}^k \theta_{j+i} \, d_{j+i} \, w_i}{\sum_{i=1}^k d_{j+i} \, w_i} \quad \text{and} \quad d_{PI} = \frac{\sum_{i=1}^k d_{j+i} \, w_i}{\sum_{i=1}^k w_i}$$