# Workshop 4: Forecasting

(there's a "four-casting" pun in there somewhere)

STAT 464/864 | Discrete Time Series Analysis Skye P. Griffith, Queen's University - Fall 2024

# Setup

Truncated Series

Times to Predict

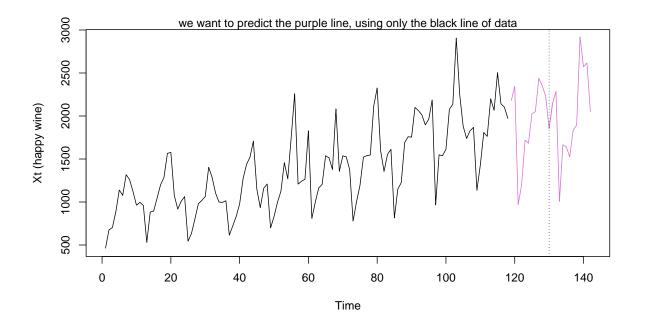
```
Dataset
Source
Happy Australian Red Wine Sales (unit = kilolitres)
Included in the ITSMR Package (no external files)

Total Times Sampled
(Monthly) Jan, 1980 — Oct, 1991 (142 total obs.)
```

Jan, 1980 - Oct, 1989 (118 obs.)

Nov, 1989 - Oct, 1991 (24 obs.)

```
t.past <- 1:118  ; wine.past <- wine[t.past ] # truncated data
t.future <- 119:142  ; wine.future <- wine[t.future] # desired prediction</pre>
```



# **Basic Forecasting using ITSMR**

### Prediction

1. Model the data's trend + seasonal components via classical time-series decomposition.

Note that the available methods include <u>differencing</u>, the effect of which is equivalent to modelling step 3 as an ARIMA process. We will discuss this in W5.

- 2. Obtain the residuals from your classical model.
- 3. Model the residuals as an ARMA(p,q) process.
- 4. Predict some h steps into the future.

## Forecasting Plot

- 1. Plot the "past data," leaving enough horizontal space for our prediction line, and enough vertical space for its 95% confidence interval.
- 2. Add our prediction and its 95% CI to the plot.

## Comparison plot

- 1. Plot the true "future data" (last 12 months of the original dataset) by itself.
- 2. Add our forecast (+ its 95% CI) to the plot, on top of the true data.

#### Interpretation

- 1. Does the true data generally fall within the 95% CI? It should, 95% of the time.
- 2. How wide is that CI? The wider this interval, the worse our estimate's stardard error is.

# Workshop 4 Models

Model	Trend Estimation	Seasonal Component Estimation	ARMA(p,q)
0	Linear Regression	S1 Method; $d = 12$	MA(3)
1	Linear Regression	Harmonic regression; $d = 4$	AR(2)
2	Linear Regression	Harmonic regression; $d = 12$	AR(2)
3	Linear Regression	Harmonic regression; $d = 4, 12$	AR(2)

#### Model 0

### Models 1,2 & 3

```
# --- Classical Models
M.1 <- c("trend", 1,  # linear regression</pre>
          "hr" , 4)
                        # Harmonic regression with period 4
M.2 <- c("trend", 1, "hr", 12)
M.3 \leftarrow c("trend", 1, "hr", c(4,12))
# --- Residuals
R.1 <- Resid(wine.past, M = M.1)
R.2 <- Resid(wine.past, M = M.2)
R.3 <- Resid(wine.past, M = M.3)
# --- AR(2), equivalently ARMA(2,0)
A.1 \leftarrow arma(x = R.1, p = 2, q = 0)
A.2 \leftarrow arma(x = R.2, p = 2, q = 0)
A.3 \leftarrow arma(x = R.3, p = 2, q = 0)
# --- Forecast
fc.1 <- forecast(wine.past, M.1, A.1, 24, 0)
fc.2 <- forecast(wine.past, M.2, A.2, 24, 0)
fc.3 <- forecast(wine.past, M.3, A.3, 24, 0)</pre>
```

# **Plotting Prep**

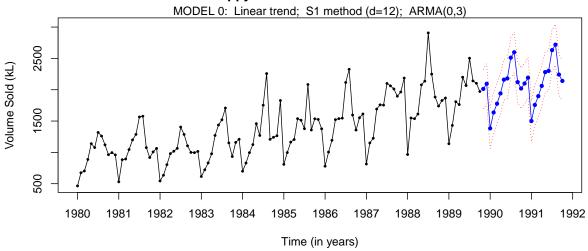
#### **Plot Function**

```
plot.wine <- function(x.range = range(t.past,t.future), # default x-axis lim</pre>
                    plot.ts(wine.past,
         xlim = x.range,
         ylim = y.range,
         # ---- the rest is all from workshop 2
         main = "Happy Austrailian Red Wine Sales", # main title
         xlab = "Time (in years)",
                                                 # x-axis label
         ylab = "Volume Sold (kL)",
                                                # y-axis label
                                                 # lines + points
         type = "o",
         pch = 20, cex = 0.6,
                                                 # bullets
         xaxt = 'n')
                                                 # NO X-AXIS TICKS
 axis(side = 1,
                         # bottom edge of plot
      at = 12*(0:12) + 1, # 1 tick every January (total = 13)
      labels = 1980:1992)  # tick labels
```

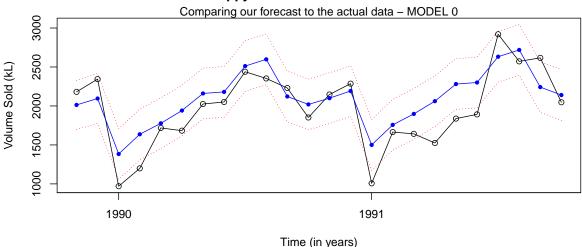
### **Forecasting Plot Function**

# Results - Model 0

### **Happy Austrailian Red Wine Sales**



### **Happy Austrailian Red Wine Sales**



### Interpretation

1. The true data exits our forecast's confidence interval 7 times.

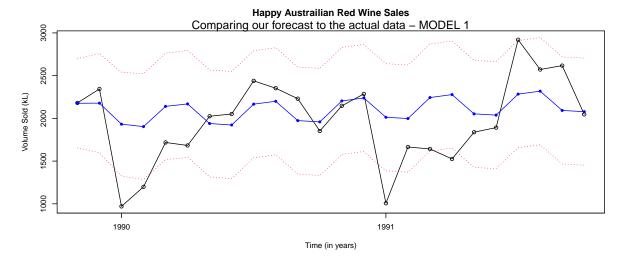
This is more than  $\alpha \times h = 0.05 \times 24 = 1.2$ , which means our CI captured the true data less than the desired 95% of the time.

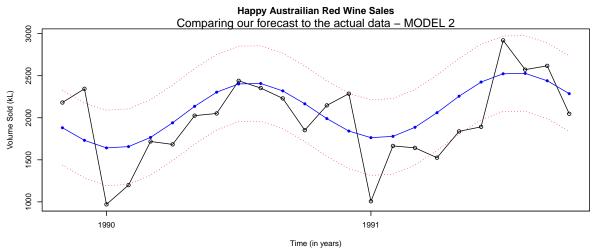
Reminder: we are not technically performing any hypothesis tests here, we're just getting an intuition for how well our forecast fits the data.

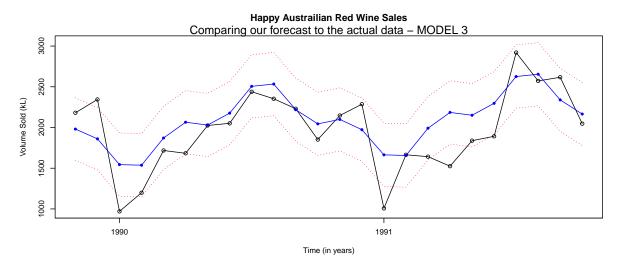
2. The width of the CI looks pretty good to me, but we haven't viewed the results of the other models yet, so we don't have much to compare it with.

# Results - Models 1, 2 & 3

```
par(mfrow = c(3,1), mar = c(4,4,4,1))
# --- Model 1
plot.wine(x.range=range(t.future), y.range=range(wine.future,fc.1$1,fc.1$u))
mtext("Comparing our forecast to the actual data - MODEL 1")
points(x = t.future, y = wine.future, type = "o") # TRUE future vals
plot.forecast(fc.1)
                                                   # ESTIMATED future vals
# --- Model 2
plot.wine(x.range=range(t.future), y.range=range(wine.future,fc.2$1,fc.2$u))
mtext("Comparing our forecast to the actual data - MODEL 2")
points(x = t.future, y = wine.future, type = "o") # TRUE future vals
plot.forecast(fc.2)
                                                   # ESTIMATED future vals
# --- Model 3
plot.wine(x.range=range(t.future), y.range=range(wine.future,fc.3$1,fc.3$u))
mtext("Comparing our forecast to the actual data - MODEL 3")
points(x = t.future, y = wine.future, type = "o") # TRUE future vals
plot.forecast(fc.3)
                                                   # ESTIMATED future vals
```







### Interpretation

- 1. The 95% CI's for Models 1 and 3 fail to capture the true data 5 times, each, over the predicted time interval.
  - Model 2's CI fails to capture said data 6 times, implying a slightly less reliable fit, but still a slight improvement from Model 0. (This discrepancy is quite small).
- 2. The tighter CI on Model 3 indicates a reduced standard error from that of Model 1.
- 3. We conclude that our best forecast is that obtained from Model 3.