

```
% J Hundley
% Lab06
% October 9, 2011
%{
Linear Equation and Regression Correlation Coefficients
Measures the strength of the linear relationship between y and x.
```

Edwin Hubble used the Mount Wilson Observatory telescopes to measure features of nebulae outside the Milky Way. He found that there is a relationship between a nebula's distance from earth and the velocity with which it was traveling from the earth. Hubble's initial data on 24 nebula is presented in Table 1 in the scenario document.

The relationship between distance and velocity led scientists to propose that the universe came into being with a Big Bang, a long time ago. If material scattered from the point of the Big Bang traveling at a constant velocity, the distance traveled can be determined.

- Ask the user to enter several pairs of velocity and distance and save them in two vectors using a counter to determine the index of the vector element
- Use least-squares to find the linear equation  $[y = mx + b]$  that fits the velocity and distance data.

- Velocity will be the independent variable(x) variable and distance dependent variable(y)
- Use fprintf() to print the the linear model equation
- Use linear equation to find the distance given a velocity, interactively
- Print the enter velocity and distance in a sentence with units, two decimal places, and no extra spaces.

```
%}
clc
clear all
```

```
%*****INITIALIZE*****
% initialize counter and accumulators
sumX      = 0; % sum of all x (velocity)
sumY      = 0; % sum of all y (distance)
sumXX     = 0; % sum of x^2 (velocity)
sumXY     = 0; % sum of x*y (velocity*distance)
nCounter  = 1; % count number of pairs entered (n)
```

```
%*****INPUT*****
% ask user to enter a velocity and distance until velocity = 0
xVel(nCounter) = input('Enter the velocity of a nebula(enter 0 to stop): ');
while xVel(nCounter) ~= 0
    yDist(nCounter) = input('Enter the distance of a nebula: ');
    nCounter = nCounter + 1;
    xVel(nCounter) = input('Enter the velocity of a nebula(enter 0 to stop): ');
end % end while
nCounter = nCounter - 1; % don't count xVel(nCounter) = 0
```

```

%*****COMPUTE*****
% accumulate into sums data
for n = 1 : nCounter
    sumX = sumX + xVel(n);           % sum of all x (velocity)
    sumY = sumY + yDist(n);         % sum of all y (distance)
    sumXX = sumXX + xVel(n) ^ 2;    % sum of x^2 (velocity)
    sumXY = sumXY + xVel(n) * yDist(n); % sum of x*y (vel*dist)
end
% compute SLOPE (m)-----
num = nCounter * sumXY - sumX * sumY;
den = nCounter * sumXX - sumX ^ 2;
mSlope = num / den;

% compute INTERCEPT (b)-----
num = sumY * sumXX - sumX * sumXY;
yIntercept = num / den;

%*****OUTPUT*****
% print velocity and distance data
fprintf('\n NEBULA INPUT DATA\n');
fprintf(' VELOCITY  DISTANCE\n');
fprintf(' km/sec  106 parsecs\n');

for n = 1 : nCounter
    fprintf(' %4.0f %5.3f\n', xVel(n), yDist(n));
end

% print LINEAR EQUATION -- y = mx + b
fprintf('\nLINEAR EQUATION: distance = %.4f * velocity + %.3f \n\n', mSlope, yIntercept);

%*****USE LINEAR EQUATION*****
% ask user for velocity
xVelocity = input('Enter a velocity of a nebula from above: ');
% compute distance using linear equation
yDistance = mSlope * xVelocity + yIntercept;
% print velocity and distance
fprintf('For velocity = %.0f, distance = %.3f\n', xVelocity, yDistance);

```

---'Save As' this file using the name in the assignment instructions.  
---Type you information.  
---Submit the completed development plan via Blackboard with you other files.

NAME: J Hundley  
ASSIGNMENT: Lab06  
DATE: October 9, 2011

PROBLEM SOLVING IN ENGINEERING AND SCIENCE  
Always use a systematic problem-solving strategy.

1. STATE THE PROBLEM:

---Describe the problem to be solved for the assignment.  
Given pairs of velocity and distance from the Hubble data.  
Use least-squares to compute the slope and y-intercept of a  
linear equation to estimate the distance for a velocity.

2. DESCRIBE THE INPUT AND OUTPUT REQUIREMENTS:

---List and describe the following as needed to solve the problem, as needed.  
---Include units where needed.

CONSTANTS (known values that don't change):  
N/A

INPUT (values needed to find the output):  
pairs of  
x - velocity km/sec  
y - distance 106 parsecs

OUTPUT (unknowns)  
slope  
y-intercept

Relevant formulas:  
(for complicated equations, it may be helpful to divide it into parts)  
 $mSlope = (nCounter * sumXY - sumX * sumY) / (nCounter * sumXX - sumX^2)$   
 $yIntercept = (sumY * sumXX - sumX * sumXY) / (nCounter * sumXX - sumX^2)$   
 $y = mx + b$  linear equation

3. WORK HAND EXAMPLES

---Solve the problem with a few hand examples.  
---Record the input values used and the results

VELOCITY	DISTANCE
km/sec	106 parsecs
170	0.032
290	0.034
-130	0.214
-70	0.263
-185	0.275

slope = -0.0006  
y-intercept = 0.172

#### 4. DEVELOP AN ALGORITHM:

---Think about the steps used to solve the problem to solve the problem by hand and list them here to create an algorithm.  
---The algorithm steps should be used as comments in your program as a guide.

\*\*\*\*\*INITIALIZE\*\*\*\*\*

initialize counter and accumulators

\*\*\*\*\*INPUT\*\*\*\*\*

while velocity not = 0  
ask user to enter a velocity and distance  
add values to vectors  
increment counter

\*\*\*\*\*COMPUTE\*\*\*\*\*

accumulate into sums data  
compute SLOPE (m)  
compute INTERCEPT (b)

\*\*\*\*\*OUTPUT\*\*\*\*\*

print velocity and distance data in table  
print LINEAR EQUATION --  $y = mx + b$

\*\*\*\*\*USE LINEAR EQUATION\*\*\*\*\*

ask user for velocity  
compute distance using linear equation  
print velocity and distance

#### 5. SOLVE THE PROBLEM:

---This step represents your writing a computer program to solve the problem.  
---NOTE: Do not type your program here. Submit it as a computer program file.  
---Use steps in your algorithm as comments in your program  
to guide the development of you program.

#### 6. TEST THE SOLUTION:

---Run your program using the values from #3 to check for correctness.  
---If there is an error, correct your program code and run again.

COMP1200-MatLab - Lab 06  
Due midnight – Thursday – October 20  
Submit [devPlan06.txt](#) and [Lab06.m](#) via Blackboard

**Before you start writing your program:**

**Read all of these instructions carefully.** The `devPlan06.txt` file at the assignment link is an incomplete development plan. You are to save the file and edit it by adding your name and the date and by completing: 1. STATE THE PROBLEM, 2. DESCRIBE THE INPUT AND OUTPUT REQUIREMENTS, and 3. WORK HAND EXAMPLES. Use the development plan as a guide when writing the m-script file solution for the following problem. **This file must be saved as a .txt file.**

For 3. WORK HAND EXAMPLES, find the slope and y-intercept using at least 4 pairs of velocity(x) and distance(y). **The values in your hand example should NOT be the ones used in the sample input and output below.**

*NOTE: You will see later that the spelling and casing of file names is very important in MATLAB. Your submitted file(s) MUST be spelled and cased as instructed. [-5 points per file for not doing so.]*

**Problem:**

**Program: Lab06.m**

Edwin Hubble used the Mount Wilson Observatory telescopes to measure features of nebulae outside the Milky Way. He found that there is a relationship between a nebula's distance from earth and the velocity with which it was traveling from the earth. Hubble's initial data on 24 nebula is presented in Table 1 in the problem scenario.

The relationship between distance and velocity led scientists to propose that the universe came into being with a Big Bang, a long time ago. If material scattered from the point of the Big Bang traveling at a constant velocity, the distance traveled can be determined.

**Problem Constants:**

See instructions.

**Problem Inputs:**

See instructions.

**Problem Outputs:**

See instructions.

**Other variables:**

See instructions.

**Relevant formulas:**

See instructions.

**Regression Definition:**

A regression is a statistical analysis assessing the association between two variables. It is used to find the relationship between two variables.

**Regression Formula:**

Regression Equation  $y = mx + b$

$$\text{Slope } (m) = \frac{n(\sum xy) - (\sum x)(\sum y)}{n(\sum x^2) - (\sum x)^2}$$

$$\text{Intercept } (b) = \frac{(\sum y)(\sum x^2) - (\sum x)(\sum xy)}{n(\sum x^2) - (\sum x)^2}$$

$n$  is the number of x,y pairs

**Instructions:**

- ☐ Insert comments at the top and throughout each file
  - o Include the follow comments at the beginning of this (and ALL) files.
    - % your name
    - % assignment number
    - % date you completed the assignment
    - % a short narrative about what the file does
  - o Use your development plan as a guide for comments throughout each file
- ☐ Use `clc` and `clear all` at the beginning of your program.
- ☐ Use descriptive variable names.
- ☐ Use Sample Input/Output as a guide.
- ☐ No extra output, i.e., use semicolons!
- ☐ Initialize the counters and accumulator.

*-5 points per file for absence of any of these required comments at the top*

- Loops:
  - Think carefully about what needs to be done before the loop, in the loop, and after the loop
  - Use a **sentinel loop** for entering velocities and distances.
  - Use **counting loops** when summing data and printing table.
- Printing:
  - Use **fprintf** for all output.
  - Decimal places:
    - velocity     0
    - distance    3
    - slope        4
    - y-intercept 3
  - Column numbers **right-justified**, i.e., right-aligned
  - No extra blank spaces in the other output.

#### New commands

fprintf  
input

#### Revisit

using index with a vector, Ch.4  
initialize counter and accumulators  
sentinel loop  
counting loop

#### Other information:

- Ask the user to enter a velocity and distance pair **until zero(0) is entered for velocity**.
- Build vectors to store the velocities and distances using an **index** to assign the values in the elements.
- Count the number of pairs (n) of velocity and distance and use to control for loops later.
- Compute the sums needed to compute the slope and y-intercept.
- Print the contents of the velocity and distance vectors in a two column table with a title and column headings.
- Print slope and y-intercept in the form of a linear equation. Use the answers in your hand example to check slope and y-intercept.
- Ask the user to enter one of the velocities entered earlier and compute the distance using the linear equation that you create. Note: The distance may not be the exact value because of the limited amount of input.

#### Sample Input/Output:

```
Enter the velocity of a nebula (enter 0 to stop): 170
Enter the distance of a nebula: .032
Enter the velocity of a nebula (enter 0 to stop): 290
Enter the distance of a nebula: .034
Enter the velocity of a nebula (enter 0 to stop): -130
Enter the distance of a nebula: .214
Enter the velocity of a nebula (enter 0 to stop): -70
Enter the distance of a nebula: .263
Enter the velocity of a nebula (enter 0 to stop): -185
Enter the distance of a nebula: .275
Enter the velocity of a nebula (enter 0 to stop): 0
```

```
NEBULA INPUT DATA
VELOCITY  DISTANCE
km/sec    106 parsecs
  170      0.032
  290      0.034
 -130      0.214
  -70      0.263
 -185      0.275
```

LINEAR EQUATION: distance = -0.0006 \* velocity + 0.172

```
Enter a velocity of a nebula from above: -70
For velocity = -70, distance = 0.211
```

**The values in  
your hand  
example should  
NOT be the ones  
used in the  
sample.**

#### Submit via Blackboard:

```
devPlan06.txt  Software development method
Lab06.m        MATLAB script file
```