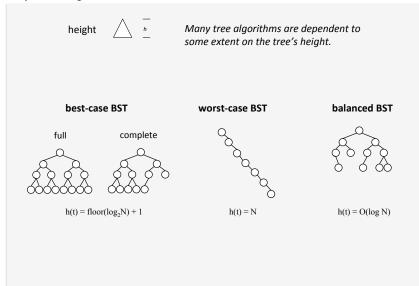
AVL Trees

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Shapes and height

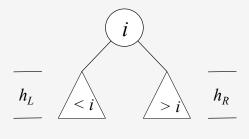


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AVL Trees

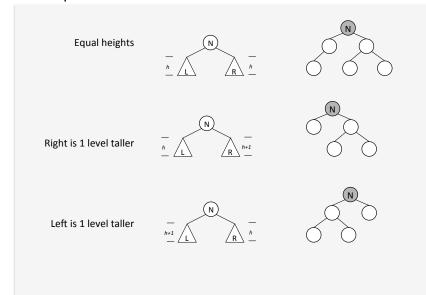
An AVL tree is a **binary search tree** which the heights of the left and right sul

in which the heights of the left and right subtree of *every* node differ by at most 1.



$$|h_R - h_L| \leq 1$$

Structural possibilities



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Balance factors

Every node in an AVL tree has a **balance factor**.





Remember to subtract heights, not balance factors.

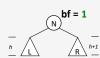


The text counts path lengths differently from



Balance factors are sometimes computed a h_L - h_R .



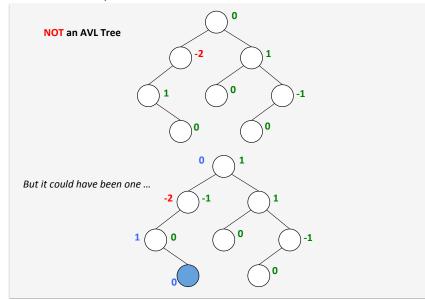






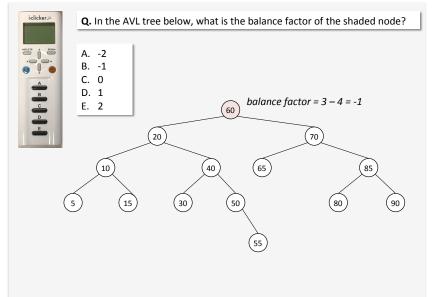
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Balance factor example



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Participation question

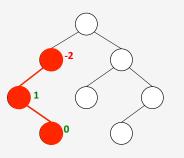


Rebalancing

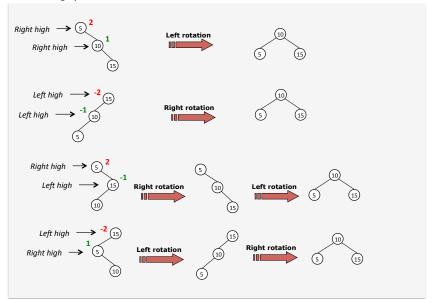
A bf of ±2 means that the subtree rooted at that node is out of balance.

Balance will be restored by subtree rotations.

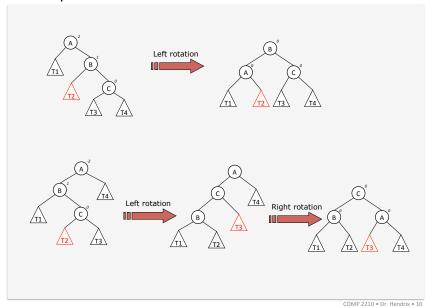
All rotations will occur in the context of a 3-node neighborhood.



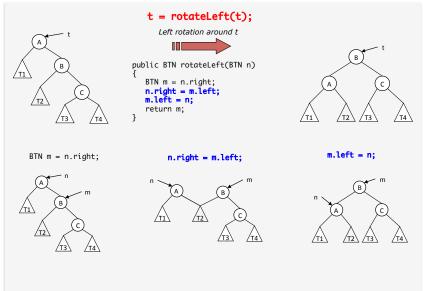
Rebalancing operations



Subtree displacement



Coding rotations



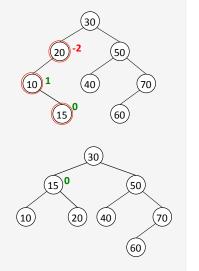
Inserting a new element

Use the standard BST insertion algorithm to insert the new node. (Ex: 15)

Beginning with the node just inserted, walk the reverse path back toward the root, recalculating balance factors.

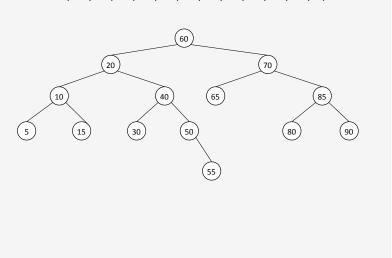
Stop at the first (lowest) node that has a balance factor of ±2. This node roots the 3-node neighborhood that will be rotated.

At most one rebalancing operation will be required per insertion.



Building an AVL tree

Insert: 10, 85, 15, 70, 20, 60, 30, 50, 65, 80, 90, 40, 5, 55



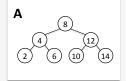
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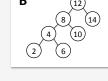
Participation question



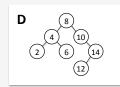
Q. Which AVL tree would result from inserting the following values in the order they are written?

14, 12, 10, 8, 6, 4, 2









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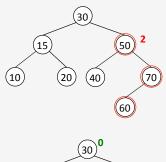
Deleting an element

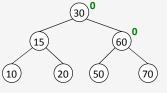
Use the standard BST deletion algorithm to delete the element. Ex: 40

Beginning at the *point of deletion*, walk the reverse path back toward the root, recalculating balance factors.

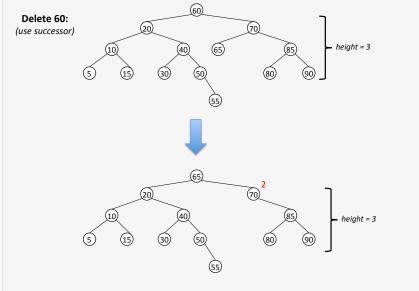
Stop at the first (lowest) node that has a balance factor of ±2. This node roots the 3-node neighborhood that will be rotated.

Multiple rebalancing operations may be required per deletion, so the reverse walk must go to the root each time.

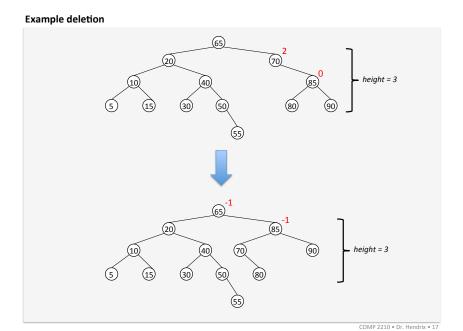


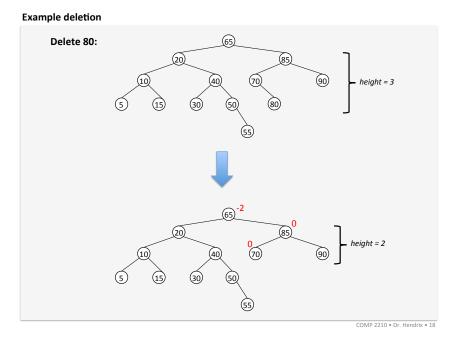


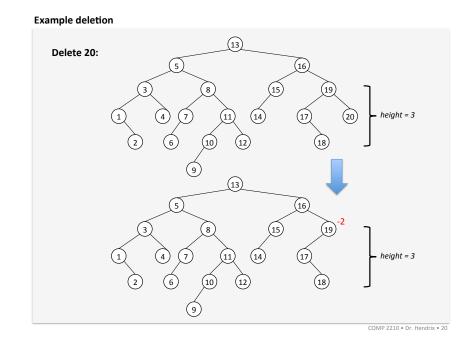
Example deletion



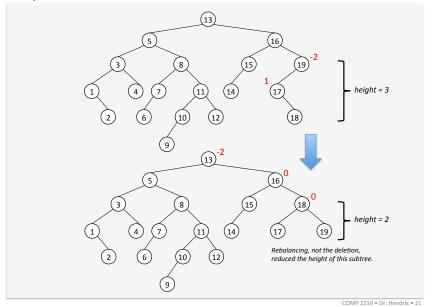
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Example deletion



Remind me: what's the point of all this?



Balanced binary search trees are like a structural implementation of the binary search algorithm.

So, now we can use binary search on a structure built with linked nodes.

AVL trees offer guaranteed O(log N) performance on all three major collection operations: add, remove, and search.

	Self-Ordered Lists		
	Array	Linked List	AVL Tree
add(element)	O(N)	O(N)	O(log N)
remove(element)	O(N)	O(N)	O(log N)
search(element)	O(log N)	O(N)	O(log N)

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Example deletion

