CS 3310 Design and Analysis of Algorithms Midterm (3/23/2023)

Name : _	
Last 4 digits of your Student ID #:	

Read these instructions before proceeding.

- Closed book. Closed notes. You can use calculator.
- You have <u>50 minutes</u> to complete this exam.
- Important Notes:
 - o During the exam, all students need to join the Zoom meeting
 - O No questions will be answered during the exam about the exam questions. Write down your assumptions and answer the best that you can. In the last 15 minutes of the exam, if you have additional questions about submitting your exams, you can ask your questions on the Chat room of Zoom Meeting and your questions will be answered there.
 - Just in case you have trouble of submitting your exam here @Canvas, alternative way is to submit your completed exam to Prof. Young by emailing

gsyoung@cpp.edu

- You can choose your own way to work on your exam, but you are required to submit your completed exam in **ONE PDF FILE** here @ Canvas.
- Two popular ways students used are:
 - Print out the exam paper. Write your answers on the exam paper. Scan your completed exam papers or take photos of them. Then turn in one PDF file here @ Canvas.
 - Read the exam from the computer screen and answer questions on your own white papers (number your answers). Scan your exam answers or take photos of them. Then turn in **one PDF file** here @ Canvas.

Q.#1 (24)	Q.#2 (20)	Q.#3 (20)	Q.#4 (18)	Q.#5 (18)	Total(100)

1. (**24 pts**) (3 pts each)

low

(a) and (b): Give the *best-case complexity and the worst-case complexity* for each of the following algorithms. No justifications are required.

(a) <i>Quicksort</i> for Best-case Comple		a list of n nun	nbers. Worst-case Complexity	
(b) Strassen's Alg Best-case Comple	_	atrix Multipli	cation. Input: two n×n matrice Worst-case Complexity	s.
(c) f(n) = O (g(n))	if and only if g((n) =	$_{-}$ (f(n)).	
(d) If $f(n) = O(g(n))$	n)) and $g(n) = \Omega$	2 (f(n)) then g(f(n) = 1 (f(n)).	
(e) If $f(n) = O(g(n))$	(a)) and $f(n) = \theta(n)$	(h(n)), then $h(n)$	(g(n))	
(f) $\sum_{i=1}^{n} a^{i} = $				
2. (20 pts)				
Rank the following functions by order of growth <i>from low to high</i> . If two or more are of the same order $(f(n))$ and $g(n)$ are in the same class if and only if $f(n) = \theta(g(n))$, group them together. No proofs are necessary.				
2 ⁿ In n	7×lg n n!	2 ⁿ⁺² lg (lg n)	$(n-1)!$ $3\times n^3 + \lg n$	

high

3. (20 pts)

Prove that f(n) = O(g(n)) where $f(n) = 1234 \times 3^n$ and $g(n) = n^n$. (Hint: Give a witness pair and show that it works)

1 (18 pts)		

4. (18 pts)

Solve the following recurrence relations using successive substitutions, where c is a constant.

$$T(n) = \begin{cases} T(n/3) + c & \text{if } n > 1 \\ c & \text{if } n = 1 \end{cases}$$

5. ((18)	pts)

"MidtermSearch" algorithm is a variant of binary search algorithm, and it splits the set into 2 sets of different sizes of one-third (1/3) and two-thirds (2/3) instead. (a) (9 pts) Give the recurrence relations of "MidtermSearch" algorithm.			
-	e best-case, worst-cas	-	e complexity of
muierm search aigo.	rithm? No Justifications	needed.	
Best-case Complexity	Worst-case Comple	xity Average-cas	se Complexity

Binary search algorithm splits the set into 2 sets of equal sizes (½ and ½).