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Given the schema  $S = \langle \{ A, B, C, D, E, F, G, H \}, FD \rangle$

Where FD consists the following dependencies:

$AF \rightarrow BC$

$A \rightarrow F$

$E \rightarrow C$

$C \rightarrow D$

$D \rightarrow H$

$E \rightarrow H$

$C \rightarrow H$

$HC \rightarrow D$

$G \rightarrow H$

- i. Find a minimal cover for the above schema  
Rules – Singleton RHS, no extraneous solution on LHS, no redundant functional dependencies

**Solution:**

$A \rightarrow B$

$A \rightarrow C$

$A \rightarrow F$

$E \rightarrow C$

$C \rightarrow D$

$D \rightarrow H$

$G \rightarrow H$

Step 1:

$A^+ \quad F^+$

$AFBC \quad F$

Step 2:

$A^+ \quad F^+$

$AF \quad F$

Step 3:

$H^+ \quad C^+$

$H \quad CH$

Step 4:

$A^+$

$ACFDH$  (no B so keep  $A \rightarrow B$ )

Step 5:

$A^+$

$BF$  (no C so keep  $A \rightarrow C$ )

Step 6:

$A^+$

ABCDH (no F so keep  $A \rightarrow F$ )

Step 7:

E+

EH (no C so keep  $E \rightarrow C$ )

Step 8:

C+

CH (no D so keep  $C \rightarrow D$ )

Step 9:

D+

D (no H so keep  $D \rightarrow H$ )

Step 10:

E+

ECDH (has H so delete  $E \rightarrow H$ )

Step 11:

C+

CDH (has H so delete  $C \rightarrow H$ )

Step 12:

G+

G (no H so keep  $G \rightarrow H$ )

- ii. Find a key for above schema

Minimal Cover:

$A \rightarrow B$

$A \rightarrow C$

$A \rightarrow F$

$E \rightarrow C$

$C \rightarrow D$

$D \rightarrow H$

$G \rightarrow H$

Keys are {A,E,G}

- iii. Find a third normal form decomposition.

R1 = {A, B, C, F}

R2 = {E, C}

R3 = {C, D}

R4 = {D, H}

R5 = {G, H}

R6 = {A, E, G}

- iv. Find a BCNF decomposition

3NF relationship also satisfies BCNF by being in 3<sup>rd</sup> normal form and every determinant is a candidate key. No changes from iii

R1 = {A, B, C, F}

$R_2 = \{E, C\}$   
 $R_3 = \{C, D\}$   
 $R_4 = \{D, H\}$   
 $R_5 = \{G, H\}$   
 $R_6 = \{A, E, G\}$

- v. Determine whether the following decompositions are lossy or loss-less .

$R_1 = \{A, B, C, D\}$   $R_2 = \{B, E, F, G, H\}$

Lossless since B is the only common attribute and it doesn't contain all candidate keys of  $\{A, E, G\}$

$R_1 = \{A, B, C, F\}$   $R_2 = \{A, E, D, G, H\}$

Lossless since A is the only common attribute and A only doesn't contain all the candidate keys of  $\{A, E, G\}$