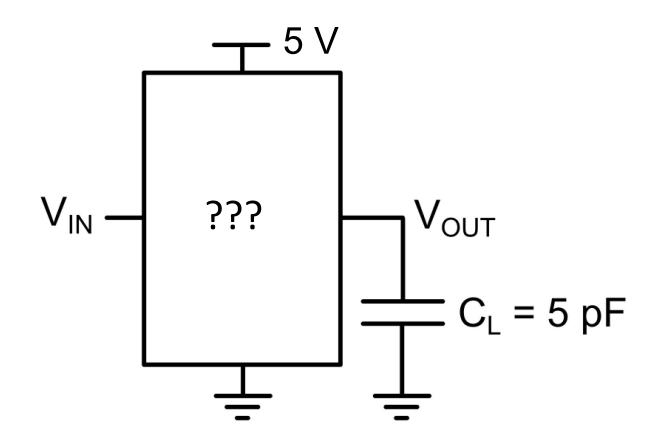
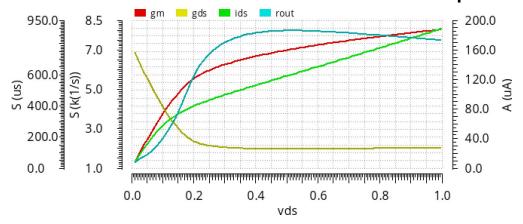
### "Design Procedure:" Example

 Goal: Design an amplifier to drive a 5 pF load that provides gain > 10, bandwidth > 1 MHz, with an output swing within 500 mV of +5 V / 0 V supply rails



Characterize the small-signal parameters of devices in the technology you are using.

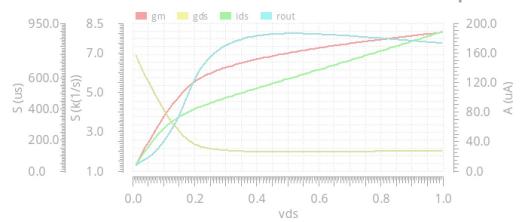
Short-channel devices (example):



Use simulator to characterize small-signal parameters vs. bias point

Characterize the small-signal parameters of devices in the technology you are using.

Short-channel devices (example):



Use simulator to characterize small-signal parameters vs. bias point

Long-channel devices (square-law model holds):

Hand calculations suffice for most parameters:

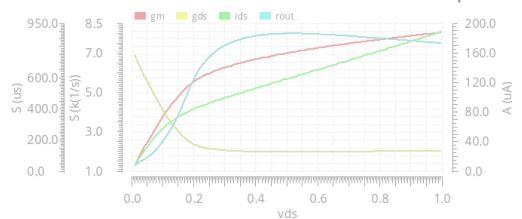
$$I_{DS} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$$

$$g_m \approx \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH}) \approx \sqrt{2\mu_n C_{ox} \frac{W}{L} I_D}$$

$$r_o = \frac{1}{\lambda I_D}$$

Characterize the small-signal parameters of devices in the technology you are using.

Short-channel devices (example):



Use simulator to characterize small-signal parameters vs. bias point

Long-channel devices (square-law model holds):

Hand calculations suffice for most parameters:

$$I_{DS} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$$

$$g_m \approx \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH}) \approx \sqrt{2\mu_n C_{ox} \frac{W}{L} I_D}$$

$$r_o = \frac{1}{2L}$$

This process technology:

Parameter	NMOS	PMOS
VTO	0.8 V	-0.8 V
KP	$90 \mu\text{A/V}^2$	$30 \mu A/V^2$
LAMBDA	0.01 V <sup>-1</sup>	0.02 V <sup>-1</sup>

Characterize the small-signal parameters of devices in the technology you are using.

#### Full process parameter list

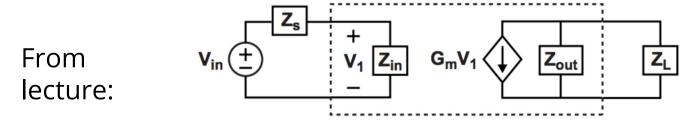
Parameter	NMOS	PMOS
Model Level	3 (in HSPICE)	3 (in HSPICE)
VTO	0.8 V	-0.8 V
KP	90 μA/V <sup>2</sup>	30 μA/V <sup>2</sup>
GAMMA	0.8 √ <i>V</i>	$0.4 \sqrt{V}$
LAMBDA	0.01 V <sup>-1</sup>	0.02 V <sup>-1</sup>
TOX	200 Å	200 Å
XJ	0.5 µm	0.5 µm
LD	0.3 µm	0.3 µm
PHI	0.7 V	0.6 V
NSUB	3.33 x 10 <sup>16</sup> cm <sup>-3</sup>	3.33 x 10 <sup>15</sup> cm <sup>-3</sup>
RSH	0 Ω	0 Ω
CGSO	500 pF/m	500 pF/m
CGDO	500 pF/m	500 pF/m
CGBO	0 F/m	0 F/m
CJ	300 μF/m <sup>2</sup>	300 μF/m <sup>2</sup>
MJ	0.5	0.5
CJSW	0 F/m	0 F/m
MJSW	0.33	0.33

Threshold voltage **Transconductance** Bulk threshold parameter Channel length modulation Gate oxide thickness Junction depth Lateral diffusion length Surface potential Substrate doping density Drain/source siddution sheet resistance Gate-source overlap capacitance Gate-drain overlap capacitance Gate-bulk overlap capacitance Bulk junction cap, 0V, bottom Bulk junction grading coeff., bottom Bulk junction cap, 0V, sidewall Bulk junction grading coeff., sidewall

Process / SPICE parameters for NMOS / PMOS transistors.

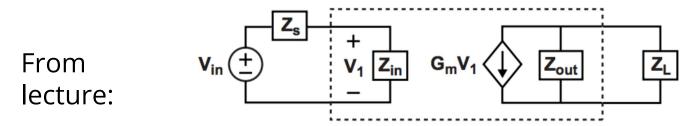
Find out how target specs impact specific parameters, and choose topology accordingly.

• Topology choice sets achievable  $G_m$  and  $R_{out}$ 



Find out how target specs impact specific parameters, and choose topology accordingly.

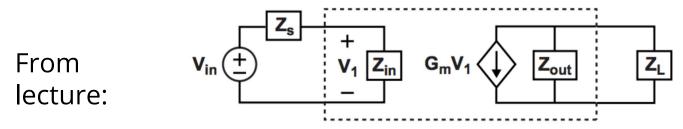
■ Topology choice sets achievable  $G_m$  and  $R_{out}$ 



• What do  $G_m$  and  $R_{out}$  need to be relative to a single device?

Find out how target specs impact specific parameters, and choose topology accordingly.

■ Topology choice sets achievable  $G_m$  and  $R_{out}$ 



• What do  $G_m$  and  $R_{out}$  need to be relative to a single device? Single device performance

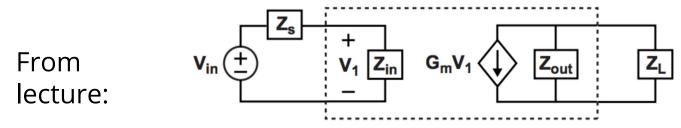
Swing constraint:  $V_{DS} > V_{GS} - V_{T}$ 

V <sub>GS</sub> =1V, W/L=5		V <sub>GS</sub> =1.3 V	, W/L=20
NMOS	PMOS	NMOS	PMOS
9 μΑ	3 μΑ	0.2 mA	75 μΑ
90 μS	30 μS	0.9 mS	0.3 mS
11 MΩ	17 ΜΩ	0.4 ΜΩ	0.7 MΩ

 $g_m$  in the 100s of  $\mu$ S,  $r_o$  in the 100s of  $k\Omega$ 

Find out how target specs impact specific parameters, and choose topology accordingly.

■ Topology choice sets achievable  $G_m$  and  $R_{out}$ 



• What do  $G_m$  and  $R_{out}$  need to be relative to a single device?

#### Single device performance

Swing constraint:  $V_{DS} > V_{GS} - V_{T}$ 

V <sub>GS</sub> =1V, W/L=5		V <sub>GS</sub> =1.3 V, W/L=20	
NMOS	PMOS	NMOS	PMOS
9 μΑ	3 μΑ	0.2 mA	75 μΑ
90 µS	30 μS	0.9 mS	0.3 mS
11 MΩ	17 ΜΩ	0.4 ΜΩ	0.7 ΜΩ

#### $g_m$ in the 100s of $\mu$ S, $r_o$ in the 100s of $k\Omega$

#### **Requirements**

#### **Bandwidth constraint:**

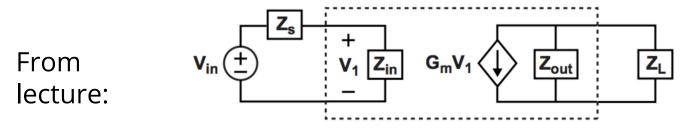
$$f_{BW} \approx \frac{1}{2\pi R_{out}C_L} \ge 1 MHz$$
  
 $R_{out} \le \frac{1}{2\pi \cdot 1MHz \cdot 5 pF} = 32 k\Omega$ 

#### **Gain constraint:**

$$A_V = G_m R_{out} \ge 10 \to G_m \ge \frac{10}{R_{out}} = 0.31 \, mS$$

Find out how target specs impact specific parameters, and choose topology accordingly.

■ Topology choice sets achievable  $G_m$  and  $R_{out}$ 



• What do  $G_m$  and  $R_{out}$  need to be relative to a single device?

#### Single device performance

Swing constraint:  $V_{DS} > V_{GS} - V_{T}$ 

V <sub>GS</sub> =1V, W/L=5		V <sub>GS</sub> =1.3 V, W/L=2	
NMOS	PMOS	NMOS	PMOS
9 μΑ	3 μΑ	0.2 mA	75 μΑ
90 µS	30 µS	0.9 mS	0.3 mS
11 MΩ	17 ΜΩ	0.4 ΜΩ	0.7 ΜΩ

 $g_m$  in the 100s of  $\mu$ S,  $r_o$  in the 100s of  $k\Omega$ 

#### **Requirements**

#### **Bandwidth constraint:**

$$f_{BW} \approx \frac{1}{2\pi R_{out}C_L} \ge 1 MHz$$
  
 $R_{out} \le \frac{1}{2\pi \cdot 1MHz \cdot 5 pF} = 32 k\Omega$ 

#### **Gain constraint:**

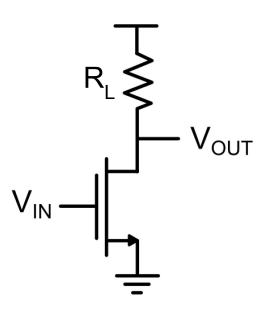
$$A_V = G_m R_{out} \ge 10 \to G_m \ge \frac{10}{R_{out}} = 0.31 \, mS$$

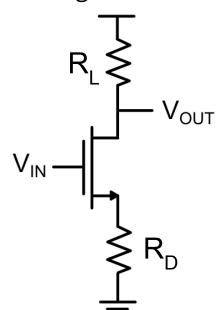
 $g_m$  about right,  $r_o$  needs to be smaller

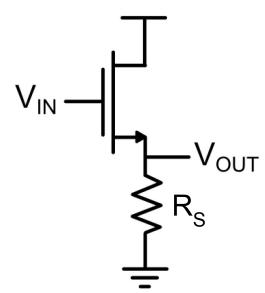
Find out how target specs impact specific parameters, and choose topology accordingly.

Common Source Amplifier Common Source Amplifier w/ Degeneration

Source Follower



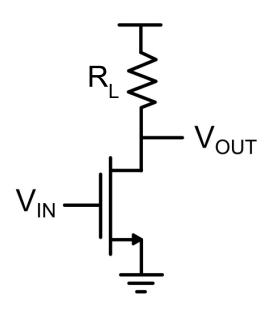


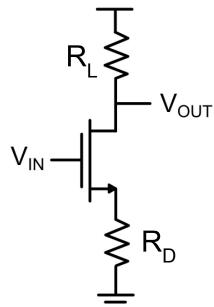


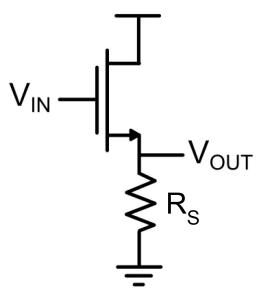
Find out how target specs impact specific parameters, and choose topology accordingly.

Common Source Amplifier Common Source Amplifier w/ Degeneration

Source Follower

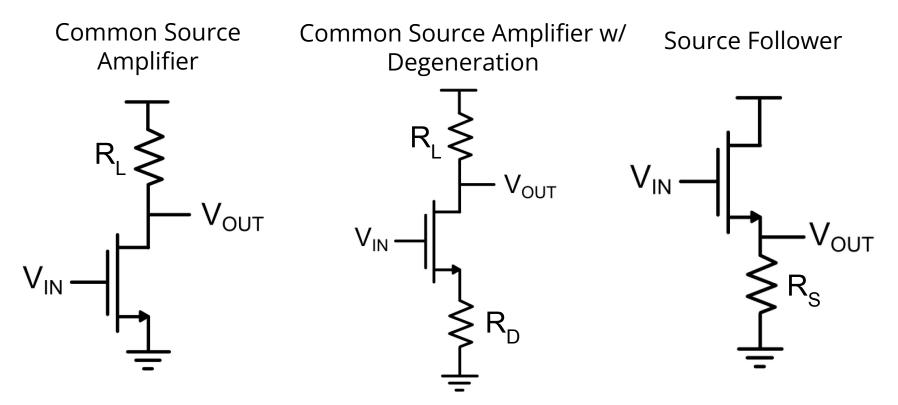






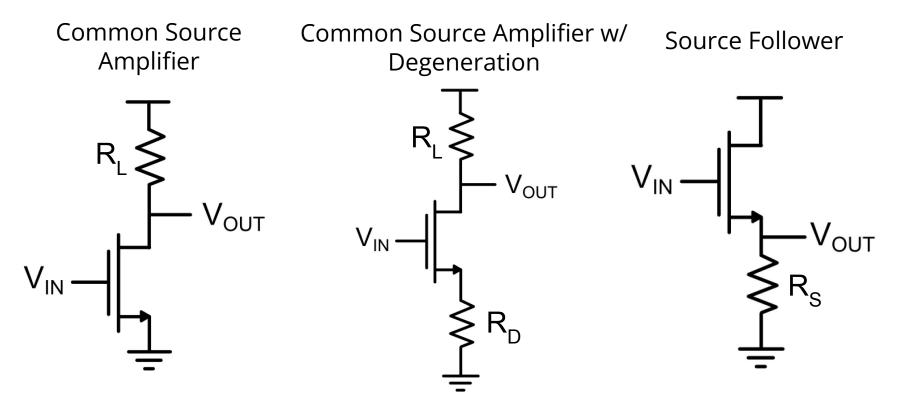
	Equation	Effect
$G_m$	$g_m$	Same
R <sub>out</sub>	$r_o//R_L$	Į.

Find out how target specs impact specific parameters, and choose topology accordingly.



	Equation	Effect	Equation	Effect
$G_m$	$g_m$	Same	$g_m/(1+g_mR_D)$	<b>₽</b>
R <sub>out</sub>	$r_o^{\prime}/R_L^{\prime}$	<b>↓</b>	$(r_o(1+g_m^{}R_D^{}))//R_L^{}$	Varies

Find out how target specs impact specific parameters, and choose topology accordingly.



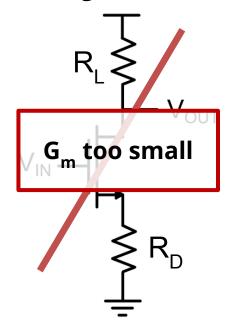
	Equation	Effect	Equation	Effect	Equation	Effect
$G_m$	$g_{_m}$	Same	$g_m/(1+g_mR_D)$	<b>↓</b>	$g_{m}$	Same
R <sub>out</sub>	$r_o^{}/ R_L^{}$	<u>+</u>	$(r_o(1+g_mR_D))/R_L$	Varies	$R_s / / (1/g_m)$	TT.

Find out how target specs impact specific parameters, and choose topology accordingly.

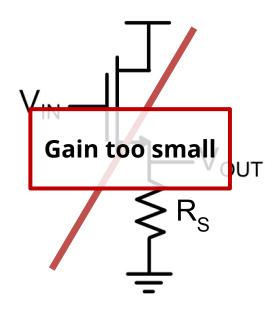
Common Source Amplifier

R<sub>L</sub> V<sub>OUT</sub>

Common Source Amplifier w/ Degeneration



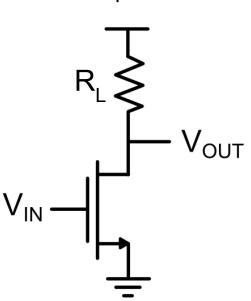
Source Follower



	Equation	Effect	Equation	Effect	Equation	Effect
G <sub>m</sub>	$g_{m}$	Same	$g_m/(1+g_mR_D)$	<b>+</b>	$\boldsymbol{g}_m$	Same
R <sub>out</sub>	r <sub>o</sub>   R <sub>L</sub>	T.	$(r_o(1+g_mR_D))/R_L$	Varies	$R_s / / (1/g_m)$	II

Make a list of relevant equations and sort out how many "free" variables you really have.

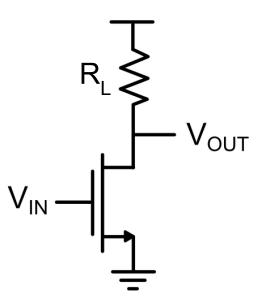
Common Source Amplifier



Design constraints	Relevant equations
Gain > 10	$A_{V} = G_{m}R_{out} = g_{m}(r_{o}//R_{L})$
BW > 1 MHz	$f_{_{BW}} \approx 1/(2\pi(r_{_{O}}  R_{_{L}})C_{_{L}})$
Output swing within 500 mV of supply rails	$V_{OUT} > V_{GS} - V_{T}$ $V_{min} = V_{GS} - V_{T}$

Make a list of relevant equations and sort out how many "free" variables you really have.

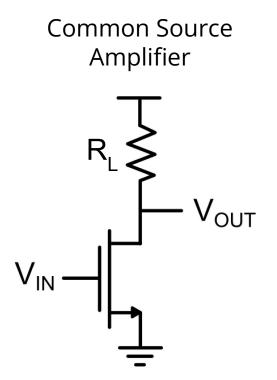




Design constraints	Relevant equations
Gain > 10	$A_{V} = G_{m}R_{out} = g_{m}(r_{o}/ R_{L})$
BW > 1 MHz	$f_{_{BW}} \approx 1/(2\pi(r_{_{o}}  R_{_{L}})C_{_{L}})$
Output swing within 500 mV of supply rails	$V_{OUT} > V_{GS} - V_{T}$ $V_{min} = V_{GS} - V_{T}$

"Free" variables:  $V_{GS}$ , W/L,  $V_{OUT}$ ,  $I_{DS}$ ,  $R_{L}$ , ???

Make a list of relevant equations and sort out how many "free" variables you really have.



Design constraints	Relevant equations
Gain > 10	$A_{V} = G_{m}R_{out} = g_{m}(r_{o}/ R_{L})$
BW > 1 MHz	$f_{_{BW}} \approx 1/(2\pi (\frac{r_{_{o}}}{ R_{_{L}}})C_{_{L}})$
Output swing within 500 mV of supply rails	$V_{OUT} > V_{GS} - V_{T}$ $V_{min} = V_{GS} - V_{T}$

"Free" variables: V<sub>GS</sub>, W/L, V<sub>OUT</sub>, I<sub>DS</sub>, R<sub>L</sub>, ???

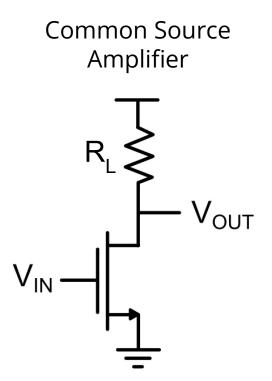
$$R_L = \frac{V_{DD} - V_{OUT}}{I_{DS}}$$

#### Full equations for $R_{out}$ and $G_m$ :

$$R_{out} = r_o || R_L = \frac{1}{I_{DS}} \frac{V_{DD} - V_{OUT}}{\left(1 + \lambda (V_{DD} - V_{OUT})\right)} \approx \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

Make a list of relevant equations and sort out how many "free" variables you really have.



Design constraints	Relevant equations
Gain > 10	$A_{V} = G_{m}R_{out} = g_{m}(r_{o}/ R_{L})$
BW > 1 MHz	$f_{BW} \approx 1/(2\pi (r_o   R_L)C_L)$
Output swing within 500 mV of supply rails	$V_{OUT} > V_{GS} - V_{T}$ $V_{min} = V_{GS} - V_{T}$

Free variables: 
$$V_{GS'}$$
, W/L,  $V_{OUT'}$ ,  $N_{DS'}$ ,  $R_{L}$ 

$$R_{L} = \frac{V_{DD} - V_{OUT}}{I_{DS}}$$

#### Full equations for $R_{out}$ and $G_m$ :

$$R_{out} = r_o || R_L = \frac{1}{I_{DS}} \frac{V_{DD} - V_{OUT}}{\left(1 + \lambda (V_{DD} - V_{OUT})\right)} \approx \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

#### **Step 3: How do constraints impact parameters?**

Solve equations to find acceptable design parameter ranges.

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$R_{out} = \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

#### Step 3: How do constraints impact parameters?

Solve equations to find acceptable design parameter ranges.

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$R_{out} = \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

1) Swing constraint: V<sub>min</sub> ≤ 500 mV

$$V_{min} = V_{GS} - V_T$$
  $\longrightarrow$   $V_{GS} - V_T \le 500 \text{ mV}$ 

Solve equations to find acceptable design parameter ranges.

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH}) \qquad \qquad R_{out} = \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

$$R_{out} = \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

1) Swing constraint: V<sub>min</sub> ≤ 500 mV

$$V_{min} = V_{GS} - V_T \qquad \longrightarrow \qquad V_{GS} - V_T \le 500 \ mV$$

2) Bandwidth & gain constraints:

Gain:  $G_m R_{out} \ge 10$ 

Solve equations to find acceptable design parameter ranges.

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$R_{out} = \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

1) Swing constraint: V<sub>min</sub> ≤ 500 mV

$$V_{min} = V_{GS} - V_T \qquad \longrightarrow \qquad V_{GS} - V_T \le 500 \ mV$$

2) Bandwidth & gain constraints:

**Gain:**  $G_m R_{out} \ge 10$ 

$$G_{m}R_{out} = k'\frac{W}{L}(V_{GS} - V_{TH})\frac{2}{k'\frac{W}{L}(V_{GS} - V_{TH})^{2}}\frac{V_{DD} - V_{OUT}}{(1 + \lambda(V_{DD} - V_{OUT}))}$$

Solve equations to find acceptable design parameter ranges.

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$R_{out} = \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

1) Swing constraint: V<sub>min</sub> ≤ 500 mV

$$V_{min} = V_{GS} - V_T \qquad \longrightarrow \qquad V_{GS} - V_T \le 500 \ mV$$

2) Bandwidth & gain constraints:

**Gain:**  $G_m R_{out} \ge 10$ 

$$\begin{split} G_{m}R_{out} &= k' \frac{W}{L} (V_{GS} - V_{TH}) \frac{2}{k' \frac{W}{L} (V_{GS} - V_{TH})^{2}} \frac{V_{DD} - V_{OUT}}{(1 + \lambda(V_{DD} - V_{OUT}))} \\ &= \frac{2}{(V_{GS} - V_{TH})} \frac{V_{DD} - V_{OUT}}{(1 + \lambda(V_{DD} - V_{OUT}))} \end{split}$$

Solve equations to find acceptable design parameter ranges.

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$R_{out} = \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

1) Swing constraint: V<sub>min</sub> ≤ 500 mV

$$V_{min} = V_{GS} - V_T \qquad \longrightarrow \qquad V_{GS} - V_T \le 500 \ mV$$

2) Bandwidth & gain constraints:

**Gain:**  $G_m R_{out} \ge 10$ 

$$G_{m}R_{out} = k'\frac{W}{L}(V_{GS} - V_{TH})\frac{2}{k'\frac{W}{L}(V_{GS} - V_{TH})^{2}}\frac{V_{DD} - V_{OUT}}{(1 + \lambda(V_{DD} - V_{OUT}))}$$

$$10 \le \frac{2}{(V_{GS} - V_{TH})}\frac{V_{DD} - V_{OUT}}{(1 + \lambda(V_{DD} - V_{OUT}))}$$

$$V_{GS} - V_{TH} \le \frac{2}{10}\frac{5V - 2.5V}{(1 + 0.01 V^{-1}(5V - 2.5V))} \approx 500 \, mV$$

Solve equations to find acceptable design parameter ranges.

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$R_{out} = \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

1) Swing constraint: V<sub>min</sub> ≤ 500 mV

$$V_{min} = V_{GS} - V_T \qquad \longrightarrow \qquad V_{GS} - V_T \le 500 \ mV$$

2) Bandwidth & gain constraints:

Gain: 
$$G_m R_{out} \ge 10$$

$$R_{out} = \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

Solve equations to find acceptable design parameter ranges.

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$R_{out} = \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

1) Swing constraint: V<sub>min</sub> ≤ 500 mV

$$V_{min} = V_{GS} - V_T \qquad \longrightarrow \qquad V_{GS} - V_T \le 500 \ mV$$

2) Bandwidth & gain constraints:

Gain: 
$$G_m R_{out} \ge 10$$

$$32 k\Omega \ge \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{I} (V_{GS} - V_{TH})^2}$$

Solve equations to find acceptable design parameter ranges.

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$R_{out} = \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

1) Swing constraint: V<sub>min</sub> ≤ 500 mV

$$V_{min} = V_{GS} - V_T \qquad \longrightarrow \qquad V_{GS} - V_T \le 500 \ mV$$

2) Bandwidth & gain constraints:

Gain: 
$$G_m R_{out} \ge 10$$

$$32 k\Omega \ge \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$
$$32 k\Omega \ge \frac{2(2.5V)}{(90 \mu A/V^2) \frac{W}{L} (0.5V)^2}$$

Solve equations to find acceptable design parameter ranges.

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$R_{out} = \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

1) Swing constraint: V<sub>min</sub> ≤ 500 mV

$$V_{min} = V_{GS} - V_T$$
  $\longrightarrow$   $V_{GS} - V_T \le 500 \text{ mV}$ 

2) Bandwidth & gain constraints:

Gain: 
$$G_m R_{out} \ge 10$$

$$32 k\Omega \ge \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$
$$32 k\Omega \ge \frac{2(2.5V)}{(90 \mu A/V^2) \frac{W}{L} (0.5V)^2}$$

$$\frac{W}{L} \ge \frac{2(2.5V)}{32 \, k\Omega \left(90 \, \mu \frac{A}{V^2}\right) (0.5V)^2} = 6.9$$

Solve equations to find acceptable design parameter ranges.

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$G_m = g_m = k' \frac{W}{L} (V_{GS} - V_{TH})$$

$$R_{out} = \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

1) Swing constraint: V<sub>min</sub> ≤ 500 mV

$$V_{min} = V_{GS} - V_T \qquad \longrightarrow \qquad V_{GS} - V_T \le 500 \ mV$$

2) Bandwidth & gain constraints:

Gain:  $G_m R_{out} \geq 10$ 

$$32 k\Omega \ge \frac{2(V_{DD} - V_{OUT})}{k' \frac{W}{L} (V_{GS} - V_{TH})^2}$$

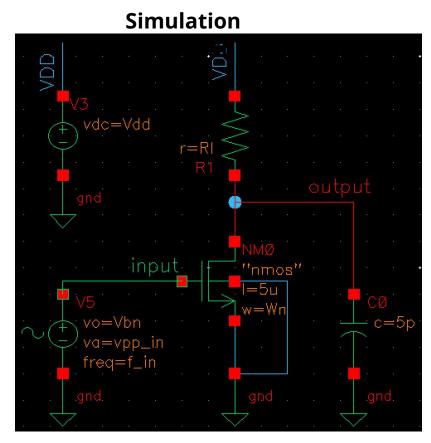
$$32 k\Omega \ge \frac{2(2.5V)}{(90 \mu A/V^2) \frac{W}{L} (0.5V)^2}$$

$$\frac{W}{L} \ge \frac{2(2.5V)}{32 k\Omega \left(90 \mu \frac{A}{V^2}\right) (0.5V)^2} = 6.9$$

Parameter	Value
W/L	7
$V_{GS}$	$0.5 \text{ V} + \text{V}_{\text{TH}} = 1.3 \text{ V}$
l <sub>DS</sub>	78 μΑ
$R_L$	$(V_{DD}-V_{OUT})/I_{DS} = 32 \text{ k}\Omega$

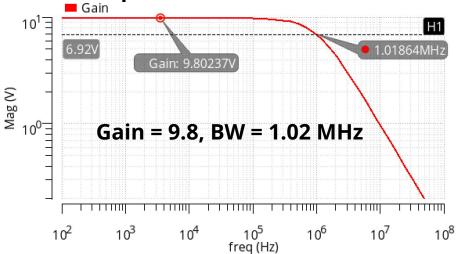
### **Step 4: Does this actually work?**

Verify your design performance in a circuit simulator.

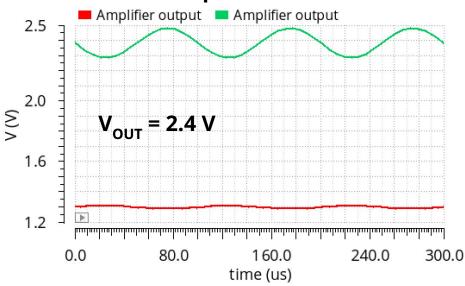


Pretty close! Gain is a little short, so let's increase W/L to boost g<sub>m</sub> since R<sub>L</sub> dominates R<sub>OUT</sub>.



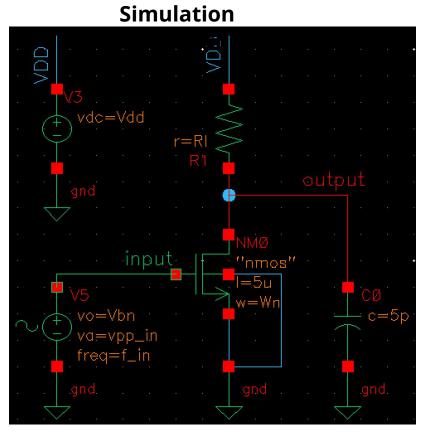


#### **Transient Response:**

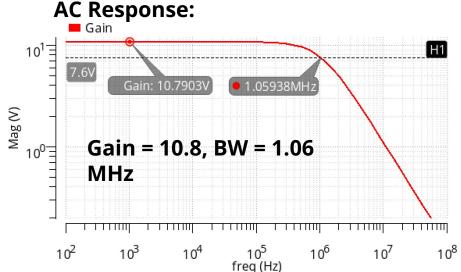


#### **Step 4: Does this actually work?**

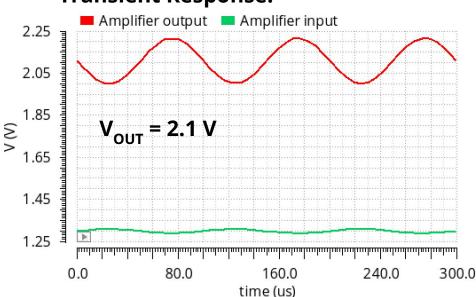
Verify your design performance in a circuit simulator.



# Looks like this will do the job!



#### **Transient Response:**



#### **Final Note**

- Design goals usually involve some sort of optimization:
  - Smallest area
  - Lowest power
  - Highest bandwidth
  - Highest gain
  - Lowest noise
  - "Best" figure of merit (combination of parameters)
- Mathematical solution:
  - Find where derivative of performance metric with respect to design parameters is 0
- Practically:
  - Choose topology carefully for target specifications
  - Identify key design parameters