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Project 1

GitHub: "<https://github.com/SkylerMalinowski/IntroToAI>"

Task 1

Our GUI as of right now is in terminal, .txt files, and .png files.

```
Terminal - (xenia)skyler@localhost: ~/Downloads/IntroToAI/Project 1
(xenia)skyler@localhost:~/Downloads/IntroToAI/Project 1$ python3 task_1.py 5
matrix:
[[1 3 1 4 3]
 [4 3 3 2 2]
 [4 1 2 3 3]
 [2 2 1 2 4]
 [1 2 4 2 0]]
(xenia)skyler@localhost:~/Downloads/IntroToAI/Project 1$
```



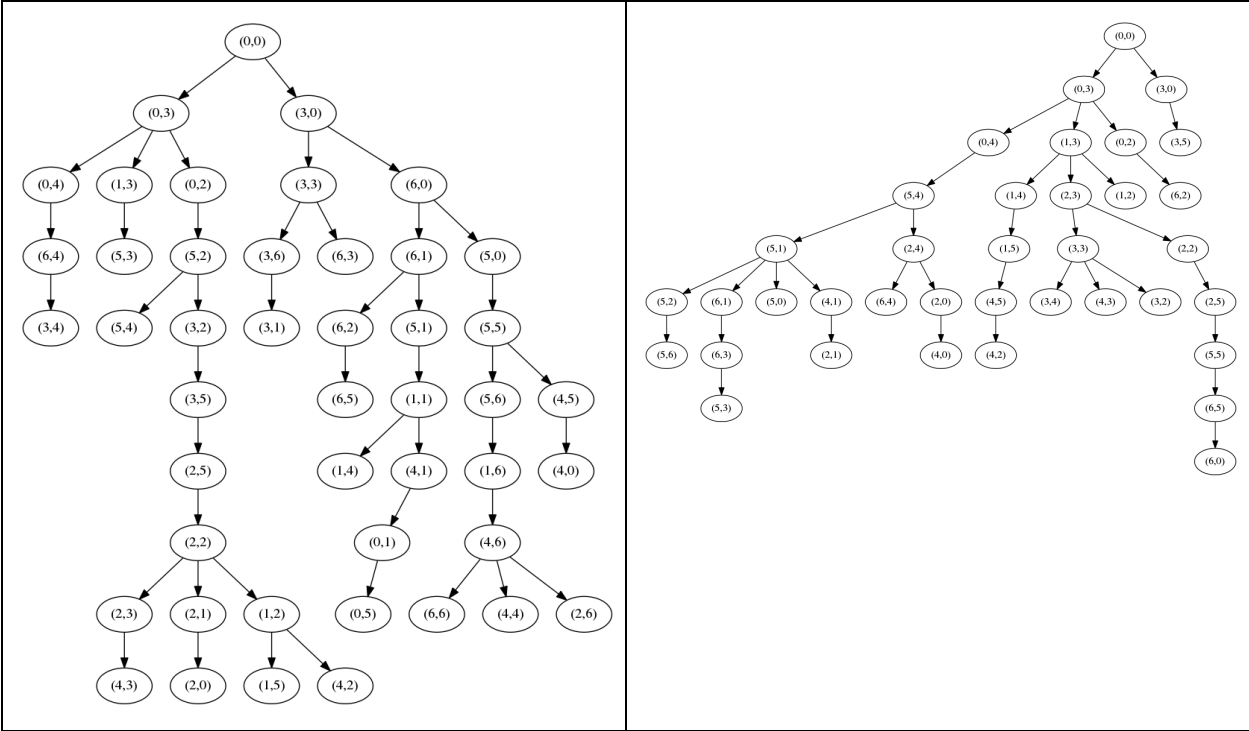
Task 2

Matrix Size = 5	
Solvable	Unsolvable

Matrix	
<div> <div>2</div><div>2</div><div>2</div><div>4</div><div>3</div> <div>4</div><div>2</div><div>1</div><div>1</div><div>4</div> <div>4</div><div>3</div><div>2</div><div>1</div><div>3</div> <div>2</div><div>3</div><div>1</div><div>1</div><div>2</div> <div>3</div><div>3</div><div>2</div><div>1</div><div>0</div> </div>	<div> <div>1</div><div>1</div><div>3</div><div>3</div><div>3</div> <div>2</div><div>1</div><div>1</div><div>2</div><div>4</div> <div>3</div><div>1</div><div>2</div><div>3</div><div>1</div> <div>2</div><div>3</div><div>2</div><div>3</div><div>4</div> <div>3</div><div>1</div><div>3</div><div>1</div><div>0</div> </div>
Evaluation Matrix	
<div> <div>0</div><div>3</div><div>1</div><div>4</div><div>2</div> <div>5</div><div>9</div><div>8</div><div>7</div><div>4</div> <div>1</div><div>3</div><div>2</div><div>6</div><div>2</div> <div>-1</div><div>5</div><div>4</div><div>5</div><div>3</div> <div>4</div><div>-1</div><div>3</div><div>5</div><div>4</div> </div>	<div> <div>0</div><div>1</div><div>2</div><div>5</div><div>-1</div> <div>1</div><div>2</div><div>2</div><div>3</div><div>5</div> <div>4</div><div>3</div><div>3</div><div>5</div><div>4</div> <div>2</div><div>4</div><div>3</div><div>4</div><div>4</div> <div>-1</div><div>-1</div><div>4</div><div>-1</div><div>-1</div> </div>
Tree	
Evaluation Function (k)	

k = 4	k = -5
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Matrix Size = 7	
Solvable	Unsolvable
Matrix	
<div>3 4 5 1 6 6 4</div> <div>1 3 3 4 5 4 3</div> <div>3 1 1 2 3 3 5</div> <div>3 4 3 3 4 1 5</div> <div>6 4 3 2 4 5 2</div> <div>5 4 2 5 5 1 4</div> <div>1 1 3 6 3 2 0</div>	<div>3 2 6 1 5 4 4</div> <div>4 1 5 1 1 3 2</div> <div>2 4 3 1 4 3 1</div> <div>5 1 3 1 4 5 6</div> <div>5 2 3 4 3 3 1</div> <div>6 1 4 3 3 1 6</div> <div>4 2 5 1 3 5 0</div>
Evaluation Matrix	
<div>0 7 2 1 2 8 -1</div> <div>-1 5 8 2 6 9 6</div> <div>9 8 7 8 -1 6 8</div> <div>1 4 4 2 4 5 3</div> <div>6 6 9 9 8 5 7</div> <div>3 4 3 3 4 4 5</div> <div>2 3 4 3 3 5 8</div>	<div>0 -1 2 1 2 -1 -1</div> <div>-1 -1 3 2 3 4 -1</div> <div>5 6 4 3 4 5 -1</div> <div>1 -1 5 4 5 2 -1</div> <div>6 5 6 5 -1 5 -1</div> <div>5 4 5 7 3 6 6</div> <div>8 5 3 6 5 7 -1</div>
Tree	



Evaluation Function (k)	
k = 8	k = -12

Matrix Size = 9	
Solvable	Unsolvable
Matrix	
5 8 7 2 3 2 4 2 8 1 1 2 3 3 1 3 7 4 1 7 5 1 5 6 3 7 8 5 2 1 1 3 3 4 5 3 8 5 3 1 3 3 3 4 7 6 2 3 5 1 1 6 2 2 5 1 5 2 1 1 6 3 1 3 2 4 2 5 6 4 2 3 1 2 6 4 3 4 5 4 0	4 4 8 4 4 6 1 7 2 3 3 4 3 7 1 1 3 5 8 7 5 5 3 4 6 1 2 8 3 4 3 2 2 6 3 8 5 2 5 1 4 2 4 5 8 2 7 6 4 5 2 5 3 4 5 4 3 1 4 6 2 7 5 6 5 1 2 6 7 7 2 5 8 6 5 2 7 3 7 6 0
Evaluation Matrix	
0 3 10 2 6 1 9 2 8 5 6 6 4 6 5 5 7 -1 4 5 4 3 4 2 -1 3 6	0 -1 -1 5 1 4 3 4 2 6 -1 -1 5 4 5 4 5 8 5 4 -1 -1 7 3 4 6 3

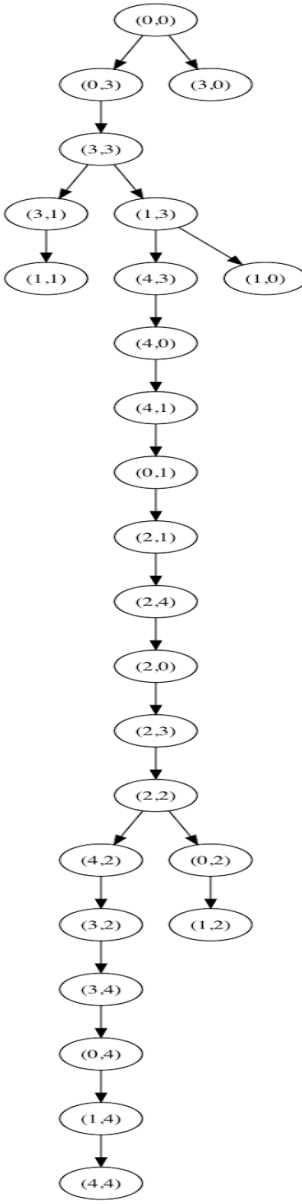
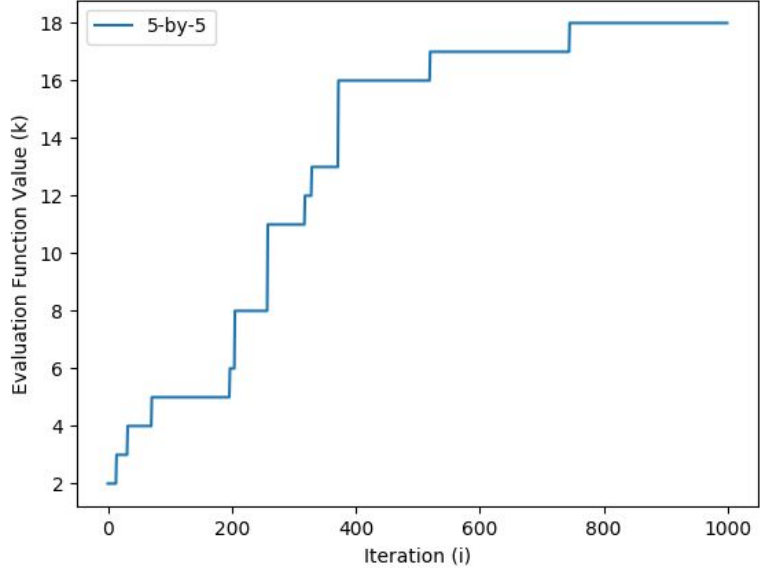
5 6 5 4 5 6 7 6 7 8 6 5 5 6 4 6 7 5 1 6 -1 6 7 8 2 -1 7 6 5 6 7 6 7 8 7 8 7 6 5 7 5 5 6 -1 8 6 4 -1 5 -1 3 -1 6 9	5 -1 7 4 8 -1 5 7 6 1 -1 4 3 2 2 -1 3 3 -1 -1 -1 4 6 -1 -1 5 -1 7 -1 6 5 6 3 -1 8 7 -1 7 8 6 -1 6 8 5 -1 -1 7 9 -1 3 -1 5 6 -1
Tree	
Evaluation Function (k)	
k = 9	k = -25

Matrix Size = 11	
Solvable	Unsolvable
Matrix	
[[8 7 4 1 7 8 9 8 9 6 7] [3 8 9 8 2 9 9 2 8 4 9] [9 8 8 6 2 7 4 3 6 8 6] [4 6 1 1 2 4 4 6 6 3 5] [6 2 5 3 4 5 3 6 5 2 5] [9 4 4 7 5 4 2 6 8 4 6] [4 6 6 2 2 5 1 7 8 7 10] [6 7 7 4 2 3 3 4 4 9 4] [10 3 2 1 1 8 7 5 6 3 5] [5 2 5 2 5 2 3 7 8 5 6] [2 10 3 9 6 8 9 1 7 3 0]]	[[3 3 10 2 10 2 3 1 10 1 8] [7 9 3 1 2 2 7 4 7 7 1] [3 4 4 5 2 1 8 7 4 8 10] [2 8 2 1 1 1 7 2 6 5 3] [2 3 7 3 1 6 6 3 5 2 3] [10 4 3 1 4 2 5 6 4 9 9] [7 5 5 2 2 4 1 5 7 6 3] [2 9 8 2 6 7 2 2 2 3 4] [1 9 8 7 6 1 1 1 1 8 5] [1 1 1 2 7 5 4 4 8 9 8] [4 1 6 2 9 6 3 7 5 3 0]]

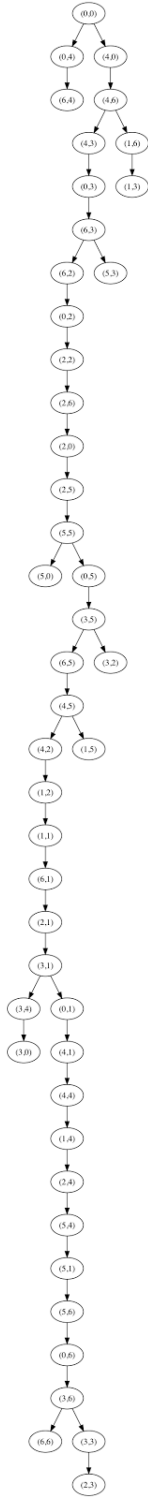
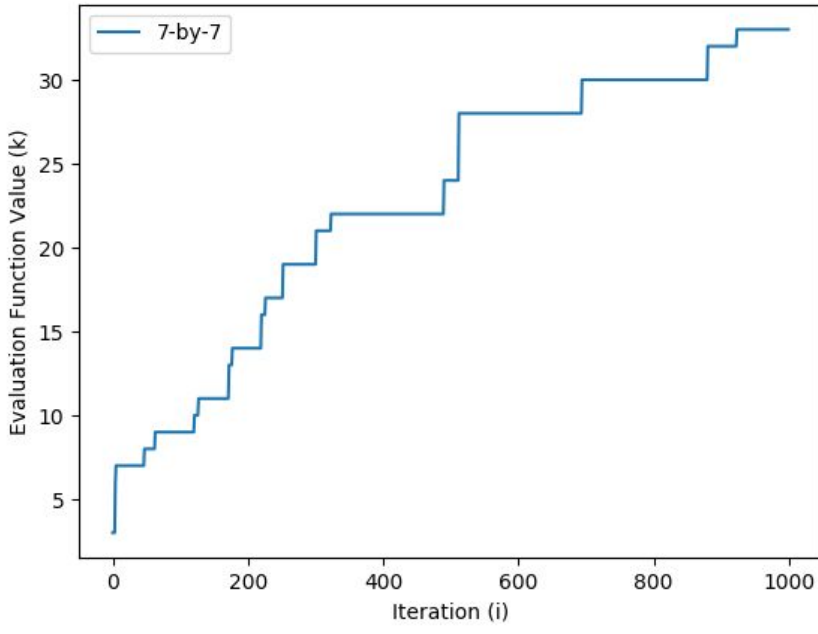
Evaluation Matrix	
[[0 8 7 7 8 4 8 -1 1 6 -1] [4 9 10 5 9 10 6 -1 3 10 -1] [10 8 8 8 7 7 8 6 -1 7 7] [-1 5 7 7 8 4 6 6 7 5 3] [4 8 8 6 8 6 5 7 9 6 7] [12 8 -1 -1 8 9 10 7 11 9 -1] [9 9 7 -1 10 10 9 10 8 6 11] [8 7 6 6 7 5 6 7 6 7 -1] [1 -1 10 9 9 3 -1 -1 -1 -1 2] [3 6 9 5 8 4 9 5 2 9 8] [5 9 6 -1 9 6 7 8 9 8 10]]	[[0 2 5 1 3 2 4 3 4 5 6] [2 5 3 4 5 4 6 3 7 6 6] [7 7 4 2 4 3 4 -1 3 6 7] [1 3 2 4 3 4 5 7 -1 4 6] [6 -1 4 5 4 5 6 6 -1 5 7] [2 4 3 4 5 4 7 4 6 -1 3] [6 5 5 5 -1 6 6 6 4 6 7] [4 4 5 3 7 4 6 7 7 7 5] [3 4 4 6 7 6 7 8 8 5 5] [4 5 6 4 6 5 7 8 7 -1 6] [5 6 6 6 4 6 5 -1 5 6 -1]]
Tree	
Evaluation Function (k)	
k = 10	k = -9

Task 3

Matrix Size = 5

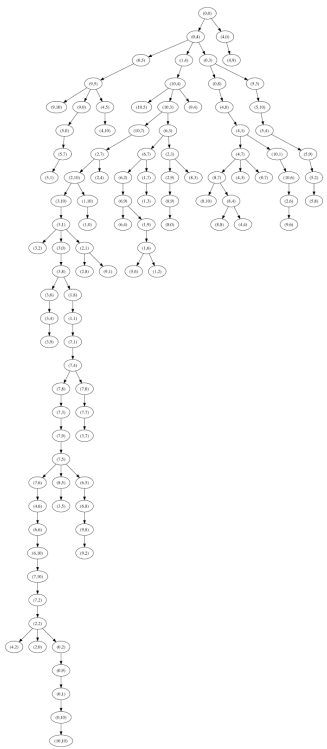
<p><i>Final Matrix</i></p>	
<p>3 2 1 3 1 3 2 3 3 3 3 3 2 1 4 3 2 2 2 3 1 4 1 3 0</p>	
<p><i>Graph</i></p>	
	
<p><i>Value Function (k)</i></p>	
<p>K = 18</p>	

Matrix Size = 7

<p><i>Final Matrix</i></p>	
<p>4 4 2 6 6 3 3 6 5 1 5 1 2 3 5 1 4 3 3 3 6 5 3 3 1 4 3 3 6 3 3 4 3 3 3 3 5 1 4 3 5 5 2 4 6 1 6 2 0</p>	
<p><i>Graph</i></p>	
	
<p><i>Value Function (k)</i></p>	
<p>k = 33</p>	

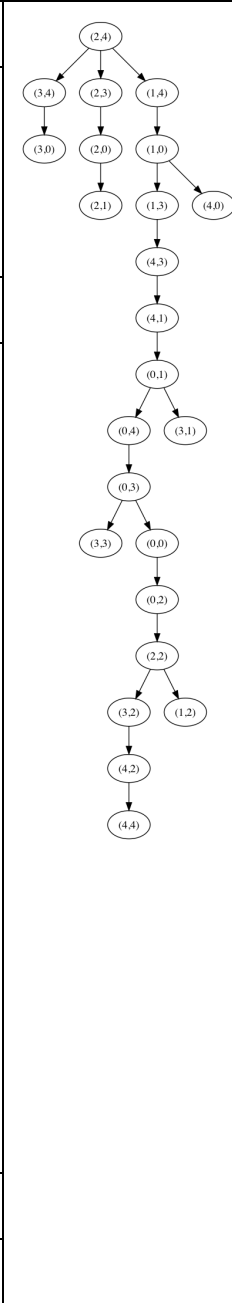
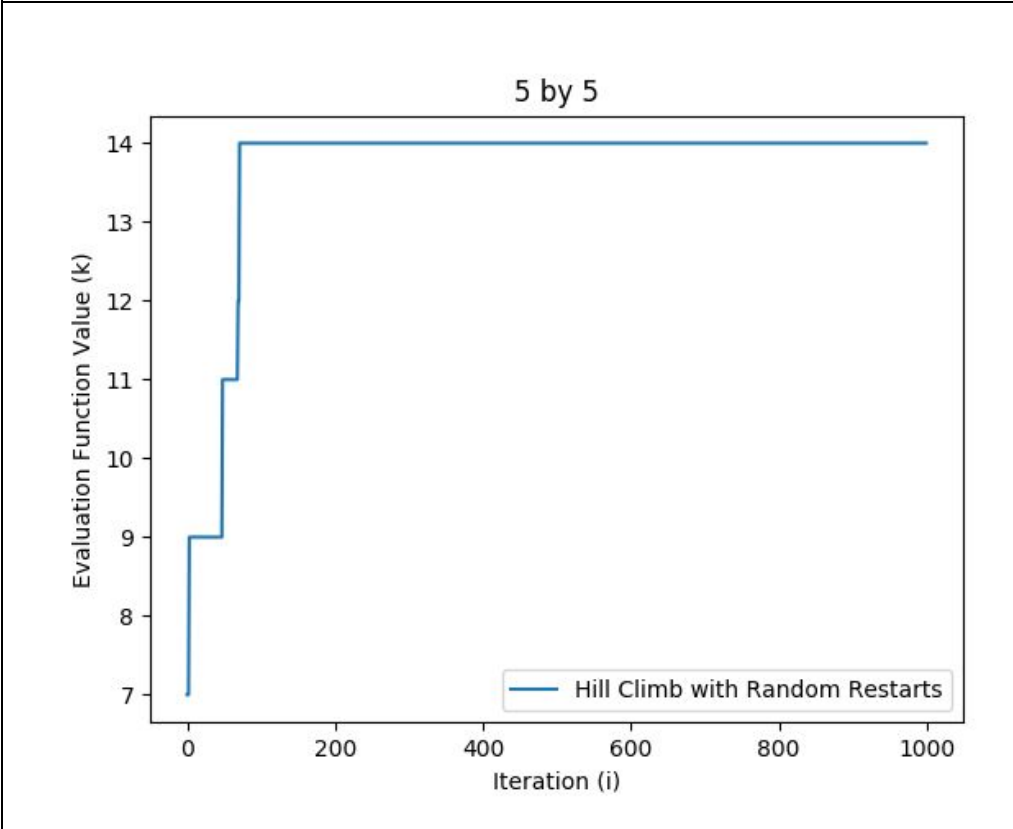
Matrix Size = 9

Final Matrix																																			
<div>4 9 7 5 1 9 4 8 4 8 10 7 6 5 4 9 9 4 4 7 3 10 6 7 2 6 7 6 7 3 1 6 1 8 1 8 3 5 7 2 5 2 8 9 9 6 1 6 6 5 2 4 7 9 9 7 6 6 7 5 2 6 6 6 7 6 3 1 7 4 5 3 4 5 3 5 1 7 3 5 6 4 1 3 4 5 4 8 9 6 3 6 4 5 6 3 8 9 10 4 4 3 7 9 5 7 4 6 9 10 4 5 9 4 1 10 8 8 10 10 0</div>																																			
Graph																																			
<div><table border="1"><caption>Approximate data points from the Graph</caption><thead><tr><th>Iteration (i)</th><th>Evaluation Function Value (k)</th></tr></thead><tbody><tr><td>0 - 50</td><td>7</td></tr><tr><td>50 - 75</td><td>8</td></tr><tr><td>75 - 100</td><td>11</td></tr><tr><td>100 - 125</td><td>15</td></tr><tr><td>125 - 480</td><td>15</td></tr><tr><td>480 - 500</td><td>16</td></tr><tr><td>500 - 720</td><td>16</td></tr><tr><td>720 - 740</td><td>18</td></tr><tr><td>740 - 760</td><td>19</td></tr><tr><td>760 - 780</td><td>23</td></tr><tr><td>780 - 800</td><td>24</td></tr><tr><td>800 - 820</td><td>26</td></tr><tr><td>820 - 840</td><td>28</td></tr><tr><td>840 - 950</td><td>28</td></tr><tr><td>950 - 970</td><td>30</td></tr><tr><td>970 - 1000</td><td>31</td></tr></tbody></table></div>		Iteration (i)	Evaluation Function Value (k)	0 - 50	7	50 - 75	8	75 - 100	11	100 - 125	15	125 - 480	15	480 - 500	16	500 - 720	16	720 - 740	18	740 - 760	19	760 - 780	23	780 - 800	24	800 - 820	26	820 - 840	28	840 - 950	28	950 - 970	30	970 - 1000	31
Iteration (i)	Evaluation Function Value (k)																																		
0 - 50	7																																		
50 - 75	8																																		
75 - 100	11																																		
100 - 125	15																																		
125 - 480	15																																		
480 - 500	16																																		
500 - 720	16																																		
720 - 740	18																																		
740 - 760	19																																		
760 - 780	23																																		
780 - 800	24																																		
800 - 820	26																																		
820 - 840	28																																		
840 - 950	28																																		
950 - 970	30																																		
970 - 1000	31																																		
Value Function (k)																																			
k = 31																																			



Task 4

Matrix Size = 5

Final Matrix		
2 3 2 3 1 3 2 2 3 4 1 3 1 3 1 4 3 1 2 4 3 4 2 2 0		
Graph		
		
Value Function (k)		
k = 14		

Matrix Size = 7	
Final Matrix	
<div>5 1 1 3 6 2 5</div> <div>4 5 1 4 2 2 1</div> <div>5 3 3 1 3 1 3</div> <div>1 4 2 2 2 2 5</div> <div>2 3 3 4 3 1 2</div> <div>3 2 5 3 5 2 3</div> <div>3 2 5 1 6 1 0</div>	
Graph	
<div>7 by 7</div>	
Value Function (k)	
k = 20	

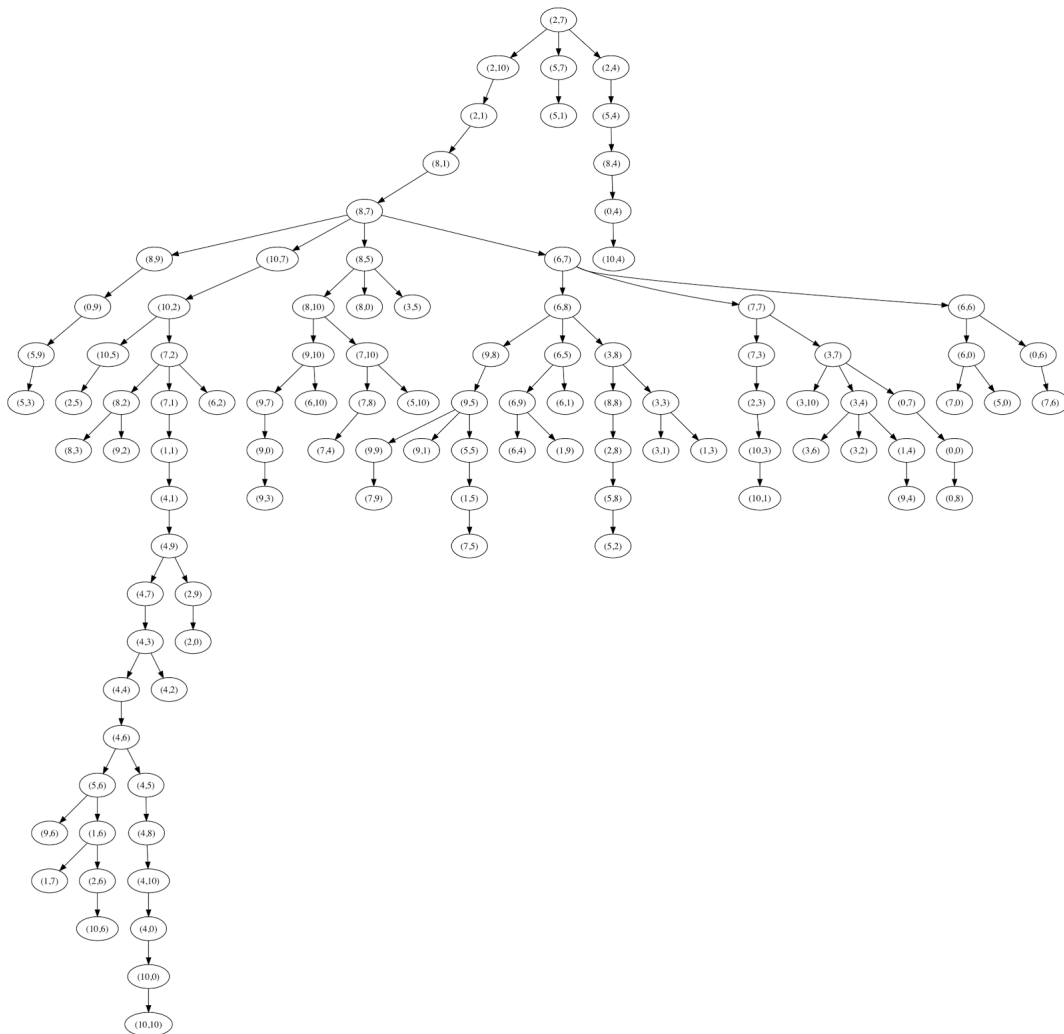
Matrix Size = 9	
Final Matrix	
<div>8 5 4 3 6 4 7 8 2</div> <div>2 7 2 5 2 5 6 3 8</div> <div>6 4 6 6 1 3 5 3 3</div> <div>6 5 5 4 5 2 2 7 8</div> <div>7 7 6 3 4 1 5 5 2</div> <div>1 5 1 3 1 4 5 1 7</div> <div>6 4 5 4 4 2 5 5 6</div> <div>4 3 6 2 7 3 7 6 2</div> <div>7 7 8 3 7 2 5 2 0</div>	
Graph	
<div>9 by 9</div>	
Value Function (k)	
k = 20	

Matrix Size = 11

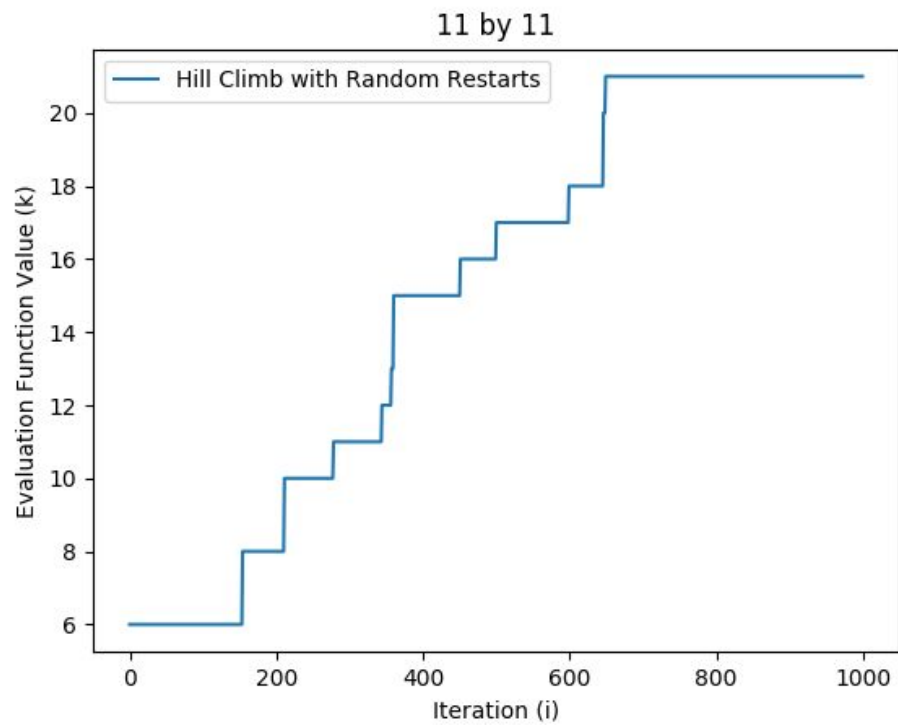
Final Matrix

8 1 3 10 10 5 7 7 9 5 3
10 3 4 6 8 6 1 4 6 5 5
5 6 5 8 3 7 8 3 3 9 9
9 6 4 2 2 7 4 3 5 2 6
6 8 7 1 2 3 1 4 2 2 10
7 3 8 6 3 4 4 6 6 6 9
1 9 7 6 5 4 6 1 3 5 9
10 6 1 5 4 6 4 4 4 7 2
9 6 1 6 8 5 5 2 6 8 1
3 7 3 8 9 4 2 7 3 2 3
10 2 3 2 8 8 8 5 6 9 0

Tree



Graph



Value Function (k)

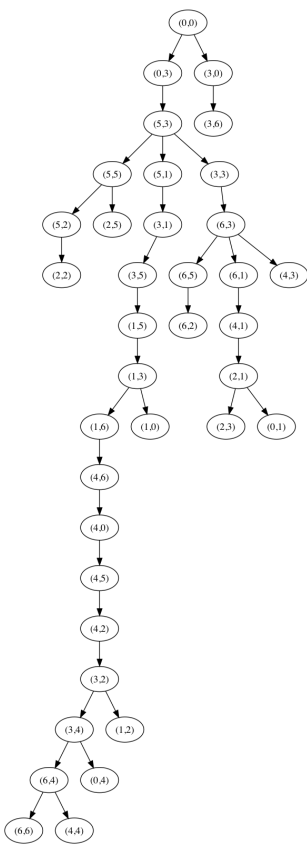
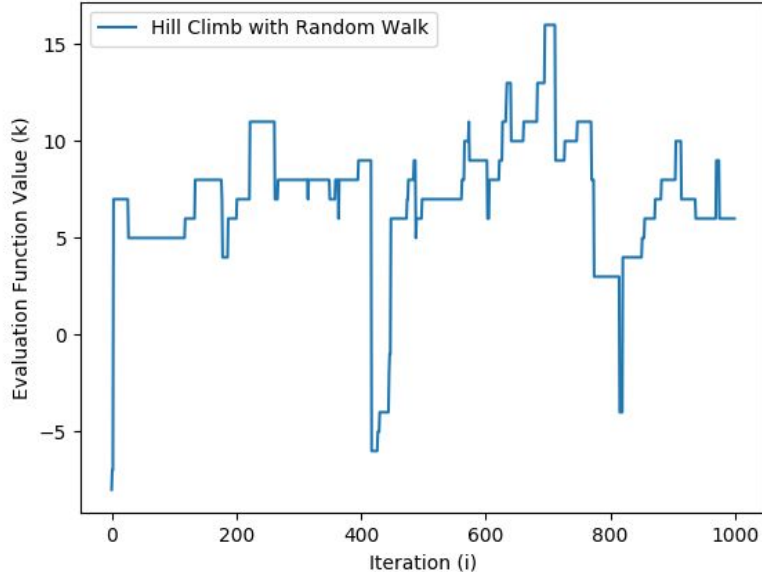
$k = 21$

Task 5

Matrix Size = 5

Final Matrix		
2 3 3 3 4 1 2 3 3 4 2 3 1 2 3 3 1 3 3 2 2 4 4 3 0		
Graph		
Value Function (k)		
k = 12		

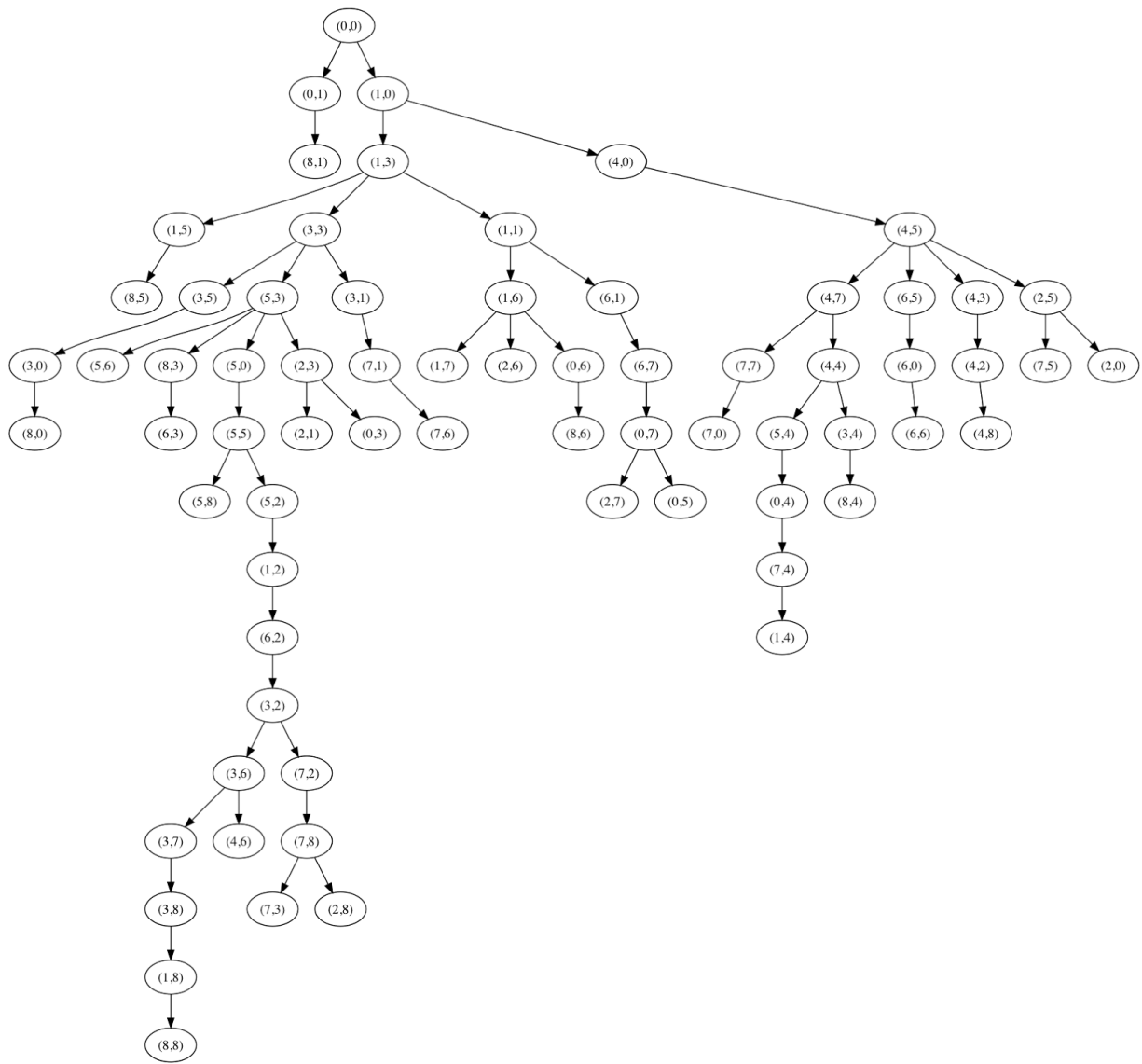
Matrix Size = 7

Final Matrix		
3 2 1 5 4 4 1 6 1 5 3 3 2 3 4 2 3 4 3 3 5 6 4 2 3 3 2 6 5 2 1 4 4 3 6 4 2 3 2 2 3 5 4 2 1 2 2 3 0		
Graph		
<div>7 by 7</div> 		
Value Function (k)		
k = 16		

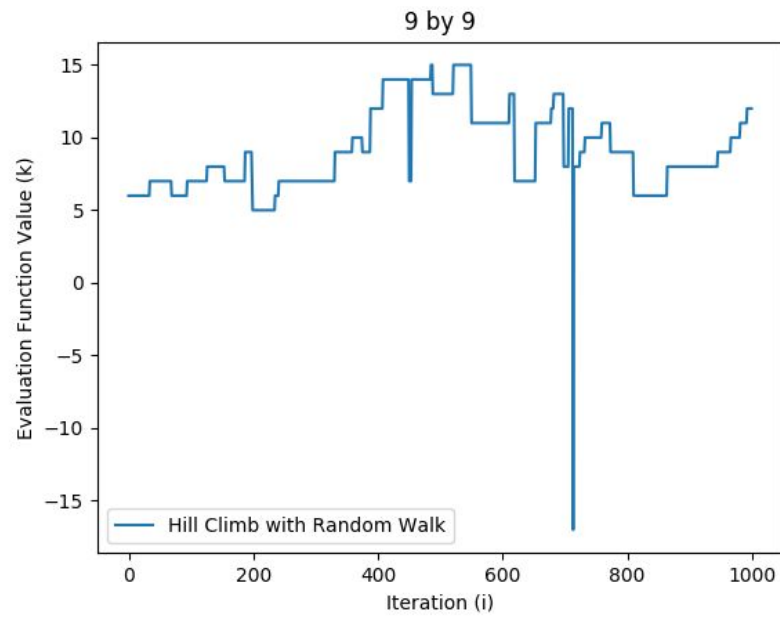
Matrix Size = 9	
<i>Final Matrix</i>	
1 8 6 4 7 6 8 2 5 3 5 5 2 3 7 1 6 7 6 4 4 2 3 5 3 4 8 5 4 4 2 5 5 1 1 2 5 6 6 1 1 2 6 3 6 5 4 4 3 5 3 6 4 6	

6 6 3 3 5 5 6 2
6 5 6 1 6 4 1 7 5
3 8 2 2 8 6 7 5 0

Tree



Graph



Value Function (k)

k = 15

Matrix Size = 11

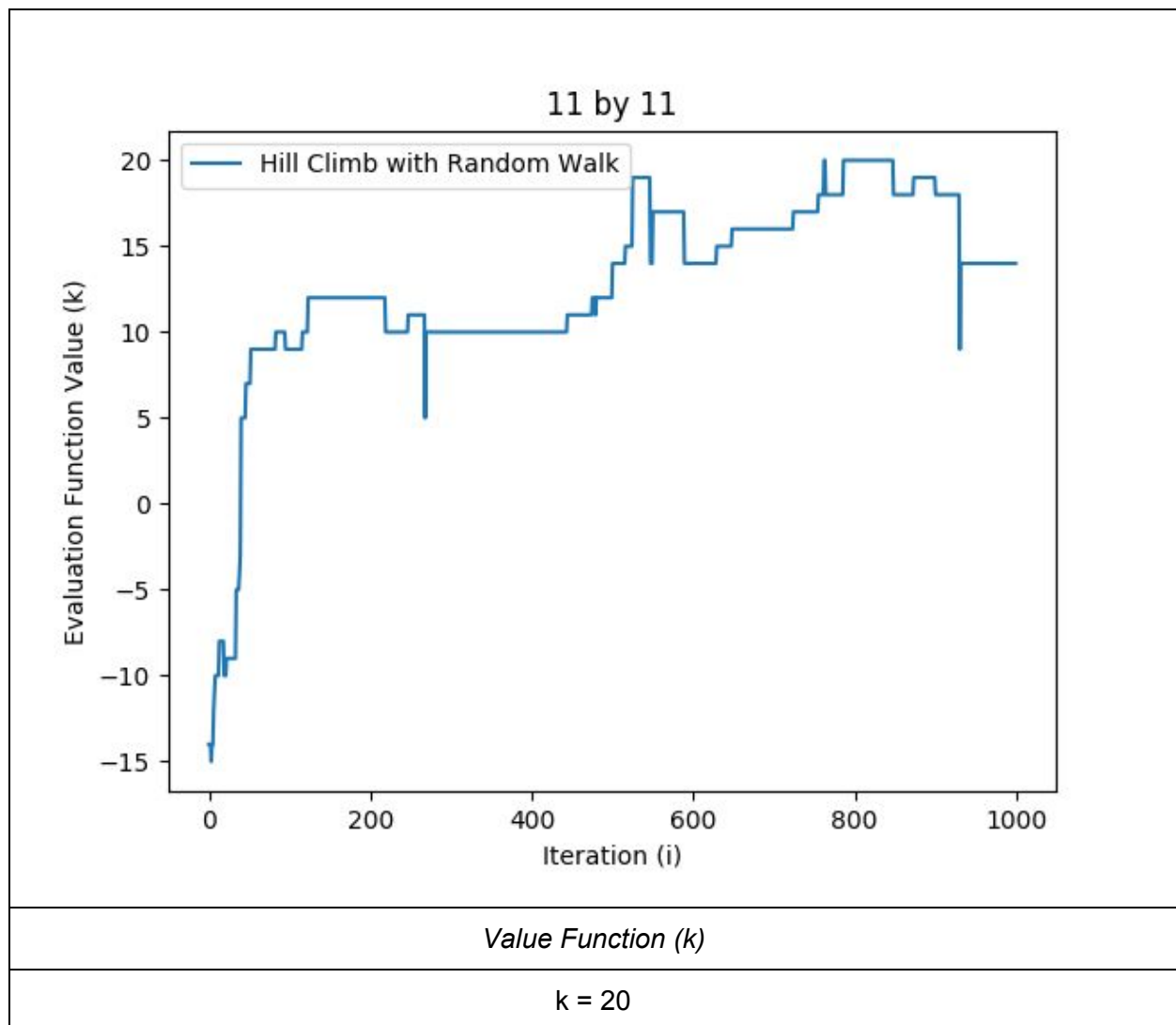
Final Matrix

```

3 2 2 9 4 6 8 7 1 4 8
5 5 4 9 2 7 2 6 7 4 7
5 4 1 4 8 6 8 4 7 2 1
8 4 2 2 1 6 7 7 8 2 6
3 5 2 3 6 6 3 5 5 3 9
7 3 2 6 5 4 1 1 6 4 1
9 8 7 3 1 3 5 6 4 9 6
3 7 4 6 3 5 6 7 8 7 3
3 5 8 6 2 2 3 7 3 3 2
5 3 6 8 6 7 9 2 9 9 7
9 5 9 5 8 6 9 5 9 10 0

```

Tree



Task 6

Matrix Size = 5

Final Matrix		
1 4 1 1 1 3 2 1 3 2 1 3 1 1 4 3 1 1 2 1 3 2 3 3 0		
Graph		
Value Function (k)		
k = 17		

Matrix Size = 7

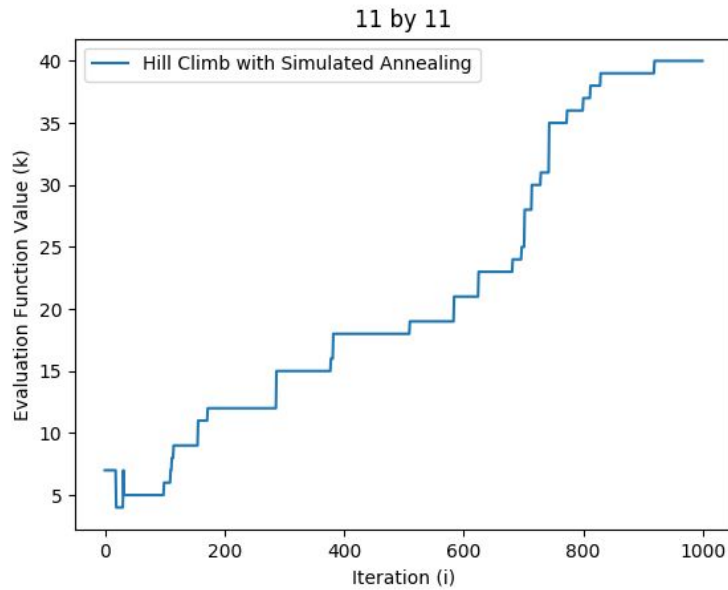
<p><i>Final Matrix</i></p>	
<p>5 6 1 6 2 5 1 2 4 5 4 5 3 2 5 2 2 2 3 3 4 2 2 3 1 1 4 2 3 4 4 2 4 4 6 5 4 1 4 4 4 3 4 1 5 1 5 3 0</p>	
<p><i>Graph</i></p>	
<p>7 by 7</p>	
<p><i>Value Function (k)</i></p>	
<p>k = 29</p>	

Matrix Size = 9	
Final Matrix	

Final Matrix

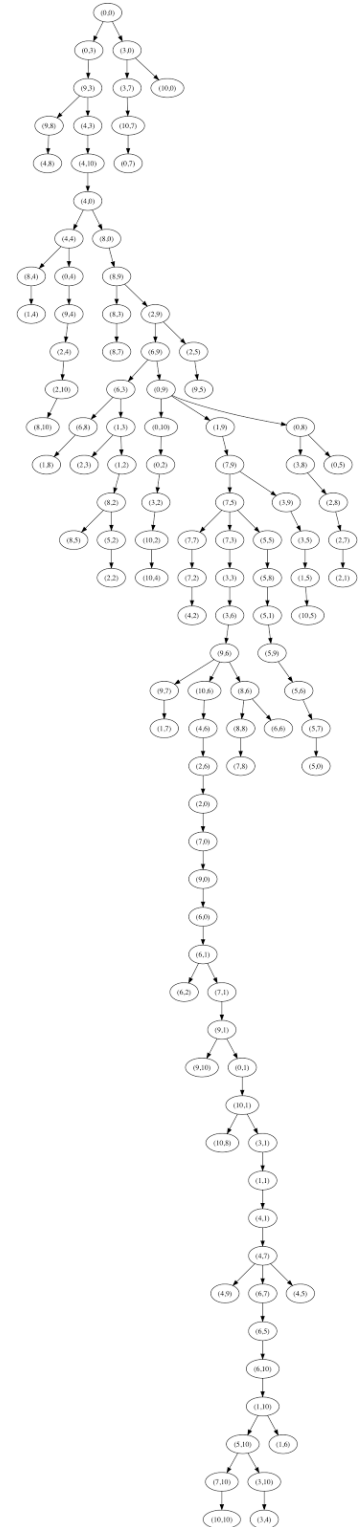
3 10 3 9 9 2 2 10 3 1 8
 7 3 7 1 8 9 7 9 5 6 4
 5 9 8 6 6 7 6 6 1 4 6
 7 2 7 3 1 2 6 7 1 4 6
 4 6 6 7 4 3 2 2 5 9 10
 7 8 3 2 4 3 1 7 7 3 2
 1 1 1 5 2 5 3 2 5 6 5
 2 2 3 4 3 2 3 5 1 4 3
 9 8 3 4 7 8 2 8 1 6 6
 3 9 9 5 7 7 1 8 5 4 9
 7 7 2 8 8 10 6 10 4 8 0

Graph



Value Function (k)

k = 40



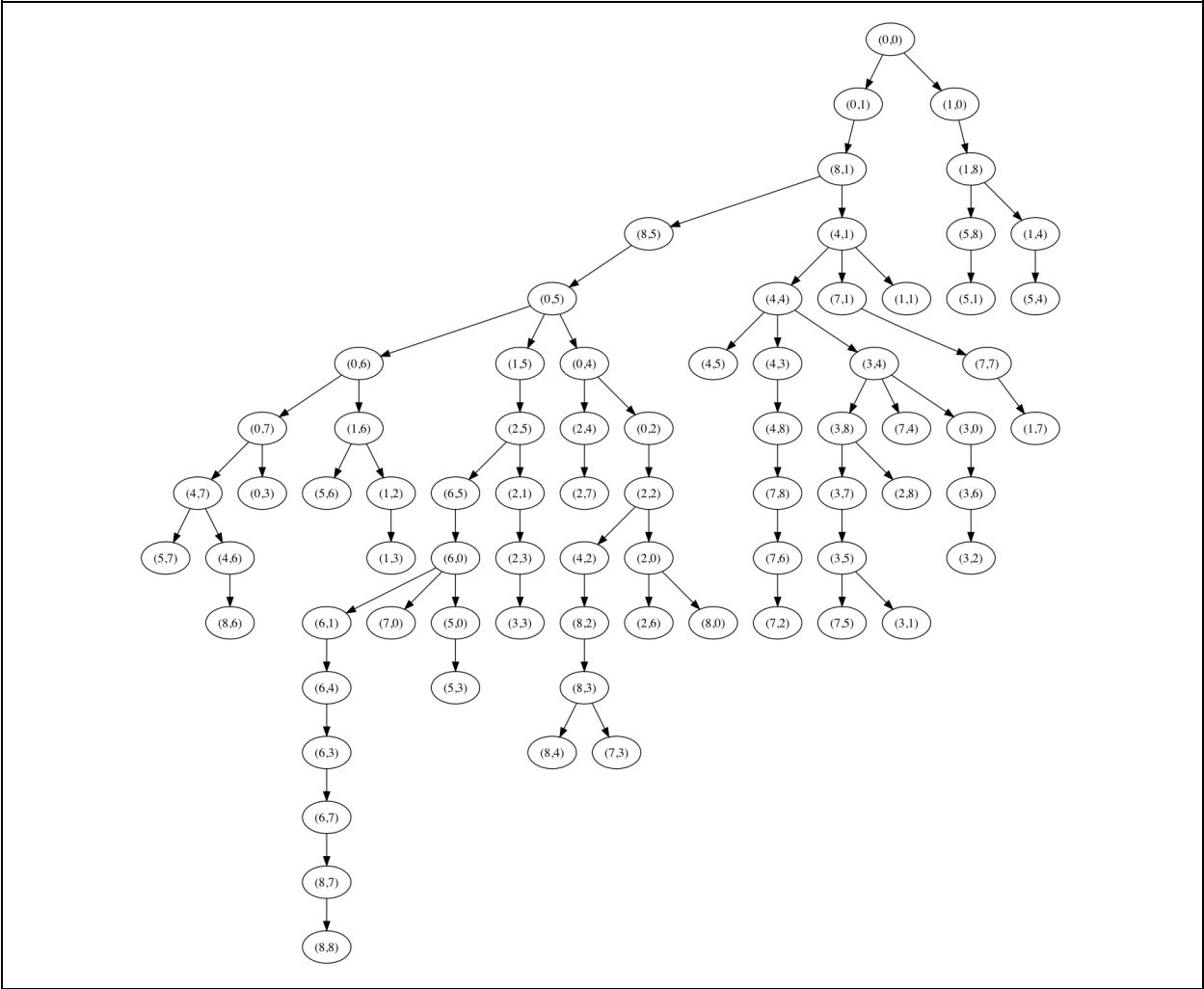
Task 7

Matrix Size = 5	
Final Matrix	
Graph	
Value Function (k)	
k = 12	

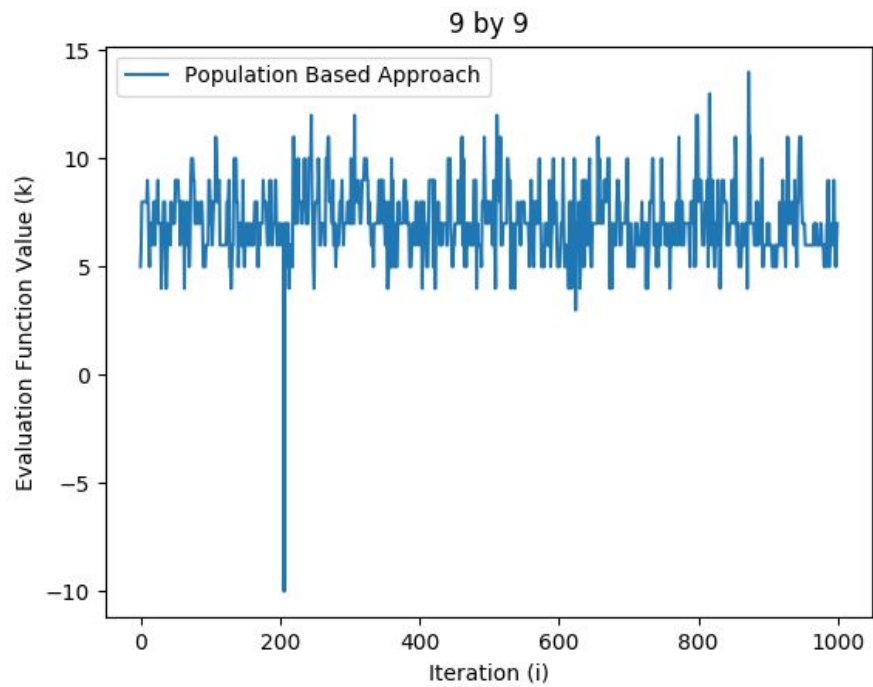
Matrix Size = 7

267771462
541118710

<i>Tree</i>



Graph



Value Function (k)

$k = 14$

Matrix Size = 11

Final Matrix

```

3 6 4 3 2 3 5 6 4 5 8
1 4 7 7 3 1 4 7 5 4 5
10 3 4 6 1 4 6 6 8 2 7
10 7 7 4 5 2 1 3 4 3 8
4 6 7 2 5 5 1 4 8 1 7
1 6 3 1 4 3 5 2 6 5 9
1 9 3 7 4 5 6 5 4 3 9
3 5 2 4 4 1 2 5 7 2 5
10 3 8 7 6 8 6 2 7 1 5
3 7 7 5 7 3 7 8 6 9 4
2 2 7 10 3 5 10 7 3 7 0

```

Tree

Task 8

Largest and Most Complex Puzzle

Matrix Size = 500
<i>Final Matrix</i>
Too large for document. See external text file ("n500_k16.txt").
<i>Value Function (k)</i>
k = 16