

## Q1.

(1) No. F don't include J, so  $F^+$  also don't include J, that's the reason why  $C \rightarrow J \notin F^+$

(2) ABJ, AEJ.

(3)  $F_m = \{AB \rightarrow E, D \rightarrow H, E \rightarrow B, E \rightarrow C, C \rightarrow D, H \rightarrow G, C \rightarrow I\}$

(4)

For  $F_m = \{AB \rightarrow E, D \rightarrow H, E \rightarrow B, E \rightarrow C, C \rightarrow D, H \rightarrow G, C \rightarrow I\}$ :

From  $AB \rightarrow E$ , derive  $R_1\{A, B, E\}$

From  $D \rightarrow H$ , derive  $R_2\{D, H\}$

From  $E \rightarrow B, E \rightarrow C$ , derive  $R_3\{E, B, C\}$

From  $C \rightarrow D, C \rightarrow I$ , derive  $R_4\{C, D, I\}$

From  $H \rightarrow G$ , derive  $R_5\{H, G\}$

None of the relation schemas contains a key of R, add one relation schema  $R_6\{A, B, J\}$

## Q2.

(1)  $2^*2^6 - 2^5 = 96$ , ABCJ, ABDJ, ABEJ, ABGJ, ABHJ

(2) 1NF. None-prime attribute CE is functionally determined by AB, which is not satisfy the 2NF.

(3)  $F_1 = \{AB \rightarrow E, E \rightarrow BCD\}$

$F_2 = \{H \rightarrow G\}$

$F_3 = \{\}$

We need to verify if  $D \rightarrow GH, C \rightarrow DI, EH \rightarrow I$  are inferred by  $F_1 \cup F_2 \cup F_3$ .

Since  $D^+ \mid F_1 \cup F_2 \cup F_3 = \{D\}$ ,  $C^+ \mid F_1 \cup F_2 \cup F_3 = \{C\}$ ,  $EH^+ \mid F_1 \cup F_2 \cup F_3 = \{BCDEHG\}$ ,  $D \rightarrow GH, C \rightarrow DI, EH \rightarrow I$  are not inferred by  $F_1 \cup F_2 \cup F_3$ . Thus,  $F_1, F_2$  and  $F_3$  are not dependency preserving regarding  $F'$ .

(4) No.

Decomposition	A	B	C	D	E	G	H	I	J
$R_1(A, B, C, D, E)$	a	a	a	a	a	b	b	b	b
$R_2(E, G, H)$	b	b	b	b	a	a	a	b	b
$R_3(E, I, J)$	b	b	b	b	a	b	b	a	a

Decomposition	A	B	C	D	E	G	H	I	J
$R_1(A,B,C,D,E)$	a	a	a	a	a	a	a	a	b
$R_2(E,G,H)$	b	a	a	a	a	a	a	a	b
$R_3(E,I,J)$	b	a	a	a	a	a	a	a	a

(5)  $F_m = \{AB \rightarrow E, D \rightarrow H, E \rightarrow B, E \rightarrow C, C \rightarrow D, H \rightarrow G, C \rightarrow I\}$

Consider  $AB \rightarrow E$  for  $F_m$  :  $R_1(A,B,E), R_2'(A,B,C,D,G,H,I,J)$

Consider  $D \rightarrow H$  for  $R_2'$  :  $R_2(D,H), R_3'(A,B,C,D,G,I,J)$

Consider  $C \rightarrow D$  for  $R_3'$  :  $R_3(C,D), R_4'(A,B,C,G,I,J)$

Consider  $C \rightarrow I$  for  $R_4'$  :  $R_4(C,I), R_5(A,B,C,G,J)$

One of the possible lossless-join decomposition is  $R_1 \sim R_5$