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$\mathbf{Q4}$

As the question mentioned, each square has n^2 trees and total $16n^2$ trees in orchard. And we already have a map with the number of apples on each tree.

First, assume we have a Sum Matrix which sum[i][j] equals to the sum of apples from left top(0,0) to right bottom (i,j) trees which called 2-dimension prefix sum. We can use 2 for loops to handle this in $O(n^2)$.

Then, we have $(3n+1)^2$ possible squares and for each square we compute the number of apples in this square by sum[i][j] - sum[i-n][j] - sum[i][j-n] + sum[i-n][j-n] in $O(n^2)$.

Finally, we can find the square contains the largest number of apples in $O(n^2) + O(n^2) = O(n^2)$.