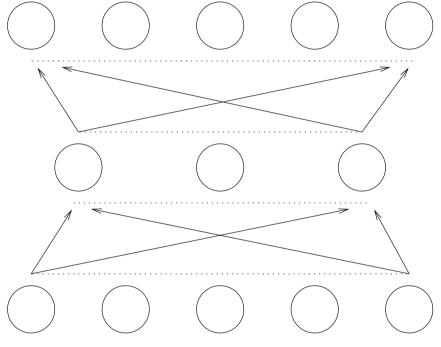
# COMP9444 Neural Networks and Deep Learning 9b. Autoencoders

Textbook, Chapter 14

#### **Outline**

- Autoencoder Networks (14.1)
- Regularized Autoencoders (14.2)
- Stochastic Encoders and Decoders (14.4)
- Generative Models
- Variational Autoencoders (20.10.3)

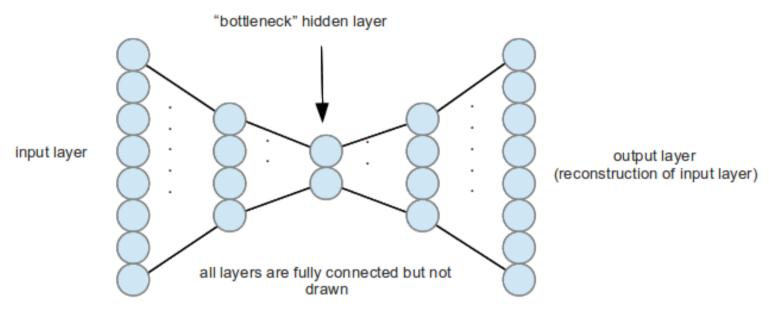
#### **Recall: Encoder Networks**



Inputs	Outputs
10000	10000
01000	01000
00100	00100
00010	00010
00001	00001

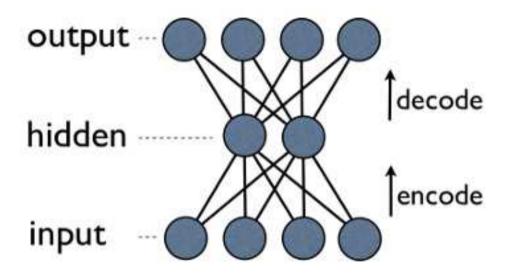
- identity mapping through a bottleneck
- also called N–M–N task
- used to investigate hidden unit representations

#### **Autoencoder Networks**



- output is trained to reproduce the input as closely as possible
- activations normally pass through a bottleneck, so the network is forced to compress the data in some way
- like the RBM, Autoencoders can be used to automatically extract abstract features from the input

#### **Autoencoder Networks**



If the encoder computes z = f(x) and the decoder computes g(f(x)) then we aim to minimize some distance function between x and g(f(x))

$$E = L(x, g(f(x)))$$

### **Autoencoder as Pretraining**

- after an autoencoder is trained, the decoder part can be removed and replaced with, for example, a classification layer
- this new network can then be trained by backpropagaiton
- the features learned by the autoencoder then serve as initial weights for the supervised learning task

# **Greedy Layerwise Pretraining**

- Autoencoders can be used as an alternative to Restricted Bolzmann Machines, for greedy layerwise pretraining.
- An autoencoder with one hidden layer is trained to reconstruct the inputs. The first layer (encoder) of this network becomes the first layer of the deep network.
- Each subsequent layer is then trained to reconstruct the previous layer.
- A final classification layer is then added to the resulting deep network, and the whole thing is trained by backpropagation.

### **Avoiding Trivial Identity**

- if there are more hidden nodes than inputs (which often happens in image processing) there is a risk the network may learn a trivial identity mapping from input to output
- we generally to avoid this by introducing some form of regularization

### Regularized Autoencoders (14.2)

- sparse autoencoders
- autoencoders with dropout at hidden layer(s)
- contractive autoencoders
- denoising autoencoders

#### **Sparse Autoencoder (14.2.1)**

- one way to regularize an autoencoder is to add a penalty term in the loss function, based on the hidden unit activations
- this is analagous to the weight decay term we previously used for supervised learning
- one popular choice is to penalize the sum of the absolute values of the activations in the hidden layer

$$E = L(x, g(f(x)) + \lambda \sum_{i} |h_{i}|$$

this is sometimes known as  $L_1$ -regularization (because it involves the absolute value rather than the square); it can encourage some of the hidden units to go to zero, thus producing a sparse representation

#### **Contractive Autoencoder (14.2.3)**

another popular penalty term is the  $L_2$ -norm of the derivatives of the hidden units with respect to the inputs

$$E = L(x, g(f(x)) + \lambda \sum_{i} ||\nabla_{x} h_{i}||^{2}$$

 $\blacksquare$  this forces the model to learn hidden features that do not change much when the training inputs x are slightly altered

#### **Denoising Autoencoder (14.2.2)**

Another regularization method, similar to contractive autoencoder, is to add noise to the inputs, but train the network to recover the original input

```
repeat: sample a training item x^{(i)} generate a corrupted version \tilde{x} of x^{(i)} train to reduce E = L\big(x^{(i)}, g(f(\tilde{x}))\big) end
```

#### **Loss Functions and Probability**

- We saw previously how the loss (cost) function at the output of a feedforward neural network (with parameters  $\theta$ ) can be seen as defining a probability distribution  $p_{\theta}(x)$  over the outputs. We then train to maximize the log of the probability of the target values.
  - squared error assumes an underlying Gaussian distribution, whose mean is the output of the network
  - cross entropy assumes a Bernoulli distribution, with probability equal to the output of the network
  - softmax assumes a Boltzmann distribution

#### **Stochastic Encoders and Decoders (14.4)**

- For autoencoders, the decoder can be seen as defining a conditional probability distribution  $p_{\theta}(x|z)$  of output x for a certain value z of the hidden or "latent" variables.
- In some cases, the encoder can also be seen as defining a conditional probability distribution  $q_{\phi}(z|x)$  of latent variables z based on an input x.
- We have seen an example of this with the Restricted Boltzmann Machine, where  $q_{\phi}(z|x)$  and  $p_{\theta}(x|z)$  were Bernoulli distributions.

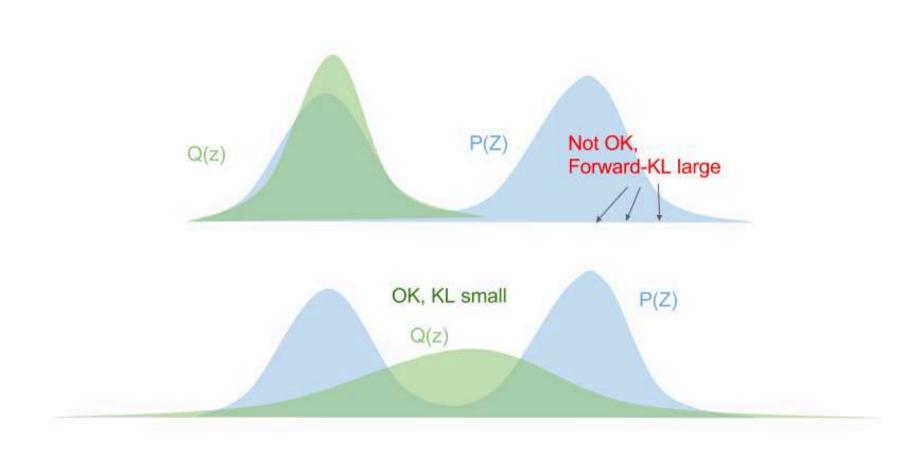
#### **Generative Models**

- Sometimes, as well as reproducing the training items  $\{x^{(i)}\}$ , we also want to be able to use the decoder to generate new items which are of a similar "style" to the training items.
- In other words, we want to be able to choose latent variables z from a standard Normal distribution p(z), feed these values of z to the decoder, and have it produce a new item x which is somehow similar to the training items.
- Generative models can be:
  - explicit (Variational Autoencoders)
  - implicit (Generative Adversarial Networks)

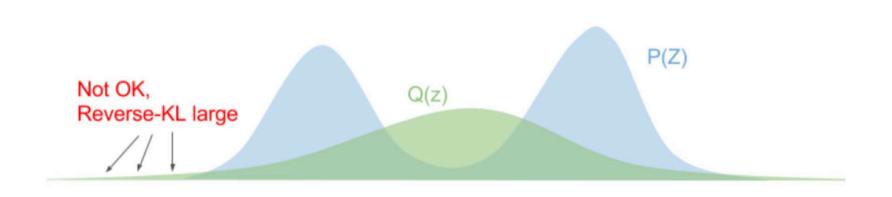
#### **Entropy and KL-Divergence**

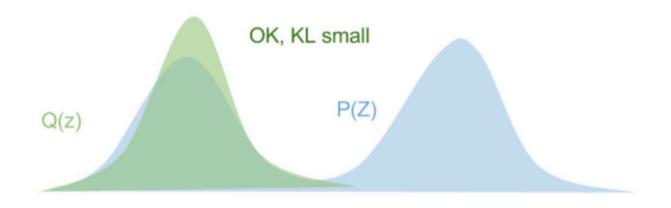
- the entropy of a distribution q() is  $H(q) = \int_{\theta} q(\theta)(-\log q(\theta))d\theta$
- in Information Theory, H(q) is the amount of information (bits) required to transmit a random sample from distribution q()
- for a Gaussian distribution,  $H(q) = \sum_{i} \log \sigma_i$
- KL-Divergence  $D_{\mathrm{KL}}(q \parallel p) = \int_{\Theta} q(\theta) (\log q(\theta) \log p(\theta)) d\theta$
- D<sub>KL</sub> $(q \parallel p)$  is the number of extra bits we need to trasmit if we designed a code for p() but then the samples are drawn from q() instead.

# **Forward KL-Divergence**



# **Reverse KL-Divergence**





### **KL-Divergence**

- KL-Divergence is an important component of Variational Autoencoders.
- KL-Divergence is also used in some policy-based deep reinforcement learning algorithms such as Trust Region Policy Optimization (TPRO) (but we will not cover these in detail).

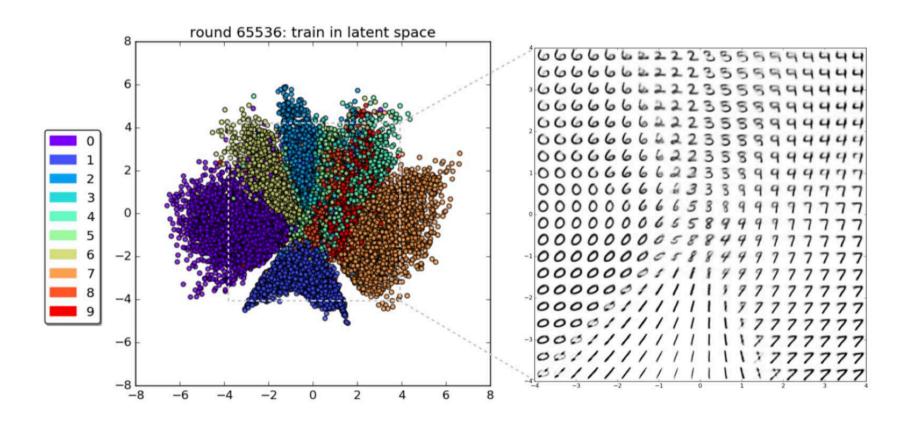
### Variational Autoencoder (20.10.3)

Instead of producing a single z for each  $x^{(i)}$ , the encoder (with parameters  $\phi$ ) can be made to produce a mean  $\mu_{z|x^{(i)}}$  and standard deviation  $\Sigma_{z|x^{(i)}}$ . This defines a conditional (Normal) probability distribution  $q_{\phi}(z|x^{(i)})$ . We then train the system to maximize

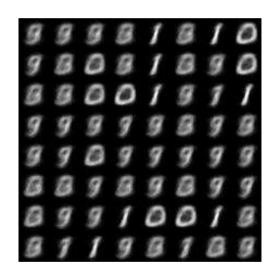
$$\mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})}[\log p_{\theta}(x^{(i)}|z)] - D_{\mathrm{KL}}(q_{\phi}(z|x^{(i)})||p(z))$$

- the first term enforces that any sample z drawn from the conditional distribution  $q_{\phi}(z|x^{(i)})$  should, when fed to the decoder, produce somthing approximating  $x^{(i)}$
- the second term encourages  $q_{\phi}(z|x^{(i)})$  to approximate p(z)
- in practice, the distributions  $q_{\phi}(z|x^{(i)})$  for various  $x^{(i)}$  will occupy complementary regions within the overall distribution p(z)

# **Variational Autoencoder Digits**



# **Variational Autoencoder Digits**



1st Epoch



9th Epoch



Original

# **Variational Autoencoder Faces**



#### **Variational Autoencoder**

- Variational Autoencoder produces reasonable results
- tends to produce blurry images
- $\blacksquare$  often end up using only a small number of the dimensions available to z

#### References:

```
http://kvfrans.com/variational-autoencoders-explained/
http://cs231n.stanford.edu/slides/2017/cs231n_2017_lecture13.pdf
https://arxiv.org/pdf/1606.05908.pdf
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