COMP9444 Neural Networks and Deep Learning
Term 3, 2019

Exercises 6: Reinforcement Learning

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Consider an environment with two states $S = \{S_1, S_2\}$ and two actions $A = \{a_1, a_2\}$, where the (deterministic) transitions δ and reward R for each state and action are as follows:

$$\delta(S_1, a_1) = S_1, \quad R(S_1, a_1) = +1$$
$$\delta(S_1, a_2) = S_2, \quad R(S_1, a_2) = -2$$
$$\delta(S_2, a_1) = S_1, \quad R(S_2, a_1) = +7$$
$$\delta(S_2, a_2) = S_2, \quad R(S_2, a_2) = +3$$

1. Draw a picture of this environment, using circles for the states and arrows for the transitions.

2. Assuming a discount factor of $\gamma = 0.7$, determine:
   a. the optimal policy $\pi^* : S \rightarrow A$
   b. the value function $V^* : S \rightarrow R$
   c. the "Q" function $Q^* : S \times A \rightarrow R$

   Write the Q values in a matrix like this:

Q	a_1	a_2
S_1		
S_2		

   Trace through the first few steps of the Q-learning algorithm, with a learning rate of 1 and with all Q values initially set to zero. Explain why it is necessary to force exploration through probabilistic choice of actions, in order to ensure convergence to the true Q values.

3. Now let's consider how the Value function changes as the discount factor γ varies between 0 and 1.
   There are four deterministic policies for this environment, which can be written as π_{11}, π_{12}, π_{21} and π_{22}, where $\pi_{ij}(S_1) = a_i$, $\pi_{ij}(S_2) = a_j$

   a. Calculate the value function $V^{\pi}{}_{(\gamma)}$: $S \rightarrow R$ for each of these four policies (keeping γ as a variable)
   b. Determine for which range of values of γ each of the policies π_{11}, π_{12}, π_{21}, π_{22} is optimal

Make sure you try answering the Exercises yourself, before checking the Sample Solutions