

Computer Vision

Exercise Session 1

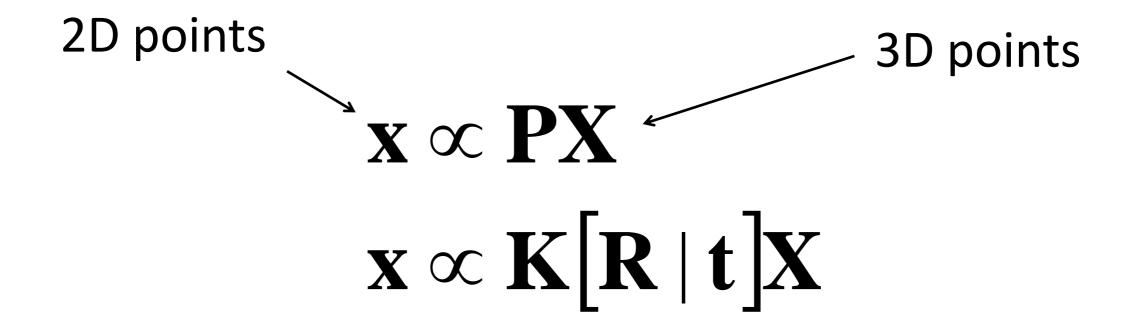




Camera Calibration

- Intrinsic parameters

 - Radial distortion coefficients

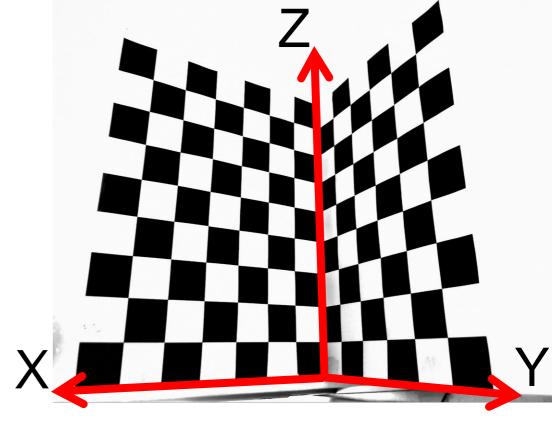




Camera Calibration

- We provide you with an input image
- Need to click points in the image and manually enter the 3D position

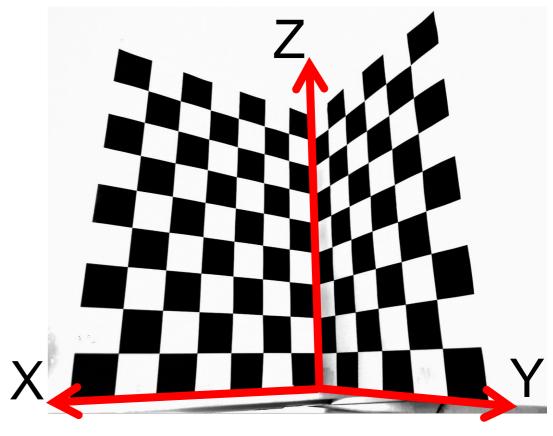
Use the coordinate system as shown





Taking your own pictures (optional)

- Use your own camera
- Build your own calibration object
 - Print checkerboard patterns
 - Stich to two orthogonal planes
- Use constant settings
 - No autofocus
 - Don't change the zoom





Camera Calibration

- 4 Tasks:
 - Data normalization
 - Direct Linear Transform (DLT)
 - Gold Standard algorithm
 - MATLAB Calibration Toolbox (optional)
- Good reference:
 Multiple View Geometry in computer vision
 (Richard Hartley & Andrew Zisserman)





Data Normalization

- Required for numeric stability
- Shift the centroid of the points to the origin
- Scale the points so that the mean distance to the origin is 1.
- Determine $\widehat{\mathbf{P}}$ using normalized points.
- Determine $P = T^{-1}\widehat{P}U$

$$\mathbf{T} = \begin{bmatrix} \mathbf{S}_{2D} & & \mathbf{C}_{x} \\ & \mathbf{S}_{2D} & \mathbf{C}_{y} \\ & & 1 \end{bmatrix}^{-1}$$

$$\mathbf{U} = \begin{bmatrix} \mathbf{S}_{3D} & & & \mathbf{C}_{x} \\ & \mathbf{S}_{3D} & & \mathbf{C}_{y} \\ & & \mathbf{S}_{3D} & \mathbf{C}_{z} \\ & & & 1 \end{bmatrix}$$

Direct Linear Transform (DLT)

$$[\mathbf{x}_i]_{\times} \mathbf{P} \mathbf{X}_i = \mathbf{0}$$

$$\mathbf{x} = \begin{pmatrix} x \\ y \\ w \end{pmatrix} \qquad \mathbf{X} = \begin{pmatrix} x \\ Y \\ Z \\ W \end{pmatrix}$$

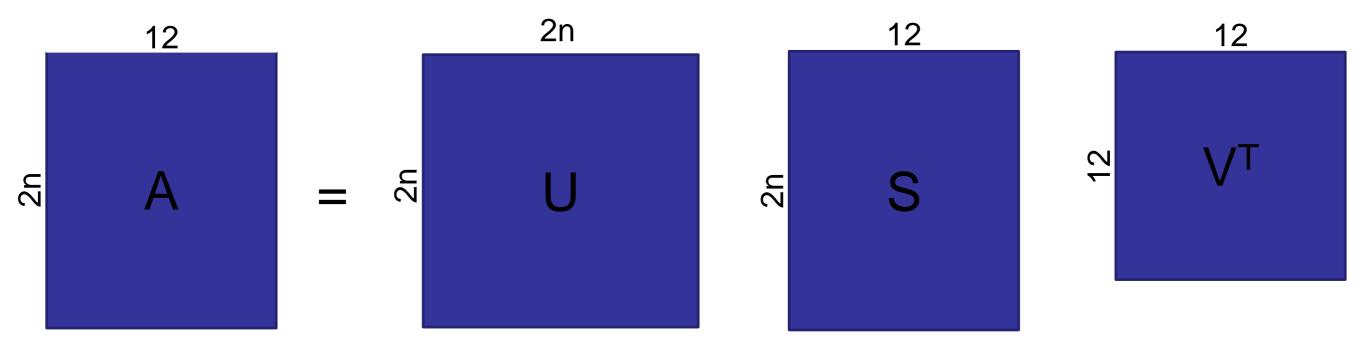
$$\rightarrow \mathbf{A}_{i}\mathbf{P} = \begin{bmatrix} w_{i}\boldsymbol{X}_{i}^{T} & 0^{T} & -x_{i}\boldsymbol{X}_{i}^{T} \\ 0^{T} & -w_{i}\boldsymbol{X}_{i}^{T} & y_{i}\boldsymbol{X}_{i}^{T} \end{bmatrix} \begin{pmatrix} \mathbf{P}^{1} \\ \mathbf{P}^{2} \\ \mathbf{P}^{3} \end{pmatrix} = 0$$

$$\begin{bmatrix} X_{ix} & X_{iy} & X_{iz} & 1 & 0 & 0 & 0 & -x_i X_{ix} & -x_i X_{iy} & -x_i X_{iz} & -x_i \\ 0 & 0 & 0 & 0 & -X_{ix} & -X_{iy} & -X_{iz} & -1 & y_i X_{ix} & y_i X_{iy} & y_i X_{iz} & y_i \end{bmatrix} \begin{pmatrix} P_{1,1} \\ P_{1,2} \\ \vdots \\ P_{3,3} \\ P_{3,4} \end{pmatrix} = 0$$



Direct Linear Transform (DLT)

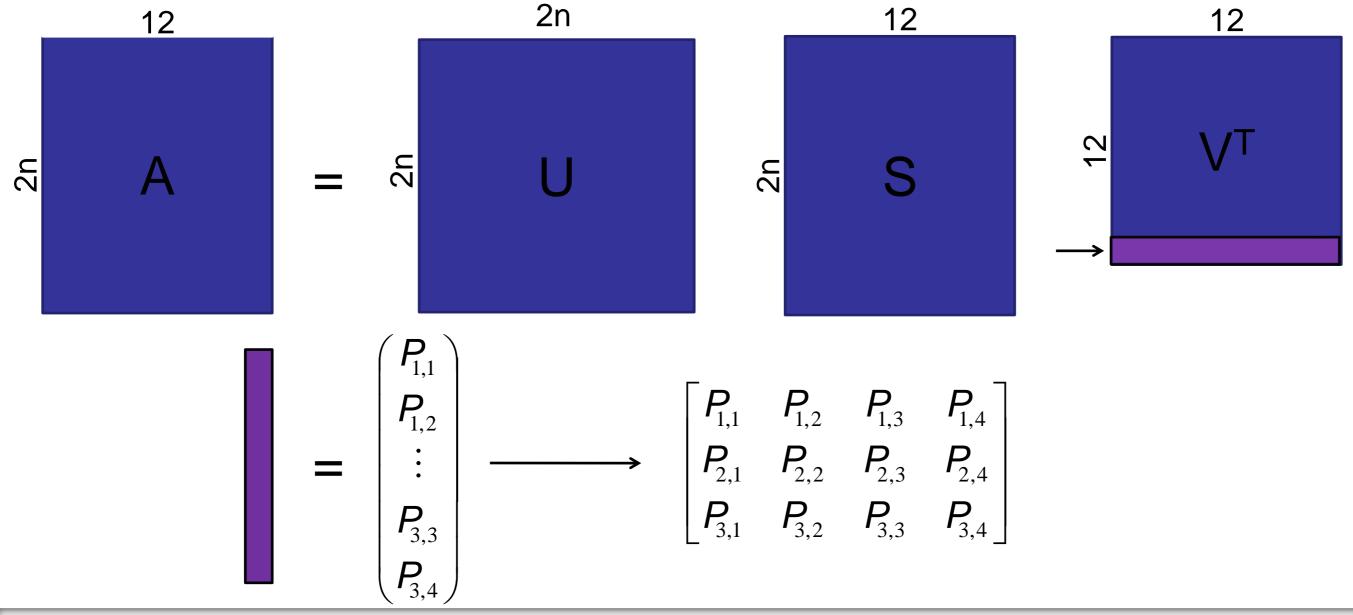
Singular Value Decomposition





Direct Linear Transform (DLT)

Singular Value Decomposition





$$P = K[R|t] = K[R|-RC] = [KR|-KRC]$$

- K is upper triangular
- R is orthonormal
- QR decomposition A = QR
 - Q is orthogonal
 - R is upper triangular





$$P = [KR \mid -KRC]$$

$$M = KR$$

$$M^{-1} = R^{-1}K^{-1}$$

- Run QR-decomposition on the inverse of the left 3x3 part of P
- Invert both result matrices to get K and R





- K should have a positive diagonal
- $\det(R) = 1$

e.g.
$$T = \begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$KR = KTT^{-1}R$$

$$\rightarrow K' = K^T \qquad R' = T^{-1}R$$



- K should have a positive diagonal
- det(R) = 1

If
$$det(R) = -1 \rightarrow R = -R$$



Camera Matrix Decomposition (C)

The camera center is the point for which

$$PC = 0$$

■ This is the right null vector of P (→ SVD)

Gold Standard Algorithm

- Normalize data
- Run DLT to get initial values
- Compute optimal $\hat{\mathbf{P}}$ by minimizing the sum of squared reprojection errors

$$\min_{\hat{\mathbf{P}}} \sum_{i=1}^{N} d(\hat{\mathbf{x}}_{i}, \hat{\mathbf{P}}\hat{\mathbf{X}}_{i})^{2}$$

Denormalize $\hat{\mathbf{P}}$



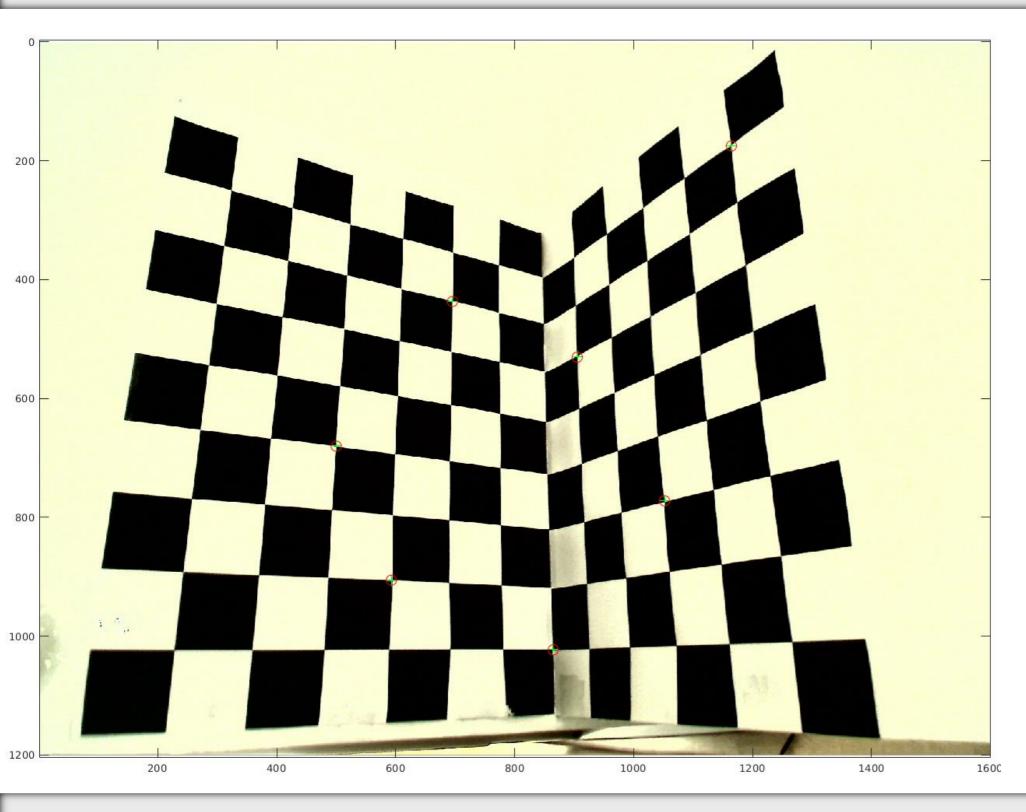
Hand-in

- Source code
- Matlab .mat-file with hand-clicked 3D-2D correspondences
- Image used for calibration (optional)
 - Use the same camera with the same settings for all tasks!
- Visualize hand-clicked points and reprojected 3D points
- Discuss values of intrinsic parameters
- Discuss average reprojection errors of all methods





Hand-in



Reprojection of the the 3D points



