

Lab Manual

Part A

1. Write a program for different types of data structures in R

```
# Creating a Numeric Vector  
n <- c(1, 2, 3, 4, 5)  
print("Numeric Vector:")  
print(n)  
  
# Creating a Character Vector  
cv <- c("apple", "banana", "cherry")  
print("Character Vector:")  
print(cv)  
  
# Creating a List  
lst <- list(1, "apple", TRUE)  
print("List:")  
print(lst)  
  
# Creating a Matrix  
m <- matrix(1:6, nrow = 2, ncol = 3)  
print("Matrix:")  
print(m)  
  
# Creating a Data Frame  
df <- data.frame(Name = c("Alice", "Bob", "Charlie"),  
                  Age = c(25, 30, 22))  
print("Data Frame:")  
print(df)
```

Output

```
[1] "Numeric Vector:"
[1] 1 2 3 4 5
[1] "Character Vector:"
[1] "apple" "banana" "cherry"

[1] "List:"
[[1]]
[1] 1
[[2]]
[1] "apple"
[[3]]
[1] TRUE

[1] "Matrix:"
 [,1] [,2] [,3]
 [1,] 1   3   5
 [2,] 2   4   6

[1] " Data Frame:"
      Name Age
1 Alice 25
2 Bob 30
3 Charlie 22
```

2. Write a program that include variables, constants, data types

```
# Constants
PI <- 3.14159
GRAVITY <- 9.81 includes
# Variables
name <- "John Doe"
age <- 30
is_student <- TRUE
grades <- c(85, 92, 78, 95, 89)
# Displaying information
cat("Name:", name, "\n")
cat("Age:", age, "\n")
cat("Is Student:", is_student, "\n")
```

```

cat("Grades:", grades, "\n")
# Data Types
nType <- typeof(name)
aType <- typeof(age)
iType <- typeof(is_student)
gType <- typeof(grades)
cat("Data Type of 'name':", nType, "\n")
cat("Data Type of 'age':", aType, "\n")
cat("Data Type of 'is_student':", iType, "\n")
cat("Data Type of 'grades':", gType, "\n")

```

Output

```

Name: John Doe
Age: 30
is Student: TRUE
Grades: 85 92 78 95 89
Data Type of 'name': character
Data Type of 'age': double
Data Type of 'is_student': logical
Data Type of 'grades': double

```

3. Write a R program that includes different operators, control structures, default values for arguments, returning complex objects

```

# Function with default argument values
calculate_area <- function(shape = "rectangle", length = 5, width = 3) {
  if (shape == "rectangle") {
    area <- length * width
  } else if (shape == "circle") {
    radius <- length / 2
    area <- pi * radius^2
  } else {
    cat("Unsupported shape:", shape, "\n")
    return(NULL)
  }

  # Conditional operator
  message <- ifelse(area > 10, "Large area", "Small area")
  result <- list(
    Shape = shape,

```

```
Length = length,  
Width = width,  
Area = area,  
Message = message  
)  
return(result)  
}  
# Using the function with default arguments  
result1 <- calculate_area()  
result2 <- calculate_area("rectangle", 8, 4)  
result3 <- calculate_area("circle", 6)  
# Displaying results  
cat("Result 1:\n")  
print(result1)  
cat("\nResult 2:\n")  
print(result2)  
cat("\nResult 3:\n")  
print(result3)
```

Output

Result 1:

\$Shape

[1] "rectangle"

\$Length

[1] 5

\$Width

[1] 3

\$Area

[1] 15

\$Message

[1] "Large area"

Result 2:

\$Shape

[1] "rectangle"

\$Length

[1] 8

\$Width

[1] 4

```

\$Area
[1] 32
\$Message
[1] "Large area"
Result 3:
\$Shape
[1] "circle"
\$Length
[1] 6
\$Width
[1] 3
\$Area
[1] 28.27433
\$Message
[1] "Large area"

```

4. Write a R program for quick sort implementation, binary search tree

```

# Quick Sort Implementation
quick_sort <- function(arr) {
  if (length(arr) == 1) {
    return(arr)
  }
  pivot <- arr[1]
  smaller <- arr[arr < pivot]
  equal <- arr[arr == pivot]
  larger <- arr[arr > pivot]
  sorted_smaller <- quick_sort(smaller)
  sorted_larger <- quick_sort(larger)
  return(c(sorted_smaller, equal, sorted_larger))
}

# Binary Search Tree Implementation
insert_node <- function(root, key) {
  if (is.null(root)) {
    return(node(key = key, left = NULL, right = NULL))
  }
  if (key < root$key) {
    root$left <- insert_node(root$left, key)
  } else if (key > root$key) {
    root$right <- insert_node(root$right, key)
  }
}

```

```
$Area  
[1] 32  
$Message  
[1] "Large area"  
Result 3:  
$Shape  
[1] "circle"  
$Length  
[1] 6  
$Width  
[1] 3  
$Area  
[1] 28.27433  
$Message  
[1] "Large area"
```

4. Write a R program for quick sort implementation, binary search tree

```
# Quick Sort Implementation  
quick_sort <- function(arr) {  
  if (length(arr) <= 1) {  
    return(arr)  
  }  
  pivot <- arr[1]  
  smaller <- arr[arr < pivot]  
  equal <- arr[arr == pivot]  
  larger <- arr[arr > pivot]  
  sorted_smaller <- quick_sort(smaller)  
  sorted_larger <- quick_sort(larger)  
  return(c(sorted_smaller, equal, sorted_larger))  
}  
  
# Binary Search Tree Implementation  
insert_node <- function(root, key) {  
  if (is.null(root)) {  
    return(list(key = key, left = NULL, right = NULL))  
  }  
  if (key < root$key) {  
    root$left <- insert_node(root$left, key)  
  } else if (key > root$key) {
```

```

root$right <- insert_node(root$right, key)
}
return(root)
}
in_order_traversal <- function(root) {
  if (!is.null(root)) {
    in_order_traversal(root$left)
    cat(root$key, " ")
    in_order_traversal(root$right)
  }
}
# Example usage of Quick Sort
arr <- c(6, 2, 8, 3, 1, 7, 5)
sorted_arr <- quick_sort(arr)
cat("Quick Sort Result:", sorted_arr, "\n")
# Example usage of Binary Search Tree
bst_root <- NULL
keys <- c(6, 2, 8, 3, 1, 7, 5)
for (key in keys) {
  bst_root <- insert_node(bst_root, key)
}
cat("In-order Traversal of BST:")
in_order_traversal(bst_root)

```

Output

Quick Sort Result: 1 2 3 5 6 7 8

In-order Traversal of BST: 1 2 3 5 6 7 8

5. Write a R program for calculating cumulative sums, and products minima maxima calculus.

```

cum <- cumsum(numbers)
cat("Cumulative Sum:", cum, "\n")

```

```

# Sample dataset
data <- c(2, 4, 1, 8, 5, 7)

```

```

# Cumulative sums
csum <- cumsum(data)
cat("Cumulative Sums:", csum, "\n")

```

```
# Cumulative products
cproduct <- cumprod(data)
cat("Cumulative Products:", cproduct, "\n")

# Minimum and Maximum
minvalue <- min(data)
maxvalue <- max(data)
cat("Minimum Value:", minvalue, "\n")
cat("Maximum Value:", maxvalue, "\n")

# Calculus: Differentiation
differentiate <- diff(data)
cat("Differentiation (First Difference):", differentiate, "\n")

# Calculus: Integration
integrate <- cumsum(data)
cat("Integration (Cumulative Sum):", integrate, "\n")
```

Output

```
Cumulative Sum: 2 6 12 20 30
Cumulative Sums: 2 6 7 15 20 27
Cumulative Products: 2 8 8 64 320 2240
Minimum Value: 1
Maximum Value: 8
Differentiation (First Difference): 2 -3 7 -3 2
Integration (Cumulative Sum): 2 6 7 15 20 27
```

6. Write a R program for finding stationary distribution of markanov chains.

```
# Install and load the markovchain package
# install.packages("markovchain")
library(markovchain)

# Define the transition matrix for your Markov chain
tm <- matrix(c(
  0.7, 0.3,
  0.2, 0.8
), byrow = TRUE, nrow = 2, dimnames = list(c("State1", "State2"), c("State1", "State2")))
# Create a Markov chain object
markov_chain <- new("markovchain", states = c("State1", "State2"), transitionMatrix = tm)
# Find the stationary distribution
```

```
stationary_distribution <- steadyStates(markov_chain)
print("Stationary Distribution:")
print(stationary_distribution)
```

Output

```
"Stationary Distribution:"
  State1 State2
[1,] 0.4 0.6
```

7. Write a R program that include linear algebra operations on vectors and matrices

```
# Create vectors
vector1 <- c(1, 2, 3)
vector2 <- c(4, 5, 6)

# Create matrices
matrix1 <- matrix(c(1, 2, 3, 4, 5, 6), nrow = 2, ncol = 3)
matrix2 <- matrix(c(7, 8, 9, 10, 11, 12), nrow = 2, ncol = 3)

# Display vectors and matrices
cat("Vector 1:\n")
print(vector1)

cat("\nVector 2:\n")
print(vector2)

cat("\nMatrix 1:\n")
print(matrix1)

cat("\nMatrix 2:\n")
print(matrix2)

# Linear algebra operations
cat("\nLinear Algebra Operations:\n")

# Vector addition
vector_sum <- vector1 + vector2
cat("Vector Addition (vector1 + vector2):\n")
print(vector_sum)
```

```
# Vector subtraction
```

```
vector_diff <- vector1 - vector2
```

```
cat("Vector Subtraction (vector1 - vector2):\n")
```

```
print(vector_diff)
```

```
# Scalar multiplication
```

```
scalar <- 2
```

```
vector_scalar_mult <- scalar * vector1
```

```
cat("Scalar Multiplication (scalar * vector1):\n")
```

```
print(vector_scalar_mult)
```

```
# Matrix addition
```

```
matrix_sum <- matrix1 + matrix2
```

```
cat("Matrix Addition (matrix1 + matrix2):\n")
```

```
print(matrix_sum)
```

```
# Matrix subtraction
```

```
matrix_diff <- matrix1 - matrix2
```

```
cat("Matrix Subtraction (matrix1 - matrix2):\n")
```

```
print(matrix_diff)
```

```
# Matrix multiplication
```

```
matrix_product <- matrix1 %*% t(matrix2) # Matrix multiplication with transpose of matrix2
```

```
cat("Matrix Multiplication (matrix1 * matrix2):\n")
```

```
print(matrix_product)
```

```
# Matrix transpose
```

```
matrix1_transpose <- t(matrix1)
```

```
cat("Matrix Transpose (transpose of matrix1):\n")
```

```
print(matrix1_transpose)
```

Output

```
Vector 1:
```

```
[1] 1 2 3
```

```
Vector 2:
```

```
[1] 4 5 6
```

```
Matrix 1:
```

```
[.1] [,2] [,3]
```

```
[1] 1 3 5
[2] 2 4 6
```

Matrix 2:

```
[,1] [,2] [,3]
[1,] 7 9 11
[2,] 8 10 12
```

Linear Algebra Operations:

Vector Addition (vector1 + vector2):

```
[1] 5 7 9
```

Vector Subtraction (vector1 - vector2):

```
[1] -3 -3 -3
```

Scalar Multiplication (scalar * vector1):

```
[1] 2 4 6
```

Matrix Addition (matrix1 + matrix2):

```
[,1] [,2] [,3]
[1,] 8 12 16
[2,] 10 14 18
```

Matrix Subtraction (matrix1 - matrix2):

```
[,1] [,2] [,3]
[1,] -6 -6 -6
[2,] -6 -6 -6
```

Matrix Multiplication (matrix1 * matrix2):

```
[,1] [,2]
[1,] 89 98
[2,] 116 128
```

Matrix Transpose (transpose of matrix1):

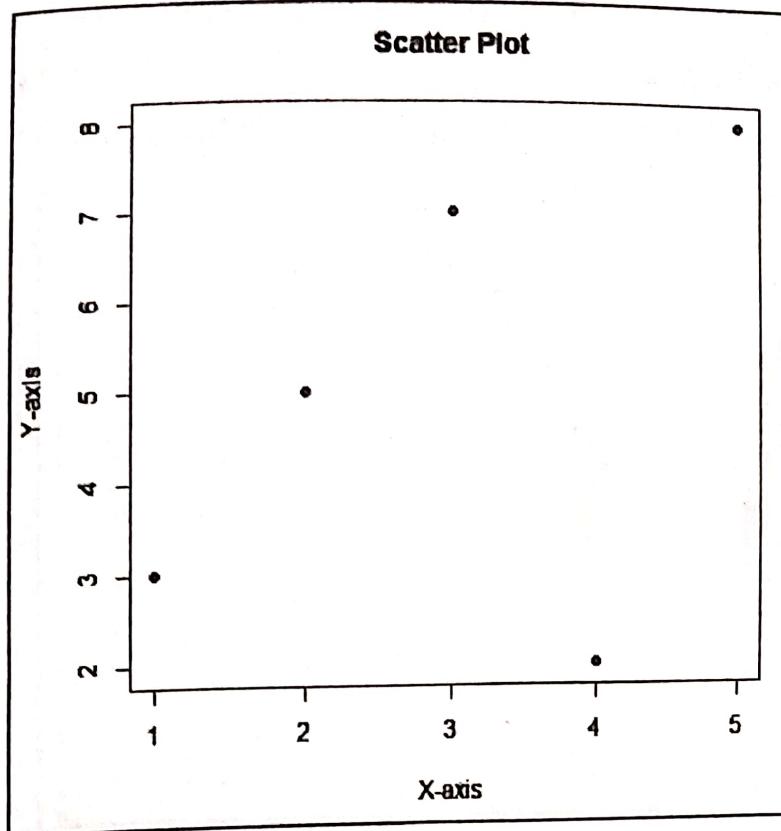
```
[,1] [,2]
[1,] 1 2
[2,] 3 4
[3,] 5 6
```

8. Write a R program for any visual representation of an object with creating graphs using graphic functions: Plot(),Hist(),Linechart(),Pie(),Boxplot(),Scatterplots().

Scatterplots()

```
x <- c(1, 2, 3, 4, 5)
y <- c(3, 5, 7, 2, 8)
```

```
plot(x, y, main = "Scatter Plot", xlab = "X-axis", ylab = "Y-axis", pch = 19, col = "blue")
```

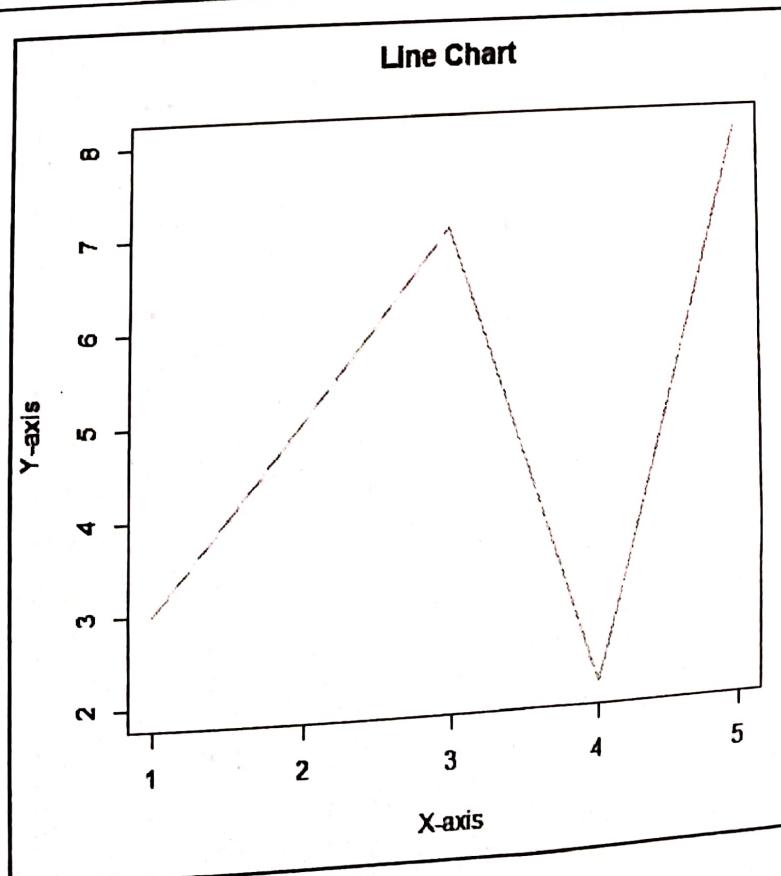


Linechart()

```
x <- c(1, 2, 3, 4, 5)
```

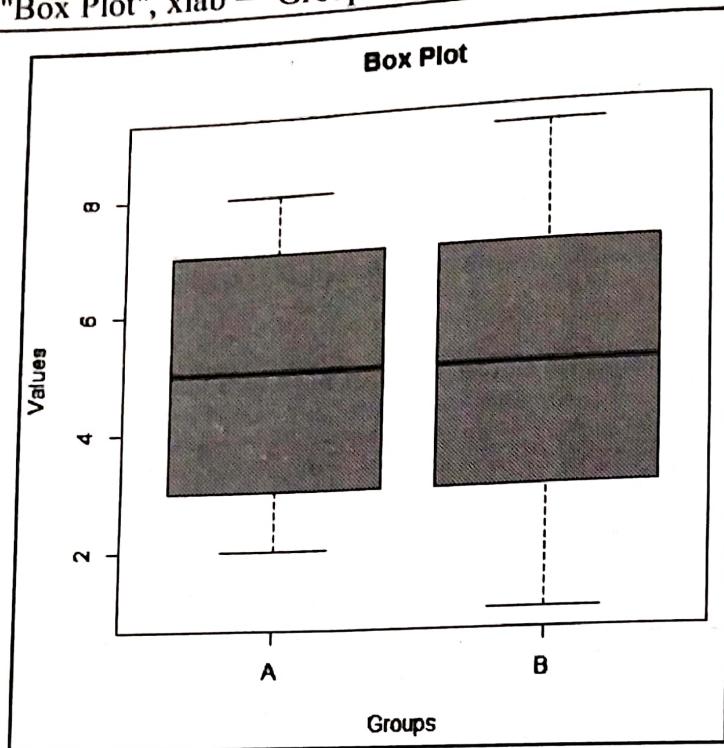
```
y <- c(3, 5, 7, 2, 8)
```

```
plot(x, y, type = "l", main = "Line Chart", xlab = "X-axis", ylab = "Y-axis", col = "green")
```

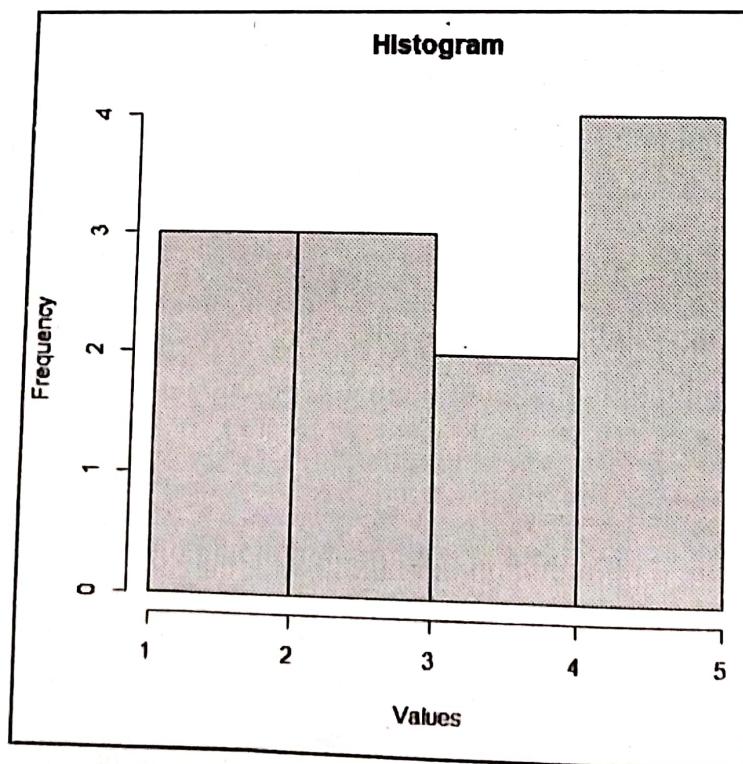


Boxplot()

```
data <- list(A = c(2, 4, 6, 8), B = c(1, 3, 5, 7, 9))
boxplot(data, main = "Box Plot", xlab = "Groups", ylab = "Values", col = "orange")
```

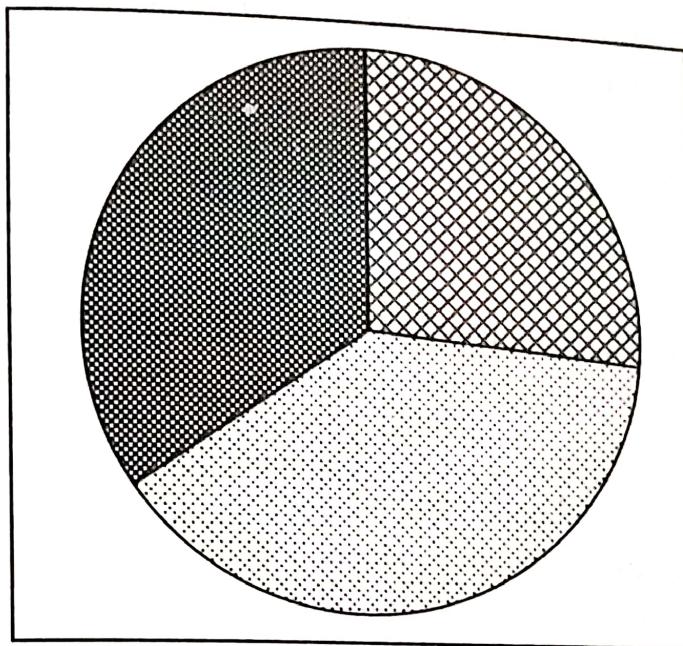
**Hist()**

```
data <- c(1, 2, 2, 3, 3, 3, 4, 4, 5, 5, 5, 5)
hist(data, main = "Histogram", xlab = "Values", ylab = "Frequency", col = "lightblue")
```



```
pie()
categories <- c("A", "B", "C")
values <- c(30, 40, 20)
pie(values, labels = categories, main = "Pie Chart", col = c("red", "green", "blue"))
```

Pie Chart



9. Write a R program for with any dataset containing dataframe objects, indexing and subsetting data frames, and employ manipulating and analyzing data.

```
# Create a sample employee dataset as a data frame
employee_data <- data.frame(
  EmployeeID = c(1, 2, 3, 4, 5),
  FirstName = c("John", "Alice", "Bob", "Carol", "David"),
  LastName = c("Smith", "Johnson", "Johnson", "Smith", "Davis"),
  Age = c(30, 25, 28, 35, 32),
  Department = c("HR", "Marketing", "Finance", "HR", "IT"),
  Salary = c(50000, 55000, 60000, 52000, 70000)
)

# Print the entire employee dataset
cat("Employee Data:\n")
print(employee_data)

# Subset and index the data frame
cat("\nSubset and Indexing:\n")
# Select employees in the HR department
hr_employees <- employee_data[employee_data$Department == "HR", ]
cat("HR Employees:\n")
print(hr_employees)
```

```

# Select employees aged 30 or older
older_employees <- employee_data[employee_data$Age >= 30, ]
cat("Employees Aged 30 or Older:\n")
print(older_employees)

# Select employees with a salary greater than $55,000
high_salary_employees <- employee_data[employee_data$Salary > 55000, ]
cat("Employees with High Salary:\n")
print(high_salary_employees)

# Manipulate and analyze the data
cat("\nData Manipulation and Analysis:\n")

# Calculate the average salary
average_salary <- mean(employee_data$Salary)
cat("Average Salary:", average_salary, "\n")

# Calculate the maximum age
max_age <- max(employee_data$Age)
cat("Maximum Age:", max_age, "\n")

# Calculate the number of employees in each department
department_counts <- table(employee_data$Department)
cat("Number of Employees in Each Department:\n")
print(department_counts)

# Calculate the total payroll for each department
department_payroll <- tapply(employee_data$Salary, employee_data$Department, sum)
cat("Total Payroll in Each Department:\n")
print(department_payroll)

```

Output:**Employee Data:**

	EmployeeID	FirstName	LastName	Age	Department	Salary
1	1	John	Smith	30	HR	50000
2	2	Alice	Johnson	25	Marketing	55000
3	3	Bob	Johnson	28	Finance	60000
4	4	Carol	Smith	35	HR	52000
5	5	David	Davis	32	IT	70000

Subset and Indexing:

HR Employees:

	EmployeeID	FirstName	LastName	Age	Department	Salary
1	1	John	Smith	30	HR	50000
4	4	Carol	Smith	35	HR	52000

Employees Aged 30 or Older:

	EmployeeID	FirstName	LastName	Age	Department	Salary
1	1	John	Smith	30	HR	50000
4	4	Carol	Smith	35	HR	52000
5	5	David	Davis	32	IT	70000

Employees with High Salary:

	EmployeeID	FirstName	LastName	Age	Department	Salary
3	3	Bob	Johnson	28	Finance	60000
5	5	David	Davis	32	IT	70000

Data Manipulation and Analysis:

Average Salary: 57400

Maximum Age: 35

Number of Employees in Each Department:

Finance	HR	IT	Marketing
1	2	1	1

Total Payroll in Each Department:

Finance	HR	IT	Marketing
60000	102000	70000	55000

10. Write a program to create an any application of Linear Regression in a multivariate context for predictive purpose

```
# Sample dataset: Salary, Years of Experience, Education Level
```

```
data <- data.frame(
```

```
Salary = c(50000, 60000, 75000, 80000, 95000, 110000, 120000, 130000),
```

```
Experience = c(1, 2, 3, 4, 5, 6, 7, 8),
```

```
Education = c(12, 14, 16, 16, 18, 20, 20, 22)
```

```
# Perform multivariate linear regression
```

```
model <- lm(Salary ~ Experience + Education, data = data)
```

```
model
```

```
# Predict salaries for new data
```

```

new_data <- data.frame(
  Experience = c(9, 10),
  Education = c(22, 24)
)
predicted_salaries <- predict(model, newdata = new_data)
# Print the predicted salaries
cat("Predicted Salaries:\n")
print(predicted_salaries)

```

Output:**Call:**

```
lm(formula = Salary ~ Experience + Education, data = data)
```

Coefficients:

(Intercept)	Experience	Education
11500	8500	2333

Predicted Salaries:

1	2
139333.3	152500.0

Part B**1. Write a Program to calculate the factorial of a number:**

```

# Function to calculate the factorial of a number
factorial <- function(n) {
  if (n == 0) {
    return(1) # The factorial of 0 is defined as 1
  } else {
    return(n * factorial(n - 1))
  }
}

```

Test the factorial function

```

result <- factorial(5) # Calculate 5!
cat("Factorial of 5 is:", result, "\n")

```

Output

Factorial of 5 is: 120

2. Program to find the sum of 2 number using function.

Defining a simple function in R

```
sum_function <- function(a, b) {
```

```
  result <- a + b # Compute the sum of the two arguments
```

```
  return(result) # Return the result
```

```
}
```

Using the function with sample arguments

```
x <- 3
```

```
y <- 4
```

```
z <- sum_function(x, y)
```

```
print(z)
```

Output

```
[1] 7
```

3. Write a program that demonstrates the use of lists:

Creating a list

```
my_list <- list(name = "John Doe",
```

```
                age = 30,
```

```
                is_student = TRUE,
```

```
                grades = c(85, 90, 95, 87, 92))
```

Printing the list

```
print(my_list)
```

Accessing elements in the list

```
print(paste("Name:", my_list$name))
```

```
print(paste("Age:", my_list$age))
```

```
print(paste("Is Student:", my_list$is_student))
```

```
print(paste("Grades:", my_list$grades))
```

Modifying elements in the list

```
my_list$name <- "Jane Doe"
```

```
my_list$age <- 25
```

```
my_list$is_student <- FALSE
```

```
my_list$grades <- c(75, 80, 85, 77, 82)
```

Printing the modified list

```
print(my_list)
```

Output

```
$name
[1] "Jane Doe"
$age
[1] 25
$is_student
[1] FALSE
$grades
[1] 75 80 85 77 82
```

4. Program to calculate the area of a triangle

```
triangle_area <- function(base, height) {
  area <- 0.5 * base * height
  return(area)
}

# Example usage of the function
base_length <- 6
height_length <- 8
area <- triangle_area(base_length, height_length)
cat("The area of the triangle is:", area, "\n")
```

Output

The area of the triangle is: 24

5. program to swap the values of two variable.

```
# Function to swap two numbers
swap_numbers <- function(a, b) {
  temp <- a
  a <- b
  b <- temp
  return(list(a = a, b = b))
}

# Example usage of the function
num1 <- 5
num2 <- 10
Cat ("Before swapping: num1 =", num1, "and num2 =", num2, "\n")
# Call the function to swap the numbers
result <- swap_numbers(num1, num2)
cat("After swapping: num1 =", result$a, "and num2 =", result$b, "\n")
```

Output

Before swapping: num1 = 5 and num2 = 10

After swapping: num1 = 10 and num2 = 5

6. Write a Program to perform basic matrix operations such as addition, subtraction, multiplication, and transpose.

Create matrices

```
matrix1 <- matrix(c(1, 2, 3, 4), nrow = 2, ncol = 2, byrow = TRUE)  
matrix2 <- matrix(c(5, 6, 7, 8), nrow = 2, ncol = 2, byrow = TRUE)
```

Print the matrices

```
cat("Matrix 1:\n")
```

```
print(matrix1)
```

```
cat("\nMatrix 2:\n")
```

```
print(matrix2)
```

Addition of matrices

```
addition_result <- matrix1 + matrix2
```

```
cat("\nAddition Result:\n")
```

```
print(addition_result)
```

Subtraction of matrices

```
subtraction_result <- matrix1 - matrix2
```

```
cat("\nSubtraction Result:\n")
```

```
print(subtraction_result)
```

Multiplication of matrices

```
multiplication_result <- matrix1 %*% matrix2
```

```
cat("\nMultiplication Result:\n")
```

```
print(multiplication_result)
```

Transpose of matrices

```
transpose_matrix1 <- t(matrix1)
```

```
transpose_matrix2 <- t(matrix2)
```

```
cat("\nTranspose of Matrix 1:\n")
```

```
print(transpose_matrix1)
```

```
cat("\nTranspose of Matrix 2:\n")
```

```
print(transpose_matrix2)
```

Output

Addition Result:

[,1]	[,2]
[1,]	6 8

[2,] 10 12

Subtraction Result:

[,1] [,2]

[1,] -4 -4

[2,] -4 -4

Multiplication Result:

[,1] [,2]

[1,] 19 22

[2,] 43 50

Transpose of Matrix 1:

[,1] [,2]

[1,] 1 3

[2,] 2 4

Transpose of Matrix 2:

[,1] [,2]

[1,] 5 7

[2,] 6 8

7. Program to demonstrate creating, modifying, and accessing data in data frames

```
# Creating a dataframe
data <- data.frame(
  Name = c("John", "Doe", "Jane", "Smith"),
  Age = c(25, 30, 28, 35),
  Salary = c(50000, 60000, 55000, 70000)
)
# Printing the dataframe
cat("Initial Dataframe:\n")
print(data)

# Adding a new column
data$Department <- c("HR", "Finance", "IT", "Marketing")
# Printing the updated dataframe
cat("\nDataframe with New Column:\n")
print(data)

# Modifying a value in the dataframe
data[3, "Salary"] <- 60000
# Printing the dataframe after modification
cat("\nDataframe after Modification:\n")
```

```
print(data)
# Accessing specific elements
cat("\nAccessing Specific Elements:\n")
cat("Second row, second column: ", data[2, 2], "\n")
cat("Name column: ", data$Name, "\n")
# Filtering data
cat("\nFiltered Dataframe (Age > 25):\n")
filtered_data <- data[data$Age > 25, ]
print(filtered_data)
```

Output

Dataframe with New Column:

	Name	Age	Salary	Department
1	John	25	50000	HR
2	Doe	30	60000	Finance
3	Jane	28	55000	IT
4	Smith	35	70000	Marketing

Dataframe after Modification:

	Name	Age	Salary	Department
1	John	25	50000	HR
2	Doe	30	60000	Finance
3	Jane	28	60000	IT
4	Smith	35	70000	Marketing

Accessing Specific Elements:

Second row, second column: 30

Name column: John Doe Jane Smith

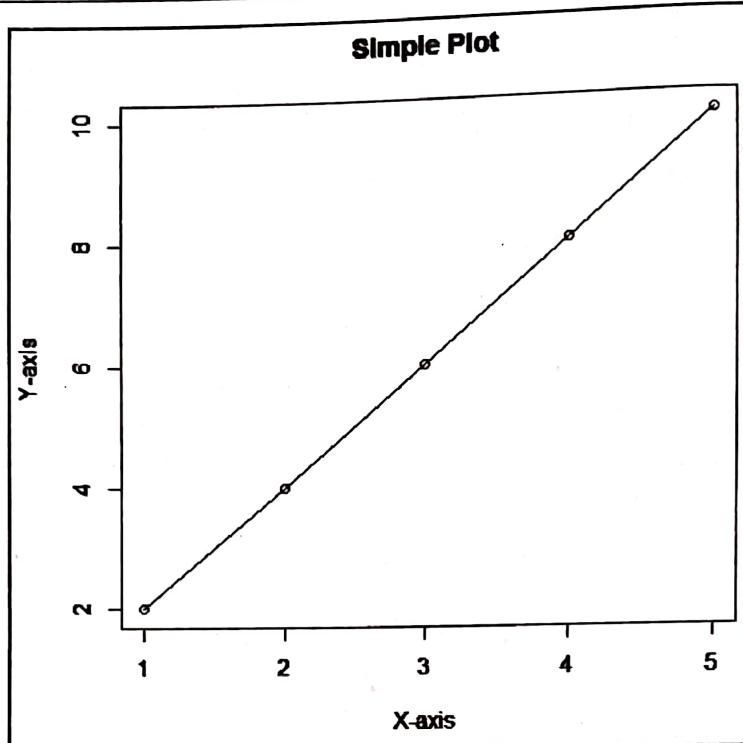
Filtered Dataframe (Age > 25)

	Name	Age	Salary	Department
2	Doe	30	60000	Finance
3	Jane	28	60000	IT
4	Smith	35	70000	Marketing

8. Program to generate a basic plot in R

```
# Creating data for the plot
x <- c(1, 2, 3, 4, 5)
y <- c(2, 4, 6, 8, 10)
# Plotting the data
plot(x, y, type = "o", col = "blue", xlab = "X-axis", ylab = "Y-axis", main = "Simple Plot")
```

```
# Adding points to the plot
points(x, y, col = "red")
# Adding a line to the plot
abline(lm(y ~ x), col = "green")
```



9. program to calculate the sum of the first 10 natural numbers

```
# Initializing sum variable
sum_result <- 0
# Using a for loop to calculate the sum of the first 10 natural numbers
for (i in 1:10) {
  sum_result <- sum_result + i
}
# Printing the result
cat("Sum of the first 10 natural numbers is:", sum_result)
```

Output

Sum of the first 10 natural numbers is: 55

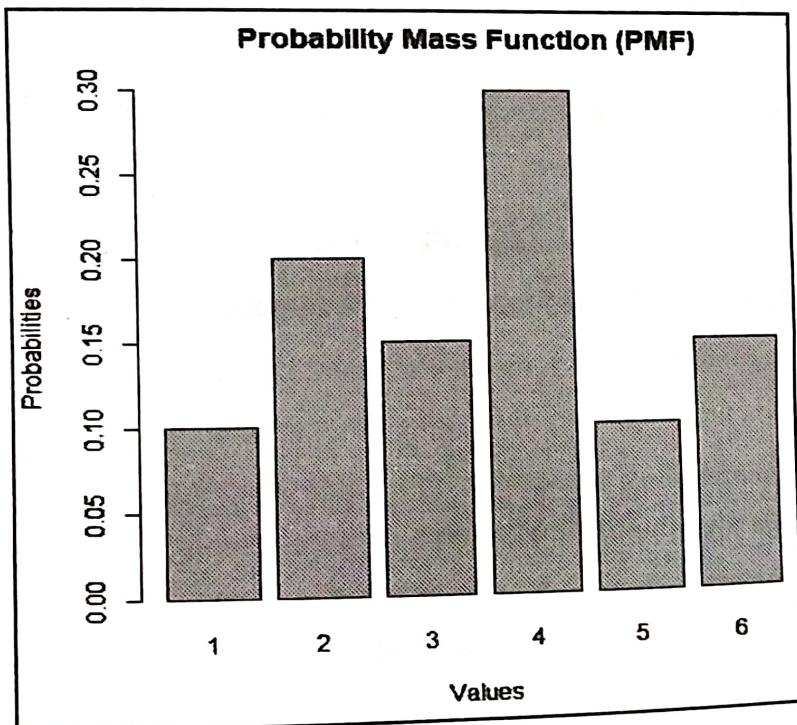
10. Program to find the mean, variance, and plot bar chart

```
# Define the probabilities for each value
pmf <- c(0.1, 0.2, 0.15, 0.3, 0.1, 0.15) # Example probabilities for values 1 to 6
# Set the corresponding values
values <- 1:6
# Print the PMF
print(pmf)
```

```
# Print the values  
print(values)  
# Calculate the mean  
mean_value <- sum(pmf * values)  
print(paste("Mean:", mean_value))  
# Calculate the variance  
var_value <- sum(pmf * (values - mean_value)^2)  
print(paste("Variance:", var_value))  
# Plot the PMF  
barplot(pmf, names.arg = values, xlab = "Values", ylab = "Probabilities", main = "Probability Mass Function (PMF)")
```

Output

```
[1] "Mean: 3.55"  
[1] "Variance: 2.3475"
```



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