# Astral permutations



Winter Workshops, Day 5. Memory limit: 512 MB.

08.01.2020

This time we get to help little Damian to pursue his passions – astronomy and big numbers. Damian has spotted n planets on the night sky. Astral trajectory of planet i can be described by number  $a_i$ . Our little boy will observe the sky for n days, each planet will be observed exactly once, and each day exactly one planet will be observe. Damian knows that observing planet i on day j would reward him with  $(a_i)^j \pmod{10^9+9}$  points of joy. Help your friend and select a permutation of planets to observer each day in order to maximize his joy.

#### **Conditions**

- $1 \le n \le 20$
- $1 \le a_i < 10^9 + 9$

### Input

n	
$a_1,, a_n$	

### Output

The first line of output should contain the maximum joy he can achieve.

## Scoring

Subtask	Constraints	Points
1	n < 10	40
2	no additional constraints	60

## Example

Input	Output
5	8476
2 3 4 5 6	
3	2349922315
917234537 118245325 642336341	
6	126
6	126
2 2 2 2 2 2	

Astral permutations