

Material & Appearance

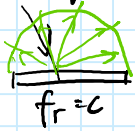
2021年9月12日

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The appearance of Natural Materials

1. Diffuse / Lambertian Material

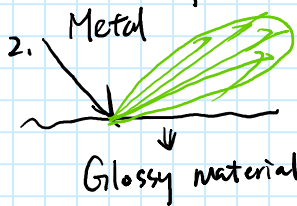
Light is equally reflected in each direction.



$$\begin{aligned} L_o(w_o) &= \int_{H^2} f_r L_i(w_i) \cos \theta_i dw_i \\ &= f_r L_i \int_{H^2} \cos \theta_i dw_i \\ &= \pi f_r L_i \end{aligned}$$

$$\therefore f_r \triangleq \frac{\rho}{\pi} \quad \rho: \text{albedo (color)}$$

for white objects, $\rho = 1$



3. Glass/Water



4. Perfect Specular Reflection BRDF

5. Specular Refraction.

"costics"

Diamond = $n = 2.42$ especially high. thus. looks special



$$n_i \sin \theta_i = n_t \sin \theta_t$$

$$\cos \theta_t = \sqrt{1 - \sin^2 \theta_t}$$

$$= \sqrt{1 - \left(\frac{n_i}{n_t}\right)^2 (1 - \cos^2 \theta_i)}$$

会发生全反射. 在 path tracing 时要注意

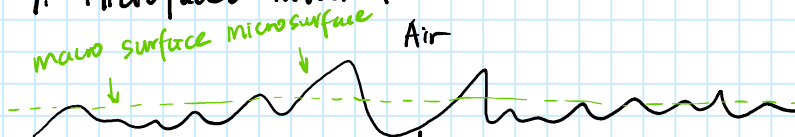
b. Fresnel Term

Schlick's approximation

$$R(\theta) = R_0 + (1 - R_0)(1 - \cos \theta)^5$$

$$R_0 = \left(\frac{n_1 - n_2}{n_1 + n_2}\right)^2$$

7. Microfacet material



Macro scale: flat & rough

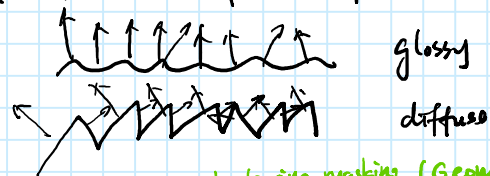
Micro scale: bumpy & specular

Microfacet BRDF

Key: distribution of microfacets' normals

↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑

Key: distribution of microfacets' normals



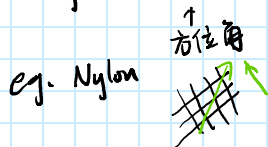
$$f(r, o) = \frac{\overset{\text{Fresnel}}{F(i, o, h)} \overset{\text{shadowing-masking (Geometry term)}}{G(i, o, h)} \overset{\text{distribution of normals}}{D(h)}}{4(n \cdot r)(n \cdot o)}$$

8. Isotropic / Anisotropic 各向同性 / 异性

"V-Ray renderer"

Anisotropic BRDF

$$f_r(\theta_i, \phi_i; \theta_r, \phi_r) \neq f_r(\theta_r, \theta_i, \phi_r - \phi_i)$$



9. Properties of BRDF

- Non-negative
- Linearity
- Reciprocity principle

$$f_r(w_r \rightarrow w_i) = f_r(w_i \rightarrow w_r)$$
- Energy conservation

$$\forall w_r \int_{H^2} f_r(w_i \rightarrow w_r) \cos \theta_i dw_i \leq 1$$

10. Measuring BRDF

MERL BRDF Database.
 $90^\circ \times 90^\circ \times 180^\circ$ measurement