# Programming Languages ML Modules

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#### Sections in Textbook

Section 8 in Elements of ML Programming

 Chapter 9 in pdf (Programming in Standard ML '97: A Tutorial Introduction)

#### Modules

For larger programs, one "top-level" sequence of bindings is poor

 Especially because a binding can use all earlier (nonshadowed) bindings

So ML has structures to define modules

```
structure MyModule = struct bindings end
```

Inside a module, can use earlier bindings as usual

Can have any kind of binding (val, datatype, exception, ...)

Outside a module, refer to earlier modules' bindings via ModuleName.bindingName

 Just like List.foldl and String.toUpper; now you can define your own modules

#### Example

```
structure MyMathLib =
struct
fun fact x =
    if x=0
    then 1
    else x * fact(x-1)
val half_pi = Math.pi / 2
fun doubler x = x * 2
end
```

#### Namespace management

- So far, this is just namespace management
  - Giving a hierarchy to names to avoid shadowing
  - Allows different modules to reuse names, e.g., map
  - Very important, but not very interesting

# Signatures

- A signature is a type for a module
  - What bindings does it have and what are their types
- Can define a signature and ascribe it to modules example:

```
signature MATHLIB =
siq
val fact : int -> int
val half_pi : real
val doubler : int -> int
end
structure MyMathLib :> MATHLIB =
struct
fun fact x = ...
val half_pi = Math.pi / 2.0
fun doubler x = x * 2
end
```

#### In general

Signatures

```
signature SIGNAME =
sig types-for-bindings end
```

- Can include variables, types, datatypes, and exceptions defined in module
- Ascribing a signature to a module

```
structure MyModule :> SIGNAME =
struct bindings end
```

 Module will not type-check unless it matches the signature, meaning it has all the bindings at the right types

# Hiding things

Real value of signatures is to to hide bindings and type definitions

So far, just documenting and checking the types

Hiding implementation details is the most important strategy for writing correct, robust, reusable software

So first remind ourselves that functions already do well for some forms of hiding...

# Hiding with functions

These three functions are totally equivalent: no client can tell which we are using (so we can change our choice later):

```
fun double x = x*2
fun double x = x+x
val y = 2
fun double x = x*y
```

Defining helper functions locally is also powerful

 Can change/remove functions later and know it affects no other code

Would be convenient to have "private" top-level functions too

- So two functions could easily share a helper function
- ML does this via signatures that omit bindings...

#### Example

Outside the module, MyMathLib.doubler is simply unbound

- So cannot be used [directly]
- Fairly powerful, very simple idea

```
signature MATHLIB =
sig
val fact : int -> int
val half pi : real
end
structure MyMathLib :> MATHLIB =
struct
fun fact x = ...
val half pi = Math.pi / 2.0
fun doubler x = x * 2
end
```

## A larger example [mostly see the code]

Now consider a module that defines an Abstract Data Type (ADT)

A type of data and operations on it

Our example: rational numbers supporting add and toString

```
structure Rational1 =
struct
datatype rational = Whole of int | Frac of int*int
exception BadFrac

(*internal functions gcd and reduce not on slide*)

fun make_frac (x,y) = ...
fun add (r1,r2) = ...
fun toString r = ...
end
```

#### Library spec and invariants

Properties [externally visible guarantees, up to library writer]

- Disallow denominators of 0
- Return strings in reduced form ("4" not "4/1", "3/2" not "9/6")
- No infinite loops or exceptions

Invariants [part of the implementation, not the module's spec]

- All denominators are greater than 0
- All rational values returned from functions are reduced

#### More on invariants

Our code maintains the invariants and relies on them

#### Maintain:

- make\_frac disallows 0 denominator, removes negative denominator (divisor), and reduces result
- add assumes invariants on inputs, calls reduce if needed

#### Rely:

- gcd does not work with negative arguments, but no denominator can be negative
- add uses math properties to avoid calling reduce
- toString assumes its argument is already reduced

## A first signature

With what we know so far, this signature makes sense:

gcd and reduce not visible outside the module

```
signature RATIONAL_A =
sig
datatype rational = Whole of int | Frac of int*int
exception BadFrac
val make_frac : int * int -> rational
val add : rational * rational -> rational
val toString : rational -> string
end
structure Rational1 :> RATIONAL_A = ...
```

#### The problem

By revealing the datatype definition, we let clients violate our invariants by directly creating values of type Rational1.rational

At best a comment saying "must use Rational1.make\_frac"

```
signature RATIONAL_A =
sig
datatype rational = Whole of int | Frac of int*int
...
```

Any of these would lead to exceptions, infinite loops, or wrong results, which is why the module's code would never return them

- Rational1.Frac(1,0)
- Rational1.Frac(3,~2)
- Rational1.Frac(9,6)

#### So hide more

Key idea: An ADT must hide the concrete type definition so clients cannot create invariant-violating values of the type directly

Alas, this attempt doesn't work because the signature now uses a type rational that is not known to exist:

```
signature RATIONAL_WRONG =
sig
exception BadFrac
val make_frac : int * int -> rational
val add : rational * rational -> rational
val toString : rational -> string
end
structure Rational1 :> RATIONAL_WRONG = ...
```

## Abstract types

So ML has a feature for exactly this situation:

In a signature:

#### type foo

means the type exists, but clients do not know its definition

```
signature RATIONAL_B =
sig
type rational
exception BadFrac
val make_frac : int * int -> rational
val add : rational * rational -> rational
val toString : rational -> string
end
structure Rational1 :> RATIONAL_B = ...
```

# This works! (And is a Really Big Deal)

```
signature RATIONAL_B =
sig
type rational
exception BadFrac
val make_frac : int * int -> rational
val add : rational * rational -> rational
val toString : rational -> string
end
```

Nothing a client can do to violate invariants and properties:

- Only way to make first rational is Rational1.make\_frac
- After that can use only Rational1.make\_frac,
   Rational1.add, and Rational1.toString
- Hides constructors and patterns don't even know whether or not Rational1.rational is a datatype
- But clients can still pass around fractions in any way

# Two key restrictions

So we have two powerful ways to use signatures for hiding:

- 1. Deny bindings exist (val-bindings, fun-bindings, constructors)
- 2. Make types abstract (so clients cannot create values of them or access their pieces directly)

(Later we will see a signature can also make a binding's type more specific than it is within the module, but this is less important)

#### A cute twist

In our example, exposing the Whole constructor is no problem

In SML we can expose it as a function since the datatype binding in the module does create such a function

- Still hiding the rest of the datatype
- Still does not allow using Whole as a pattern

```
signature RATIONAL_C =
sig
type rational
exception BadFrac
val Whole : int -> rational
val make_frac : int * int -> rational
val add : rational * rational -> rational
val toString : rational -> string
end
```

# Signature matching

Have so far relied on an informal notion of, "does a module type-check given a signature?" As usual, there are precise rules...

#### structure Foo :> BAR is allowed if:

- Every non-abstract type in BAR is provided in Foo, as specified
- Every abstract type in BAR is provided in Foo in some way
  - Can be a datatype or a type synonym
- Every val-binding in BAR is provided in Foo, possibly with a more general and/or less abstract internal type
  - Discussed "more general types" earlier in course
  - Will see example soon
- Every exception in BAR is provided in Foo

Of course Foo can have more bindings (implicit in above rules)

## Equivalent implementations

A key purpose of abstraction is to allow *different implementations* to be *equivalent* 

- No client can tell which you are using
- So can improve/replace/choose implementations later
- Easier to do if you start with more abstract signatures (reveal only what you must)

#### Now:

Another structure that can also have signature **RATIONAL\_A**, **RATIONAL B**, or **RATIONAL C** 

 But only equivalent under RATIONAL\_B or RATIONAL\_C (ignoring overflow)

#### Next:

A third equivalent structure implemented very differently

#### Equivalent implementations

#### Example (see code file):

- structure Rational2 does not keep rationals in reduced form, instead reducing them "at last moment" in toString
  - Also make gcd and reduce local functions
- Not equivalent under RATIONAL\_A
  - Rational1.toString(Rational1.Frac(9,6)) = "9/6"
  - Rational2.toString(Rational2.Frac(9,6)) = "3/2"
- Equivalent under RATIONAL\_B or RATIONAL\_C
  - Different invariants, but same properties
  - Essential that type rational is abstract

## More interesting example

Given a signature with an abstract type, different structures can:

- Have that signature
- But implement the abstract type differently

Such structures might or might not be equivalent

Example (see code):

- type rational = int \* int
- Does not have signature RATIONAL\_A
- Equivalent to both previous examples under RATIONAL\_B or RATIONAL C

#### More interesting example

```
structure Rational3 =
struct
type rational = int * int
exception BadFrac

fun make_frac (x,y) = ...
fun Whole i = (i,1) (* needed for RATIONAL_C *)
fun add ((a,b)(c,d)) = (a*d+b*c,b*d)
fun toString r = ... (* reduce at last minute *)
end
```

## Some interesting details

- Internally make\_frac has type int \* int -> int \* int,
   but externally int \* int -> rational
  - Client cannot tell if we return argument unchanged
  - Could give type rational -> rational in signature, but this is awful: makes entire module unusable – why?
- Internally Whole has type 'a -> 'a \* int but externally int -> rational
  - This matches because we can specialize 'a to int and then abstract int \* int to rational
  - Whole cannot have types 'a -> int \* int
    or 'a -> rational (must specialize all 'a uses)
  - Type-checker figures all this out for us

#### Can't mix-and-match module bindings

Modules with the same signatures still define different types

So things like this do not type-check:

- Rational1.toString(Rational2.make\_frac(9,6))
- Rational3.toString(Rational2.make\_frac(9,6))

This is a crucial feature for type system and module properties:

- Different modules have different internal invariants!
- In fact, they have different type definitions
  - Rational1.rational looks like Rational2.rational, but clients and the type-checker do not know that
  - Rational3.rational is int\*int not a datatype!