Programming Languages Thunks, Laziness, Streams, Memoization

Jiwon Seo

Delayed evaluation

For each language construct, the semantics specifies when subexpressions get evaluated. In ML, Racket, Java, C:

- Function arguments are eager (call-by-value)
 - Evaluated once before calling the function
- Conditional branches are not eager

It matters: calling factorial-bad never terminates:

Thunks delay

We know how to delay evaluation: put expression in a function!

Thanks to closures, can use all the same variables later

A zero-argument function used to delay evaluation is called a *thunk*

As a verb: thunk the expression (also freeze and thaw)

This works (but it is silly to wrap **if** like this):

The key point

Evaluate an expression e to get a result:

е

- A function that when called, evaluates e and returns result
 - Zero-argument function for "thunking"

```
(lambda () e)
```

Evaluate e to some thunk and then call the thunk

- Next: Powerful idioms related to delaying evaluation and/or avoided repeated or unnecessary computations
 - Some idioms also use mutation in encapsulated ways

Avoiding expensive computations

Thunks let you skip expensive computations if they are not needed

Great if take the true-branch:

```
(define (f th)
(if (...) 0 (... (th) ...)))
```

But worse if you end up using the thunk more than once:

```
(define (f th)
  (... (if (...) 0 (... (th) ...))
      (if (...) 0 (... (th) ...))
      ...
      (if (...) 0 (... (th) ...)))
```

In general, might not know many times a result is needed

Best of both worlds

Assuming some expensive computation has no side effects, ideally we would:

- Not compute it until needed
- Remember the answer so future uses complete immediately
 Called lazy evaluation

Languages where most constructs, including function arguments, work this way are *lazy languages*

Haskell

Racket predefines support for *promises*, but we can make our own

Thunks and mutable pairs are enough

Delay and force

An ADT represented by a mutable pair

- **#f** in *car* means *cdr* is unevaluated thunk
 - Really a one-of type: thunk or result-of-thunk
- Ideally hide representation in a module

Using promises

```
(define (f p)
  (... (if (...) 0 (... (my-force p) ...))
        (if (...) 0 (... (my-force p) ...))
        ...
        (if (...) 0 (... (my-force p) ...))))
```

```
(f (my-delay (lambda () e)))
```

Lessons From Example

See code file for example that does multiplication using a very slow addition helper function

- With thunking second argument:
 - Great if first argument 0
 - Okay if first argument 1
 - Worse otherwise
- With precomputing second argument:
 - Okay in all cases
- With thunk that uses a promise for second argument:
 - Great if first argument 0
 - Okay otherwise

Streams

- A stream is an *infinite sequence* of values
 - So cannot make a stream by making all the values
 - Key idea: Use a thunk to delay creating most of the sequence
 - Just a programming idiom

A powerful concept for division of labor:

- Stream producer knows how create any number of values
- Stream consumer decides how many values to ask for

Some examples of streams you might (not) be familiar with:

- User actions (mouse clicks, etc.)
- UNIX pipes: cmd1 | cmd2 has cmd2 "pull" data from cmd1
- Output values from a sequential feedback circuit

Using streams

We will represent streams using pairs and thunks

Let a stream be a thunk that when called returns a pair:

```
'(next-answer . next-thunk)
```

So given a stream s, the client can get any number of elements

- First: (car (s))
- Second: (car ((cdr (s))))
- Third: (car ((cdr ((s))))))

(Usually bind (cdr (s)) to a variable or pass to a recursive function)

Example using streams

This function returns how many stream elements it takes to find one for which tester does not return #f

Happens to be written with a tail-recursive helper function

- (stream) generates the pair
- So recursively pass (cdr pr), the thunk for the rest of the infinite sequence

Streams

Coding up a stream in your program is easy

We will do functional streams using pairs and thunks

Let a stream be a thunk that when called returns a pair:

```
'(next-answer . next-thunk)
```

Saw how to use them, now how to make them...

Admittedly mind-bending, but uses what we know

Making streams

- How can one thunk create the right next thunk? Recursion!
 - Make a thunk that produces a pair where cdr is next thunk
 - A recursive function can return a thunk where recursive call does not happen until thunk is called

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Getting it wrong

This uses a variable before it is defined

```
(define ones-really-bad (cons 1 ones-really-bad))
```

This goes into an infinite loop making an infinite-length list

```
(define ones-bad (lambda () (cons 1 (ones-bad))))
(define (ones-bad) (cons 1 (ones-bad)))
```

This is a stream: thunk that returns a pair with cdr a thunk

```
(define ones (lambda () (cons 1 ones)))
(define (ones) (cons 1 ones))
```

Attendance (for video lectures)

- Don't worry about it
- I have argued with the admin office

Memoization

- If a function has no side effects and does not read mutable memory, no point in computing it twice for the same arguments
 - Can keep a cache of previous results
 - Net win if (1) maintaining cache is cheaper than recomputing and (2) cached results are reused
- Similar to promises, but if the function takes arguments, then there are multiple "previous results"
- For recursive functions, this memoization can lead to exponentially faster programs
 - Related to algorithmic technique of dynamic programming

How to do memoization: see example

- Need a (mutable) cache that all calls using the cache share
 - So must be defined outside the function(s) using it
- See code for an example with Fibonacci numbers
 - Good demonstration of the idea because it is short, but, as shown in the code, there are also easier less-general ways to make fibonacci efficient
 - (An association list (list of pairs) is a simple but sub-optimal data structure for a cache; okay for our example)

Fibonacci

Fibonacci

Fibonacci

```
(define (fib2 x)
  (letrec ([f (lambda (acc1 acc2 y)
              (if (= y x))
                 (+ acc1 acc2)
                 (f (+ acc1 acc2) acc1 (+ y 1)))])
   (if (or (= x 1) (= x 2))
       (f 1 1 3))))
(define (fib3 x)
  (letrec ([memo null] ;memo=(4 . 3) (3 . 2) (1 . 1) (2 . 1))
          [f (lambda (x)
              (let ([ans (assoc x memo)])
               (if ans (cdr ans)
                 (let ([new-ans (if (or (= x 1) (= x 2))
                              (+ (f (-x 1)) (f (-x 1)))))
                  (begin
                    (set! memo (cons (cons x new-ans) memo))
                     new-ans))))))))
 f))
```

assoc

• Example uses assoc, which is just a library function you could look up in the Racket reference manual:

(assoc v lst) takes a list of pairs and locates the first element of lst whose car is equal to v according to is-equal?. If such an element exists, the pair (i.e., an element of lst) is returned. Otherwise, the result is #f.

 Returns #f for not found to distinguish from finding a pair with #f in cdr