

- Quartum Chromodynamics- by Walter Greiner
   Churchurch to high-energy Heavy-lon Collisions- by Cheuk-Yin Wong
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   Works (Interactions by Howard George)
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   CQC Dum miles, a modern perspective.

- onvention: 
  $$\begin{split} & g^{pp} = \operatorname{diag}(1,-1,-1,-1) \\ & = \% \text{ means degger} \\ & \cdot \langle \vec{p} | \vec{p}' \rangle = \left[ a_p, a_p^{\psi_0^1} \right]_{\pm} = (2\pi)^3 \delta^3(\vec{p} \vec{p}') \\ & \cdot \int \frac{\mathrm{d}^3 \vec{p}}{(2\pi)^3} | \vec{p} \rangle \langle \vec{p} | = I \text{ is Lorentz invariant} \end{split}$$
- So is  $\int \frac{d^4p}{(2\pi)^4} 2\pi \delta(p^2 m^2)\theta(p^0) = \int \frac{d^3\vec{p}}{2E_p(2\pi)^3}$
- $\rightarrow \sqrt{2E_p}\sum_{s}|p,s\rangle$  is Lorentz invarinal If  $a^{\mu}$  is a Lorentz vector, so is  $2\sqrt{E_{p}E_{p}^{\prime}}\sum_{x,v}(p,s|a^{\mu}|p^{\prime},s^{\prime})$

- Chinal perturbation theory
  QCD sum rule
  QCD vacua & soliton & Dual-Mei:
  QCD in hot medium

- $\begin{array}{ll} \frac{3}{4} & \frac{3}{4} & \frac{1}{4} & \frac{3}{4} & \frac{3}{4}$

- matrices.  $C_1 = \frac{4}{3}I_3$ ,  $C_2 = 10/9 I_3$
- $\begin{array}{ll} = \frac{1}{2}, \quad f_{2} = 11/9 I_{3} \\ \text{in an Worthand} \\ \text{In ladder operators (notist the states in the flavor space):} \\ \text{In ladder operators (notist the states in the flavor space):} \\ \text{In ladder (D, 1)} \\ \text{In$



- Lay angian for Goldstone (pseudo-scalar) boson under  $L_{g_{R}} = \frac{f}{4} \mathrm{tr} [\partial_{\mu} U^{n} \partial^{\mu} U], \qquad U = \exp\left(\frac{2i\pi^{n} \tau_{n}}{f}\right) \\ [f] = [m] = 1 \rightarrow f = f_{n} \Lambda_{QCD} \\ \text{Invariant under } U \rightarrow LUR^{n} \\ \text{If } L = R \rightarrow \text{mortal } \text{LOBAL } SUf(3) \text{ transformation } \\ \text{If } L = R^{n} \rightarrow \text{chiral } \text{LOBAL } SU_{n}^{4}(3) \text{ transformation }$
- tright  $a_{\mu}$   $a_{\mu}$
- Extension of chiral QCD:  $L_{QCD} \rightarrow L_{QCD} (y_0 \omega \ o \ o \ o \ o \ o \ f \ (x_0, x_0)) = (x_0, x_0) + (y_0, x_0) + (y_$

- $\mathcal{L}_{\mu \pi} \rightarrow \mathcal{L}_{\mu \pi} + v \frac{f^2}{4} tr [s\%U + sU\%]$
- $$\begin{split} & f_{gg} f_{ug} + b^-_{u_1} + b^-_{u_2} + b^-_{u_3} \\ & [v] = 1 \\ & [v] = 1 \\ & [v] = 1 \\ & [v] + b^-_{u_1} + b^-_{u_2} + b^-_{u_3} + b^-_{u_3} \\ & [v] + b^-_{u_3} + b^-_{u_3} + b^-_{u_3} + b^-_{u_3} \\ & \frac{1}{2} \sqrt{\frac{1}{4}} \chi [\frac{1}{2} N_0 + 2f^-_{u_3}] + \frac{1}{2} \sqrt{\frac{1}{4}} \chi [\frac{1}{2} N_0 +$$

- Leading order:  $\frac{v^2}{2}(m_u+m_d+m_e)-vtr[M_0\tau_e\tau_b]\varpi^n\varpi^b+O(f^{-2})$  Mass of the o-flavor pseudo-scalar meson:  $M_o^2=2vtr[M_0\tau_e\tau_b]$  . List of the squared meson mass:  $\frac{v}{2}[m_u+m_{d'},m_u+m_{d'},m_u+m_{e'},m_u+m_{e'},m_u+m_{e'},m_u+m_{e'},m_{e'}+m_{e'},m_u+m_{e'},m_{e'}]$

- pion,  $K^{\pm}$ ,  $K^{0}(K^{0})$ ,  $\eta$ Break of isospin symmetry:  $m_{u} = v^{-1}(m_{u}^{2} + m_{e}^{2} + m_{e}^{2})$   $m_{d} = v^{-1}(m_{\pi}^{2} + m_{\pi}^{2} + m_{\pi}^{2})$   $m_{\pi} = v^{-1}(m_{\pi}^{2} + m_{\pi}^{2} + m_{\pi}^{2})$   $m_{\pi} = v^{-1}(m_{\pi}^{2} + m_{\pi}^{2} + m_{\pi}^{2})$   $m_{u} : m_{d} : m_{\pi} \approx 1: 1.5: 31.7$

- Not due to DM Interaction since to curries more charge Isospin symmetrical down interaction of the data neutrinon is recording. The property of the modern of the control isospin flavor by numerity approximately preserved since both the u/d/s masses are much smaller than  $A_{QG}$  and  $\delta$  break down of  $\Omega(A(1)$  symmetry. Generation:  $f = \frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  and  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  and  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac{1}{2} (m_0 + m_0 + m_0) \approx 0.53 M_{\chi}^2$  for the control isospin  $\frac$

- In reality:  $M_{\eta} \simeq 548 \, \mathrm{MeV} < M_{\eta'} \simeq 958 \, \mathrm{MeV} \rightarrow U_A(1)$  is not even an approximate symmetry of QCD.

- ew of Pre-QCD Era: overy of the strong force: 1932, discovery of neutron, by C Strong force provided:

  - overy of the strong force:

    \$120, discovery of nection, by Challeria
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    10. (a) Their begrey 1915, notes.

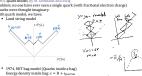
    11. (b) The station  $(\frac{1}{2}\sqrt{2} + \frac{1}{2}\frac{1}{2} + \frac{1}{2}\sqrt{2} + \frac{1}{2}\sqrt{2}\frac{1}{2}\frac{1}{2} + \frac{1}{2}\sqrt{2}\frac{1}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}$

  - 0. small join mass (127 MeV) and large nucleon mass (197804) due to spontaneous om  $(a_{n_{1}}, b_{1}, b_{2}, b_{2}, b_{3}, b_{3})$  (2008) solved irition). The state of the

  - TO Smort STEIR

    - F:\_suV F:\_sonst = Prin.

  - □ Modern view: barrow string is flux tube of gluonic field = later development: in suggest the conflux potential V = 0 suggest the conflux potential V = 0. Since V = 0 is suggest the conflux in its PTHIA string V = 0. The potential V = 0 is the potential V = 0 in the potential V = 0 is the potential V = 0 in V = 0. The potential V = 0 is the potential V = 0 in V = 0 is the potential V = 0 in V = 0



- - 11 J/ $\psi$  is NOT comprises  $\omega_r$ .

    2. True reason:

    a.  $J/\psi \rightarrow D(qc)\bar{D}$  is forbidden since  $M_{J/\psi} > 2 M_D \sim 3.6 \, \text{GeV}$ b.  $J/\psi \rightarrow 3\pi \cdots$  are suppressed due t

    OZI rule



Q: Is the progress in fundamental research slowing down compared to 50 years ago?

## Deep-Inelastic scattering $(e^- + P \rightarrow e^- + X)$

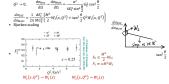


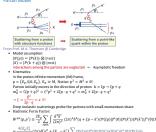
- $$\begin{split} &q^2 = q^2 = -(l-l)^2 = 2l \cdot 1 \cdots , \\ & \sim z \cdot \frac{Q^2}{2^2} \\ & \sim M^2 = 2^0 p^2 = q \cdot (p+p') = q \cdot (2p+q) \rightarrow Q^2 = 2p \cdot q \Delta M^2 \\ & = z 1 \frac{\Delta M^2}{2^2} \\ & = 1 \frac{\Delta M^2}{2^2} \\ & = 1 \frac{\Delta M^2}{2^2} \\ & = \frac{1}{2^2} + \frac{\Delta M^2}{2^2} + \frac{1}{2^2} + \frac{1}{2^2} + \frac{1}{2^2} + \frac{1}{2^2} + \frac{1}{2^2} + \frac{1}{2^2} \\ & = \frac{1}{2^2} + \frac{1}{2^2}$$
- Scattering amplitude:  $^{NaC_{L}/L}$   $M_{fl} = \left(l', X \middle| Te^{-i\int_{0}^{t} d^{*}N \operatorname{Sac}(x)} \middle| I, N(p) \right)$ For EM Interaction,  $\mathcal{H}_{tot} = A \cdot J \cdot \text{Electric current}$ The Intial & find 18 states are approximately the direct product of the e.g.,  $|I, X\rangle \simeq |I\rangle \otimes |X\rangle$
- $a_{\infty}^{\mu}$  [i, X]  $= \{j \in [M], M_{\infty}^{\mu} = \{j \in M, M_{\infty}^{\mu} = \{$
- $= -\int \frac{d^4q}{(2\pi)^4} d^4x d^4y \, \overline{D}^{\mu\nu}(q) e^{4q \cdot x} \left\{ l' \left[ e^{i\beta \cdot x} J_{\mu}(0) e^{-i\beta \cdot x} \right] l \right\} e^{-4q \cdot y} (X | e^{i\beta \cdot y} J_{\nu}(0) e^{-i\beta \cdot y} | N(p) \right\}$
- $= -(2\pi)^4 \int d^4q \, \bar{D}^{\mu\nu}(q) \delta^4(l'-l+q) \langle l'| J_{\mu}(0) | l \rangle \delta^4(p'-p-q) \langle X| J_{\nu}(0) | N(p) \rangle$
- $= -(2\pi)^{-1} \alpha^{2} \theta^{-1}(\theta) e^{-(1-\epsilon)} + q(t) |_{L^{2}(\Omega)} |_{L^{2}(\Omega)} e^{-(1-\epsilon)} = q(t) |_{L^{2}(\Omega)} e^{-(1-\epsilon)} e^{$  $q_{\mu}(l^{\nu}|J^{\mu}(0)|l) = 0$ Normalization to the total Charge  $\langle p, s|\bar{Q}|X, S' \rangle = q\langle p, s|X, S' \rangle = q(2\pi)^3 \delta^3(p - p'_X) \delta_{XS'} \delta_{W_0}$
- $$\begin{split} & \left( \kappa_1 \beta [|X,S] q(x) |X,S] q(x) |X,S] q(x) |X_0 q_{x_1}|X_0 q_{x_2}|X_0 q_{x_2}|X_$$
- $$\begin{split} & \frac{\Psi_{1}(L) \langle \cdots \rangle_{r}}{e^{-J}} \int_{\sqrt{LE_{p}}} d\gamma \frac{dx_{p}}{dz} \\ & = -\frac{e}{(2\pi)^{4}} \sum_{\vec{p}, \vec{p}} \int_{\sqrt{LE_{p}}} \frac{d^{3}\vec{p}}{\sqrt{2E_{p}}} \frac{a(\vec{p}, \sigma) \varphi^{\mu} u(\vec{p}, \sigma') (l', r') \alpha^{3\epsilon}(\vec{p}, \sigma) a(\vec{p}, \sigma') |l, s\rangle}{e^{-J}} \end{split}$$
   $= -\frac{e}{2\sqrt{E_l E_l^\prime}} \bar{u}\left(\vec{l}^\prime, s^\prime\right) \gamma^\mu u\left(\vec{l}, s\right)$  Under Lorentz gauge

- Under Lorentz gings  $D^{\mu\nu}(\alpha) = \frac{1}{\alpha^2 + 10^{12}} \left(g^{\mu\nu} + (\alpha 1)\frac{\eta^2 \pi^2}{g^2}\right)$ The second term vanishes in the product with the current matrix dem  $\mathcal{T}_{12} = \frac{1}{\alpha^2 + 10^{12}} \left(\frac{1}{10} \int_{0.00}^{\infty} |\nabla f_{\mu}(0)| \langle Q | \Psi(0) \rangle \langle 0 \rangle \right)$ Spite severaged inclusive cross section in the FT-drame.  $da = \frac{(2\alpha)^2 e^2 f^2}{(2\alpha^2)^2} \sum_{n \neq 0}^{\infty} \prod_{j=1}^{n} \frac{d^2 f^2_{ij}}{(2\alpha)^2} e^2 \left(\frac{1}{i} + p \sum_{n=1}^{\infty} \sum_{j=1}^{n} \left| |\nabla_{ij}|^2 \right|^2 \right)$
- $\begin{aligned} & \mathbb{E}[S] \left( 2\pi^{2} + 4 \frac{f_{\mathrm{sig}}}{f_{\mathrm{sig}}} \right) \frac{1}{h_{\mathrm{s}}} \frac{1}{h$

- $$\begin{split} & c \ \, \int_{\mathbb{R}^{3}} (\mathcal{L}) & = \frac{4d_{0}^{2} f_{0}^{2}}{2} \sum_{n} \left[ \psi_{j}(n) | \hat{\phi}(0) / (n) | \hat{\phi}(0) \right] \frac{e^{2}}{n^{2}} \sum_{n} d(0) \gamma_{j} u_{n}^{2} (t) u_{n}^{2} (t) \gamma_{m} u_{n}^{2} (t) \frac{e^{2}}{n^{2}} T_{1}^{2} [u(t) u(t) (t) u_{n}^{2} (t) \frac{e^{2}}{n^{2}} T_{1}^{2} [u(t) v_{n}^{2} u_{n}^{2} (t) u_{n}^{2} (t) u_{n}^{2} (t) u_{n}^{2} (t) u_{n}^{2} (t) u_{n}^{2} (t) u_{n}^{2} u_{n}^{2} (t) u_{n}^{2} u_{n}^{2} (t) u_{n}^{2} u_{n}^{2} (t) u_{n}^{2} u_{n}$$
- $= L_{\mu\nu}(l,q) = 2e^2 \left[ 2 \left( l_{\perp\mu} \frac{q_{\mu}}{2} \right) \left( l_{\perp\nu} \frac{q_{\nu}}{2} \right) + l_{\perp\mu} q_{\nu} + l_{\perp\nu} q_{\mu} q^{\mu} q^{\nu} \Delta_{\mu\nu} l \cdot q + \frac{q^{\mu} q^{\nu}}{q^2} l \cdot q \right]$
- $$\begin{split} & L_{BC}(N_{c}) = 2e^{2} \left[ 2 \left( L_{b} \frac{\alpha}{2} \right) \left[ 4 \left( L_{b} \frac{\alpha}{2} \right) + \frac{1}{4} L_{b} + \frac{\alpha}{2} + \frac{1}{4} L_{b} \frac{\alpha}{2} N^{2} \frac{1}{2} \Delta_{b} + \frac{1}{4} + \frac{1}{4} \frac{1}{2} L_{b} \right] \right] \\ & = 2e^{2} \left[ 2 \left[ 2 L_{b} L_{b} \frac{\alpha}{2} \frac{\alpha}{2} \frac{1}{2} \right] + \frac{1}{2} C_{b} R^{2} + \frac{1}{4} L_{b} \frac{1}{4} R^{2} \frac{\alpha}{4} R^{2} \frac{1}{4} R^{2} + \frac{1}{2} R_{b} R_{b} \right] \right] \\ & = 2e^{2} \left[ 2 \left[ 2 L_{b} L_{b} \frac{\alpha}{2} \frac{\alpha}{2} \right] \frac{1}{4} R^{2} R$$

- $$\begin{split} & = q \operatorname{Till}_{2}(2r) + 4 \operatorname{E}_{2}^{r} \operatorname{Rel}_{2}(2r) + 2 \operatorname{E}_{2}^{r} + 2r) + 2 \operatorname{Rel}_{2}^{r} + 2r \operatorname$$
- for an  $\frac{W}{2}$  EV W ( $\frac{Z}{2}$  ) where  $\frac{W}{2}$  is a substitute of the expectation of the expectation





- $=\frac{\frac{4\xi E_p E_k'}{2\times 2\xi E_k'}(2\pi)\delta\left(q^\theta+\xi E_p-k_0'\right)}{2\times 2\xi E_k'}\sum_{p=0}^{p+1}(\mathcal{P}(\xi p)|J^p(0)|\mathcal{P}(k'))(\mathcal{P}(k')|J^p(0)|\mathcal{P}(\xi p))$
- $= \frac{1}{2\xi E_k'} (2\pi) \delta(q^0 + \xi E_p k_0') L^{\mu\nu}(\xi p, \xi p + q)$
- $$\begin{split} &\frac{2\delta}{6}\mathbb{E}_{k}\left[\left(q^{2}+\delta E_{p}\right)^{2}-k_{p}^{2}\right)2q^{2}\left[2\xi^{2}p_{\mu\nu}p_{\nu\nu}+\frac{Q^{2}}{2}\Delta_{\mu\nu}\right]\\ &=\left(2\pi\right)\delta\left(k^{2}-m_{0}^{2}\right)q^{2}\left[4\xi p_{\mu\nu}p_{\nu\nu}+\frac{Q^{2}}{2}\Delta_{\mu\nu}\right]\\ &=\left(2\pi\right)\delta(k^{2}-m_{0}^{2})q^{2}\left[4\xi p_{\mu\nu}p_{\nu\nu}+\frac{Q^{2}}{2}\Delta_{\mu\nu}\right]\\ &+W_{1}(x,Q^{2})=8\pi(q_{0}r)^{2}\delta(k^{2}-m_{0}^{2})x, \quad W_{1}(x,Q^{2})=2\pi(q_{0}r)^{2}\delta\left(k^{2}-m_{0}^{2}\right)\frac{1}{2}x, \quad W_{2}(x,Q^{2})=2\pi(q_{0}r)^{2}\delta\left(k^{2}-m_{0}^{2}\right)\frac{1}{2}x, \quad W_{3}(x,Q^{2})=2\pi(q_{0}r)^{2}\delta\left(k^{2}-m_{0}^{2}\right)\frac{1}{2}x, \quad W_{3}(x,Q^{2})=2\pi(q_{0}r)^{2}\delta\left(k^{2}-$$
- $\begin{aligned} & 10(x/Q^2) = \sin(x/Q^2) \, d(x^2 m_0^2), \qquad 80(x/Q^2) = \sin(x/Q^2) \cos(x/Q^2) \sin(x/Q^2) \sin(x/Q$
- n of Bjorken scaling → Strong i