

# Deep Residual Learning for Image Recognition

arXiv 2015, 66424 citation

## Identity Mappings in Deep Residual Networks

arXiv 2016, 4839 citation

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# Main Problem – Deeper network

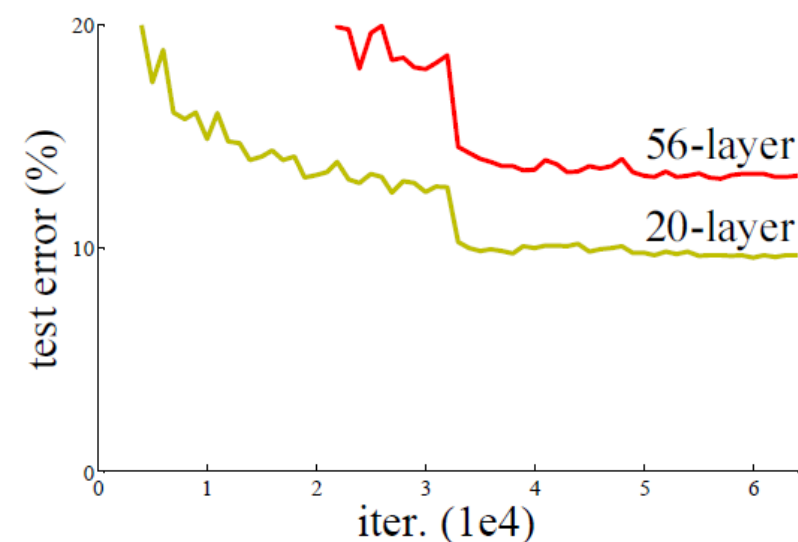
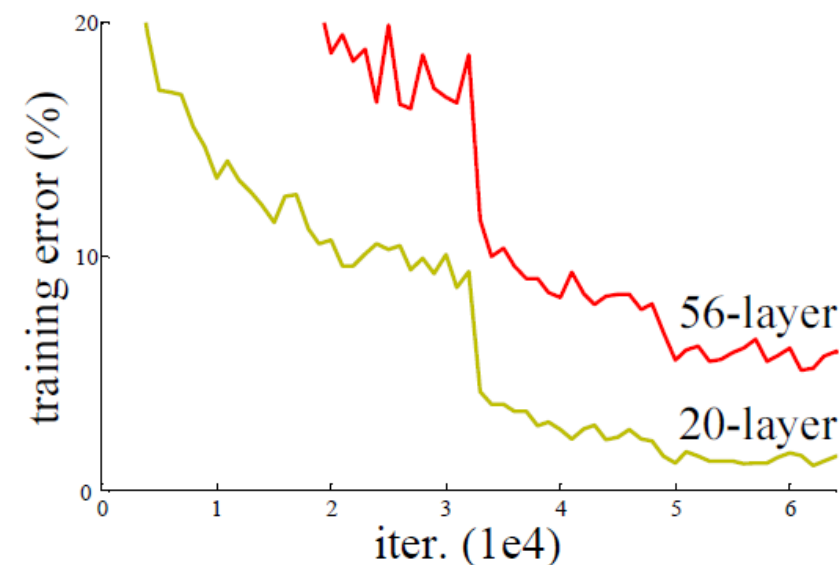
## Advantage

Deeper network

- > Better extracting representative concepts in the learning data
- > Better Result

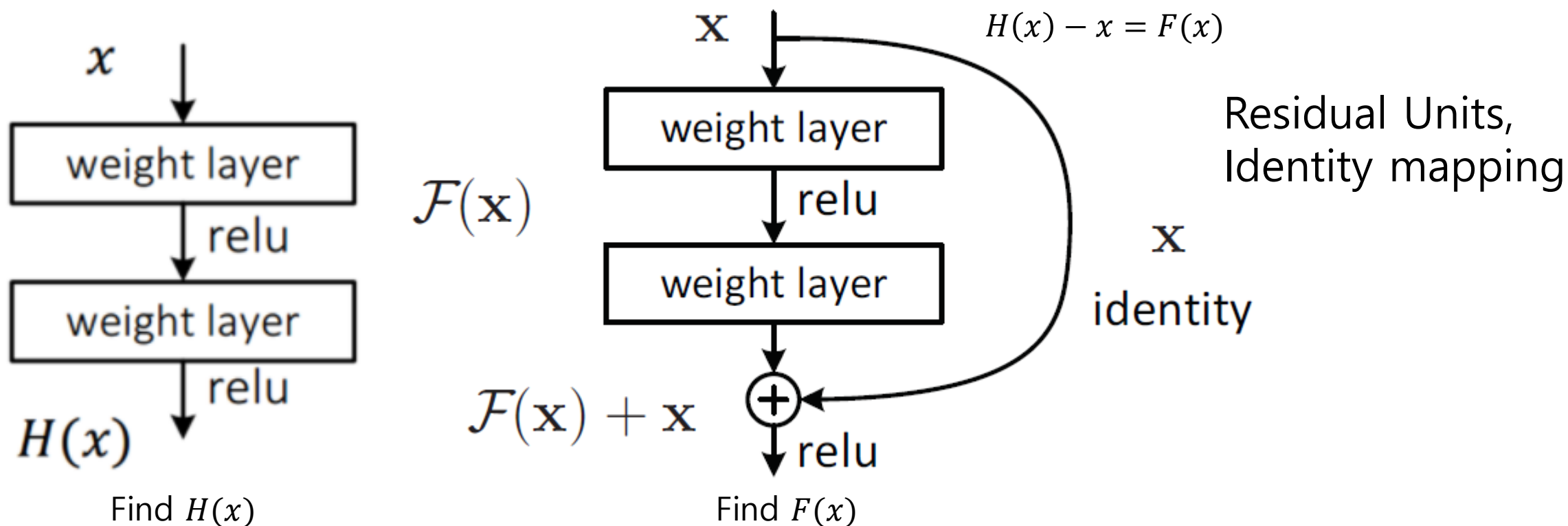
## Disadvantage

1. Deeper network
  - > Degradation problem
  - > Increase error
2. Deeper network
  - > Big number of parameters
  - > Lots of computation, Increase error



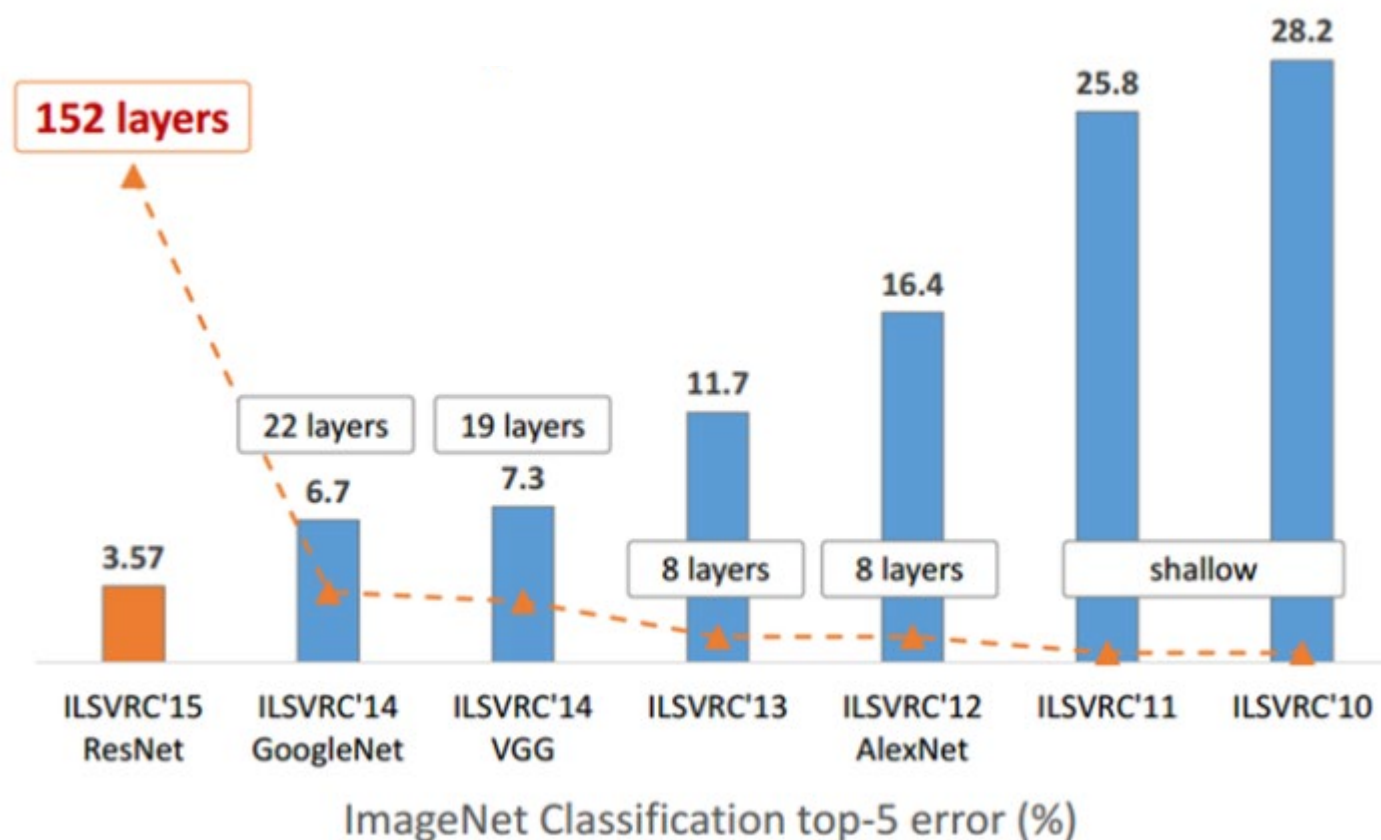
# Residual Learning

For making deeper network (more than 100 layers), getting effect of deep layer

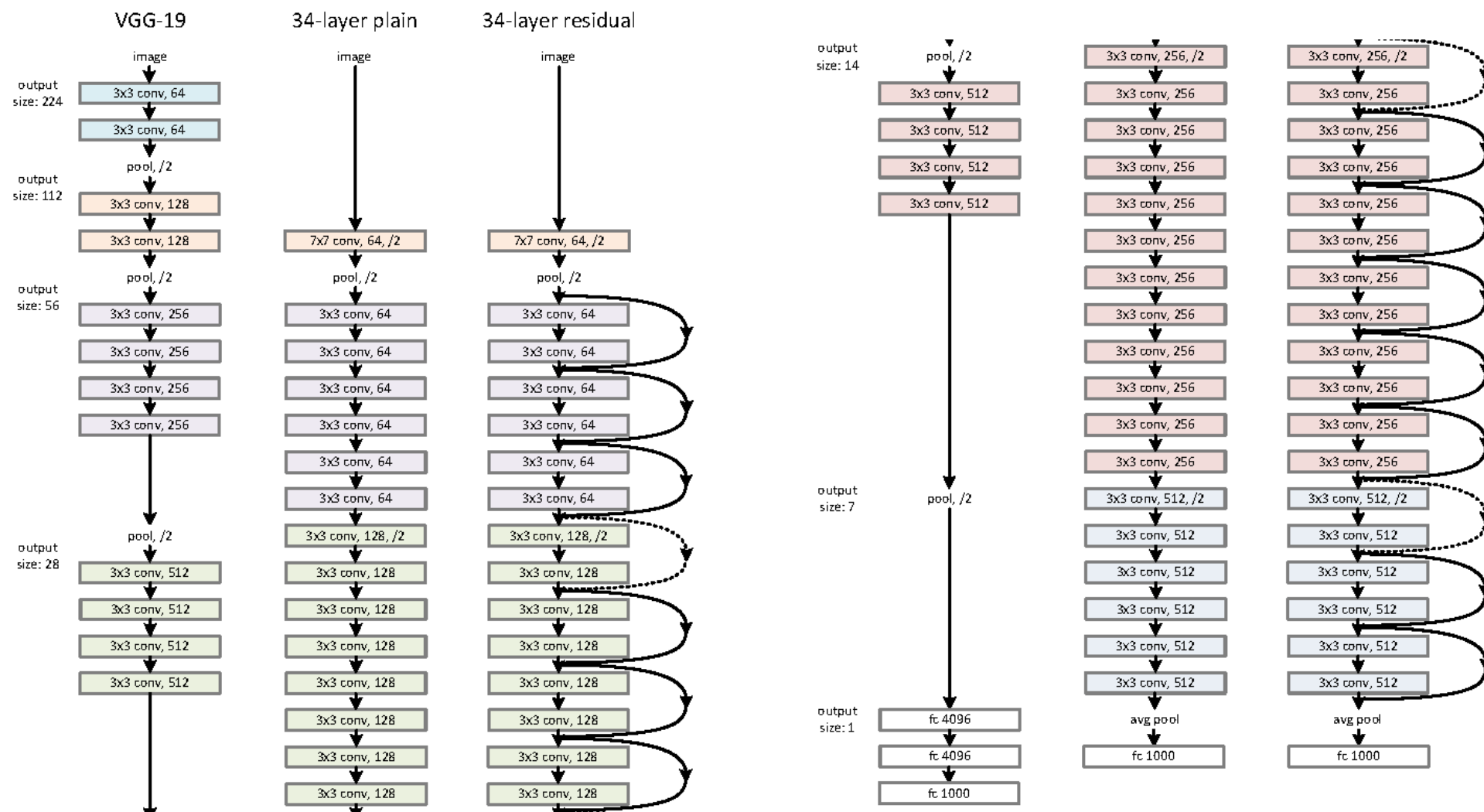


# Advantages of Residual Learning

1. No changes of number of parameters
2. Easier optimization for deep network
3. Increase accuracy by deeper network



# Experiment for ResNet



# Experiment for ResNet with ImageNet dataset

3x3 kernel convolutional layer – similar with VGGNet

No max-pooling (except last layer)

No hidden FC layer

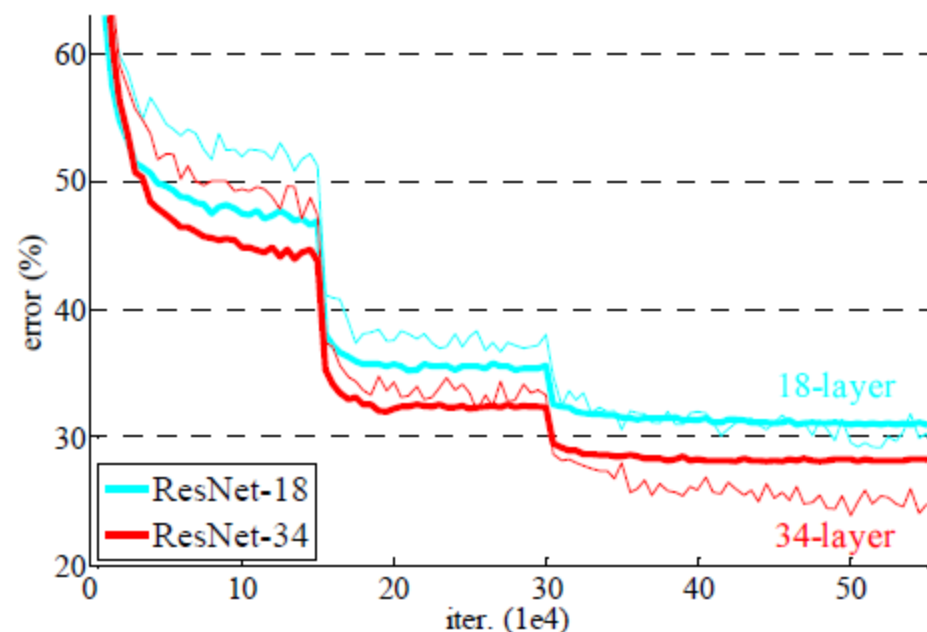
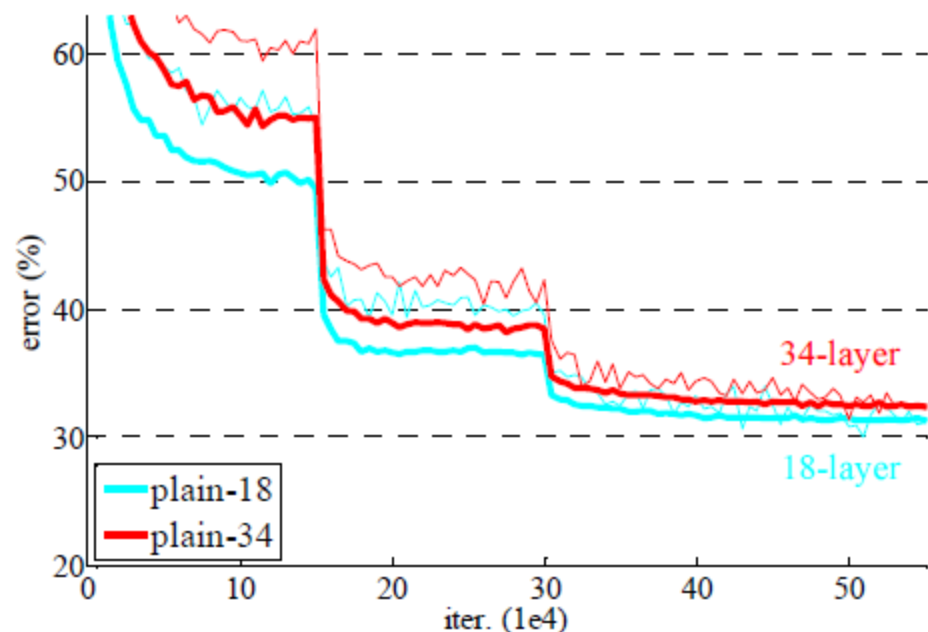
No dropout

} Lower complexity, Less computation

layer name	output size	18-layer	34-layer	50-layer	101-layer	152-layer
conv1	112×112	7×7, 64, stride 2				
conv2_x	56×56	3×3 max pool, stride 2				
		$\begin{bmatrix} 3 \times 3, 64 \\ 3 \times 3, 64 \end{bmatrix} \times 2$	$\begin{bmatrix} 3 \times 3, 64 \\ 3 \times 3, 64 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$
conv3_x	28×28	$\begin{bmatrix} 3 \times 3, 128 \\ 3 \times 3, 128 \end{bmatrix} \times 2$	$\begin{bmatrix} 3 \times 3, 128 \\ 3 \times 3, 128 \end{bmatrix} \times 4$	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 4$	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 4$	$\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 8$
conv4_x	14×14	$\begin{bmatrix} 3 \times 3, 256 \\ 3 \times 3, 256 \end{bmatrix} \times 2$	$\begin{bmatrix} 3 \times 3, 256 \\ 3 \times 3, 256 \end{bmatrix} \times 6$	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 6$	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 23$	$\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 36$
conv5_x	7×7	$\begin{bmatrix} 3 \times 3, 512 \\ 3 \times 3, 512 \end{bmatrix} \times 2$	$\begin{bmatrix} 3 \times 3, 512 \\ 3 \times 3, 512 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$
	1×1	average pool, 1000-d fc, softmax				
FLOPs		$1.8 \times 10^9$	$3.6 \times 10^9$	$3.8 \times 10^9$	$7.6 \times 10^9$	$11.3 \times 10^9$

VGGNet 19-layer: 19.6 billion FLOPs, ResNet 34-layer Plain: 3.6 billion FLOPs

## Experiment for ResNet – layer 18 and 34



	plain	ResNet
18 layers	27.94	27.88
34 layers	28.54	<b>25.03</b>

Better Accuracy, Faster learning!

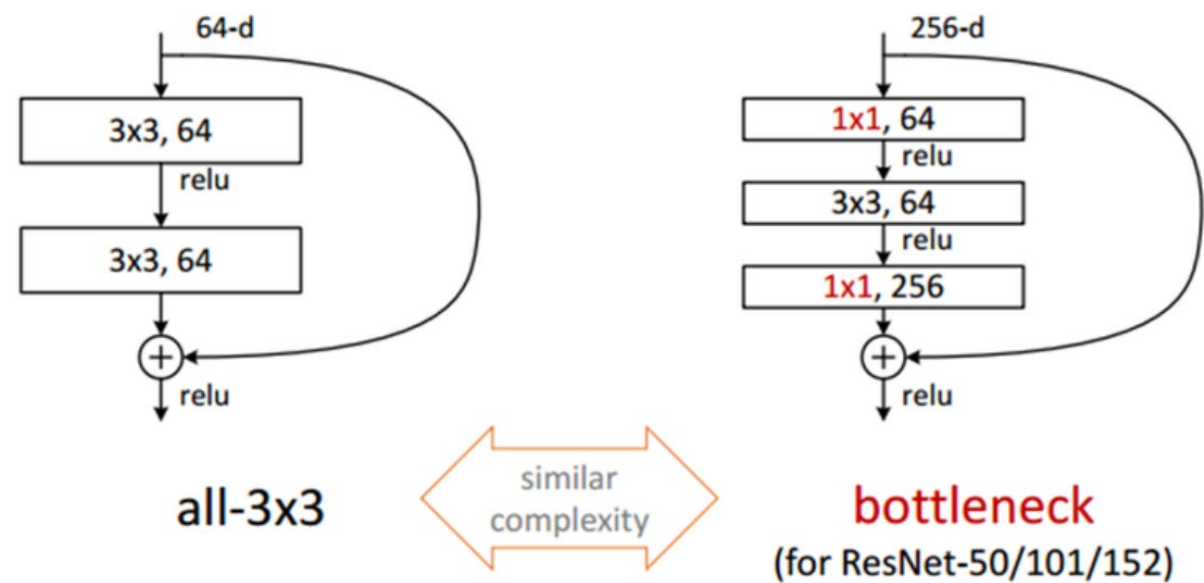
# Experiment for ResNet

model	top-1 err.	top-5 err.
VGG-16 [41]	28.07	9.33
GoogLeNet [44]	-	9.15
PReLU-net [13]	24.27	7.38
plain-34	28.54	10.02
ResNet-34 A	25.03	7.76
ResNet-34 B	24.52	7.46
ResNet-34 C	24.19	7.40
ResNet-50	22.85	6.71
ResNet-101	21.75	6.05
ResNet-152	<b>21.43</b>	<b>5.71</b>

method	top-5 err. ( <b>test</b> )
VGG [41] (ILSVRC'14)	7.32
GoogLeNet [44] (ILSVRC'14)	6.66
VGG [41] (v5)	6.8
PReLU-net [13]	4.94
BN-inception [16]	4.82
<b>ResNet (ILSVRC'15)</b>	<b>3.57</b>



# Deeper Bottleneck Architectures



First 1x1 convolution: Reduce Dimension  
Last 1x1 convolution: Expand Dimension

Reduce Computation!

layer name	output size	18-layer	34-layer	50-layer
conv1	112×112	7×7, 64, stride 2		
		3×3 max pool, stride 2		
conv2_x	56×56	$\begin{bmatrix} 3\times3, 64 \\ 3\times3, 64 \end{bmatrix} \times 2$	$\begin{bmatrix} 3\times3, 64 \\ 3\times3, 64 \end{bmatrix} \times 3$	$\begin{bmatrix} 1\times1, 64 \\ 3\times3, 64 \\ 1\times1, 256 \end{bmatrix} \times 3$
conv3_x	28×28	$\begin{bmatrix} 3\times3, 128 \\ 3\times3, 128 \end{bmatrix} \times 2$	$\begin{bmatrix} 3\times3, 128 \\ 3\times3, 128 \end{bmatrix} \times 4$	$\begin{bmatrix} 1\times1, 128 \\ 3\times3, 128 \\ 1\times1, 512 \end{bmatrix} \times 4$
conv4_x	14×14	$\begin{bmatrix} 3\times3, 256 \\ 3\times3, 256 \end{bmatrix} \times 2$	$\begin{bmatrix} 3\times3, 256 \\ 3\times3, 256 \end{bmatrix} \times 6$	$\begin{bmatrix} 1\times1, 256 \\ 3\times3, 256 \\ 1\times1, 1024 \end{bmatrix} \times 6$
conv5_x	7×7	$\begin{bmatrix} 3\times3, 512 \\ 3\times3, 512 \end{bmatrix} \times 2$	$\begin{bmatrix} 3\times3, 512 \\ 3\times3, 512 \end{bmatrix} \times 3$	$\begin{bmatrix} 1\times1, 512 \\ 3\times3, 512 \\ 1\times1, 2048 \end{bmatrix} \times 3$
	1×1	average pool, 1000-d fc,		
FLOPs		$1.8 \times 10^9$	$3.6 \times 10^9$	$3.8 \times 10^9$

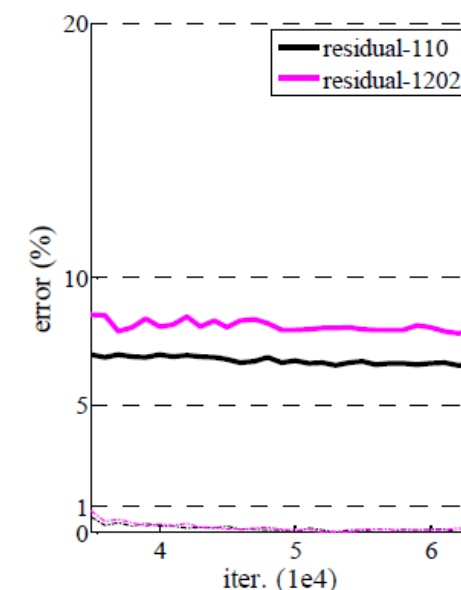
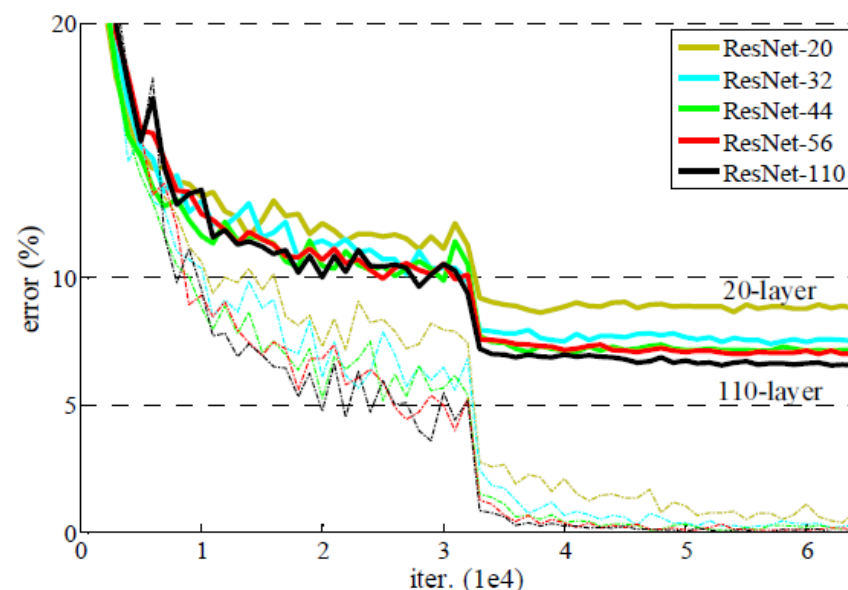
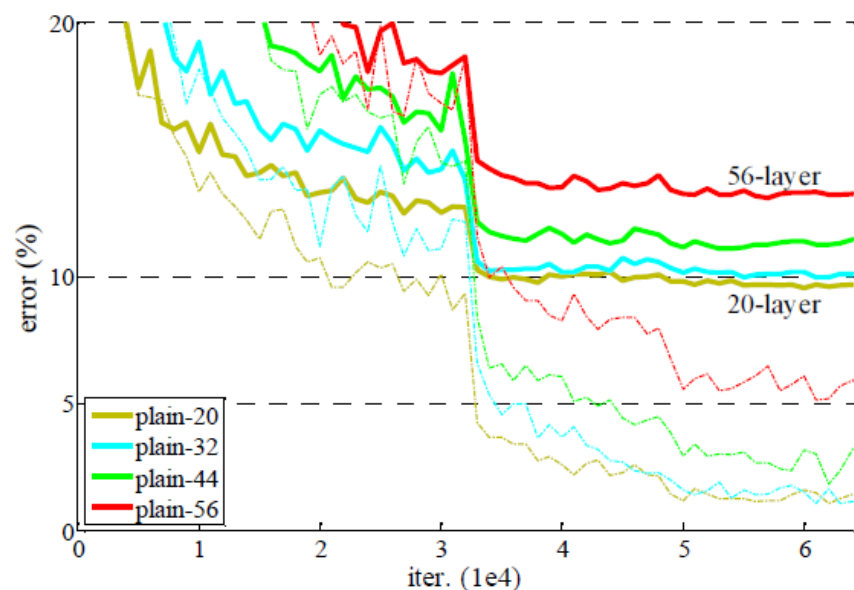
# Experiment with CIFAR-10 dataset

32x32 pixel size (smaller than ImageNet dataset: 224x224)

10 classes, total 60k images

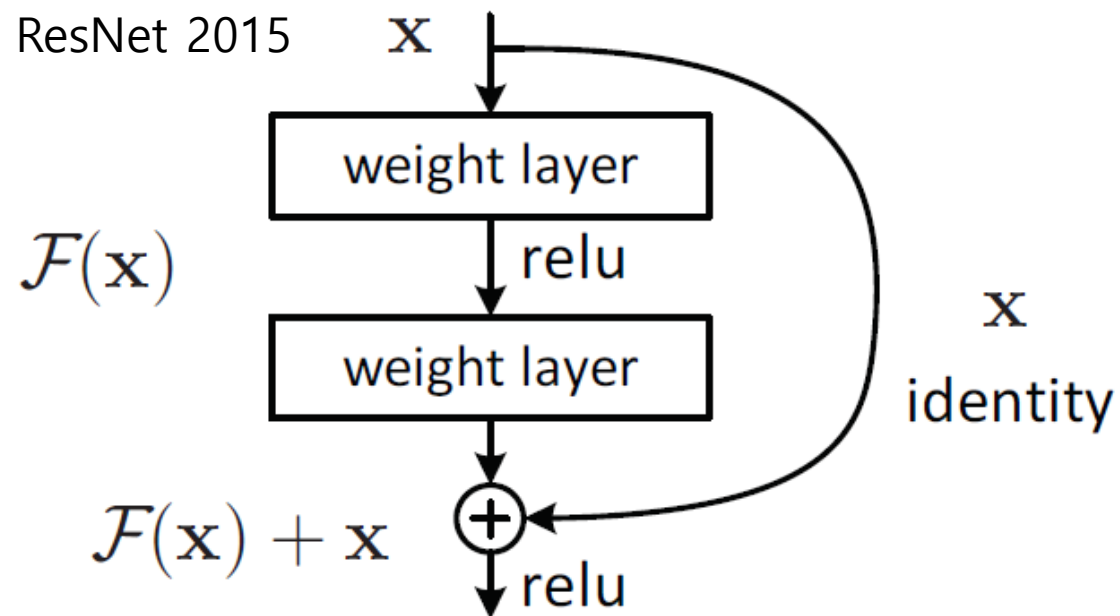
output map size	$32 \times 32$	$16 \times 16$	$8 \times 8$
# layers	$1+2n$	$2n$	$2n$
# filters	16	32	64

method			error (%)
Maxout [10]			9.38
NIN [25]			8.81
DSN [24]			8.22
	# layers	# params	
FitNet [35]	19	2.5M	8.39
Highway [42, 43]	19	2.3M	7.54 (7.72±0.16)
Highway [42, 43]	32	1.25M	8.80
ResNet	20	0.27M	8.75
ResNet	32	0.46M	7.51
ResNet	44	0.66M	7.17
ResNet	56	0.85M	6.97
ResNet	110	1.7M	<b>6.43</b> (6.61±0.16)
ResNet	1202	19.4M	7.93



But  
Why Residual Learning?  
Why Identity Mapping?

# Shortcut with identity mapping



$$y_l = h(x_l) + F(x_l, W_l),$$

$$x_{l+1} = f(y_l)$$

Original Residual Unit

$$y_l = x_l + F(x_l, W_l),$$

$$x_{l+1} = y_l,$$

$h$  is identity  
ReLU

$$x_{l+1} = x_l + F(x_l, W_l),$$

$$x_L = x_l + \sum_{i=l}^{L-1} F(x_i, W_i)$$

$$\frac{\partial \varepsilon}{\partial x_l} = \frac{\partial \varepsilon}{\partial x_L} \frac{\partial x_L}{\partial x_l} = \frac{\partial \varepsilon}{\partial x_L} \left( 1 + \frac{\partial}{\partial x_l} \sum_{i=l}^{L-1} F(x_i, W_i) \right)$$

# Shortcut with identity mapping

$\frac{\partial \varepsilon}{\partial x_L}$ : Directly Propagate

$\frac{\partial \varepsilon}{\partial x_L} \frac{\partial}{\partial x_l} \sum_{i=l}^{L-1} F(x_l, W_l)$ : Propagate through weights

$$y_l = x_l + F(x_l, W_l),$$

$$x_{l+1} = y_l,$$

$$x_{l+1} = x_l + F(x_l, W_l),$$

$$x_L = x_l + \sum_{i=l}^{L-1} F(x_l, W_l)$$

$$\frac{\partial \varepsilon}{\partial x_l} = \frac{\partial \varepsilon}{\partial x_L} \frac{\partial x_L}{\partial x_l} = \frac{\partial \varepsilon}{\partial x_L} \left( 1 + \frac{\partial}{\partial x_l} \sum_{i=l}^{L-1} F(x_l, W_l) \right)$$

# Shortcut with identity mapping

$h$  is identity

$$y_l = x_l + F(x_l, W_l),$$

$$x_{l+1} = y_l,$$

$$x_{l+1} = x_l + F(x_l, W_l),$$

$$x_L = x_l + \sum_{i=l}^{L-1} F(x_i, W_i)$$

$$\frac{\partial \varepsilon}{\partial x_l} = \frac{\partial \varepsilon}{\partial x_L} \frac{\partial x_L}{\partial x_l} = \frac{\partial \varepsilon}{\partial x_L} \left( 1 + \frac{\partial}{\partial x_l} \sum_{i=l}^{L-1} F(x_i, W_i) \right)$$

$h(x_l) = \lambda_l x_l$

$$y_l = \lambda_l x_l + F(x_l, W_l),$$

$$x_{l+1} = y_l,$$

$$x_{l+1} = \lambda_l x_l + F(x_l, W_l),$$

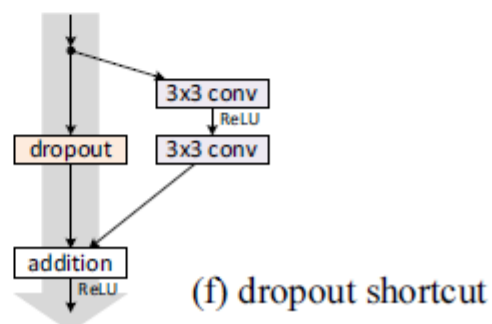
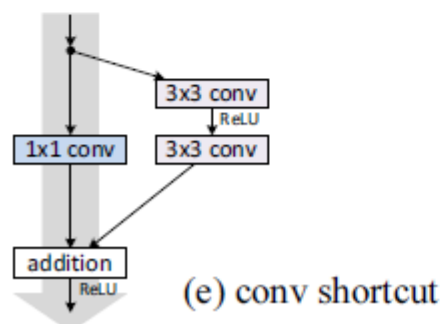
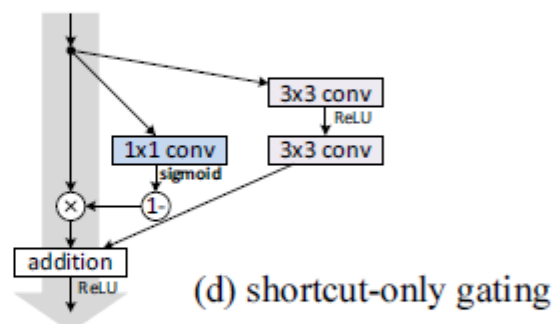
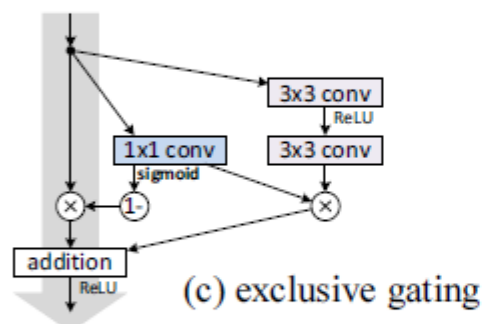
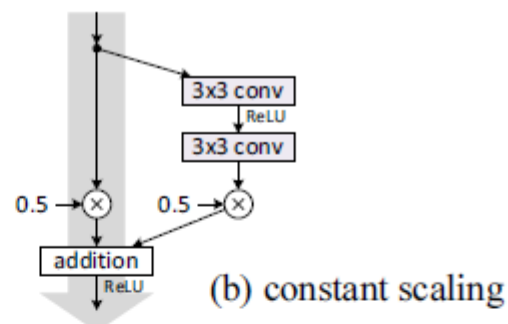
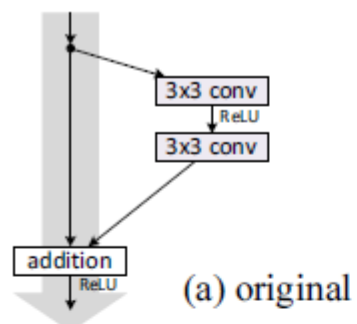
$$x_L = \left( \prod_{i=l}^{L-1} \lambda_i \right) x_l + \sum_{i=l}^{L-1} \hat{F}(x_i, W_i)$$

$$\frac{\partial \varepsilon}{\partial x_l} = \frac{\partial \varepsilon}{\partial x_L} \left( \left( \prod_{i=l}^{L-1} \lambda_i \right) + \frac{\partial}{\partial x_l} \sum_{i=l}^{L-1} \hat{F}(x_i, W_i) \right)$$

If  $\lambda_l < 1$ , exponentially small and vanish

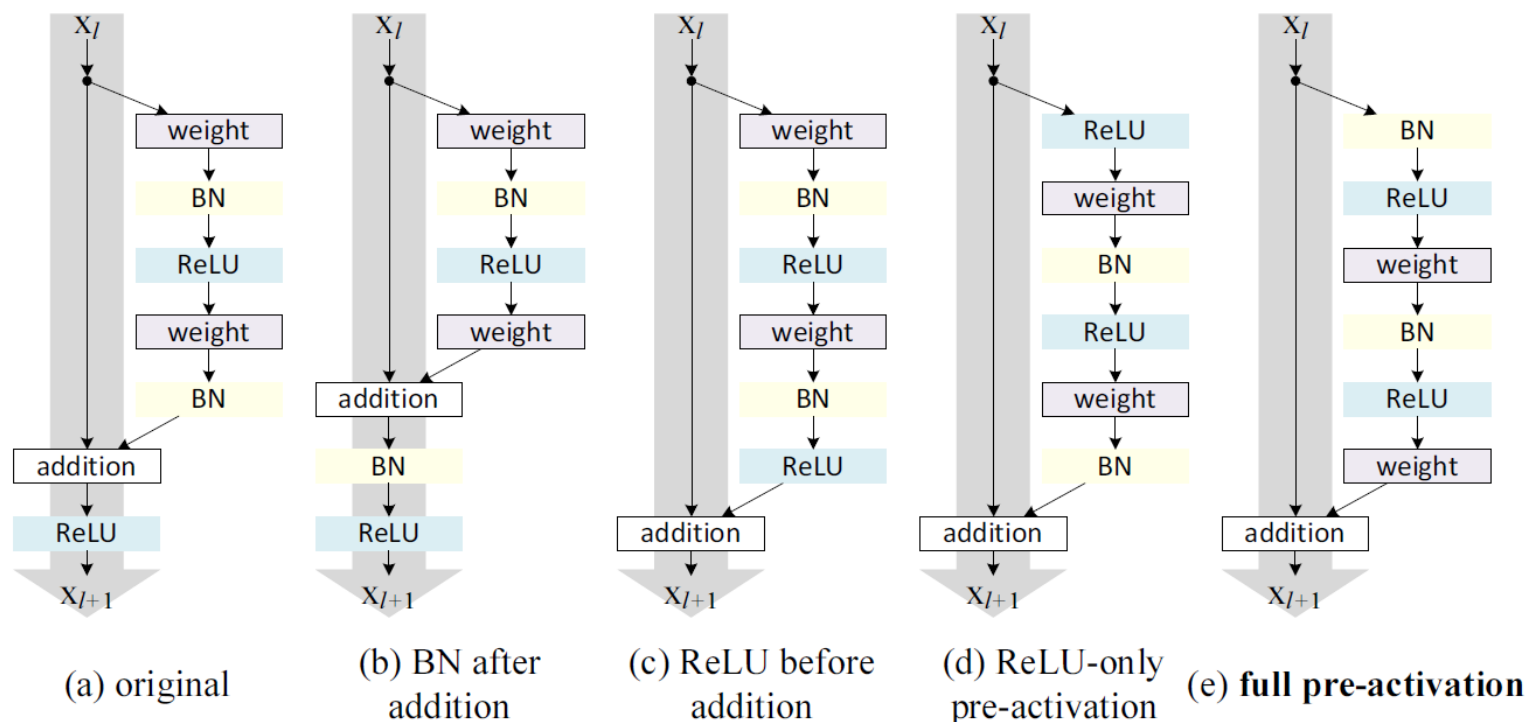
If  $\lambda_l > 1$ , exponentially large

# Various types of shortcut connections



case	Fig.	on shortcut	on $\mathcal{F}$	error (%)
original [1]	Fig. 2(a)	1	1	<b>6.61</b>
constant scaling	Fig. 2(b)	0	1	fail
		0.5	1	fail
		0.5	0.5	12.35
exclusive gating	Fig. 2(c)	$1 - g(x)$	$g(x)$	fail
		$1 - g(x)$	$g(x)$	8.70
		$1 - g(x)$	$g(x)$	9.81
shortcut-only gating	Fig. 2(d)	$1 - g(x)$	1	12.86
		$1 - g(x)$	1	6.91
$1 \times 1$ conv shortcut	Fig. 2(e)	$1 \times 1$ conv	1	12.22
dropout shortcut	Fig. 2(f)	dropout 0.5	1	fail

# Various usages of activation



case	Fig.	ResNet-110	ResNet-164
original Residual Unit [1]	Fig. 4(a)	6.61	5.93
BN after addition	Fig. 4(b)	8.17	6.50
ReLU before addition	Fig. 4(c)	7.84	6.14
ReLU-only pre-activation	Fig. 4(d)	6.71	5.91
<b>full pre-activation</b>	Fig. 4(e)	<b>6.37</b>	<b>5.46</b>



# Application to CIFAR-100 and more than 1k layers

dataset	network	baseline unit	pre-activation unit
CIFAR-10	ResNet-110 (1layer skip)	9.90	<u>8.91</u>
	ResNet-110	6.61	<u>6.37</u>
	ResNet-164	5.93	<u>5.46</u>
	ResNet-1001	7.61	<u>4.92</u>
CIFAR-100	ResNet-164	25.16	<u>24.33</u>
	ResNet-1001	27.82	<u>22.71</u>

# Conclusion

Deeper Network can be optimized by Residual Network without degradation problem

We can reduce the number of parameters with Bottleneck architecture in deep network

Identity mapping is the best way for shortcut connection

We can solve vanishing gradient problem with identity mapping

We can increase the performance in shortcut connection with pre-activation

# References

## Deep Residual Learning for Image Recognition

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## Identity Mappings in Deep Residual Networks

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