# LSTM: A Search Space Odyssey

IEEE Transactions on Neural Networks and Learning Systems, 2017

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### **Basic Information**

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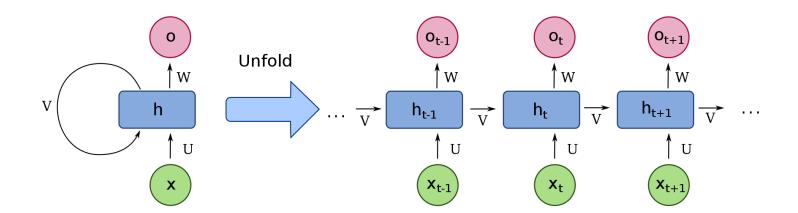
Journal: IEEE Transactions on Neural Networks and Learning Systems, 2017

Citations: 2982

- RNNs and LSTM
- Variants of LSTM
- Analysis of LSTM

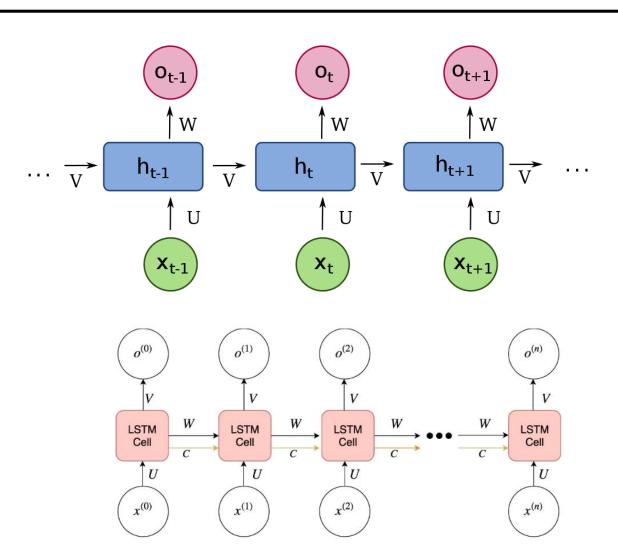
### Introduction: RNNs

- RNN: Recurrent Neural Networks
  - NN that can input/output sequences of vectors of variable length
  - Internal state of previous events (memory) used in processing
  - FFNN hidden nodes connected along 'temporal sequence'
- Applications of RNN
  - Time series : Stock market predictions, cryptocurrency
  - NLP: Translation, sentiment analysis



### Introduction: Problems of RNNs

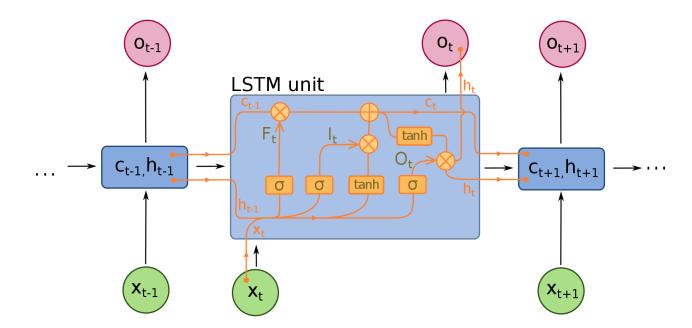
- Vanishing Gradient Problem
  - Problem more prominent than in DNNs;
     same weight V used over all hidden layers
- Skip Connections
  - Reduced rate of parameter vanishing
  - Layers that influence each other are independent from others; acts like DNN
- Gated Recurrent Networks
  - Leaky Recurrent Parameters
  - Set parameter for each time step; new parameter for network to design
  - GRU, LSTM etc.



### Introduction: LSTM

#### • LSTM

- Most popular variant of GRN
- Memory cell & Gating Units
- LSTM Unit, Cell State
  - Value passed between LSTM units
  - Each cell can decide to reset it, write to it, or read from it
  - Explicitly expressed in forms of 'gates';
     Forget, Input, Output

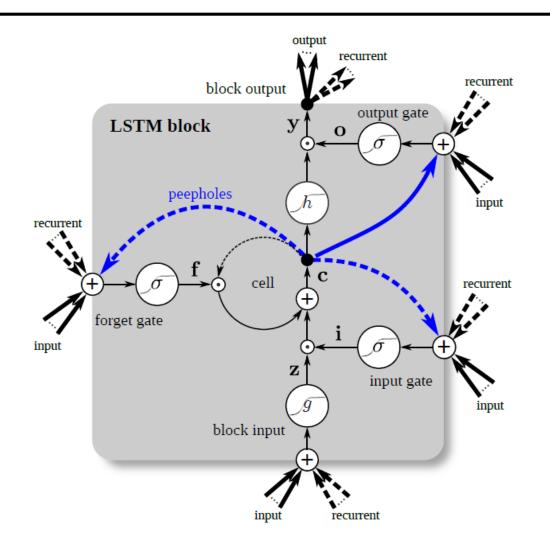


### Introduction: Vanilla LSTM

#### Vanilla LSTM

- Peephole connections
- Full BPTT

$$\begin{split} & \mathbf{\bar{z}}^t = \mathbf{W}_z \mathbf{x}^t + \mathbf{R}_z \mathbf{y}^{t-1} + \mathbf{b}_z \\ & \mathbf{z}^t = g(\mathbf{\bar{z}}^t) & block input \\ & \mathbf{\bar{i}}^t = \mathbf{W}_i \mathbf{x}^t + \mathbf{R}_i \mathbf{y}^{t-1} + \mathbf{p}_i \odot \mathbf{c}^{t-1} + \mathbf{b}_i \\ & \mathbf{i}^t = \sigma(\mathbf{\bar{i}}^t) & input \ gate \\ & \mathbf{\bar{f}}^t = \mathbf{W}_f \mathbf{x}^t + \mathbf{R}_f \mathbf{y}^{t-1} + \mathbf{p}_f \odot \mathbf{c}^{t-1} + \mathbf{b}_f \\ & \mathbf{f}^t = \sigma(\mathbf{\bar{f}}^t) & forget \ gate \\ & \mathbf{c}^t = \mathbf{z}^t \odot \mathbf{i}^t + \mathbf{c}^{t-1} \odot \mathbf{f}^t & cell \\ & \mathbf{\bar{o}}^t = \mathbf{W}_o \mathbf{x}^t + \mathbf{R}_o \mathbf{y}^{t-1} + \mathbf{p}_o \odot \mathbf{c}^t + \mathbf{b}_o \\ & \mathbf{o}^t = \sigma(\mathbf{\bar{o}}^t) & output \ gate \\ & \mathbf{y}^t = h(\mathbf{c}^t) \odot \mathbf{o}^t & block \ output \end{split}$$



### **LSTM Variants**

- One aspect each tuned
  - No peepholes
  - Full Gate Recurrence
     Recurrent connections between all gates

$$\begin{split} &\bar{\mathbf{z}}^t = \mathbf{W}_z \mathbf{x}^t + \mathbf{R}_z \mathbf{y}^{t-1} + \mathbf{b}_z \\ &\mathbf{z}^t = g(\bar{\mathbf{z}}^t) & block input \\ &\bar{\mathbf{i}}^t = \mathbf{W}_i \mathbf{x}^t + \mathbf{R}_i \mathbf{y}^{t-1} + \mathbf{p}_i \odot \mathbf{c}^{t-1} + \mathbf{b}_i \\ &\mathbf{i}^t = \sigma(\bar{\mathbf{i}}^t) & input gate \\ &\bar{\mathbf{f}}^t = \mathbf{W}_f \mathbf{x}^t + \mathbf{R}_f \mathbf{y}^{t-1} + \mathbf{p}_f \odot \mathbf{c}^{t-1} + \mathbf{b}_f \\ &\mathbf{f}^t = \sigma(\bar{\mathbf{f}}^t) & forget gate \\ &\mathbf{c}^t = \mathbf{z}^t \odot \mathbf{i}^t + \mathbf{c}^{t-1} \odot \mathbf{f}^t & cell \\ &\bar{\mathbf{o}}^t = \mathbf{W}_o \mathbf{x}^t + \mathbf{R}_o \mathbf{y}^{t-1} + \mathbf{p}_o \odot \mathbf{c}^t + \mathbf{b}_o \\ &\mathbf{o}^t = \sigma(\bar{\mathbf{o}}^t) & output gate \\ &\mathbf{y}^t = h(\mathbf{c}^t) \odot \mathbf{o}^t & block output \end{split}$$

NIG: No Input Gate:  $\mathbf{i}^t = \mathbf{1}$ NFG: No Forget Gate:  $\mathbf{f}^t = \mathbf{1}$ NOG: No Output Gate:  $\mathbf{o}^t = \mathbf{1}$ NIAF: No Input Activation Function:  $g(\mathbf{x}) = \mathbf{x}$ NOAF: No Output Activation Function:  $h(\mathbf{x}) = \mathbf{x}$ CIFG: Coupled Input and Forget Gate:  $\mathbf{f}^t = \mathbf{1} - \mathbf{i}^t$ NP: No Peepholes:  $\mathbf{i}^t = \mathbf{W}_i \mathbf{x}^t + \mathbf{R}_i \mathbf{y}^{t-1} + \mathbf{b}_i$ 

$$\bar{\mathbf{f}}^t = \mathbf{W}_f \mathbf{x}^t + \mathbf{R}_f \mathbf{y}^{t-1} + \mathbf{b}_f$$
$$\bar{\mathbf{o}}^t = \mathbf{W}_o \mathbf{x}^t + \mathbf{R}_o \mathbf{y}^{t-1} + \mathbf{b}_o$$

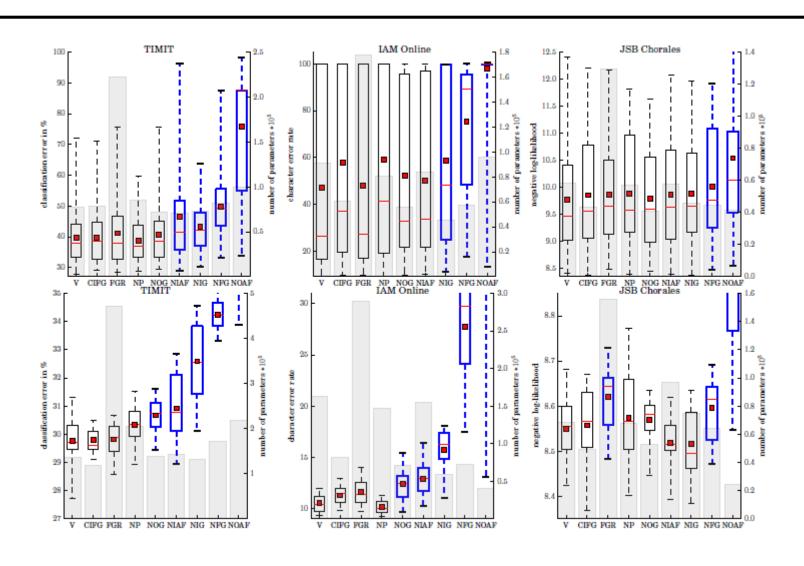
**FGR:** Full Gate Recurrence:

$$\bar{\mathbf{i}}^{t} = \mathbf{W}_{i}\mathbf{x}^{t} + \mathbf{R}_{i}\mathbf{y}^{t-1} + \mathbf{p}_{i} \odot \mathbf{c}^{t-1} + \mathbf{b}_{i} \\
+ \mathbf{R}_{ii}\bar{\mathbf{i}}^{t-1} + \mathbf{R}_{fi}\mathbf{f}^{t-1} + \mathbf{R}_{oi}\mathbf{o}^{t-1} \\
\bar{\mathbf{f}}^{t} = \mathbf{W}_{f}\mathbf{x}^{t} + \mathbf{R}_{f}\mathbf{y}^{t-1} + \mathbf{p}_{f} \odot \mathbf{c}^{t-1} + \mathbf{b}_{f} \\
+ \mathbf{R}_{if}\bar{\mathbf{i}}^{t-1} + \mathbf{R}_{ff}\mathbf{f}^{t-1} + \mathbf{R}_{of}\mathbf{o}^{t-1} \\
\bar{\mathbf{o}}^{t} = \mathbf{W}_{o}\mathbf{x}^{t} + \mathbf{R}_{o}\mathbf{y}^{t-1} + \mathbf{p}_{o} \odot \mathbf{c}^{t-1} + \mathbf{b}_{o} \\
+ \mathbf{R}_{io}\bar{\mathbf{i}}^{t-1} + \mathbf{R}_{fo}\mathbf{f}^{t-1} + \mathbf{R}_{oo}\mathbf{o}^{t-1}$$

### Evaluation

- Datasets
  - TIMIT : Speech corpus, acoustic modelling benchmark
  - IAM Online: Handwriting database, time series of pen movement
  - JSB Chorales : Next-step prediction for music
- Network Architecture
  - JSB Chorales : Single-layer LSTM
  - TIMIT, IAM Online : Bi-directional LSTM
- Hyperparametres evaluated by random search

## Results & Discussion



### Conclusion

- LSTM attempts to improve upon RNN
- Vanishing gradient solved by non-linear output activation function, forget gate; ability to 'memorise' and 'forget'
- Empirical analysis backs the assertion

# References

- Websites
  - <a href="https://en.wikipedia.org/wiki/Recurrent neural network">https://en.wikipedia.org/wiki/Recurrent neural network</a>