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# **Advanced Databases 23-24**

## Notes

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M.Sc. in Computer Science

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# Chapter 1

## Introduction

The most common use of information technology is to store and retrieve data, be it text, images, video, or audio files. As the amount of data generated by several processes increases as time goes on, storage systems must evolve to guarantee reliable access to the data, as well as fast and efficient retrieval. Data is typically stored into **databases (DBs)**, which are housed in a permanent memory.

The technology on which permanent memory is based uses magnetic **disks**, containing a set of platters that rotate at relatively slow speeds (compared to CPU speed), which can be interacted with by using heads attached to moving arms. Each platter has on both surfaces a set of rings, called **tracks**, which, except for the innermost and outermost ones, are used to store information. Each track is subdivided into **sectors** of the same size, which correspond to the smallest unit of transfer allowed by the hardware. Typical sector sizes are 512 bytes, 1 KB, 2 KB, or 4 KB. There are from 500 to 1000 sectors per track, and about 100K tracks per surface of a single platter.

The **access time** needed to read a section of the disk is given by the seek time (needed to move the head), the rotational delay (given by the spinning of the disk itself), and the transfer time (needed to read/write the data). These operations take several milliseconds to be completed, which are definitely slower than any operation relative to the **main memory (RAM)**, taking only a few nanoseconds in total.

Despite this disparity, disks are still today the preferred technology to store data. Main memory is, in fact, volatile: once the machine stops receiving electricity powering it on, any information on the RAM is lost forever. On the other hand, disks provide reliable storage: the information written on them can be retrieved even if the machine is turned off and on. A newer technology, called **solid state storage**, and, in particular, **flash memory**, has risen in popularity in the last years. It provides the reliability of disks and much faster operations, although they still haven't become the new standard since they tend to be expensive.

# Chapter 2

## Overview of a DBMS

This chapter will give a general overview of the structure of a centralized **DBMS** (**Data Base Management System**) based on the relational data model, describing its components and their respective functionalities.

### 2.1 Architecture

A database is a collection of homogeneous sets of data, with relationships defined among them, stored in permanent memory, and used via a DBMS.

#### DBMS

A DBMS is a software that provides the following functionalities:

- A language to describe the **schema** of the database (a collection of definitions that describe the data structures), restrictions on the allowed data types, and the relationships among data sets;
- The data structures for storage and efficient retrieval of large amounts of data;
- A language to guarantee secure access to the data only to authorized users;
- A **transactions** mechanism to protect data from HW/SW malfunctions and errors during concurrent access.

The architecture of a DBMS provides the following basic components:

- The **Storage Engine**, which includes modules supporting:
  - **Permanent Memory Manager**;
  - **Buffer Manager**;
  - **Storage Structures Manager**;
  - **Access Methods Manager**;
  - **Transaction and Recovery Manager**;
  - **Concurrency Manager**.
- The **Relational Engine**, which includes modules supporting:
  - **Data Definition Language**;
  - **Query Manager**;
  - **Catalog Manager**.

In real systems the functionalities of these modules are not completely separated in different components (as in Figure 2.1), but this overview can help in understanding the purpose of each of them.

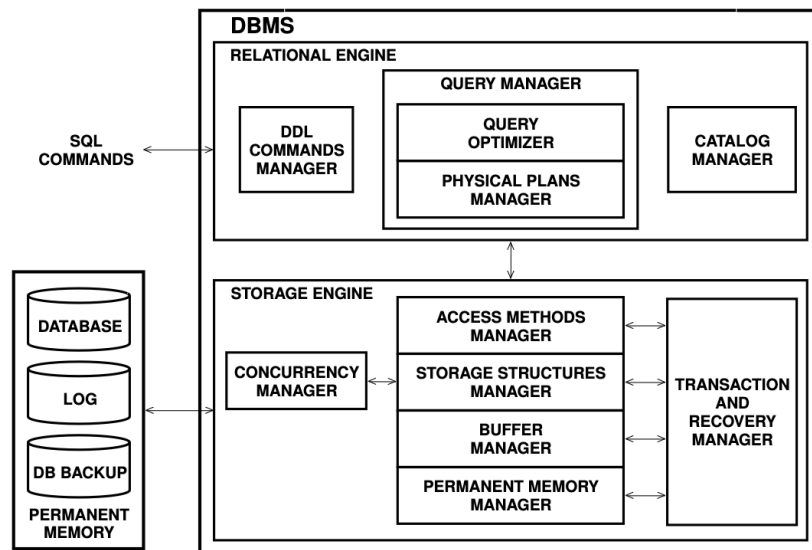


Figure 2.1: The architecture of a DBMS.

### 2.1.1 Permanent Memory Manager

The PMM manages page allocation and deallocation on disk storage. It hides the disk characteristics and the operating system, as it provides an abstraction of the memory as a set of databases, each consisting of a set of logical files of **physical pages** (or blocks) of fixed size. The physical pages of a file are numbered consecutively starting from 0, and their number can grow dynamically with the only limitation being the available space in the permanent memory. Each collection of records (table or index) of a database is stored in a logical file, which can also be realized as an actual separate file of the operating system or as part of a file in which the database is stored.

Once a physical page is transferred to main memory, it is called a **page**, and it is represented with a specific, complex structure.

### 2.1.2 Buffer Manager

The Buffer Manager is tasked with transferring pages between temporary and permanent memory. It allows transactions to get the pages they need minimizing the number of disk accesses. In general, the performance of operations on a database depends on the number of pages transferred to temporary memory. If a big enough buffer is used, and there's a high number of access requests for a specific page, there's a high likelihood that such page will be in the buffer. Figure 2.2 illustrates the basic structure of a Buffer Manager.

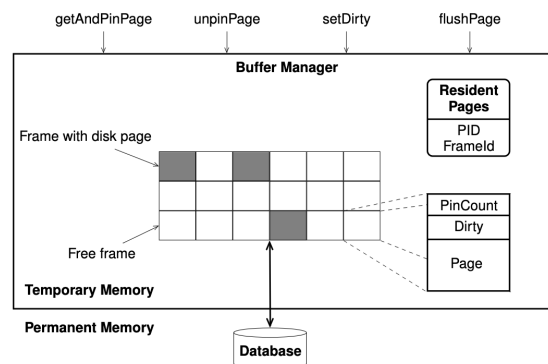


Figure 2.2: The components of the Buffer Manager.

The **buffer pool** is an array of **frames**, each containing a copy of a page present in permanent memory, and some additional bookkeeping information. The pool has a fixed size, so when there are no more free frames, a page must be freed with an appropriate algorithm. Each frame stores two variables, the **pin count** and the **dirty**. The former counts the number of transactions currently using the page hosted on that



frame; its value starts at 0, and increases by 1 each time it is requested, and decreases by 1 each time it is released. The latter indicates whether the page was modified since it was copied into the buffer, signaling that the modification must be reflected on disk as well. The **resident pages** table is a hash table that is used to know which page in permanent memory (identified by a PID) is stored in which frame.

A commonly used replacement policy is the **Least Recently Used (LRU)** policy. Once the buffer pool is full, the frame chosen to be ejected is the one that was the earliest one to be pinned. The idea is that since the page hasn't been requested for a relatively long time, it probably won't be requested any time soon. However, this policy may not always be the best: for example, in a join loop between two tables, the LRU policy may be optimal for one table, while the optimal one for the other is Most Recently Used (MRU).

### 2.1.3 Storage Structures Manager

The Storage Structure Manager implements databases as tables of records, representing the files of pages provided by the Permanent Memory Manager. Above the Storage Structure Manager, the unit of access is a record; below, the unit of access is a page. For this reason, the unit of costs considered for now will be a single page access (read or write), and we assume that memory operations have 0 cost, since they're so much faster than disk operations their addition to the overall cost is negligible. The most important type of file is the **heap file**, which stores records in no particular order.

A **record** is a collection of one or more **attributes**, and contains some extra information, called **record header**, needed for record management. We assume records are not larger than a page (a few KB big), and that each attribute is either separated from the others using a separator, or all attributes are stored sequentially and are indexed by using an offset. Each record is uniquely identified by a **RID**, which specifies the page and the offset the record can be found at. Sometimes this offset may be logical, i.e., it actually indicates a position on an array of actual pointers to records; this way, records can be moved around without having to externally modify their RID.

Collections of pages may be stored using different data structures. Usually, pages are stored with two alternatives. The first uses two doubly linked list, one containing free pages, the other containing full ones. The other alternative consists in a **directory**, where each entry contains a pair PID-available space. If the directory grows and cannot be stored in the header page of the file, it is organized as a linked list. For efficiency reasons, the free space existing in different spaces cannot be compacted into new free pages. If the available free space is plenty but there's no actual free pages available, it may be necessary to reorganize the database.

## 2.2 External Sorting

A frequent operation done in DBMS is **sorting**. Sorting collections of records may be done for different reasons: it may be needed to perform a join operation, delete duplicates, or load them into physical organizations.

Since typically temporary memory cannot hold all of the records of a file at the same time, merging is done by using **external sorting algorithms**, of which most widely used one is **merge-sort**. Let  $N_{pag}(R)$  be the number of pages in the file, and  $B$  the number of available pages on the buffer. Merge-sort operates in two phases:

1. The **sort phase**, in which  $B$  pages are read into the buffer, sorted, and written to disk. This creates exactly  $n = \lceil N_{pag}(R)/B \rceil$  sorted subsets of records, called **runs**. Each run is stored in a separate numbered auxiliary file, and contains the same number of pages (except for the last one, which may contain less if the number of file pages isn't divisible by the number of free buffer pages);
2. The **merge phase**, which fuses the sorted runs to reconstruct the file. In each merge pass,  $Z = B - 1$  runs are merged using one buffer page left free to produce the output. The number of runs at the end of a merge pass becomes  $n = \lceil n/Z \rceil$ . Merges are repeated until  $n < 1$ .

Once the algorithm terminates, the final auxiliary file contains the sorted data.  $Z$  is called the **merge order**, and a total of  $Z + 1$  buffer pages are needed to execute a  $Z$ -merge (since as stated above, one page must be left free).

The cost of the algorithm is evaluated in terms of how many read/write operations are needed in total, Since we're ignoring operations directly involving records. The overall cost is given by two terms:

$$\begin{aligned} C_{sort}(R) &= SortCost + MergeCost = \\ &= 2 \times N_{pag}(R) + 2 \times N_{pag}(R) \times MergePasses \end{aligned}$$

If the number of file pages is less than  $B^2$ , (or, more precisely,  $B(B - 1)$ ), the data can be sorted in a single pass, so the cost becomes:

$$C_{sort} = 2 \times N_{pag}(R) + 2 \times N_{pag}(R) \times 1 = 4 \times N_{pag}(R)$$

The number of passes is a function of the number of file pages  $N_{pag}(R)$ , the number of initial runs  $S$ , and  $Z$ .  $S$  also depends on the number of file pages and the number of buffer pages available at the start:

$$S = \lceil N_{pag}/B \rceil$$

At each merge pass, the algorithm merges together  $Z$  runs. At the start, the runs will be  $S$ . After one merge pass, they will be  $S/Z$ . At the second pass, they will be  $S/Z * 1/Z = S/Z^2$ , and so on until only one run remains. Since the number of runs decreases exponentially, we can write that the total number of passes will be:

$$k = \lceil \log_Z S \rceil$$

The total cost can be rewritten as:

$$C_{sort} = 2 \times N_{pag}(R) + 2 \times N_{pag}(R) \times \lceil \log_Z(S) \rceil .$$

## 2.3 Data Organizations

### 2.3.1 Heap and Sequential Organizations

The data can be arranged either via **heap organization**, or **sequential organization**. With heap organization, every new record is added to the end of the file: insertion is easy and efficient in terms of memory used. It is ideal for situations where insertion is more common than search, or files where massive search is common. This is also the standard organization for DBMS.

With sequential organization, data is kept sorted on a **search key**  $K$ , picked as a single attribute of the records. This makes equality and range search on  $K$  very efficient. On the other hand, insertion is more problematic, since the ordering of the records must be maintained at all times. Insertion may use a **static solution**, where each page is filled normally, and for each insertion, the record is placed at the correct spot in the ordering, moving all other records after it. A **dynamic solution** instead keeps some fraction of the total space in a page free. Once a page has filled up enough, its contents are split into new pages. This way, pages always have some extra space at the end to accommodate new insertions: when a record is added, the shifting of the records after it will only involve the ones in the same page. Alternatively, a **differential file** may be used to keep track of which changes must be applied to which pages, so that all insertions can be done all at once in a second moment.

Table 2.1 shows a comparison between the two organization types.  $N_{pag}(R)$  refers to the number of pages required to store the records. The **selectivity factor**  $sf$  is an estimate of the fraction of pages occupied by records that satisfy the condition of a range search, and is calculated as:

$$sf = \frac{(k_2 - k_1)}{(k_{max} - k_{min})} ,$$

Type	Memory	Eq. Search ( $C_s$ )	Range Search	Insertion	Deletion
Heap	$N_{pag}(R)$	$\left\lceil \frac{N_{pag}(R)}{2} \right\rceil$	$N_{pag}(R)$	2	$C_s + 1$
Seq.	$N_{pag}(R)$	$\lceil \log_2 N_{pag}(R) \rceil$	$C_s - 1 +$ $\lceil sf \times N_{pag}(R) \rceil$	$C_s + 1$ $+ N_{pag}(R)$	$C_s + 1$

Table 2.1: Comparison between heap and sequential organization.

with  $k_1$  and  $k_2$  being the two extremes of the range, and  $k_{max}$  and  $k_{min}$  the highest and lowest values in the domain of the attribute.

The equality search is faster for the sequential one since it uses a binary search algorithm, while the heap one has to compare the record against all pages since no specific ordering is imposed. The cost estimation is also only valid if the data distribution is uniform; if it follows some other distribution, e.g., Gaussian, the actual cost may be high (worst case exactly  $N_{pag}(R)$ ).

The range search for the heap organization costs  $N_{pag}(R)$  since it must read all pages to make sure it collects all records falling within the specified range. For sequential organization, it costs an equality search to find the starting record of the range, plus the number of pages needed to store the records in that range. The “−1” is added because the first page has already been found with the binary search.

The final biggest difference lies in the costs for insertions: it is constant for heap organization, while for sequential organization it costs a search to find the spot to insert the record, and all subsequent  $N_{pag}/2$  pages must be read and written to move their records forward. If the page the record is added to is not completely full, the insertion will still cost  $C_s + 1$ .

### 2.3.2 Key-based Organizations

A table organization based on a key allows the retrieval of a record with a specified key in as few accesses as possible, 1 being the optimum. The set of records in the table is **mapped** to a set of keys, via either a **primary organization** or a **secondary organization**.

### Primary and Secondary Organizations

A table organization is primary if it determines the way the records are physically stored, and therefore how they can be retrieved. Otherwise, it is a secondary organization.

For a primary organization, the mapping can be done using a **hash function** or a **tree structure**. It can be either **static** or **dynamic**.

### Static and Dynamic Primary Organization

A primary organization is static if the performance degrades gradually as insertions and deletions are performed, requiring reorganization.

A primary organization is dynamic if once created, it evolves with insertions and deletions, preserving efficiency of operations.

In a secondary organization, the mapping from key to record is implemented with the **tabular method/index**, listing all inputs and outputs.

### Static Hashing Organization

This is the simplest methods for a primary table organization. We assume to have  $N$  records all of the same fixed size, and that keys are integers. The records of the same table  $R$  are stored in the **primary area**, divided into  $M$  buckets, each of which may consist of one or several pages. For now, we will assume each bucket to contain only one page of capacity  $c$ , and that pages are numbered from 0 to  $M - 1$ .

A record is inserted into a specific bucket chosen by calculating its address via a **hashing function**  $H$ , applied to the record key value. The ratio:

$$d = \frac{N}{(M \times c)}$$

is called the primary area **loading factor**, which represents how full the primary area is. The hash function should produce addresses uniformly distributed in the interval  $[0, M - 1]$ , and it may return the same address for different keys. This causes a **collision**. Records hashed to the same page are stored in order of insertion. When an insertion is attempted in a page that is completely full, an **overflow** occurs, and must be appropriately managed.

The design of a static hashing organization depends on the choices done for the following parameters:

1. The **hashing function**: a good hashing function must randomly assigning keys to elements in the address space. There's no single "ideal" hash function, but generally, simpler functions tend to perform better than complex ones. A common choice is the **modulo function**:  $H(k) = k \bmod M$ , with  $M$  a prime number.
2. The **overflow management technique**: two commonly used techniques are **open overflow** and **chained overflow**. Open overflow performs a primary area linear search to find the first empty space to insert the record; when the last page has been searched, the process restarts from the initial page. Chained overflow collects overflow records chained together in a separate area, pointed to from the home page.
3. The **loading factor**: low loading factors and higher page capacities give better performances, but occupy more memory. For low ( $d < 0.7$ ) loading factors, retrieving a record requires a single access on average. For high values ( $d > 0.8$ ), the primary area size is reduced, increasing the probability of overflow; open overflow deteriorates rapidly, while chained overflow still performs well.
4. The **page capacity**: higher values of page capacity reduce the number of overflows, which are the main culprit in performance degradation of hashing organizations.

As for overall performances, for page capacities less than 10 it is preferable to give up hash organizations. A static hashing has excellent performances as long as there are no overflows to manage, with the average cost of an equality search being 1. As overflows start to happen, reorganization is needed, which requires the creation of a new primary area, choosing a new hash function, and reloading all the data.

A big drawback of static hashing is that it does not support efficient range queries, since records with similar keys will typically not end up in the same bucket.

## Dynamic Hashing Organization

Dynamic hashing organizations can be divided into two groups: those that use a primary area and an auxiliary data structure whose size changes with the primary area size, and those in which only the primary area size changes dynamically. In both cases, the hashing function changes automatically when the structure changes dimension, maintaining the average access time equal to 1. We will see two types of dynamic

organizations with auxiliary data structures (Virtual Hashing and Extendible Hashing), and two without (Linear Hashing and Spiral Hashing).

**Virtual Hashing** Virtual hashing works as follows:

1. The data area initially contains  $M$  contiguous pages of capacity  $c$ . Each page is identified by its address (between 0 and  $M - 1$ ).
2. A bit vector  $\mathcal{B}$  is created, indicating with a 1 which page contains at least a record.
3. An initial function  $H_0$  is used to map each key to an address  $m$ . If an overflow happens, then the data area is doubled, maintaining the pages as contiguous, the hashing function is replaced with a new one ( $H_1$ ) that maps keys to addresses in the range  $[0, 2M - 1]$ , and the hashing function is applied to all keys and all records in the overflowing page  $m$ . These records end up being distributed between  $m$  itself and some other new page  $m'$ .

This method defines a series of hashing functions,

$$H_0, H_1, H_2, \dots, H_r,$$

where  $H_i$  produces a page address in the range  $[0, 2^i M - 1]$ . The function chosen as the hash function must satisfy the following constraints:

$$H_{j+1}(k) = H_j(k)$$

or

$$H_{j+1}(k) = H_j(k) + 2^j \times M, \quad j = r, r - 1, \dots, 0$$

for all keys  $k$ . This means that the new hash function chosen either returns the same address the key already corresponds to, or a new address that is equal to the original one plus half of the new address space. A common function is  $H_r(k) = k \bmod (2^r \times M)$ .

To find a record, known its key and  $r$  (the number of times the data area has been doubled), a recursive function is used:

---

**Algorithm 1** PageSearch pseudocode.

---

```

1: if  $r < 0$  then
2:   The key does not exist.
3: else if  $\mathcal{B}(H_r(k)) == 1$  then
4:   Return  $H_r(k)$ 
5: else
6:   PageSearch( $r - 1, k$ )
7: end if

```

---

This technique requires memory equal to the one occupied by the data area and the bit vector  $\mathcal{B}$ . The memory is not very well used however, because of the frequent need to double the data area.

**Extendible Hashing** Instead of using a bit vector, extendible hashing uses a fixed set of data pages with a **directory**  $\mathcal{B}$ , containing a set of pointers to data pages. The directory is smaller in size than the primary area, and is doubled as needed.

Let  $r$  be a record with key  $k$ . The value produced by  $H(k)$  is a binary value of  $b$  bits (usually 32), called hash key. The hash key does not represent an actual address; instead, pages are allocated on demand as records are inserted into the file, considering only the initial  $p$  bits of  $b$ , which are used as an offset into the directory  $\mathcal{B}$ . The value of  $p$  grows and shrinks with the number of pages used by data, and the number of entries in the directory is always  $2^p$ .  $p$  is called the **directory level**. Each entry in the directory is a pointer to a data page containing records with the same first  $p'$  bits of their hash key, with  $p' \in [0, p]$ .  $p'$  is called **data page level**.

The hash structure is initially empty, with  $p = 0$ , and is a directory with one entry containing a pointer to an empty page of capacity  $c$ . The first  $c$  records are inserted in the page; as we try to insert a new record into a full page, there are two possibilities:

- If  $p' = p$ ,  $\mathcal{B}$  is doubled and  $p$  becomes  $p + 1$ . Let  $w$  be the bits of the previous value of  $p$ . Then, the entries in the doubled directory indexed by  $w_0$  and  $w_1$  each contain a pointer to the same data page that  $w$  used to point to.
- If  $p' < p$ , then the data page is split in two, creating a new page, and each of the halves' level  $p'$  take value  $p' + 1$ . The records in the original page are distributed across the halves, based on the value of the first high-order bit of their hash keys. Records whose key has 0 in the  $(p' + 1)^{th}$  bit stay in the old page, while those with a 1 will go in the new one. The pointers in the directory are updated so that those that pointed to the original page now point to the new half, depending on the value of the  $(p' + 1)^{th}$  bit.

The advantage of this method is that performance does not degrade as the file grows, and the directory  $\mathcal{B}$  keeps the memory overhead low. The retrieval of a record has an additional level of indirection since  $\mathcal{B}$  must be accessed first, but this has very little impact on the performance, since most of the directory will be in main memory.

**Linear Hashing** Linear hashing increases the number of data pages as soon as an overflow occurs, but the page which is split is not the one that flows over; instead, it



is the page pointed by the current pointer  $p$ , initially equal to 0, and incremented to 1 each time an overflow happens.

Initially,  $M$  pages are allocated, and the hash function used is  $H_0(k) = k \bmod M$ . When an overflow happens in a page with address  $m \geq p$ , an overflow chain is maintained for page  $m$ , and a new page is also added. All records in page  $p$  are distributed between page  $p$  and the new page, using the new hash function  $H_1(k) = k \bmod 2M$ .

As page  $M$  overflows, a total of  $M$  duplications have happened, bringing the memory to  $2M$  pages. Pointer  $p$  is reset, and  $H_0$  is replaced by  $H_1$ .  $H_1$  is in turn replaced by  $H_2(k) = k \bmod 2^2M$ , and so on. After  $r$  doublings, the function  $H_r(k) = k \bmod 2^rM$  will be used. To retrieve a record with key value  $k$ , the page address is calculated as:

---

**Algorithm 2** PageAddress pseudocode.

---

```

1: if  $H_i(k) < p$  then
2:    $H_{i+1}(k)$ 
3: else
4:    $H_i(k)$ 
5: end if

```

---

Linear hashing has similar performances to extendible hashing.

**Spiral Hashing** Spiral hashing considers the memory as if it were organized on a spiral instead of a line. Like linear hashing, spiral hashing requires no index, but has better performances and storage utilization because of three particular property: the hashing function distributes records unevenly, accumulating records in the pages at the beginning of the address space, while the pages at the end have a lower load. The page that is split is one that is very unlikely to overflow.

## Tree-structure Organizations

All the previous organizations have the big disadvantage of not supporting the range equality search operation. An alternative organization commonly used in DBMSs use dynamic tree structures to store pages. The **order** of a tree is the maximum number of children a node can have. The **level** of a node is the number of nodes encountered in the path from the root to the node itself. The **height** of the tree is the maximum level of a node. A tree is **balanced** if the levels of all leaf nodes differ by at most 1.

The types of trees most commonly used are B-trees and B<sup>+</sup>-trees, since unlike binary trees they manage to keep a relatively low height even with an high number of pages. One solution may be to store the nodes of the binary tree in main memory, such that each page contains the same number of nodes. In the example shown in Figure 2.3, each

page contains 8 nodes, each of which refers to 8 different pages. Using this strategy, the depth of the tree in terms of pages to access is greatly reduced: an equality search has a complexity of  $\log_8(N_{pag}(R))$  instead of  $\log_2(N_{pag}(R))$ .

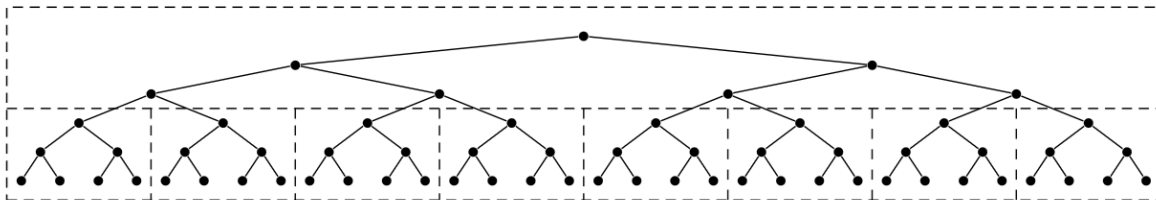


Figure 2.3: A paged binary tree: each page in main memory is delimited by a dashed line.

Still, this structure must be kept balanced when insertions or deletions are performed, and algorithms that maintain binary trees can be very costly. The following sections will explain how using multiway trees can be a solution.

**B-trees** A B-tree is a perfectly balanced search tree, in which each node has a variable number of children. We will indicate a key as  $k$  and the full record associated with it  $k*$ . Also, we'll assume that all keys are integers and that all records have the same fixed size. An example of B-tree can be seen in Figure 2.4.

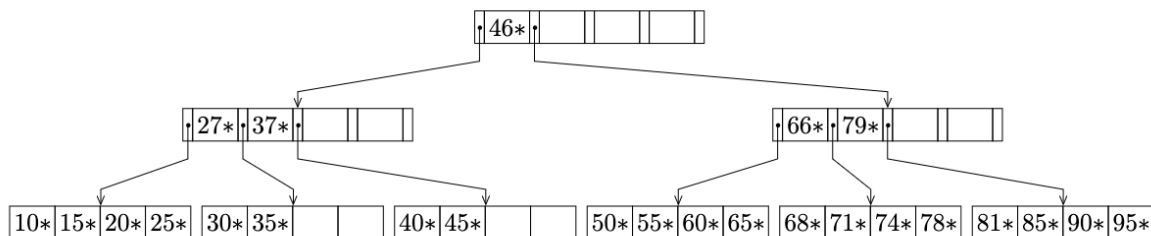


Figure 2.4: A B-tree.

A B-tree is defined as follows:

## B-tree

A B-tree of order  $m \geq 3$  is an  $m$ -way search tree that is either empty or of height  $h \geq 1$ , and satisfies the following properties:

- Each node has at most  $m - 1$  keys, and, except for the root, at least  $\lceil m/2 \rceil - 1$  keys;
- A node with  $j$  keys will have  $j + 1$  pointers to children, undefined in the leaves, and  $K(p_i)$  is the set of all keys in the  $i^{th}$  child node;
- All leaves are on the same level;
- Each non-leaf node has the same following structure:

$$[p_0, k_1^*, p_1, k_2^*, \dots, k_j^*, p_j],$$

where each  $p_i$  is a pointer to a child node such that, for all  $0 < i < j$ :

$$\forall k \in K(p_i), k_{i-1} < k < k_{i+1}$$

There is a strict relationship between the height of the tree  $h$ , the order  $m$ , and the number of keys  $N$ . Since the non-root nodes are constrained in the number of keys they must maintain, the following inequality holds true:

$$\log_m(N + 1) \leq h \leq \log_{\lceil m/2 \rceil}(\frac{N + 1}{2}) + 1$$

The left size of the inequality corresponds to a B-tree with all of its nodes completely filled, while the right side to a B-tree where each node has the least acceptable amount of keys.

The following is a summary of the costs of operations using a B-tree. An equality search for a specific key  $k$  starts at the root; if the key is not in the root (and  $h > 1$ ), the search continues in the child that will likely contain the key (since keys are ordered, the chosen pointer is the one right after the biggest key smaller than  $k$ ). The overall cost is  $1 \leq C_s \leq h$ .

As for the range search, to retrieve all records with keys in increasing order, the tree must be visited in the **in-order traversal**, starting from the leftmost leaf and gradually moving to the right. Let  $sf = (k_2 - k_1)/(k_{max} - k_{min})$  be the selectivity factor for the search; the overall cost will be  $C_{range} = sf \times N_{nodes}$ , since keys will be “scattered” across different nodes of the tree at different levels. The following bond

holds true:  $h \leq C_{range} \leq N_{nodes}$ . It will always require traveling to a leaf, and in the worst case scenario, it may have to read all nodes in the tree.

Insertion in a non-full leaf is easy: the new key is simply added to a leaf so that the keys are correctly sorted. The cost is  $h$  reads and 1 write. If the leaf is full, then the node must be split, so that the old node will retain the first half of keys, and the new node will get the second half. The median key is inserted into the parent node, and the new node is pointed by the pointer on its right. In case the parent node is full as well, the operation repeats. The cost for a worst case scenario is  $h$  reads and  $2h + 1$  writes.

For deletion, there's three possibilities:

- If the key is in a leaf, and the removal keeps the number of keys within the acceptable range, the cost is  $h$  reads and 1 write;
- If the key is a node, and no other operations are needed, the cost is  $h$  reads and 2 writes (the key is replaced with the next following one);
- If the key is in a leaf node and the final number of keys is less than  $\lceil m/2 \rceil - 1$  elements, then a **rotation** or a **merge** are needed.

A node is merged with one of its brothers which contains  $\lceil m/2 \rceil - 1$  keys, moving all of them to the first node. Additionally, the key in the parent node that was between the pointers of the two children involved in the merging is also removed and added to the merged child. In case this produces an underflow in the parent node, the operation is repeated until the whole tree is balanced.

When a merge is not possible because all brothers are too full, a rotation is performed instead. When the key is deleted, the maximum key from the left brother is moved into the parent, and the key in the parent is moved into the underfull node.

When either of these operations are needed for all nodes from root to leaf, the cost is  $2h - 1$  reads and  $h + 1$  writes.

Table 2.2 summarizes all the operation costs.

**B<sup>+</sup>-trees** B<sup>+</sup>-trees are a variant of B-trees that perform especially well for range searches. In a B<sup>+</sup>-tree, all the records  $k*$  are stored sorted in the leaf nodes, organized in a doubly linked list. Each non-leaf node stores the highest key of the child pointed by the previous pointer. An example of B<sup>+</sup>-tree can be seen in Figure 2.5.

It can be thought of as the combination of a sparse index and a sequential file. Records are part of the tree structure stored in one file, so to read all records in a sorted order, the tree structure must be necessarily used to locate the first data page.

	<b>Eq. Search</b> ( $C_s$ )	<b>Range Search</b>	<b>Insertion</b>	<b>Deletion</b>
Best case	1	$sf \times N_{nodes} = h$	$h + 1$	$h + 1$ or $(h + 2)$
Worst case	$h$	$sf \times N_{nodes} = N_{nodes}$	$2h + 1$	$(2h - 1) + (h + 1)$

Table 2.2: Costs for B-tree organization.

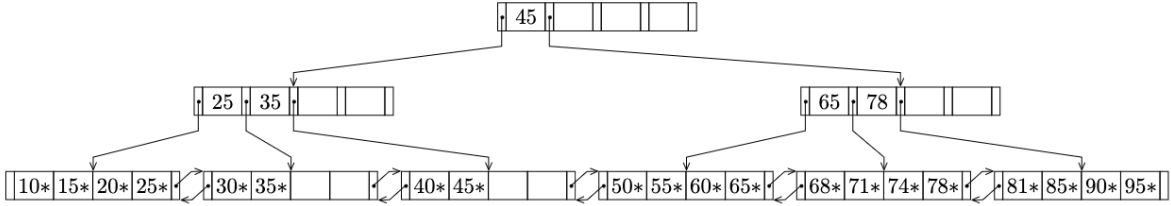


Figure 2.5: A B<sup>+</sup>-tree.

Compared to B-trees, B<sup>+</sup>-trees tend to be much shallower, since the non-leaf nodes only contain keys but not records, which can be found in the leaves, connected together. This makes any sequential/range scan of the data faster: the cost for a ranged search is  $sf \times N_{leaves}$ . For the equality search, since we're assuming the tree to have a level equal to no more than 3, will take from 1 to 3 read operations.

Another big difference is that in deletion, there's no need to replace it in the father node, unless the deletion requires a merge or rotation (in which case the operations are the same as the B-tree).

## Index (Secondary) Organizations

A secondary organization is defined as follows:

### Secondary Organization

An index  $I$  on a key  $K$  of a set of records  $R$  is a sorted table  $I(K, RID)$  on  $K$ , where  $N_{rec}(R) = N_{rec}(I)$ . An element of the index is a pair  $(k_i, r_i)$ , where  $k_i$  is the key of a record, and  $r_i$  is the corresponding RID.

An index is a tabular data structure that supports fast retrieval of records by exploiting the ordering of the keys. It can be defined on one or more keys. An index is typically stored in a B<sup>+</sup>-tree structure.

If the order of the data records is approximately the same as the order of the entries in the index, then it is called a **clustered index**. When the index is first created, a sort is performed on the actual data records, matching the index order. As insertions are performed, this ordering may be gradually lost, also reducing the effectiveness of such organization, so the clustered index may have to be recreated from time to time. If instead the data records do not follow the same order as the index records, it is called an **unclustered index**.

The cost for searches done using this organization can be broken down into two terms:

$$C_s = C_I + C_D,$$

where  $C_I$  is the cost of accessing the index pages to find the *RIDs* needed, and  $C_D$  is the cost of accessing the actual data pages containing the records. Table 2.3 summarizes the differences between the two types of indexes.

	<b>Eq. Search</b> ( $C_s$ )	<b>Range Search</b>
Clustered	$C_I = 1, C_D = 1$	$C_I = sf \times N_{leaf},$ $C_D = sf \times N_{pag}$
Unclustered	$C_I = 1, C_D = 1$	$C_I = sf \times N_{leaf},$ $C_D = sf \times N_{rec}$

Table 2.3: Costs clustered vs. unclustered indexes.

In ranged search, both types need the same time to retrieve the relevant indexes: either way, they are always sorted by key and easily accessed since they're all part of the same doubly linked list; we're still assuming that since a B<sup>+</sup>-tree structure is used, the tree will be pretty shallow. Using clustered indexes, the order in which indexes are found is the same as the order of the actual data on disk: the cost of accessing the data depends only on the number of pages the file is made up of, and we will only have to access  $sf$  of them in order. With unclustered indexes, the data is not ordered in the same way as the index. There's no way to know exactly where each record is stored in relation to the pages, so each *RID* returned by the key retrieval corresponds to an individual page access.

### 2.3.3 Non-Key Attribute Organizations

Up until now, all operations were done on keys, i.e., attributes that uniquely identify records. In many cases, however, we may be interested in retrieving records based on the values taken by other attributes. For example, imagine a table representing students attending the same school, each uniquely identified by a numeric code, and containing information about their name and age. An operation we may want to find all students within a specific age range, or all students who share the same surname. This section will describe how such operations can be done efficiently.

Specifically, the three types of operations that can be performed on non-key attributes are the equality search, the range search, and the **boolean search**, which consists in the previous operations combined together with boolean logical operators.

#### Inverted Indexes

##### Inverted Index

An inverted index  $Idx$  on a non-key attribute  $K$  of a table  $R$  is a sorted collection of entries, each in the form

$$(k_1, n, p_1, p_2, \dots, p_n),$$

where each value  $k_i$  of  $K$  is followed by the number of records  $n$  with that value, and the **sorted** RID list of these records.

Each entry in the inverted index has variable length, depending on how many records in the table  $R$  have the same value for the attribute. Also, RIDs are added or removed as records are added or removed from the table. Despite the need to manage these indexes, they are still widely used, especially for cases in which searches are more common than insertions or deletions.

To evaluate performances, we will introduce these terms:  $N_{key}(Idx)$  and  $N_{leaf}(Idx)$ , which are the number of distinct keys and leaf nodes in the index  $Idx$ . Also, all estimates are done assuming that index-key values are uniformly distributed, as well as records, and the index organization is a  $B^+$ -tree with the RID lists stored in the leaves. Each cost will be broken down into  $C_I$  and  $C_D$ , as seen before.

For the equality search, the cost of accessing the index is simply  $sf(\psi) \times N_{leaf}(Idx)$ ,

or, alternatively,  $\lceil N_{leaf}(Idx)/N_{key}(Idx) \rceil$ . Here,  $sf$  is calculated as:

$$sf(\psi) = \frac{1}{N_{key}(Idx)},$$

since we're assuming uniform distribution of the values. All RIDs can be found close together since the leaves are sorted by key (i.e., the non-key attribute of the original table).

For  $C_D$ , the cost is different whether the data is sorted or not on the index key, so whether the index is clustered or unclustered. If it is unclustered, the operation must read all relevant records with no way to estimate where they are; for each record, the whole page must be read. Potentially, we may need to read an entire RID list worth of records, whose size is given by:

$$E_{rec} = sf(\psi) \times N_{rec}(R) = \left\lceil \frac{N_{rec}(R)}{N_{key}(Idx)} \right\rceil$$

The cost of retrieving the data is:

$$C_D = \lceil \Phi(E_{rec}, N_{pag}(R)) \rceil,$$

where  $\Phi()$  is called **Cardenas' formula**, and is estimated as:

$$\Phi(k, n) = n(1 - (1 - \frac{1}{n})^k) \leq \min(k, n)$$

So, the cost will be less or equal than the smallest term: if there's a lot more records than pages, chances are that a single page may contain multiple relevant records, while if the number of records is lower than that of pages, records will rarely appear together in the same page. If the index is clustered, then the cost is:

$$C_D = \lceil sf(\Psi) \times N_{pag}(R) \rceil$$

Also, if the RID lists are unsorted, then the cost is always  $E_{rec}$ .

For the range search,  $C_I$  remains the same, except that  $sf(\Psi)$  is calculated as the ratio between the interval and the attribute's range.  $C_D$  is calculated as the product between the number of index key values, and the number of pages to access to retrieve the records indicated by the RID lists. The first term is  $\lceil sf(\Psi) \times N_{key}(Idx) \rceil$ , because we will retrieve a certain number of records for each index key included in the range. The second term again depends on whether the index is clustered or unclustered.

If the index is unclustered, then  $C_D$  is estimated as:

$$C_D = \lceil sf(\Psi) \times N_{key}(Idx) \rceil \times \left\lceil \Phi\left(\left\lceil \frac{N_{rec}(R)}{N_{key}(Idx)} \right\rceil, N_{pag}(R)\right) \right\rceil,$$



while, if it is clustered, it is:

$$C_D = \lceil sf(\Psi) \times N_{key}(Idx) \rceil \times \left\lceil \frac{1}{N_{key}(Idx)} \times N_{pag}(R) \right\rceil = \lceil sf(\Phi) \times N_{pag}(R) \rceil$$

If the RID lists are unsorted, then the second term is always  $\lceil N_{rec}(R)/N_{key}(Idx) \rceil$ .

The summary of performances is shown in Table 2.4.

	Eq. Search	Range Search
Sorted RID lists, unclustered	$C_I = \frac{1}{N_{key}(Idx)} \times N_{leaves}(Idx),$ $C_D = \Phi(E_{rec}, N_{pag})$	$C_I = \frac{v2 - v1}{v_{max} - v_{min}} \times N_{leaves}(Idx),$ $C_D = sf(\Psi) \times N_{key}(Idx) \times \Phi\left(\frac{N_{rec}(R)}{N_{key}(Idx)}, N_{pag}(R)\right)$
Sorted RID lists, clustered	$C_I = \text{as above,}$ $C_D = \frac{1}{N_{key}(Idx)} \times N_{pag}(R)$	$C_I = \text{as above,}$ $C_D = sf(\Psi) \times N_{pag}(R)$
Unsorted RID lists	$C_I = \text{as above, } C_D = E_{rec}$	$C_I = \text{as above, } C_D = sf(\Psi) \times N_{key}(Idx) \times \frac{N_{rec}(R)}{N_{key}(Idx)}$

Table 2.4: Costs for inverted indexes.

## Bitmap Indexes

### Bitmap Index

A bitmap index  $Idx$  on a non-key attribute  $K$  of a table  $R$  with  $N$  records, is a sorted collection of entries in the form  $(k_i, B)$ , where each  $k_i$  of  $K$  is followed by a sequence of  $N$  bits such that the  $j^{th}$  bit is set to 1 if the  $j^{th}$  record has value  $k_i$  for attribute  $K$ , 0 otherwise.

Bitmap indexes are used in DBMS where data is never updated, such as data warehouses, since operations that modify this type of index can be complex, especially when it's compressed. They can also easily solve multi-attribute queries, since the answer can be found by doing a bit-wise AND between two or more bitmaps.

Indicating with  $L_k$  and  $L_{RID}$  the amount of bytes needed to store a key  $k$  and a  $RID$ , and  $D_{pag}$  the page size of the leaves, the number of leaves of a full inverted index

is:

$$N_{leaf} = \frac{N_{key} \times L_k + N_{rec} \times L_{RID}}{D_{pag}} \approx \frac{N_{rec} \times L_{RID}}{D_{pag}}$$

while the number of leaves for a bitmap index is:

$$N_{leaf} = \frac{N_{key} \times L_k + N_{key} \times N_{rec}/8}{D_{pag}} \approx N_{key} \times \frac{N_{rec}}{D_{pag} \times 8}$$

Using these approximations, if the number of distinct values of the attribute is low, then a bitmap index is more convenient than an inverted index (as seen in Figure 2.6).

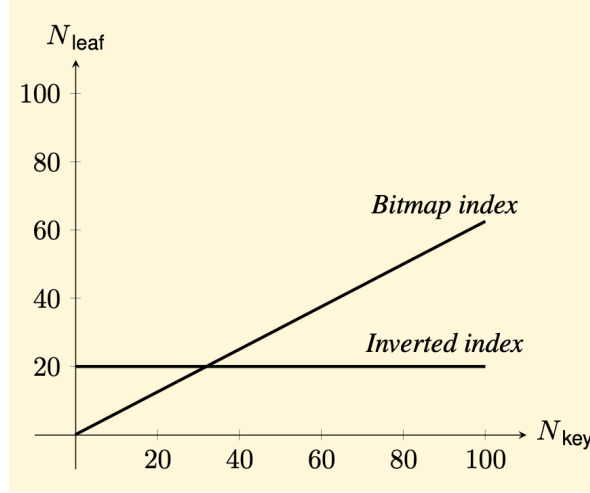


Figure 2.6: Memory usage of bitmap and inverted indexes.

### 2.3.4 Multidimensional Data Organization

Multidimensional (or spatial) data is used to represent geometric objects and their position in a multidimensional space. Each record represents a point in the space, has a certain number of attributes that each represent the coordinates. Some common queries in multidimensional datasets are searching for points that fall within a specified rectangular area, and searching for a point's nearest neighbor(s). A typical organization with a B<sup>+</sup>-tree may not be a good solution, since it does not capture “closeness” among points on more than one attribute at a time (the one chosen as key).

A way to solve this issue is to partition the space into areas with the same amount of points, so that each partition can be mapped to a separate page and allow quick retrieval of points that are spatially close together. Consider the dataset represented in Figure 2.7, and suppose that pages have a capacity of 2. The data space is first divided choosing a division value  $d$  on one coordinate, so that all points whose attribute value for that coordinate is less than  $d$  are inserted into a page, those with a higher value are

inserted into the other one.  $d$  is usually chosen as the half of the range or the median value. The first split is in Figure 2.8 (a), done on the  $x$  axis. If the partitions are still too big to fit into pages, then a split is repeated considering another axis (Figure 2.8 (b)). The splits continue alternating axes until each partition contains a small enough number of records. All the records belonging to the same partition will be found in the same page.

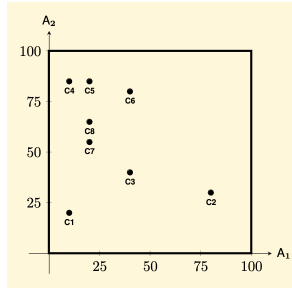


Figure 2.7: Graphical representation of a two-dimensional dataset.

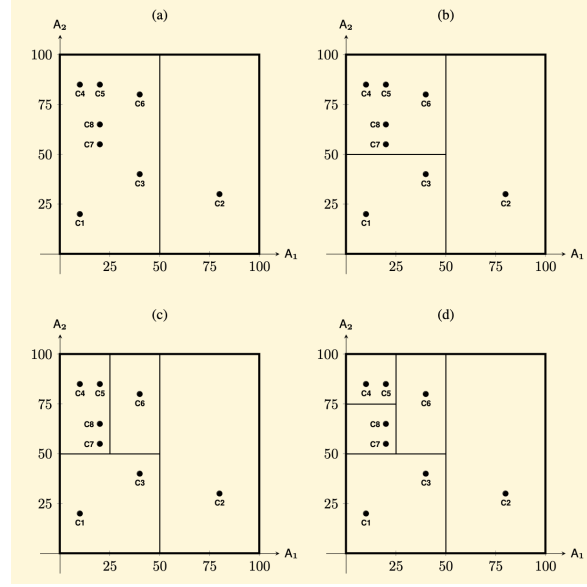


Figure 2.8: Division of the space into partitions.

## G-trees

G-trees are the data structure used to store multidimensional indexes, where each partition is identified by a **partition code**. As the space is partitioned, a sort of “decision tree” is built, where each node corresponds to an attribute test condition, alternating the attributes at each level. Partition codes are assigned as follows:

- The initial, intact, region is identified by the empty string;
- After the first split, the two partitions produced are identified with the strings “0” and “1”;
- When each partition of the previous step is split along the other axis, the new partitions will be “00” and “01”, and “10” and “11”, and so on.

- In general, when a partition  $R$  is split, the subpartitions will have a code that is equal to the code of the parent and 0/1 appended at the end.

Each partition code is then padded so that they all reach  $M$  bits, where  $M$  is the maximum number of splits made. The G-tree stores these codes like a B<sup>+</sup>-tree, where the leaves contain all the codes and the internal nodes alternate pointers to leaves and duplicate keys. After the tree has been constructed, point search, insertion, deletion,

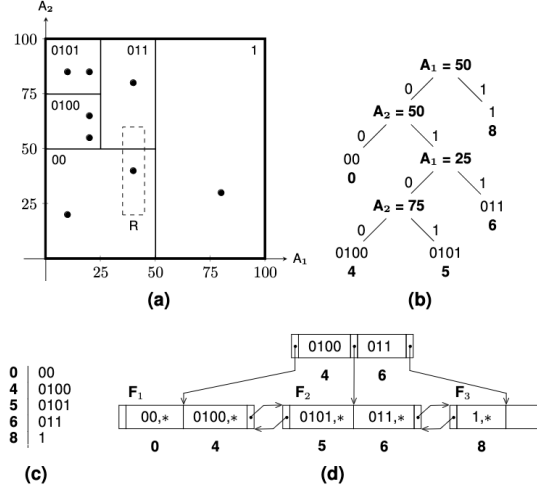


Figure 2.9: Example of partition coding.

and spatial range search can be done efficiently. To search a point  $P$  with coordinates  $(x, y)$ , the partition code of the point is retrieved (if it is present), and the code is then used to search in the G-tree.

Range search is done by specifying a range for each axis. The search starts by identifying the lower left and upper right vertices of the rectangle area; the G-tree is searched for the nodes that contain these vertices, and for each leaf between them, the elements are searched, selecting all leaves that directly intersect with the search region.

For point insertion, first the G-tree is searched to find the partition that should contain the point; then, if that partition/leaf is not full, the point is simply inserted, otherwise, the partition must be split into two. Each partition is associated with the correct partition code, and if needed (the split adds a new level to the split tree) all other codes' padding is adjusted. The points in the original partition are distributed between the pages referred by the two leaves accordingly, and the parent node is updated with the new pointer and the duplicate key. If an overflow happens in the parent node, the same procedure seen for B<sup>+</sup>-trees happens.

To delete a point, it is first searched in the G-tree, and the record is deleted. If the partition becomes empty, its code is removed from the tree. If the partition is the

result of a split, and it can be merged with its sibling, then the merge is done and the two partition codes are replaced by the partition code of their parent.

# Chapter 3

## Access Method Management

The Access Methods Manager provides an interface with several operations to interact with the organizations and indexes implemented by the Storage Structure Manager, so that data can be transferred between main and permanent memory. The language used to implement these operations transform the machine into an **abstract database machine**, called the database management system. Abstract database machines are divided into two parts:

- **Relational Engine**, or abstract machine for the logical data model. Includes modules to support the execution of SQL commands;
- **Storage Engine**, or abstract machine for physical data model. Includes modules to execute operations on the data in permanent memory.

### 3.1 Storage Engine

The interface of the Storage Engine depends on the data structures used in permanent memory. Normally, it is not directly available to the user, who will instead interact with the Relational Engine which in turn will communicate with the Storage Engine. We will consider an interface inspired by that of the relational system JRS, which stores relations into heap files and provides B<sup>+</sup>-tree indexes.

#### Data and Transactions

- $beginTransaction : null \mapsto TransactionId$
- $commit : TransactionId \mapsto null$
- $abort : TransactionId \mapsto null$

- $createDB : Path \times DBName \times TransactionId \mapsto DB$
- $createHF : DB \times Path \times HFName \times TransactionId \mapsto HF$
- $createIdx : DB \times Path \times IdxName \times HFName \times Attr \times Ord \times Unique \times TransactionId \mapsto Idx$
- $dropBD : DBName \times TransactionId \mapsto null$
- $dropHF : HFName \times TransactionId \mapsto null$
- $dropIdx : IdxName \times TransactionId \mapsto null$

## Heap File

- $HFopen : DB \times HFName \times TransactionId \mapsto HF$
- $HFCclose : HF \mapsto null$
- $HFgetRecord : HF \times RID \mapsto Record$
- $HFdeleteRecord : HF \times RID \mapsto null$
- $HFupdateRecord : HF \times RID \times FieldNum \times NewField \mapsto null$
- $HFinsertRecord : HF \times Record \mapsto RID$
- $HFgetNPage : HF \mapsto int$
- $HFgetNRec : HF \mapsto int$

## Indexes

- $Iopen : DB \times IdxName \times TransactionId \mapsto Idx$
- $Iclose : Idx \mapsto null$
- $IdeleteEntry : Idx \times Entry \mapsto null$  ( $Entry = Value \times RID$ )
- $IinsertEntry : Idx \times Entry \mapsto null$
- $IgetNKey : Idx \mapsto int$
- $IgetNLeaf : Idx \mapsto int$
- $IgetMin : Idx \mapsto Value$
- $IgetMax : Idx \mapsto Value$

## 3.2 Access Method Operators

The following operations transfer data between main and permanent memory. Records of a heap file or of an index are accessed by scans: a heap file scan operator reads each record one after the other, while an index scan operator provides a way to efficiently retrieve the RID of the records. Heap file and index scan operators are implemented using a **cursor** (or **iterator**), which is an object with methods that can return one record at a time and move across records. The typical structure of program that scans heap files/indexes is: Here  $C$  is the cursor object.

---

**Algorithm 3** Typical structure of program that uses scan operators.

---

```
1: while ! $C.isDone()$  do
2:    $Val = C.getCurrent()$ 
3:   ...
4:    $C.next()$ 
5: end while
```

---

### Heap File Scan

- $HFS_{open} : HF \mapsto HFS$
- $HFS_{isDone} : HFS \mapsto bool$
- $HFS_{getCurrent} : HFS \mapsto RID$
- $HFS_{next} : HFS \mapsto null$
- $HFS_{reset} : HFS \mapsto null$
- $HFS_{close} : HFS \mapsto null$

### Index Scan

- $IS_{open} : Idx \times fstKey \times lstKey \mapsto IS$
- $IS_{isDone} : IS \mapsto bool$
- $IS_{getCurrent} : IS \mapsto null$
- $IS_{reset} : IS \mapsto null$
- $IS_{close} : IS \mapsto null$



### 3.3 Physical Plans

When a SQL query must be executed, it is first represented as a **logical plan**, which is a tree representation of the query, and is eventually transformed in a form that can be more efficiently evaluated. This transformed logical plan is then translated into a **physical plan**, which contains as nodes the actual physical operators that can implement that query. Each operator in a plan is an iterator that uses a “pull” interface: when an operator receives a request from above, it “pulls” on its input node(s) and computes the result, returning it to its parent operator. An operator interface provides the necessary methods *open*, *next*, *isDone*, and *close*, implemented using the Storage Engine interface.

# Chapter 4

## Physical Relational Operators

One of the most important components in a DBMS is the **Query Manager**, which is responsible of scheduling queries and directing them to the correct tables. Part of the Query Manager is the **Query Optimizer**, which has the task of determining how to execute a query in the most efficient way possible, considering the physical parameters involved, the data organization, and the presence or absence of indexes.

This chapter will deal with how different physical operators are implemented, for the following operations:

- Projection;
- Selection;
- Grouping;
- Set operations;
- Join.

Then, it will discuss how the optimizer uses these operators to generate efficient physical plans. In general, the problem will be studied under certain assumptions, illustrated in the next sections.

### 4.1 Selectivity Factors

The selectivity factor of a condition is an estimate of the percentage of the records in a relation which satisfy that condition. The simplest way to estimate this percentage is by assuming the data is uniformly distributed. The selectivity factor of different conditions is reported in table 4.1. The last column is a constant value that is used if

not enough information is known to calculate the actual  $sf$ , or when the attribute is non-numeric.

Condition	Calculated $sf$	Approx. $sf$
$A = v$	$\frac{1}{N_{key}}$	$\frac{1}{10}$
$A > v$	$\frac{\max(A) - v}{\max(A) - \min(A)}$	$\frac{1}{3}$
$A < v$	$\frac{v - \min(A)}{\max(A) - \min(A)}$	$\frac{1}{3}$
$v_1 < A < v_2$	$\frac{v_2 - v_1}{\max(A) - \min(A)}$	$\frac{1}{4}$
$A_1 = A_2$	$\frac{1}{\max(N_{key}(A), N_{key}(B))}$	$\frac{1}{10}$
$\psi_1 \wedge \psi_2$	$sf(\psi_1) \times sf(\psi_2)$	-
$\psi_1 \vee \psi_2$	$sf(\psi_1) + sf(\psi_2) - sf(\psi_1) \times sf(\psi_2)$	-

Table 4.1: Selectivity factors of different conditions.

In many cases, however, attribute values follow non-uniform distributions, making these estimates wrong. The selectivity factor of a condition can be better approximated by knowing the actual distribution of the data, but storing the information needed to have full knowledge about it would occupy too much space. The solution preferred by DBMSs is to use an histogram with binned ranges of values in order to approximate the actual distribution.

There's two types of histograms: **equi-width** and **equi-height**. Equi-width histograms are obtained by binning values so that each bin has the same amount of elements  $n$ . For each bin, the sum of the counts of all elements inside that bin is stored. To find the selectivity factor for an equality search given a value  $v$ , it will be given by the sum associated with the bin  $v$  belongs to, divided by  $n$ . For inequality/range searches, the selectivity factor will consider the sum associated with all the bins completely included in the range, plus the term that is given by the bin(s) corresponding to the extreme(s) of the condition.

The problem with equi-width histograms is that while they provide better approximations than a blind uniform distribution assumption, they are not able to correctly

approximate the distribution of data to a sufficiently high precision. This is why equi-height histograms are used instead. These histograms are divided into bins such that the sum of counts of values within each (their “height”) is equal across all of them. To store this type of histogram, the only information needed is the number of elements in each bin.

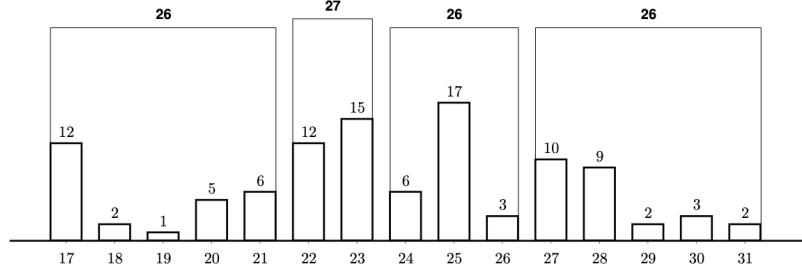


Figure 4.1: An equi-height histogram.

Still, the approximation done by these histograms may not be accurate if the distribution within a bin is not uniform. For example, in Image 4.1, the third bin has follows a Gaussian distribution. If a query requests all records whose values for that attribute is equal to 24, the selectivity factor approximation will be much higher than the real one; if a query instead requests records with value 25, the approximation will be much lower.

## 4.2 Physical Operators

### 4.2.1 Operators for Relation

**TableScan( $R$ )** Returns all the records in  $R$ , in the same order as they are stores. It costs

$$C = N_{pag}(R)$$

The result size is

$$E_{rec} = N_{rec}(R)$$

**SortScan**( $R, \{A_i\}$ ) Returns all the records in  $R$  sorted in ascending order on the attribute  $A_i$ . Sorting is done with a merge sort algorithm. It costs

$$C = \begin{cases} N_{pag}(R) & N_{pag}(R) < B \\ 3 \times N_{pag}(R) & N_{pag}(R) \leq B \times (B - 1) \\ N_{pag}(R) + 2 \times N_{pag}(R) \times \lceil \log_{B-1}(N_{pag}(R)/B) \rceil & \text{else} \end{cases}$$

The result size is

$$E_{rec} = N_{rec}(R)$$

**IndexScan**( $R, I$ ) Returns the records of  $R$  sorted by the attribute the index  $I$  is defined on. It costs

$$C = \begin{cases} N_{leaf}(I) + N_{pag}(R) & \text{if } I \text{ is clustered} \\ N_{leaf}(I) + N_{rec}(R) & \text{if } I \text{ is on a key of } R \\ N_{leaf}(I) + \lceil N_{key}(I) \times \phi(\lceil N_{rec}(R)/N_{key}(I) \rceil, N_{pag}(R)) \rceil & \text{else} \end{cases}$$

The result size is

$$E_{rec} = N_{rec}(R)$$

**IndexSequentialScan**( $R, I$ ) Returns the records of  $R$ , stored with the primary organization  $I$ , sorted in ascending order on the primary key values. It costs

$$C = N_{leaf}(I) \tag{4.1}$$

The result size is

$$E_{rec} = N_{rec}(R)$$

## 4.2.2 Operators for Projection

**Project**( $O, \{A_i\}$ ) Projects the records of  $O$  over the attributes  $\{A_i\}$ . It costs

$$C = C(O)$$

The result size is

$$E_{rec} = E_{rec}(O)$$

**IndexOnlyScan**( $R, I, \{A_i\}$ ) Returns the sorted records of  $R$ , projecting them over the attributes  $\{A_i\}$  on which the index  $I$  is on (or contains them as prefix). It costs

$$C = N_{leaf}(I)$$

If a tuple of values for the attributes  $\{A_i\}$  is associated with  $n$  different RIDs, it is returned  $n$  times. The result will not contain duplicates if the attributes are relation keys (they uniquely identify records). The result size is

$$E_{rec} = N_{rec}(R)$$

### 4.2.3 Operators for Duplicate Elimination

**Distinct**( $O$ ) Returns the records of  $O$  eliminating all duplicates. This operator requires that the records of  $O$  are **grouped** (if  $r_i = r_j$ , and  $i < l < j$ , then  $r_i = r_l = r_j$ ). When a collection of records is sorted, it is also grouped. It costs

$$C = C(O)$$

If there's only one attribute in  $O$ , then the result size is

$$E_{rec} = N_{key}(A)$$

If instead it contains multiple attributes, the result size is

$$E_{rec} = \min(|O|/2, \prod_i N_{key}(A_i))$$

This is a pessimistic estimate: it assumes that there is a record for each set of values taken from the attributes in  $O$ , but this is often not the actual result. For example, imagine a database containing data about students enrolled at a university, and the two attributes represent their first name and last name respectively: it is unrealistic to expect that there will be a different student for each first name-last name combination, since the two attributes are loosely correlated.

**HashDistinct**( $O$ ) Returns the records of  $O$  without duplicates using and hash technique. This technique has two phases: **partitioning** and **duplicate elimination**. Assume the query processor has  $B + 1$  buffer pages. In the partitioning phase, for each record in  $O$  the hash function  $h_1$  is applied, distributing records uniformly across the  $B$  pages. Once a page  $i$  is full, it is written to the  $T_i$  partition file. At the end of the phase, all records will be scattered across  $B$  files, each of which contains records with the same hash value; this means that duplicates are found in the same partition.

In the duplicate elimination phase, the process becomes an intra-partition problem. Each  $T_i$  file is read page-by-page, eliminating duplicates using the hash function  $h_2$ . A record is deleted when it collides with another record with the same hash value according to  $h_2$  and the two records are identical. Assuming each partition occupies at most  $B$  pages, at the end of the partition, the  $B$  pages are cleared, and the duplicate elimination is applied to the records in the next partition. If the number of pages is greater than  $B$ , then a hash-based projection technique is applied recursively by dividing the partition into subpartitions. This degrades performances. The operator costs:

$$C = C(O) + 2 \times N_{pag}(O)$$

The result size is the same as Distinct, so

$$E_{rec} = N_{key}(A)$$

if there's only one attribute in  $O$ , and

$$E_{rec} = \min(|O|/2, \prod_i N_{key}(A_i))$$

if  $O$  contains multiple attributes.

#### 4.2.4 Operators for Sort

**Sort**( $O, \{A_i\}$ ) Returns the records of  $O$  sorted on the attributes  $\{A_i\}$ . The sorting algorithm used is merge sort, so its cost is

$$C = \begin{cases} C(O) & N_{pag}(R) < B \\ C(O) + 2 \times N_{pag}(O) & N_{pag}(O) \leq B \times (B - 1) \\ C(O) + 2 \times N_{pag}(O) \times \lceil \log_{B-1}(N_{pag}(O)/B) \rceil & \text{else} \end{cases}$$

The result size is

$$E_{rec} = N_{rec}(O)$$

#### 4.2.5 Operators for Selection

**Filter**( $O, \psi$ ) Returns the records of  $O$  that satisfy the condition  $\psi$ . It costs

$$C = C(O)$$

The result size is

$$\lceil sf(\psi) \times N_{rec}(O) \rceil$$

**IndexFilter**( $R, I, \psi$ ) Returns the records of  $R$  that satisfy the condition  $\psi$  using the index  $I$ , defined on the attributes involved in  $\psi$ , sorted according to  $I$ . The condition is a predicate or a conjunction of predicates that only involve the attributes found in the prefix of the index search key.

IndexFilter always appears as a leaf node in a physical plan. This operator uses the index to find the sorted set of RIDs of all records that satisfy the condition, then it retrieves the records from disk. The cost can be broken down as

$$C = C_I + C_D$$

- If the index is clustered:

$$\begin{aligned} C_I &= \lceil sf(\psi) \times N_{leaf}(I) \rceil \\ C_D &= \lceil sf(\psi) \times N_{pag}(R) \rceil \end{aligned}$$

- If the index is unclustered:

$$\begin{aligned} C_I &= \lceil sf(\psi) \times N_{leaf}(I) \rceil \\ C_D &= \lceil sf(\psi) \times N_{key}(I) \rceil \times \lceil \Phi(\lceil N_{rec}(R)/N_{key}(I) \rceil, N_{pag}(R)) \rceil \end{aligned}$$

If the index is defined on a key of  $R$ , then

$$C_D = \lceil sf(\psi) \times N_{rec}(R) \rceil$$

The result size is

$$E_{rec} = \lceil sf(\psi) \times N_{rec}(R) \rceil$$

**IndexSequentialFilter**( $R, I, \psi$ ) Returns the sorted records of  $R$ , stored with the primary organization  $I$ , satisfying the condition  $\psi$ , which involves only the attributes of the index search key. It costs

$$C = \lceil sf(\psi) \times N_{leaf}(I) \rceil$$

The result size is

$$E_{rec} = \lceil sf(\psi) \times N_{rec}(R) \rceil$$

**IndexOnlyFilter**( $R, I, \{A_i\}, \psi$ ) Returns the sorted records of the projection on  $R$  returning only the values for  $\{A_i\}$  that satisfy  $\psi$ , using only the index  $I$ . It costs

$$C = \lceil sf(\psi) \times N_{leaf}(I) \rceil$$

The result size is

$$E_{rec} = \lceil sf(\psi) \times N_{rec}(R) \rceil$$



## 4.2.6 Operators for Grouping

**GroupBy**( $O, \{A_i\}, \{f_i\}$ ) Returns the records of  $O$  sorted on  $\{A_i\}$ , applying the aggregation functions  $\{f_i\}$ . The records in  $O$  must already be sorted beforehand. It costs

$$C = C(O)$$

**HashGroupBy**( $O, \{A_i\}, \{f_i\}$ ) Returns the records of  $O$  grouped by  $\{A_i\}$ , applying the aggregation functions  $\{f_i\}$ . The records are not sorted on  $\{A_i\}$ . The grouping is done using two phases, like HashDistinct. In the first phase, called partitioning phase, a partition is created using the hash function  $h_1$ ; in the second phase, called grouping, the records of each partition are grouped using the hash function  $h_2$  applied to all grouping attributes. When two records with the same grouping attributes are found, a step to compute the aggregate function is applied. The operator costs

$$C = C(O) + 2 \times N_{pag}(O)$$

For both the previous two operators, the result size is calculated as for the duplicate elimination. If there's only one attribute in  $O$ , then the result size is

$$E_{rec} = N_{key}(A)$$

If instead it contains multiple attributes, the result size is

$$E_{rec} = \min(|O|/2, \prod_i N_{key}(A_i))$$

## 4.2.7 Operators for Join

**NestedLoop**( $O_E, O_I, \psi_J$ ) Joins the external operand  $O_E$  with the internal operand  $O_I$  with the following algorithm:

---

```

for  $r \in O_E$  do
  for  $s \in O_I$  do
    if  $\psi_J$  then
      If  $\psi_J$ , add  $\langle r, s \rangle$  to the result.
    end if
  end for
end for

```

---

It costs

$$C = C(O_E) + E_{rec}(O_E) \times C(O_I)$$

The result size is

$$E_{rec} = sf(C_j) \times E_{rec}(O_E) \times E_{rec}(O_I)$$

**PageNestedLoop**( $O_E, O_I, \psi_J$ ) Joins the external operand with the internal operand by scanning  $O_I$  once per page of  $O_E$  (and not once per record, as for NestedLoop). The algorithm used is the following:

---

```

for  $p_r$  of  $O_E$  do
  for  $p_s$  of  $O_I$  do
    for  $r \in p_r$  do
      for  $s \in p_s$  do
        If  $\psi_J$ , add  $\langle r, s \rangle$  to the result.
      end for
    end for
  end for
end for

```

---

The cost of the operator is

$$C = C(O_E) + N_{pag}(O_E) \times C(O_I)$$

The algorithm cost is lower when the external operand is the one with fewer pages. The result size is

$$E_{rec} = sf(C_j) \times E_{rec}(O_E) \times E_{rec}(O_I)$$

**BlockNestedLoop**( $O_E, O_I, \psi_J$ ) Joins the external operand  $O_E$  with the internal operand  $O_I$  by extending PageNestedLoop using more memory for a group of pages of the external operand. Assume the operands are TableScan of tables  $R$  and  $S$ , and that the query processor has  $B+2$  pages in the buffer.  $B$  pages are used for the external operand, 1 page for an input page of  $S$ , and 1 page is reserved as the output buffer. For each record  $r$  of a page group of  $R$ , and for each joining record  $s$  of a page in  $S$ ,  $\langle r, s \rangle$  is written to the output buffer page.

The cost of the operator is

$$C = N_{pag}(R) + \lceil N_{pag}(R)/B \rceil \times N_{pag}(S)$$

The cost is lower if the external relation has fewer pages than the internal one. If the  $B$  pages are enough to contain one of the two relations, then the cost is reduced to

$$N_{pag}(R) + N_{pag}(S)$$

The result size is

$$E_{rec} = sf(C_j) \times E_{rec}(O_E) \times E_{rec}(O_I)$$

This operator is not convenient to use when the operators require too many pages (i.e.,  $N_{pag}R \geq B^2$ ).

**IndexNestedLoop**( $O_E, O_I, \psi_J$ ) This operator requires that there is an index on the join column of the internal operand, and performs a join with the following algorithm:

---

```

for  $r \in O_E$  do
  for  $s \in \text{IndexFilter}(O_I, I, O_E.e1 = O_I.i1)$  do
    Add  $\langle r, s \rangle$  to the result.
  end for
end for

```

---

It costs

$$C = C(O_E) + E_{rec}(O_E) \times (C_I + C_D)$$

where  $C_I$  and  $C_D$  are the costs to retrieve the relevant index records and the data from disk. If the internal operand is an  $\text{IndexFilter}(S, I, \psi_J)$ , the result size is

$$E_{rec} = \lceil sf(\psi_J) \times E_{rec}(O_E) \times N_{rec}(S) \rceil$$

if instead it is a  $\text{Filter}(\text{IndexFilter}(S, I, \psi_J), \psi)$ , the result size is

$$E_{rec} = \lceil sf(\psi_J) \times E_{rec}(O_E) \times (sf(\psi) \times N_{rec}(S)) \rceil$$

**MergeJoin**( $O_E, O_I, \psi_J$ ) This operator requires that  $O_E$  and  $O_I$  are sorted on the same join attributes, and that in the join condition,  $O_E.A_i$  is a key of  $O_E$ . Since this join attribute has distinct values in  $O_E$ , the algorithm reads the records of  $O_E$  one by one, and reads all records of  $O_I$  with the same values (which will be found one after the other). This operator costs

$$C = C(O_E) + C(O_I)$$

The result size is

$$E_{rec} = \lceil sf(\psi_J) \times E_{rec}(O_E) \times E_{rec}(O_I) \rceil$$

**HashJoin**( $O_E, O_I, \psi_J$ ) Returns the join result with a hash technique in two phases. In the first phase, called partitioning phase, the records of both operands are partitioned using the hash function  $h_1$ , similarly to HashDistinct. In the second phase, called **probing** (or **matching**), for each  $B_i$  partition, the records of  $O_E$  are read and inserted into the buffer hash table with  $B$  pages using the hash function  $h_2$ . The records of  $O_I$  are read one page at a time,  $h_2$  is applied to them, and if there is a match with the records in  $O_E$ , the joined record is added to the result.

Assuming  $N_{pag}(O_E)/B < B$  and that the pages are uniform, the cost of the operator is

$$C = C(O_E) + C(O_I) + 2 \times (N_{pag}(O_E) + N_{pag}(O_I))$$

where  $(C(O_E) + C(O_I) + (N_{pag}(O_E) + N_{pag}(O_I)))$  is the cost of the partitioning phase, and  $(N_{pag}(O_E) + N_{pag}(O_I))$  is the cost of the probing phase. However, if the pages are not uniform, the resulting partitions will not have the same size, they may not fit in  $B$ . The cost can be generalized to

$$C = (\log_B(N_{pag}(O_E)) \times 2 - 2) \times (N_{pag}(O_E) + N_{pag}(O_I))$$

If  $N_{pag}(O_E) < B$ , the cost is 0.

The result size is

$$E_{rec} = \lceil sf(\psi_J) \times E_{rec}(O_E) \times E_{rec}(O_I) \rceil$$

# Chapter 5

## Query Optimization

The optimizer is a key component of the Query Manager. Its role is to select the optimal physical plan to execute queries using the operators and data structures provided by the Storage Engine. This chapter will show how functional dependencies are used for not only relational schema design, but also for optimization.

### 5.1 Query Processing and Execution

In general, there are many strategies to execute a query, in particular when it is complex. The problem of optimizing a query is influenced by the fact that a query can be written in several equivalent ways, and relational algebra operators can be implemented using different physical operators.

Query processing is divided into four stages:

- **Query analysis**, in which the correctness of the SQL query is checked, and the query is translated into its internal form, typically based on relational algebra;
- **Query transformation**, in which the logical plan is transformed into an equivalent one that provides a better query performance;
- **Physical plan generation**, in which alternative physical plans are generated and evaluated, of which the one with the lowest cost is chosen;
- **Query evaluation**, in which the chosen physical plan is executed.

Query transformation and Physical plan generation are often considered part of the same phase, and are called Query optimizer.

The most interesting transformations regard Distinct elimination, GroupBy elimination, Where-subquery elimination, and View elimination.

## 5.2 Functional Dependencies

### Functional Dependency

Given a relation schema  $R$  and  $X, Y$  subsets of attributes of  $R$ , a functional dependency  $X \rightarrow Y$  (read as “ $X$  determines  $Y$ ”) is a constraint such that, for every possible instance  $r$  of  $R$  and for any two tuples  $t_1, t_2 \in r$ :

$$t_1[X] = t_2[X] \implies t_1[Y] = t_2[Y]$$

A functional dependency is **trivial** if the consequent contains attributes also found in the antecedent:

$$XY \rightarrow X$$

A functional dependency is **atomic** if the consequent is composed of only one attribute:

$$X \rightarrow A$$

A functional dependency  $X \rightarrow A$  is **canonical** if:

$$X \rightarrow A$$

holds true, but

$$X' \rightarrow A, \forall X' \subset X$$

does not. Every non-trivial dependency also contains one or more canonical dependencies, obtained by removing extraneous attributes.

A **key** is a set of attributes  $K$  such that:

$$K \rightarrow T$$

holds and is canonical.

The **union rule** states that:

$$X \rightarrow A_1 \dots A_n \iff X \rightarrow A_1, \dots, X \rightarrow A_n$$

To specify that an attribute has a constant value for all tuples, the rule used is:

$$\emptyset \rightarrow Y$$

### Logical Implication

Given a set of functional dependencies  $F$  on a relation schema  $R$ , a functional dependency  $X \rightarrow Y$  is derived (implied) from  $F$  if every instance of  $R$  that satisfies  $F$  also satisfies  $X \rightarrow Y$ :

$$F \vdash X \rightarrow Y$$

This property holds if  $X \rightarrow Y$  can be derived from  $F$  using any of **Armstrong's axioms**:

- $Y \subseteq X \implies X \rightarrow Y$  (Reflexivity)
- $X \rightarrow Y, Z \subseteq T \implies XZ \rightarrow YZ$  (Augmentation)
- $X \rightarrow Y, Y \rightarrow Z \implies X \rightarrow Z$  (Transitivity)

To test whether a functional dependency is implied by a set of functional dependencies, the **closure** of the antecedent can be calculated.

### Closure of Attribute Set

Given a schema  $R \langle T, F \rangle$ , and  $X \subseteq T$ , the closure of  $X$  is:

$$X^+ = \{A_i \in T \mid F \vdash X \rightarrow A_i\}$$

The following theorem holds true.

### Theorem

$$F \vdash X \rightarrow Y \iff Y \subseteq X^+$$

Consider a query on a set of tables  $R_1(T_1), \dots, R_n(T_n)$ , such that no attribute name appears in two tables. After joining the tables and performing a Select, assuming the Where condition  $C$  is in CNF, these dependencies hold on the final result:

- $K_{ij} \rightarrow T_i \ \forall K_{ij} \text{ key of } T_i$ ;
- $\emptyset \rightarrow A \ \forall A = c \text{ in } C$ ;
- $A_i \rightarrow A_j \text{ and } A_j \rightarrow A_i \ \forall A_i = A_j$ .

## 5.3 Eliminations

### 5.3.1 Distinct Elimination

Distinct normally requires a physical plan with duplicate elimination, and data must be grouped, usually via a sort operation (which is expensive). A query with a Distinct clause is translated into a relational algebra expression with the projection and duplicate elimination operators. To decide whether this duplicate elimination operator is unnecessary, a functional dependency theory algorithm is used. Specifically, the following theorem is used:

#### Theorem

Let  $A$  be the set of attributes of the result and  $K$  the union of the attributes of the key for every table used in the query. If  $A \rightarrow K$ , then the duplicate elimination is unnecessary.

To find out whether  $A \rightarrow K$ , the closure of  $A$  is computed.

If the query contains a GroupBy clause, then the theorem holds for  $G$  (the grouping attributes) instead of  $K$ .

### 5.3.2 GroupBy Elimination

GroupBy also usually requires a sort operation. A GroupBy can be eliminated if either each group only has one record, or if there is only one group. The first case can be tested for as seen for Distinct, since it's equivalent to checking if the result contains duplicates. For the second case, we must check that the value of the grouping attributes is the same for each tuple; this is done by verifying that the closure of the empty set ( $\{\}^+$ ) contains all the grouping attributes.

If aggregation functions are used, Count will be replaced by 1, and  $\text{Min}(A)$ ,  $\text{Max}(A)$ ,  $\text{Sum}(A)$ , and  $\text{Avg}(A)$  will be replaced by  $A$ .

### 5.3.3 Where-subquery Elimination

This is one of the most common and important transformations. In general, to execute these queries, the optimizer will generate a physical plan for the subquery, which will be executed for each record processed by the outer query. We will assume all subqueries



have been converted to an equivalent form using Exists, and that no GroupBy appears in the subquery. Given a query in the form

```

SELECT  R1.A1,...,R1.An
FROM    R1
WHERE   [Condition C1 on R1 AND]
        EXISTS ( SELECT *
                  FROM    R2
                  WHERE   Condition C2 on R2 and R1 );

```

it is equivalent to

```

SELECT  DISTINCT R1.A1,...,R1.An
FROM    R1, R2
WHERE   Condition C2 on R1 and R2
        [AND Condition C1 on R1];

```

The Distinct is necessary in the join form when a (1:N) relationship exists between R1 and R2. Note that if only a subset of R1's attributes appears in the Select clause, this transformation will not be correct unless the original query has a Distinct in the outer query.

If the subquery has an aggregation function, then the unnested equivalent requires a GroupBy clause on the projection attributes. A well-known problem is the **count bug problem**, which arises when the aggregation function is Count. In this case, the unnested query join must be replaced by an outer join. An outer join is represented by a NATURAL RIGHT JOIN, NATURAL LEFT JOIN, or NATURAL FULL JOIN operator; the first one preserves all records from the left operand, the second one preserves all records from the right operand, and the third one preserves all records.

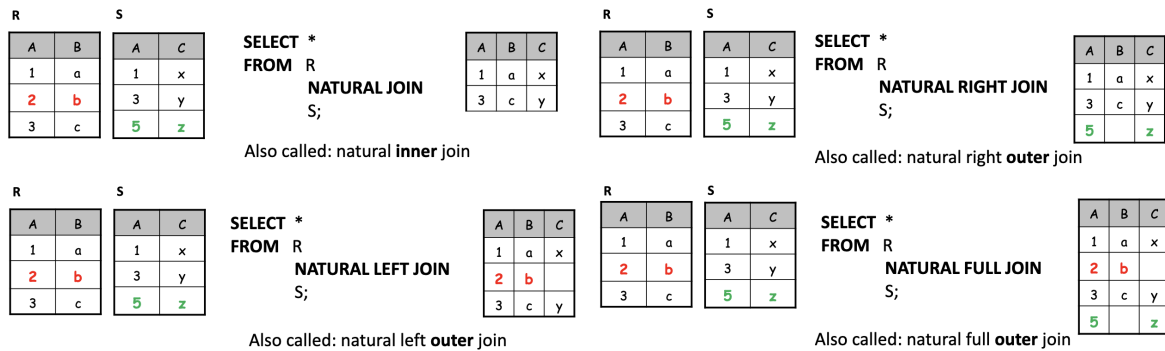


Figure 5.1: Types of join.

### 5.3.4 View Merging

Complex queries are easier to understand if views are used. The With clause defines temporary views available only to the query in which the clause occurs. When a query generates a view, the optimizer generates a physical sub-plan for the Select that defines the view, and optimizes the query considering the scan as the only operation available for the result of the view; with this technique, the view is optimized separately from the rest of the query.

In the logical plan, the transformation is made by replacing the reference to a view name with the corresponding logical plan. The new logical plan is then rewritten using equivalence rules of relational algebra to put it in the following canonical form:

$$\pi^b(\sigma(\gamma(\sigma(\bowtie_J R_i))))$$

The transformation of a query to avoid the use of views defined with a GroupBy generally requires pulling the GroupBy above a join, using the following algebraic equivalence rule:

$$(X_R \gamma_F(R)) \bowtie_{f_k=p_k} S \equiv X_{R \cup A(S)} \gamma_F(R \bowtie_{f_k=p_k} S),$$

where  $X_R$  is a set of attributes of  $R$ ,  $f_k \in X_R$  the foreign key of  $R$ , and  $p_k$  the primary key of  $S$  of attributes  $A(S)$ .

## 5.4 Physical Plan Generation

With eliminations, a “random” physical plan is generated for the query, which is then optimized. Generation, on the other hand, directly finds the best possible physical plan, in two steps: generation of alternative physical query plans, and choice of physical query plan with the lowest estimated cost. To estimate the cost of the entire plan, it is necessary to estimate the cost of the physical operator and the size of the result of every node in the tree (in a bottom-up fashion). The following sections will show how to choose the physical query plan of minimum cost for different types of queries.

### 5.4.1 Single-Relation Queries

For these queries, the only question to solve is whether to use indexes when accessing the data instead of performing a simple TableScan. Some relations may have single or multiple indexes defined on one or more of their attributes; in that case, the cost of reading the entire table is compared against the cost of reading the index and retrieving the data using the RIDs contained in the index. Usually, using an index is better if the selectivity factor of the query is restrictive enough. A special case happens when the

attributes appearing in the Select are included in the prefix of the key of an index of the relation; the query can be evaluated by only reading the index itself, which is much faster than reading the whole table.

### 5.4.2 Multiple-Relation Queries

The most important issue in these queries is the order in which the relations are joined. Every permutation of relations yields the same result but corresponds to a different plan; given  $n$  relations, there are  $n!$  different permutations, each of which generates a huge number of candidates depending on the specific joins performed in the plan. Additionally, there are different choices for the specific physical operator used to implement the join, increasing the total number of possible plans.

The full search in the space of candidates starts by finding which relation is cheaper to access (representing the operator as a standalone plan). Then, the second cheapest plan is chosen among the ones not selected in the previous step and the ones that would be generated by a join of the previously chosen relation with a different one, and so on until the entire query is covered by the physical plan. At each step, the only plans evaluated are the ones behind a so-called “frontier”, meaning all plans that are direct children of either the (empty) root of the entire search or a plan that has been selected as a minimum cost one.

This algorithm can be incredibly efficient for simpler queries and incredibly slow for complex ones. In the latter case, the algorithm will tend to backtrack to higher levels in the “tree” of physical plans explored. A simple pseudocode for this algorithm is presented below.

---

**Algorithm 4** Full search pseudocode.

---

```

1: Initialize Plans to the best plans to access each relation in the query.
2: loop
3:   Extract the fastest plan  $P$  from Plans.
4:   if  $P$  is complete then
5:     return  $P$ 
6:   end if
7:   for  $R$  not in  $P$  do
8:     Put the best plan between  $P \bowtie R$  and  $R \bowtie P$  in Plans.
9:   end for
10:  Remove  $P$ .
11: end loop

```

---

Several heuristics have been proposed that can help speed up the algorithm, meaning

that the algorithm may not find the optimal physical plan but one that is good enough. The most commonly used heuristics are:

- **Limitation in the number of successors:** each permutation is evaluated by associating the join operators only to the left, creating **left-deep** trees, where each node from the root up until the second-to-last level has a join as a left child and a relation as a right child (as opposed to **right-deep** and **bushy** trees). A left-deep tree has the advantage of allowing the use of an index nested loop join operator.

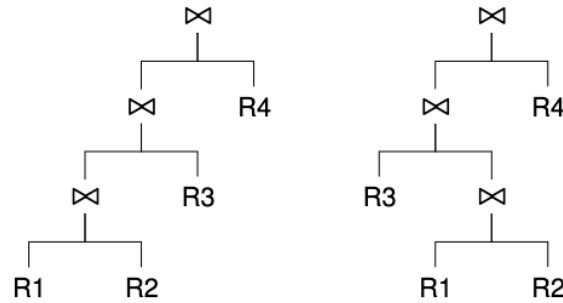


Figure 5.2: Left-deep tree on the left, bushy tree on the right.

- **Greedy search:** once the logical node of minimum cost has been expanded, the other nodes are not considered anymore, avoiding any backtracking. In general, solutions found using a greedy search are suboptimal, but thanks to the fact that it is found in less time, this search is usually the default one used by DBMSs.
- **Iterative full search:** a possibility is to use a mixed approach. The full search is made up to a predetermined number of levels, then the best node to expand is chosen, and, as in the greedy search, the other nodes will not be considered any longer. The full search will continue for the predetermined number of levels, and so on.
- **Interesting orders:** when the merge-join operator is available, and the query result must be sorted because of the presence of an OrderBy or a GroupBy, it is useful to organize the search as follows: at each step, for each logical query subexpression, the preserved query plans will be the one with minimum cost as well as the best plans producing an interesting order of the records potentially useful for the final query plan.

### 5.4.3 Other Queries

#### Queries With GroupBy

If the GroupBy is necessary, the optimizer produces a physical plan for the Select only, sorting the data on the grouping attributes; this plan is then extended with the physical operator for the GroupBy and the one for the Project over the Select attributes. If an Having clause was specified, the physical plan is also extended with a selection operator, and the GroupBy computes whatever aggregation function used in the Having and Select clauses.

**Exchanging with a Join** If the query requires a Join, it may be convenient to GroupBy before the Join (with the constraint that the GroupBy is done on the same attributes used in the Join); often, however, Joins are submultiplicative, so moving it above the GroupBy may make the plan more expensive. The equivalence rules for this transformation are done under these assumptions:

- The tables do not have null values, and primary and foreign keys have only one attribute;
- The queries are a single Select with GroupBy and Having, but without any sub-select, Distinct, or OrderBy clauses;
- The Select includes all grouping attributes.

Then, the pre-grouping problem is: when does this equivalence rule:

$$X\gamma_F(R \bowtie_{f_k=p_k} S) \equiv ((X'\gamma_{F'}(R)) \bowtie_{f_k=p_k} S)$$

hold?

The fundamental condition is that the join is unary w.r.t. the attributes  $X$ , meaning that it produces exactly one record for each value of that attribute. This is true under the following conditions:

- Let  $C_j$  be the Join condition; then  $C_j \vdash X \rightarrow A(S)$ , producing one record from  $S$  for every group;
- Each aggregate function only uses attributes from  $R$ .

**Exchanging with a Filter** For this transformation, we need to find if the following equivalence rule holds:

$$\sigma_\phi(X\gamma_F(E)) \equiv X\gamma_F(\sigma_\phi(E))$$

This equivalence rule is typically used when the query contains an Having clause, or it uses a view that specifies a condition on its attributes. There's two possible cases; either the selection is done on the dimensions of a table, or it is done on the results of aggregate functions in the GroupBy.

The first case is simple:

$$\sigma_{\phi_X}(X\gamma_F(E)) \equiv X\gamma_F(\sigma_{\phi_X}(E))$$

If the restriction is done on the same attributes on which the GroupBy is performed, it can be moved below. However, this rule is rarely used, since these conditions are normally specified in the Where clause and not the Having clause, so they already appear below GroupBys.

The second case is more complicated:

$$\sigma_{\phi_F}(X\gamma_{AGG(A_1) \text{ AS } F_1, \dots, AGG(A_n) \text{ AS } F_n}(E))$$

Equivalence rules can be built only in these two case

$$\begin{aligned} \sigma_{\phi_{Mb \geq v}}(X\gamma_{MAX(b) \text{ AS } Mb}(E)) &\equiv X\gamma_{MAX(b) \text{ AS } Mb}(\sigma_b \geq v(E)) \\ \sigma_{\phi_{mb \leq v}}(X\gamma_{MIN(b) \text{ AS } mb}(E)) &\equiv X\gamma_{MIN(b) \text{ AS } mb}(\sigma_b \leq v(E)) \end{aligned}$$

# Chapter 6

## Transactions

The Storage Engine offers features aimed at solving recovery and concurrency problems, guaranteeing that each operation performed by the user is executed such that the user does not notice any underlying failure, and that there are no interferences with other operations running concurrently. The solutions to these problems are based on a mechanism called **transaction**.

### Transaction

A transaction is a sequence of operations on the database and on temporary data, with the following properties:

- **Atomicity:** only successful transactions change the state of the database; if a transaction is interrupted the database must remain unchanged as if the transaction was never started;
- **Isolation:** when a transaction is executed concurrently with others, the final effect must be the same as if it was executed alone;
- **Durability:** the effects of committed transactions must survive system and media failures.

Often, the acronym **ACID** (**A**tomicity, **C**onsistency, **I**solation, and **D**urability) is used to refer to the properties of transactions. The Recovery Manager ensures Atomicity and Durability, while the Concurrency Control Manager ensures Isolation. Consistency is guaranteed by the implementation of integrity constraints and code correctness.

For the DBMS, a transaction  $T$  requires a number of read/write operations on the database. Each transaction starts and ends with the following transaction operations:

- *beginTransaction*, signaling the start of the transaction;
- *commit*, signaling the successful termination of the transaction, and requiring the system to make its updates durable;
- *abort*, signaling the abnormal termination of the transaction, requiring the system to undo its updates.

While a *commit* is only used as a command in the code, **abort** can be either specified in the code or it can be used by the system. The execution of a **commit** does not automatically mean that the transaction will successfully terminate, because its updates may not be written on permanent memory. Figure 6.1 shows the state transition diagram for transaction execution. To read a page ( $r_i[x]$ ), it is brought into the buffer

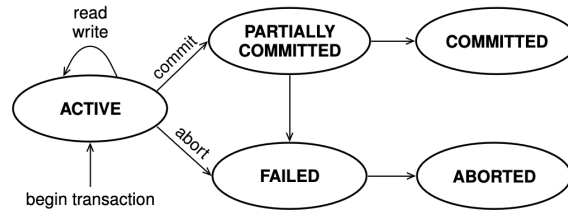


Figure 6.1: State transition diagram for transaction execution.

from the disk (if it's not already in the buffer), and then read. To write a page ( $w_i[x]$ ), an in-memory copy is modified, which will later be written to disk when the Buffer Manager find it appropriate to do so. This delayed writing has to be compatible with Atomicity and Durability, since multiple transactions may want to write to the same page.

## 6.1 Failures

A database can become inconsistent because of three types of failures:

- **Transaction failure**, an interruption of a transaction which does not damage the content of either the main memory or the permanent memory. A transaction can be interrupted because either it meets certain conditions, it violates integrity constraints, or the concurrency manager chooses to abort it because it is involved in a deadlock;
- **System failure**, an interruption (crash) of the system (DBMS or OS) in which the content of the main memory is lost, but the content of the content of the



permanent memory remains intact. After crashes occur, the system is restarted, automatically or by an operator;

- **Media failure** (also called **disaster**), an interruption of the system in which content of the permanent memory is lost or damaged. When a media failure happens, the Recovery Manager uses a backup to restore the database.

Other than database backups, another protection from failures is represented by **log files**: these files contain lines recording each transaction operation executed in the system, including aborted transactions. For each transaction, the information written is when it starts, when it commits, when it aborts, and when it modifies a records, specifying the page the record is in, and the old and new values (called **before image** and **after image**). Each record is uniquely identified by a LSN (Log Sequence Number), assigned in a strictly increasing order.

A recovery algorithm requires an **undo** if an update of some committed transaction is stored in the database. An *undo* is needed when a transaction or system failure occurs, copying the before image of the page from the log to the database. A recovery algorithm requires a **redo** if a transaction is committed before all of its updates are stored in the database (after a system failure), copying the after image in the log to the database.

The downtime of the system is given by the product between the failure rate and the recovery rate. The failure rate cannot be reduced, as we cannot know in advance if a transaction contains an error, or a system/media failure happens. The way to reduce downtime is to reduce recovery time. In practice, this is done via **checkpoints**. There's different types of checkpoints:

- **Commit-consistent checkpoint**: when a checkpoint starts, the activation of new transactions is suspended, and the system waits the termination of active transactions; all “dirty” pages in the buffer are written to permanent memory; the checkpoint is written to the log file, and a pointer to the corresponding record is stored in a special file called **restart file**. The system then resumes normal activity. This strategy is simple but inefficient, since the system has to regularly stop.
- **Buffer-consistent checkpoint - Version 1**: similar to the previous type, but once the checkpoint starts, it also suspends the execution of currently active transactions. This strategy is more efficient than the previous, but it is still slow because of the buffer flushing operations.

- **No stop checkpoint:** once the checkpoint starts, the checkpoint is written to the log file, along with the ids of currently active transactions; a new thread is started, which scans the buffer and flushes the dirty pages it finds in parallel with the standard transactions, guaranteeing that all pages that were dirty at the beginning of the checkpoint are flushed before its end.

### 6.1.1 Recovery from System and Media Failures

In order to recover the database, the *restart* operator is invoked, bringing the database in its committed state with respects to the execution up to the system failure, and restarting the normal system operations. The first task is done using a recovery algorithm of which a simple version will be described. This algorithm has two phases, **rollback** and **rollforward**. In the rollback phase the log is read backwards, to undo updates of transactions that were not terminated before the crash, and to find the identifiers of the transactions which terminated successfully. In particular, two sets are constructed: the **redo-list** and the **undo-list**. Until the first checkpoint record is found, these operations are done:

1. If a record is  $(commit, T_i)$ ,  $T_i$  is added to the redo-list.
2. If a record is an update of a transaction  $T_i$  not in the redo-list, it is added to the undo-list.
3. If a record is  $(begin, T_i)$ ,  $T_i$  is removed from the undo-list.
4. If a record is a checkpoint  $(CKP, L)$ , for each  $T_i \in L$  if  $T_i$  is not in the redo-list it is added to the undo-list. If the undo-list is not empty, the rollback phase continues until it is completely emptied.

In the rollforward phase, the log is read onward from the first record after the checkpoint, redoing all operations of the transactions in the redo-list.

The restart is executed at the buffer level, not on the persistent store: undos and redos are done by first loading the data in the buffer, and then pages are eventually flushed in a second time.

The algorithm described above is the standard Undo-Redo algorithm, but there exist variants:

- **NoUndo-Redo:** requires that all the updates of a transaction must be in the database after the transaction has committed. It uses a **NoSteal (Pin) Policy**, where all the buffers used by transactions are pinned, and those pages will not be flushed to disk until the transaction commit. This way, no operation ever needs

to be undone. It is dangerous because it pins all those pages used by the active transactions, limiting the freedom of the buffer manager.

- **Undo-NoRedo**: requires that all the updates of a transaction must be in the database before the transaction has committed. It uses a **Force** policy, where buffer pages used by transactions are forcibly flushed before committing. This approach has two problems: it does not work for media failures, and it is costly since it requires a lot of writes to disk.
- **NoUndo-NoRedo**: requires that all the updates of a transaction must be in the database neither before nor after the transaction has committed. It uses NoSteal and Force policies.

Undo-Redo uses Steal and NoForce policies.

NoUndo-NoRedo requires a way to write many pages atomically. This is done using **shadow pages**. When a transaction updates a page for the first time, a new database page is created, called **current page**, with a certain address  $p$ . The old page in the database is unchanged, and becomes a shadow page. The **New Page Table** (a copy of the Page Table containing all physical addresses of pages) is updated so that the first element contains the physical address  $p$  of the current page. All subsequent write and read operations on that page will operate on the current page.

Once the transaction reaches the commit point, the system substitutes all shadow pages with an atomic actions: first, all the pages updated in the buffer are written to the permanent memory, while the Page Table is left unchanged; then, the descriptor of the database is updated with an atomic operation, replacing the pointer to the Page Table with that to the New Page Table, which becomes the Page Table.

There are some optimizations of the algorithm:

- Setting the log granularity at a record level instead of page level;
- Buffering the log;
- Writing in pages the LSN of the last operation executed;
- Logging undo actions;
- Adding to each log entry the LSN of the previous entry for the same transaction.

# Chapter 7

## Concurrency

When transactions are executed concurrently, their operations are often interleaved, meaning that the execution of the operations of one transaction alternates with the execution of the operations of the other. This may cause interferences that leave the system in an inconsistent state, and it is responsibility of the Concurrency Manager to prevent this from happening. We assume all transactions are consistent, so if a transaction were to be executed in isolation it would not violate any constraint. There are three types of possible conflicts arising during concurrent execution:

- **Dirty Reads (Write-Read conflicts)**: one uncommitted transaction writes on some data  $x$ , and the other reads that same  $x$  after the write operation has been completed. If the first transaction aborts, the changes to  $x$  should not have had an effect on the execution of the second one.
- **Unrepeatable Read (Read-Write conflict)**: a transaction reads the same data  $x$  twice, but between the two reads, a write operation on  $x$  by another transaction is scheduled. The first transaction will read two different values of  $x$ , despite expecting them to be the same for both reads.
- **Lost Update (Write-Write Conflict)**: two transactions read the value of the same data  $x$  (with no conflict), but then both update  $x$  with a new value. Whichever transaction gets to update  $x$  last is the one whose change will have an effect on the database, regardless of when it started w.r.t. the other one.

A simple way to avoid interference is to allow only **serializable execution**.

### Serial Execution

An execution of a set of transactions  $T = \{T_1, \dots, T_n\}$  is serial if, for every pair of transactions  $T_i$  and  $T_j$ , all the operations of  $T_i$  are executed before the ones of  $T_j$ , or vice-versa.

However, serial execution is unpractical, since one transaction is executed at a time, stopping the others from accessing the data for potentially long periods of time. To make sure that the database stays in a consistent state, it is sufficient that the system guarantees that the execution of interleaved transactions is **serializable**.

### Serializable Execution

An execution of a set of transactions  $T$  is serializable if it has the same effect in the database of some serial execution of the set of committed transactions  $T' \subseteq T$ .

Aborted transactions are ignored since they should not change the state of the database. Since serial executions are correct, any serializable execution is also correct by virtue of having the same final effect.

## 7.1 Histories

A transaction is a sequence of read/write operations. An **history** is used to represent the interleaved execution of multiple transactions.

### History

Let  $T = \{T_1, \dots, T_n\}$  a set of transactions. A history  $H$  on  $T$  is an ordered set of operations such that:

- The operations of  $H$  are those of  $T_1, \dots, T_n$ ;
- $H$  preserves the ordering between the operations belonging to the same transaction.

A history is an actual (or potential) execution order of the operations of a set of transactions; for example, given the transactions:

$$T_1 = r_1[x], r_1[y], w_1[x], c_1$$

$$T_2 = r_2[y], r_2[z], c_2$$

$$T_3 = w_3[x], w_3[y], c_3$$

a history may be:

$$H = r_1[x], r_2[y], r_1[y], w_3[x], w_3[y], w_1[x], c_1, r_2[z], c_3, c_2$$

In an history, two operations of different transactions can be **in conflict**, i.e., they are on the same data item and at least one of them is a write operation. In the example above,  $r_1[x]$  and  $w_3[x]$  are in conflict.

### Equivalent Histories

Two histories  $H$  and  $L$  are equivalent if:

- They are defined on the same set of transactions;
- They produce the same final effect on the database.

A history is serializable if it is equivalent to a serial history. Equivalence between histories can be defined taking only into account the order of operations in conflict:

### c-Equivalent Histories

Two histories  $H$  and  $L$  are c-equivalent (conflict-equivalent) if:

- They are defined on the same set of transactions;
- They have the same order of operations in conflict of committed transactions.

This definition of c-equivalence is motivated by the fact that the result of concurrent execution of  $T_1, \dots, T_n$  depends only on the order of execution of the operation in conflict: if two operations are not in conflict, they will always have the same final result on the database regardless of their ordering.

### c-Serializable History

A history of transactions  $T$  is c-serializable if it is c-equivalent to a serial history on the same transactions of  $T$ .

c-serializability always implies serializability, but not vice-versa.

Although it is possible to examine a history  $H$  and decide whether or not it is c-serializable using reordering of operations, there is another simpler way to proceed based on the analysis of a particular graph derived from  $H$ , called **serialization graph**.

### Serialization Graph

Let  $H$  be a history of committed transactions  $T = \{T_1, \dots, T_n\}$ . The serialization graph of  $H$ , denoted  $SG(H)$ , is a directed graph such that:

- There is a node for every committed transaction in  $H$ ;
- There is a directed arc  $T_i \rightarrow T_j, i \neq j$ , if and only if some operation  $p_i$  in  $T_i$  appears before and conflicts with some operation  $p_j$  in  $T_j$ .

Two transactions  $T_i$  and  $T_j$  in  $H$  are in conflict if the arc  $T_i \rightarrow T_j$  appears in  $SG(H)$ .

### c-Serializability Theorem

A history  $H$  is c-serializable if and only if its serialization graph is acyclic.

If the serialization graph is acyclic, a serial schedule can be obtained with a topological ordering on the graph.

## 7.2 Serializability with Locking

Analyzing the serialization graph can verify a posteriori if a history is c-serializable; in practice, serialization graphs are not constructed. The c-serializability theorem, however, can be used to prove that the scheduling algorithm for the concurrency control used by a scheduler is correct.

### 7.2.1 Strict Two-Phase Locking (2PL)

Strict Two-Phase Locking is the most commonly used scheduling protocol in commercial systems. Under this protocol, each data item used by a transaction has a lock associated with it, a **read lock** (shared), or a **write lock** (exclusive). Two rules are followed:

- If a transaction wants to read (write) a data item, it first requests a shared (exclusive) lock on the data item. Before a transaction can access a data item, the scheduler first examines the lock associated with the data item. If no other transaction holds the lock, then the data item is locked; otherwise, the transaction must wait until the lock is released.
- All locks held by a transaction are released together the moment it commits or aborts.

Lock-granting policies are described by the **compatibility matrix**, where each row corresponds to a lock that is already held on an element  $x$  by another transaction, and each column corresponds to the mode of a lock on  $x$  that is requested (here “S” stands for “shared” and “X” stands for “exclusive”): In short, if an item has a read lock, it

	S	X
S	y	n
X	n	n

Table 7.1: Compatibility matrix for shared/exclusive locks.

can receive more read locks but no write locks. If it has a write lock, no more locks of any kind can be placed.

Locks are handled by a scheduler, which tracks all locks granted to transactions and on which data items: each lock is a triple  $(T, mode, x)$ . When a transaction asks for a lock on an item, it is granted if possible (according to the above table), otherwise the transaction is suspended and added to a **wait queue** (hashed on the item). Once a transaction commits or aborts, all the locks it held are released, and any waiting transaction is notified according to a specific policy.

#### Theorem

A strict 2PL protocol ensures c-serializability.



## 7.2.2 Deadlocks

The scheduler needs a strategy to detect **deadlocks**, situations in which a transaction  $T_i$  has locked an item  $A$  and requests a lock on item  $B$ , while at the same time, a transaction  $T_j$  has locked item  $B$  and requests a lock on item  $A$ . A deadlock occurs because none of the transactions can proceed.

### Deadlock Detection

A simple strategy is using a **wait-for graph** in which each node is a transaction, and a directed edge between two transactions  $T_i$  and  $T_j$  means that  $T_i$  is waiting for  $T_j$  to release a lock on one of its objects. If a cycle occurs in the graph, a deadlock has occurred, and one of the transactions involved must abort, usually the youngest (chosen on the basis of some metric, such as newest timestamp, lowest number of locks, etc.).

In real applications, managing this graph can become very expensive. Either the existence of wait cycles may be controlled at predetermined time intervals, or the graph is not constructed and instead a timeout strategy is used: if a transaction waits to get a lock on a data item for more than *timeout*, the scheduler assumes a deadlock has happened and aborts the transaction. This solution, however, causes thrashing: the system may accidentally start killing transactions which are not involved in deadlocks, in turn slowing down transaction execution. In some DBMSs (such as PostgreSQL), a shorter deadlock timeout is used instead; if this timeout expires, the system builds a local wait-for graph for that transaction, and if the graph contains a loop the transaction is killed.

### Deadlock Prevention

Another strategy that instead prevents deadlocks from ever happening is the following: each transaction  $T_i$  receives a timestamp  $t_s(T_i)$  when it starts; if  $t_s(T_i) < t_s(T_j)$ , then  $T_i$  is older than  $T_j$ . Each transaction has a priority assigned to it, such that the older is a transaction, the higher priority it has.

When a transaction  $T_i$  requests a lock on a data item that is already locked on by another transaction  $T_j$ , two algorithms are possible:

- **Wait-Die:** if  $T_i$  is older than  $T_j$  it waits until  $T_j$  terminates, otherwise aborts.
- **Wound-Wait:** if  $T_i$  is older than  $T_j$  it aborts it, otherwise it waits until  $T_j$  terminates.

In both cases, when the killed transaction is restarted, it keeps the same priority (timestamp) it had originally. Both algorithms ensure no starvation. Wait-Die tends to roll

back more transactions, but those transactions are also the ones who tend to have done less work since they're younger.

Wait-Die and Wound-Wait are easier to implement than wait-for graphs, and they also tend to kill a huge amount of transaction (as opposed to wait-for graphs who only kill transactions which are presumed to be involved in a deadlock).

## 7.3 Serializability without Locking

The previous methods are called **pessimistic**, because they assume that operations of different transactions are very likely to conflict, and act accordingly. Methods that don't use locks are called **optimistic**: transactions are free to execute their operations, and the system only controls that no errors have happened.

One such method, used by Oracle, is **snapshot isolation**. In this solution, all reads and writes are done without locks. Each transaction  $T_i$  reads the data out of a database version called **snapshot**, containing the state of all data items as they were modified by all transactions committed before it. All the write operations done by the transaction are collected in a dedicated **write set**  $WS_i$  and they are visible only by  $T_i$  but not other transactions. If a transaction executes a write, it can only commit if its write set does not intersect with another committed transaction's write set. If the intersection is not empty, the transaction is aborted: this is called the "First-Committer-Wins" rule.

This solution permits non-serializable executions.

## 7.4 Multiple-Granularity Locking

The locking techniques presented up until now assume that locks are taken for single records. In real applications, transactions may operate on collections of records, so these record-level locks are not enough to guarantee a consistent state of the database. On the other hand, if only table-level locks are provided by the DBMS, transactions that only write on single records will have to lock the entire table they are found in, slowing down execution.

Other techniques have been developed to support locks with different granularity (database, files, page, record, fields), such that an inclusion relationship is defined across the levels. If a transaction gets an **explicit** lock on a data object, it also has an **implicit** lock on any "child" object as well; i.e., if a transaction has a lock on a table, it also has a lock on its records and each record's field. Low granularity locks allow more concurrency, but also cause more lock overhead and higher deadlock probability.

High granularity locks allow less concurrency, but cause less overhead and less chance of deadlock.

To manage these locks, the *S* and *X* locks are not enough, so a new type is introduced, called **intention locks**. If a data object is locked in an intention mode, explicit locking is done at a finer granularity. Before a transaction can acquire an explicit lock on the object, it must also already hold an intention lock on all ancestors of that object in the granularity hierarchy. The intention lock types are:

- **Intentional Shared lock (IS)**: allows the explicit locking of the object's descendants in *S* or *IS* mode;
- **Intentional Exclusive lock (IX)**: allows the explicit locking of the object's descendants in *S*, *IS*, *X*, *IX*, or *SIX* mode;
- **Shared Intentional Exclusive lock (SIX)**: implicitly locks all descendants of the object in *S* mode, and allows the explicit locking of the object's descendants in *X*, *SIX*, or *IX* mode.

The need for the *SIX* lock is justified by the fact that some transactions may want to only read an object higher in the hierarchy, but write on objects lower in the hierarchy. If only *S* and *IX* locks were used, the transaction would have to hold both those lock types on the object higher in the hierarchy. The compatibility table for these locks is the one below (where the rows represent locks already held, and columns are locks requested by some other transaction).

	S	X	IS	IX	SIX
S	y	n	y	n	n
X	n	n	n	n	n
IS	y	n	y	y	y
IX	n	n	y	y	n
SIX	n	n	y	n	n

Table 7.2: Compatibility matrix of multi-granularity locks.

A problem that arises with multi-granularity locks is **phantom locking**. Imagine two transactions,  $T_1$  and  $T_2$ , which are executing the following operations:

- $T_1$ : SELECT \* FROM Students
- $T_2$ : insert into Students values (100, 'Rossi')
- $T_2$ : commit

- $T_1$ : SELECT \* FROM Students

$T_1$  locks the table record by record. Even if strict 2PL protocol is used, this history is still possible. This is because even if  $T_1$  has a lock on the data objects in the table Students,  $T_2$  is not updating or deleting an existing record, but inserting a new one, and  $T_1$  obviously cannot lock an object that cannot exist yet.

The same problem can be seen for the following cases:

- $T_1$ : SELECT \* FROM Students WHERE Surname='Rossi'
- $T_2$ : insert into Students values (100, 'Rossi')
- $T_2$ : commit
- $T_1$ : SELECT \* FROM Students WHERE Surname = 'Rossi'

and

- $T_2$ : DELETE FROM Students WHERE Surname='Rossi'
- $T_1$ : SELECT \* FROM Students WHERE Surname='Rossi'
- $T_2$ : abort
- $T_1$ : SELECT \* FROM Students WHERE Surname = 'Rossi'

In the latter case, the records on which an exclusive lock is held by  $T_2$  are deleted, thus deleting the lock as well.

To fix this problem, a new protocol is introduced, extending the strict 2PL one. This protocol is called **Multi-granularity Strict 2PL**, and adds these two rules:

1. A (non-root) node can be locked by a transaction  $T_i$  in *S* or *IS* mode only if the parent is locked by  $T_i$  in *IS* or *IX* mode;
2. A (non-root) node can be locked by a transaction  $T_i$  in *X*, *IX*, or *SIX* mode only if the parent is locked by  $T_i$  in *SIX* or *IX* mode.

# Chapter 8

## Physical Database Design

The design of a relational database has four phases:

- Requirements analysis, for the specification of data to be taken into account and the services to be implemented;
- Conceptual design, defining the representation of the entities of interest and their properties, associations, and integrity constraints;
- Logical design, defining the logical schema;
- **Physical design**, defining the appropriate storage structures used for the DBMS in order to guarantee the desired performances.

The information needed in order to work on the physical design of a database are:

- **Statistics**: information about number of records in each relation, record size, number of pages used, distinct values per attribute, maximum and minimum values, and a distribution (if not uniform);
- **Workload description**: a description of critical queries and updates and their frequency, along with their respective expected performances. For each critical query, this description specifies the relations and attributes used, the attributes used in selection and join conditions, and the selectivity factor of conditions. For updates, it also specifies the type (INSERT/DELETE/UPDATE).

This information is usually represented using **ISUD** (Insert, Select, Update, Delete) tables: for each application, they specify the execution frequency, the percentage of data used, and the type of operation;

- **Knowledge about the DBMS**: data organizations, indexes, and query processing techniques supported.

Once this information is known, decisions can be made for storage structures and indexes.

## 8.1 Database Design

### 8.1.1 Storage Structures

For the storage structures, a solution can be selected from the ones seen in the first chapter: sequential, heap, hash, or index organization. Heap organization is best for small databases where insertions are more frequent than searches, sequential organization is best if it's interesting to keep static data sorted on a key, hash organization is best if the most common operation is record search by a key, and finally index organizations can both keep data sorted on a key and support efficient equality and range searches.

### 8.1.2 Indexes

The main goal of indexes is to avoid a relation scan when few records are looked for. Systems will usually automatically define indexes on primary and secondary keys. They can speed up searches, but they occupy memory and can slow down updates of the attributes on which they are defined, since any change to the actual records must be reflected in the index as well. In general, indexes are unnecessary for relations that occupy very few pages, or for attributes that are not very selective. The problem of selecting useful indexes does not have a trivial solution, due to the large number of possibilities, which is why most commercial systems provide tools to assist in the resolution. In the absence of such tools, we must consider which are the critical queries and which plan the optimizer chooses for them, evaluating whether an index may improve performances.

For example, we should consider defining indexes on attributes used in queries that require sorting (OrderBy, GroupBy, Distinct, Set operations); on selective attributes in the WHERE clause, choosing the appropriate structure depending on the type of search (equality, range, multi-attribute); to improve joins with IndexNestedLoop. Indexes can be defined for single queries (local view) or for workloads (global view).

An index  $I$  is unnecessary if it is **subsumed** by another  $I_2$ , meaning that the attributes of  $I_1$  are included as prefix within those of  $I_2$ . For example, an index on a single attribute  $A$  is subsumed by an index on  $(A, B)$ , and both are subsumed by an index on  $(A, B, C)$ .

Two indexes supporting two queries can be **merged** together into one index supporting both queries. For example, if two queries caused the creation of indexes on  $(A, B)$  and  $(A, C)$ , respectively, they can be merged into  $(A, C, B)$ .

From the global viewpoint, a way to create indexes is to start by defining useful indexes on single critical queries; then, indexes that can be subsumed are removed from the set of all indexes, and the benefit/cost ratio is evaluated for the remaining ones.

**Use of Clustered Indexes** Clustered indexes are best used for equality and range searches on non-key attributes, even if the selectivity factor is not very restrictive. It can also be useful for queries in which data must be sorted (usually when the query has a GroupBy).

**Multi-Attribute Indexes** Indexes defined on multiple attributes at once can be used for queries with equality-equality searches, or equality-range searches. It's important to consider the order in which the index attributes are specified: the first one should be the one used for mostly equality searches.

Since each element in the index contains several attributes, there is a greater chance that the optimizer will generate plans using only the index. However, multi-attribute indexes must be updated each time an update is done on an attribute on which it is defined, and occupies more memory than an index on a single attribute.

**Indexes for Join** Clustered indexes on a non-key join attribute of the internal table can improve the performances of an IndexNestedLoop, since it requires an IndexFilter as its inner operand.

**Index-Only Plans** In some cases, it is possible to execute Index-Only plans for a query, i.e., plans in which only indexes are accessed instead of the actual data. These plans can be generated if an index has been defined on the attributes appearing in the SELECT DISTINCT clause, or the GROUPBY clause.

Also, if indexes are defined for the inner operand on a foreign key needed for a join, the plan can use IndexOnlyFilter instead of IndexFilter.

## 8.2 Database Tuning

Database tuning includes all activities carried out to meet requirements regarding the performance of database applications. By “performance”, we refer to runtime performance, so **throughput** (number of operations completed in a unit of time), **response**

**time** (time to execute an application), and **resource consumption** (temporary or permanent memory used). For each potential decision to be taken, the trade-off between its costs and benefits is evaluated. Costs include any monetary cost (hardware, software), working hours, technical costs, while benefits include any improvement in performances (sometimes quantified in monetary effects, although often not easy to do).

Tuning considers the following aspects:

- Applications: user queries and transactions;
- DBMS: configurations, parameters, database schema, storage structures;
- Operating system: system parameters and configuration for I/O, network communication;
- Hardware: components used for CPU, main and permanent memory.

A basic idea at the basis of database tuning is Pareto principle: by applying 20% of the effort one can achieve 80% of the desired effects, meaning that a fully optimized system may be unnecessary, and the process should instead focus on smaller (but with significant improvements) changes. This is a complex and continuous process which

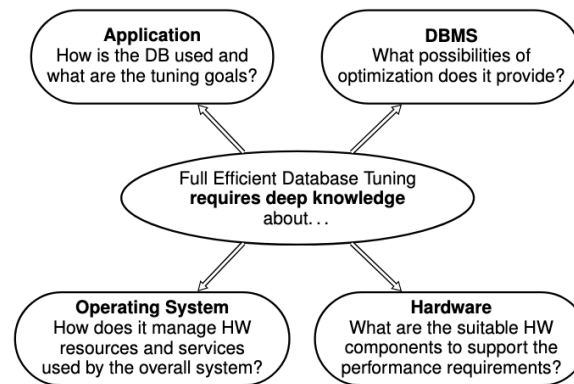


Figure 8.1: The DBMS tuning *quadrilemma*.

involves different professional figures:

- Database and applications designers, who have knowledge about applications and the DBMS, but may have little knowledge about OS or hardware;
- Database administrators, who have good knowledge about DBMS, OS, and hardware, and may have little knowledge about applications;



- Database experts, who usually have strong knowledge in DBMS, OS, and hardware, but very limited knowledge about applications.

### 8.2.1 Index Tuning

The initial choice of indexes could be revised for different reasons: the workload of the database may reveal that some queries initially considered critical are not actually executed that often, while others which had initially been thought of as infrequent turned out to be important. In some cases, the optimizer does not generate the physical plan that was expected. Either way, changing indexes can improve performances.

### 8.2.2 Query Tuning

If the optimizer does not transform SQL queries, they can be explicitly rewritten with two set of rules:

#### Semantically Equivalent Rewriting

- If a query has an Or condition, it may be rewritten using an Union of different queries, or using the In predicate specifying both conditions;
- If a query has an And of different predicates, it can be rewritten as a condition with Between (if the values in the predicates describe a range);
- Avoid arithmetic expressions on attributes used in conditions (e.g., instead of writing “Salary\*2 = 100”, write “Salary = 50”, because for the first condition the optimizer may not use an index);
- Subqueries can be rewritten as joins;
- Avoid temporary views. If the optimizer cannot rewrite the query without views, the physical plan will have an higher cost;
- Redundant Having and GroupBy should be removed.

#### Semantically Non-Equivalent Rewriting

- Avoid useless Distinct and OrderBy clauses;
- Avoid cartesian products.

### 8.2.3 Transaction Tuning

Another common cause of inefficiency in DBMS is the way transactions are programmed. In particular, they should be as short as possible to reduce the duration of the locks they hold over data objects (although as seen before many modern systems use more sophisticated locks instead of read-write locks, so this problem is not as big), and they should not block data during database loading and during read-only transactions.

Complex transactions should be split into smaller ones. Also, if a transaction has to stop because user input is being asked, it should commit and restart after input has been received. Each transaction should have the appropriate block granularity (record, page, table, etc.), as well as the appropriate isolation level:

- **READ UNCOMMITTED:** the reads of records are performed without requesting any locks, so dirty reads are possible;
- **READ COMMITTED:** the transaction obtains locks on records, released right after reading, and exclusive locks before writing (held until the end). This prevents dirty reads but not non-repeatable reads.
- **REPEATABLE READ:** the transaction holds both read and write locks on records released at the end. This avoids
- **READ COMMITTED:** the transaction obtains locks on records, released right after reading, and exclusive locks before writing (held until the end). This prevents dirty reads but not non-repeatable reads, but introduces the problem of **phantom records**: for example, if a transaction reads a set of records from a table which satisfy a condition  $\psi$ , and right after a second transaction writes a new set of records in that table which also satisfy  $\psi$ , the first transaction will never see those new records.
- **SERIALIZABLE:** the default isolation level, where read and write locks are of different sizes. Any read lock on a table will be in conflict with any update. It avoids all problems seen before, but reduces the number of concurrent transactions executable per unit of time.

Commercial DBMS don't necessarily provide all previous levels of isolation, or may have different default levels. Also, some of them provide the SNAPSHOT isolation level.

### 8.2.4 Logical Schema Tuning

If the physical design is not able to provide adequate performances, it may be necessary to modify the logical schema, using two types of restructuring: **partitioning** and **denormalization**.

**Partitioning** Partitioning can be either vertical or horizontal.

**Vertical partitioning** reduces the volume of data transferred from/to permanent memory and cache, splitting a relation separating its attributes into two sets, such that one set should contain the most frequently accessed attributes. Each partition will still have the primary key of the original relation as a subset of its attributes.

**Horizontal partitioning** reduces the cost of accessing a large relation by splitting it into sets of records, separating frequently accessed records from the others. Each partition will have all the original attributes of a disjoint subset of the original records.

**Denormalization** Normalization is the process of decomposing a table into smaller ones to reduce redundancy; denormalization is the opposite, so the process of adding columns to tables to improve the performance of read-only queries. This is useful when two or more tables are often read after joins, so instead of having to compute it every time, their information can be stored together in a single table.

## 8.3 DBMS tuning

If all else fails, the database system must be tuned. The most important things to consider can be divided into three levels that interact with each other:

- **Transaction Management:** intervening on parameters such as log storage, frequency of checkpoints and dumps, etc. The more frequent they are, the faster the database can be fully restarted after a system failure or disaster, but the system performances also degrade, since they subtract resources from normal activity;
- **Database Buffer Size:** if the buffer is larger, performance of application improves, but it shouldn't be so big it does not fit in main memory;
- **Disk Management:** adding disks or using RAID systems if disk I/O is a bottleneck, adding more memory, or using a faster processor;
- **Parallel Architectures:** this is an issue that strictly depends on the system in use.

An alternative is database **self-tuning**.

# Chapter 9

## Decision Support Systems

Decision support systems are a type of **information system**. An information system is an organized collection of resources, people, and procedures finalized to collect, store, process and communicate information needed to support the on-going activities. Information can be represented as images, text, audio, or really any kind of data.

Traditional applications that use databases are called **OLTP (On Line Transactional Processing)**, while decision support applications are called **OLAP (On Line Analytical Processing)**. The key difference between the two is that OLTP systems are used for mostly day-by-day operations, using transactions, while OLAP systems are used to analyze the data to try and extract some hidden knowledge without updating the data. Table 9.1 compares the two in more detail. While in traditional systems

	<b>OLTP</b>	<b>OLAP</b>
<b>Function</b>	Operations	Decisions
<b>Users</b>	Operatives (clerk, IT professional)	Knowledge workers (managers, analysts)
<b>Detail</b>	Analytic	May be aggregated
<b>Usage</b>	Repetitive	Ad hoc
<b>Data</b>	Current	Historic
<b>Data origin</b>	Internal	Internal and external
<b>Items per operation</b>	Few (tens)	Many (millions)
<b>Updates</b>	Frequent, small	Rare, massive
<b>Stored in</b>	Database	Data Warehouse/DSS

Table 9.1: Comparison between OLTP and OLAP systems.

there is usually only a single database containing all the information, in DSS there are multiple data warehouses, one for each analysis.

## 9.1 Data Warehouses

More formally, a data warehouse can be defined as follows:

### Data warehouse

A data warehouse is a subject-oriented, integrated, non-volatile, and time-varying collection of data in support of management's decisions.

- **Subject-oriented** means that data is stored by subject, not by applications, unlike traditional databases.
- **Integrated** means that data is gathered from a variety of sources and merged.
- **Non-volatile** means data is not changed interactively, but may be updated periodically.
- **Time-varying** means that data is assumed to be historical, collected over a long period of time, not necessarily up-to-date, in order to gather knowledge about the operations to be analyzed.

### 9.1.1 Architecture

The term “data warehousing” is used to refer to the process of organizing data in a data warehouse to allow end users to analyze it with business intelligence applications. The most common architecture is a three-layer one, composed of the **data sources**, **data staging**, and **data warehouse**.

The data warehouse is loaded with data extracted via **ETL (Extract, Transform, and Load)** applications from the many different sources of data in the previous layer, bringing them into a consistent form and performing any kind of cleaning needed, and finally storing them into the data staging. The complexity of data staging depends on the quality of the data sources.

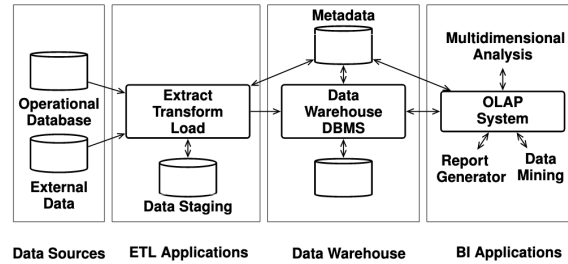


Figure 9.1: Scheme of a data warehouse architecture.

## 9.1.2 Modeling

The creation of a data warehouse takes place gradually, at different levels of abstraction: it starts with a conceptual model, then a logical model, and finally, a multidimensional cube model.

### Conceptual Model

The **Dimensional Fact Model** is a graphical conceptual model for data warehouses. It allows the representation of the following basic information:

- **Facts:** the most important abstraction mechanism is the collection of facts, which are the observations of the performance of a business process. They are usually transactions or events (e.g., sales, clicks, complaints, visits), and may be **periodic** (one fact for a group of transactions made over a period of time), or **accumulating** (one fact for the entire life of the event, evolving over time).

Facts are modeled by **fact tables**, each of which is a rectangle divided in two parts, one containing the fact name, and the other containing the measures.

- **Measures:** measures are quantitative information whose aggregation is of interest. The aggregation function is often the sum, but may also be a count, average, max, min, and so on.

Measures are specified inside the fact tables.

- **Dimensions:** dimensions give facts a context: they explain “who, what, why, when, where” a fact is happening. A dimension can be described as a set of attributes used to qualify, categorize, or summarize facts in reports.

Dimensions are represented by a circle connected to the fact table with a straight line, and one additional circle for each attribute of that dimension.

In the presence of dimensions, an hierarchical relationship can be modeled among them. For example, imagine a fact table with dimensions relating to dates (Year, Quarter, Month, Week, Day). A hierarchy can be constructed (Day  $\rightarrow$  Week  $\rightarrow$  Month  $\rightarrow$  Quarter  $\rightarrow$  Year) such that each element is more general than those coming before it, and less general than those after. In this case, Month is more general than Day, but is less general than Quarter. Formally, each arc of the hierarchy models a **functional dependency** between the two attributes. Graphically, hierarchies are represented as a directed tree, rooted in a dimension, and with the leaves representing the most general dimensions.

The presence of a hierarchy increases the possibilities of data analysis from different perspectives (so-called multidimensional analysis). If we already analyzed sales by year, we can also analyze them at a deeper level, considering months or days.

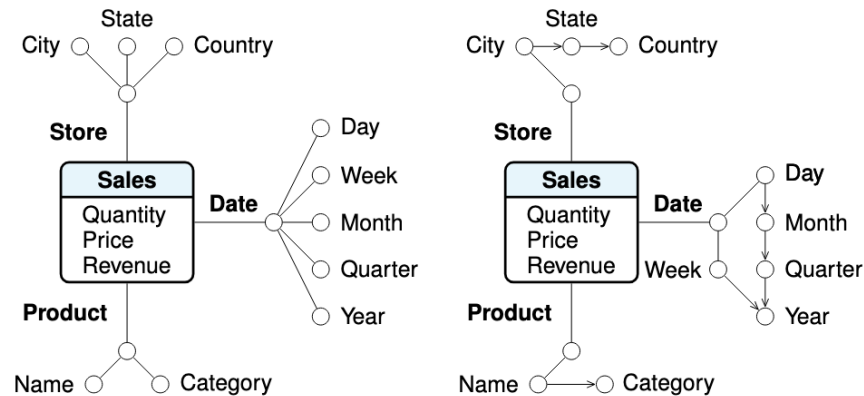


Figure 9.2: Conceptual design without and with hierarchies.

## Relational Model

A conceptual model can be transformed into a relational schema by applying a set of mapping rules. The most common schemas are the star schema, the snowflake schema, and the constellation schema.

In a **star schema**, the fact table is placed at the center, and a foreign key is added for each dimension. Dimensions are also transformed into tables (simply adding all the attributes, without considering hierarchies), and connected to the fact table with a one-to-many relationship.

A **snowflake schema** is similar to a star schema, but some dimension tables are also normalized, splitting the data into additional tables.

A **constellation schema** has multiple fact tables that share dimension tables.

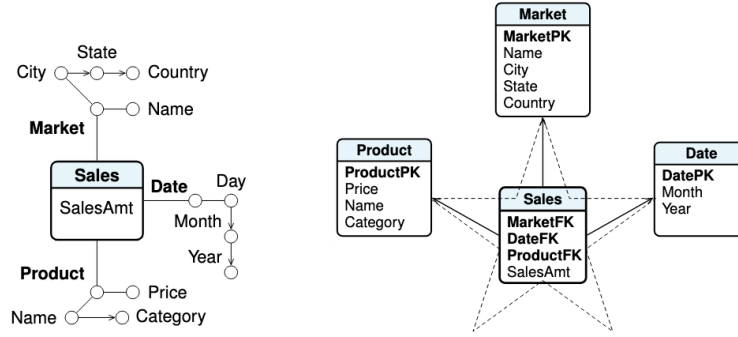


Figure 9.3: Star schema.

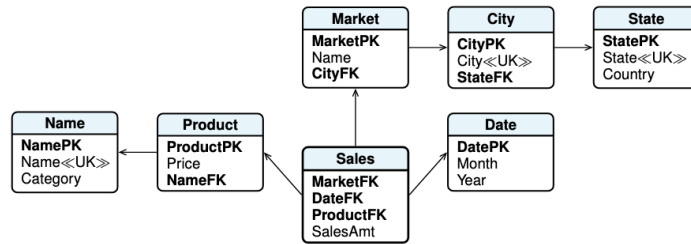


Figure 9.4: Snowflake schema.

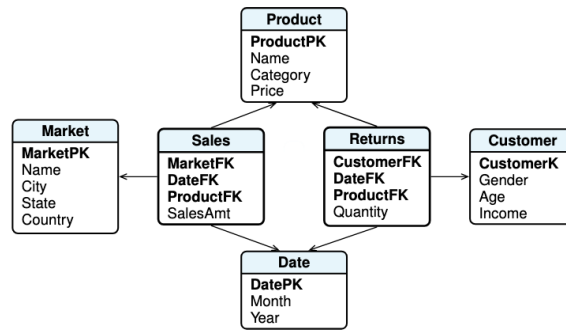


Figure 9.5: Constellation schema.

## Multidimensional Cube Model

A **multidimensional data model** (data cube) represents facts with  $n$  dimensions as points in an  $n$ -dimensional space. A point (fact) is identified by the values of its dimensions, and has an associated set of measures. This view is an intuitive way to think about OLAP queries and their results.

For example, imagine a fact table with information about store sales. Each record in the original data has three attributes: a store id, a product id, and an associated



quantity. We can see this data as 2-dimensional: the two dimensions are the store and the product id, while the measure is the quantity. Obviously, this is a very simple case.

StoreId	ProductId	Qty
S1	P1	300
S2	P1	500
S3	P1	50
S1	P2	300
S2	P2	10
S3	P2	30
S1	P3	40
S3	P3	20

Figure 9.6: Fact table.

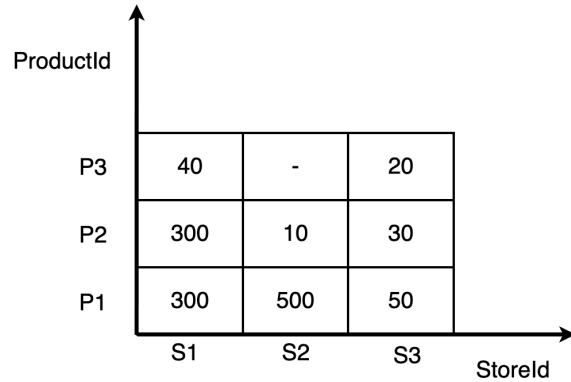


Figure 9.7: Example data cube.

In real applications, the number of dimensions can be higher than 2 or 3, so the data cube cannot be visualized in its entirety. These cubes can be manipulated via a specific geometric language, of which we can define these basic operations:

- **Slice:** slicing means “cutting” the cube by selecting on a specific value for one dimension.
- **Dice:** dicing is similar to slicing, but selects on two or more dimensions.
- **Pivot:** pivoting performs a rotation of the data axes, providing an alternative presentation of the data.
- **Roll-up:** rolling-up compresses the cube across a dimension, summarizing the information provided by that dimension. It can be seen as similar to a GroupBy done on all other dimensions not involved in the roll-up.
- **Drill-down:** it is the reverse of roll-up. It produces more detailed data across a dimension.

Assume that, given a data cube, each dimension is extended with an additional value, “\*”, representing summarization along that dimension. Then, the cube can be extended with borders containing the values of the sum along each possible combination of dimensions. When we select a subcube by specifying a dimension instead of its value (e.g., (StoreId, \*)), we get a roll-up of the original data across all other dimensions, called **cuboid**.

An order relation can be defined between cuboids:  $C1 \preceq C2$  if  $C1$  can be computed from  $C2$ . This order is visualized using a **data warehouse lattice**. In the example below, we can see how the cuboid (StoreId) can be computed from (StoreId, ProductId), but (StoreId, ProductId, DateId) cannot be computed from (StoreId, ProductId). So, how do we choose which of these cuboids to store? Obviously, the source data allows us to compute all other cuboids. However, if the queries most commonly executed only consider a subset of the dimensions, we may store those (or store one of those above them).

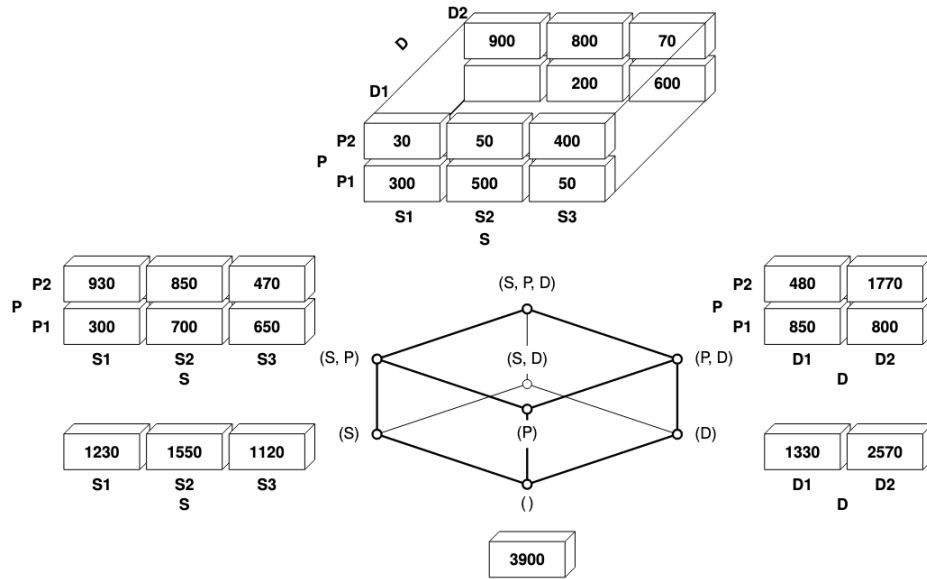


Figure 9.8: A data warehouse lattice. The data cube it corresponds to has three dimensions: StoreId, ProductId, and Date.

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