Tooth Growth Dataset Analysis

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We were asked to analyze the Tooth Growth dataset in R. From the R help file: "the response is the length of odontoblasts (teeth) in each of 10 guinea pigs at each of three dose levels of Vitamin C (0.5, 1, and 2 mg) with each of two delivery methods (orange juice or ascorbic acid)." The variable "len" is the tooth length in mm, "supp" is the supplement type delivery method (OJ = orange juice, VC = ascorbic acid), and "dose" is the dose level of vitamin C (0.5, 1, 2 mg).

Exploratory Data Analysis

There are a total of 60 observations in this dataset. A summary of the data can be seen below.

```
library(plyr)
summary(ToothGrowth)
##
         len
                                  dose
                    supp
##
          : 4.20
                    OJ:30
                                    :0.500
   Min.
                            Min.
##
    1st Qu.:13.07
                    VC:30
                             1st Qu.:0.500
##
  Median :19.25
                            Median :1.000
  Mean
           :18.81
                            Mean
                                  :1.167
   3rd Qu.:25.27
                             3rd Qu.:2.000
##
   Max.
           :33.90
                             Max.
                                    :2.000
ddply(ToothGrowth, "supp", summarize, avg=mean(len))
##
     supp
       OJ 20.66333
## 1
       VC 16.96333
ddply(ToothGrowth, "supp", summarize, StDev=sd(len))
##
     supp
             StDev
## 1
       OJ 6.605561
       VC 8.266029
ddply(ToothGrowth, "dose", summarize, avg=mean(len))
##
     dose
             avg
## 1 0.5 10.605
## 2 1.0 19.735
## 3 2.0 26.100
ddply(ToothGrowth, "dose", summarize, StDev=sd(len))
##
     dose
             StDev
## 1 0.5 4.499763
## 2 1.0 4.415436
## 3 2.0 3.774150
```

ddply(ToothGrowth,c("supp","dose"),summarize, avg=mean(len))

```
##
     supp dose
                  avg
## 1
       OJ
           0.5 13.23
## 2
           1.0 22.70
           2.0 26.06
## 3
       OJ
## 4
       VC
           0.5 7.98
## 5
       VC
           1.0 16.77
## 6
       VC
           2.0 26.14
```

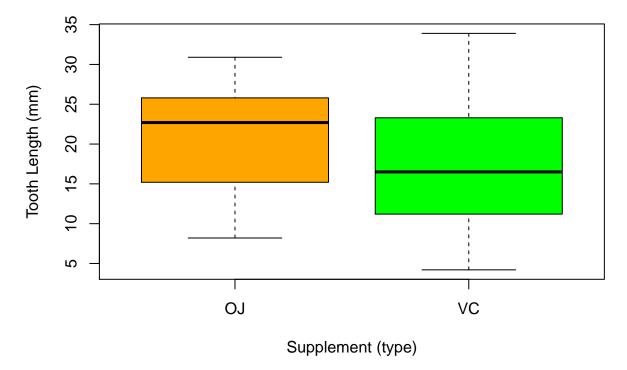
ddply(ToothGrowth,c("supp","dose"),summarize, StDev=sd(len))

```
##
     supp dose
                  StDev
## 1
       OJ
           0.5 4.459709
           1.0 3.910953
## 2
       OJ
## 3
       OJ
           2.0 2.655058
       VC
           0.5 2.746634
## 4
## 5
       VC
           1.0 2.515309
## 6
       VC
           2.0 4.797731
```

The first plot shows the tooth length by supplement type. From the boxplot, it appears that they are not very dissimilar.

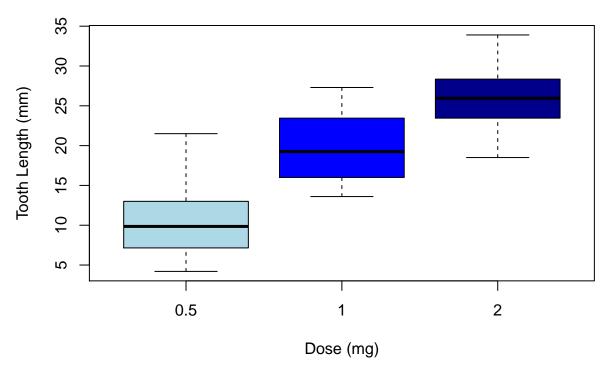
```
boxplot(ToothGrowth$len~ToothGrowth$supp,col=c("orange","green"),
    main="Tooth Length by Supplement",ylab="Tooth Length (mm)",
    xlab="Supplement (type)")
```

Tooth Length by Supplement



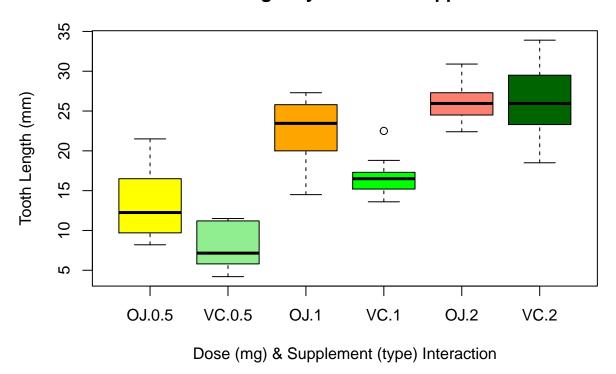
The next plot shows the tooth length by dose, 0.5, 1, and 2 mg. There does appear to be a difference between these, especially between the 0.5 and 2 mg doses.

Tooth Length by Dose



The next plot shows the interaction between dose and supplement type. When dose is considered, it appears that both supplement types increase the tooth length.

Tooth Length by Dose and Supplement



$Hypothesis\ Tests$

There are many hypothesis tests that could be performed with this dataset. The plots above already give an idea of which tests could prove to be significant. We can already surmise that for tooth length, there is probably a highly significant difference between doses, but perhaps not a significant difference between supplement types. Two sample t-tests were performed. The assumptions underlying this test are: The populations from which the samples were drawn are normally distributed. The standard deviations of the populations are equal. The samples were randomly drawn.

```
# T test for Supplement type
VC=subset(ToothGrowth, supp=="VC")
OJ=subset(ToothGrowth, supp=="OJ")
t.test(VC$len,OJ$len)
##
##
   Welch Two Sample t-test
##
## data: VC$len and OJ$len
## t = -1.9153, df = 55.309, p-value = 0.06063
\#\# alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -7.5710156 0.1710156
## sample estimates:
  mean of x mean of y
    16.96333 20.66333
# T test for doses
dose0.5=subset(ToothGrowth, dose==0.5)
dose2=subset(ToothGrowth,dose==2.0)
t.test(dose0.5$len,dose2$len)
```

```
##
## Welch Two Sample t-test
## data: dose0.5$len and dose2$len
## t = -11.799, df = 36.883, p-value = 4.398e-14
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -18.15617 -12.83383
## sample estimates:
## mean of x mean of y
      10.605
                26.100
tdose=round(t.test(dose0.5$len,dose2$len)$p.value,14)
dose0.5=subset(ToothGrowth, dose==0.5)
dose1=subset(ToothGrowth, dose==1.0)
t.test(dose0.5$len,dose1$len)
##
##
  Welch Two Sample t-test
## data: dose0.5$len and dose1$len
## t = -6.4766, df = 37.986, p-value = 1.268e-07
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -11.983781 -6.276219
## sample estimates:
## mean of x mean of y
      10.605
##
                19.735
t.test(dose1$len,dose2$len)
##
## Welch Two Sample t-test
## data: dose1$len and dose2$len
## t = -4.9005, df = 37.101, p-value = 1.906e-05
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -8.996481 -3.733519
## sample estimates:
## mean of x mean of y
      19.735
               26.100
# T test for supplement and dose
VCdose.5=subset(ToothGrowth,dose==0.5 & supp=="VC")
OJdose.5=subset(ToothGrowth,dose==0.5 & supp=="OJ")
t.test(VCdose.5$len,OJdose.5$len)
##
   Welch Two Sample t-test
##
```

```
## data: VCdose.5$len and OJdose.5$len
## t = -3.1697, df = 14.969, p-value = 0.006359
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -8.780943 -1.719057
## sample estimates:
## mean of x mean of y
        7.98
                 13.23
##
VCdose1=subset(ToothGrowth,dose==1.0 & supp=="VC")
OJdose1=subset(ToothGrowth, dose==1.0 & supp=="OJ")
t.test(VCdose1$len,OJdose1$len)
##
##
   Welch Two Sample t-test
##
## data: VCdose1$len and OJdose1$len
## t = -4.0328, df = 15.358, p-value = 0.001038
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -9.057852 -2.802148
## sample estimates:
## mean of x mean of y
##
       16.77
                 22.70
VCdose2=subset(ToothGrowth,dose==2.0 & supp=="VC")
OJdose2=subset(ToothGrowth,dose==2.0 & supp=="OJ")
t.test(VCdose2$len,OJdose2$len)
##
##
   Welch Two Sample t-test
##
## data: VCdose2$len and OJdose2$len
## t = 0.0461, df = 14.04, p-value = 0.9639
\#\# alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -3.63807 3.79807
## sample estimates:
## mean of x mean of y
##
       26.14
                 26.06
```

Almost all of the t-tests performed resulted in significant differences in the means of the tooth length at the p=0.05 level.

The t-test for the supplement type resulted in a p-value of 0.0606, just barely higher than the 0.05 significant level. Here we have very slight evidence that the tooth length means of the supplement types are not dissimilar.

We have strong evidence that dose results in different mean lengths for teeth. Between the 0.5 and 2.0 mg dose, a p-value of less than 0.000000001 is produced. This is highly significant.

When dose and supplement are considered, there are two significant difference at the 0.5 and 1.0 mg dose levels, between supplement types. The p-values for these tests (dose of 0.5 mg, by supplement type and dose of 1.0 mg, by supplement type) were 0.0063586 and 0.0010384 respectively.

Conclusion

Overall, we can conclude that as the dose of vitamin C increases, so does the tooth length. The supplement type only appears to play a significant role at the 0.5 and 1.0 mg dose levels.