US Covid-19 Cases Time Series Analysis

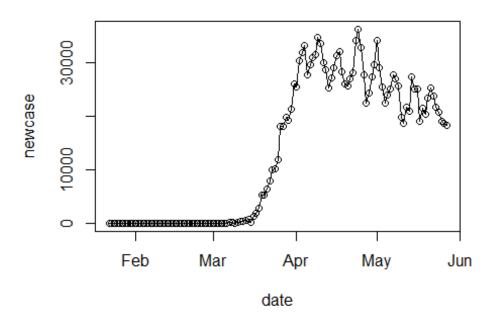
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```
#importing Covid Data from Johns Hopkins
uscases <-
read.csv(url("https://raw.githubusercontent.com/CSSEGISandData/COVID-
19/master/csse covid 19 data/csse covid 19 time series/time series covid19 co
nfirmed_US.csv"))
usdeaths <-
read.csv(url("https://raw.githubusercontent.com/CSSEGISandData/COVID-
19/master/csse_covid_19_data/csse_covid_19_time_series/time_series_covid19_de
aths_US.csv"))
uscases <- uscases[,-c(1:5,8:11)]
usdeaths <- usdeaths[,-c(1:5,8:12)]
n <- ncol(uscases)-2</pre>
date <- 1:n
date <- as.Date(date, origin = "2020-01-21")</pre>
format(date,format = "%b %d %y")
     [1] "Jan 22 20" "Jan 23 20" "Jan 24 20" "Jan 25 20" "Jan 26 20" "Jan 27
##
20"
     [7] "Jan 28 20" "Jan 29 20" "Jan 30 20" "Jan 31 20" "Feb 01 20" "Feb 02
##
20"
    [13] "Feb 03 20" "Feb 04 20" "Feb 05 20" "Feb 06 20" "Feb 07 20" "Feb 08
##
20"
    [19] "Feb 09 20" "Feb 10 20" "Feb 11 20" "Feb 12 20" "Feb 13 20" "Feb 14
##
20"
##
   [25] "Feb 15 20" "Feb 16 20" "Feb 17 20" "Feb 18 20" "Feb 19 20" "Feb 20
20"
## [31] "Feb 21 20" "Feb 22 20" "Feb 23 20" "Feb 24 20" "Feb 25 20" "Feb 26
20"
   [37] "Feb 27 20" "Feb 28 20" "Feb 29 20" "Mar 01 20" "Mar 02 20" "Mar 03
##
20"
## [43] "Mar 04 20" "Mar 05 20" "Mar 06 20" "Mar 07 20" "Mar 08 20" "Mar 09
20"
## [49] "Mar 10 20" "Mar 11 20" "Mar 12 20" "Mar 13 20" "Mar 14 20" "Mar 15
20"
   [55] "Mar 16 20" "Mar 17 20" "Mar 18 20" "Mar 19 20" "Mar 20 20" "Mar 21
##
20"
    [61] "Mar 22 20" "Mar 23 20" "Mar 24 20" "Mar 25 20" "Mar 26 20" "Mar 27
##
20"
    [67] "Mar 28 20" "Mar 29 20" "Mar 30 20" "Mar 31 20" "Apr 01 20" "Apr 02
##
## [73] "Apr 03 20" "Apr 04 20" "Apr 05 20" "Apr 06 20" "Apr 07 20" "Apr 08
20"
```

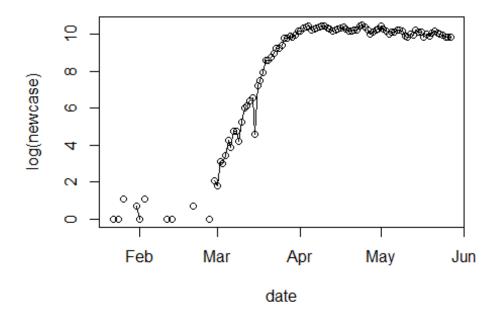
```
## [79] "Apr 09 20" "Apr 10 20" "Apr 11 20" "Apr 12 20" "Apr 13 20" "Apr 14
20"
## [85] "Apr 15 20" "Apr 16 20" "Apr 17 20" "Apr 18 20" "Apr 19 20" "Apr 20
20"
## [91] "Apr 21 20" "Apr 22 20" "Apr 23 20" "Apr 24 20" "Apr 25 20" "Apr 26
20"
## [97] "Apr 27 20" "Apr 28 20" "Apr 29 20" "Apr 30 20" "May 01 20" "May 02
20"
## [103] "May 03 20" "May 04 20" "May 05 20" "May 06 20" "May 07 20" "May 08
20"
## [109] "May 09 20" "May 10 20" "May 11 20" "May 12 20" "May 13 20" "May 14
20"
## [115] "May 15 20" "May 16 20" "May 17 20" "May 18 20" "May 19 20" "May 20
20"
## [121] "May 21 20" "May 22 20" "May 23 20" "May 24 20" "May 25 20" "May 26
20"
## [127] "May 27 20"
#finding total cases and turning them into a time series object
library(TSA)
##
## Attaching package: 'TSA'
## The following objects are masked from 'package:stats':
##
##
       acf, arima
## The following object is masked from 'package:utils':
##
##
       tar
totcase <- colSums(uscases[,3:(n+2)])
newcase \leftarrow rep(0,n)
newcase[1] <- totcase[1]</pre>
newcase[2:n] <- diff(totcase)</pre>
newcase \leftarrow ts(data=newcase, start=c(2020,01,22), frequency = 365)
#trying various transformations
wkday <- c("W","T","F","S","S","M","T")
plot(date, newcase, type="o", main="Untransformed time series")
```

Untransformed time series

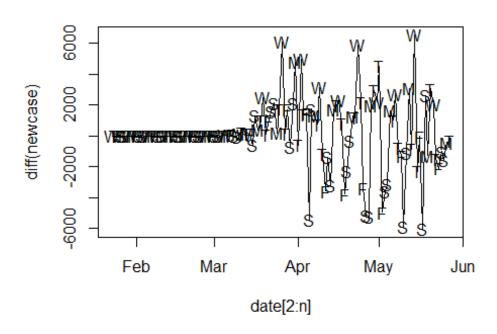


plot(date,log(newcase),type="o",main="Log time series")

Log time series

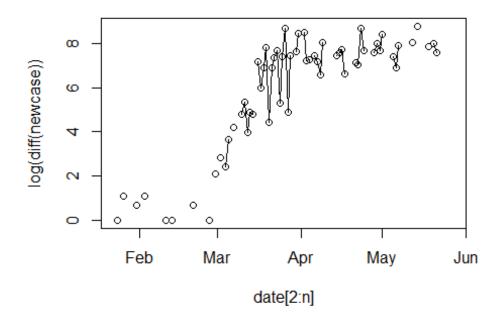


First difference time series



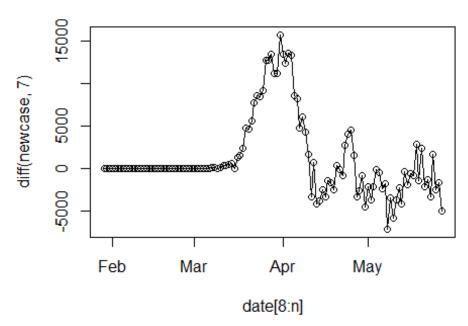
plot(date[2:n],log(diff(newcase)),type="o",main="Log of first difference time
series")
Warning in log(diff(newcase)): NaNs produced

Log of first difference time series

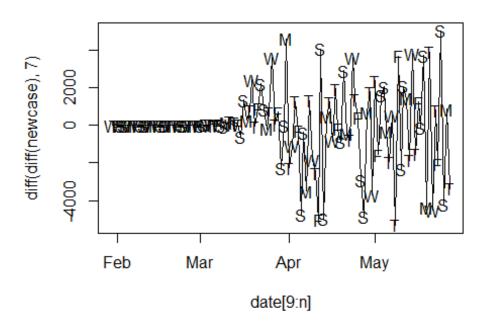


plot(date[8:n],diff(newcase,7),type="o",main="First weekly difference time
series")

First weekly difference time series

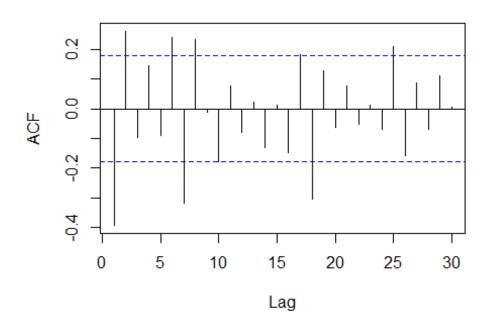


First and weekly difference time series



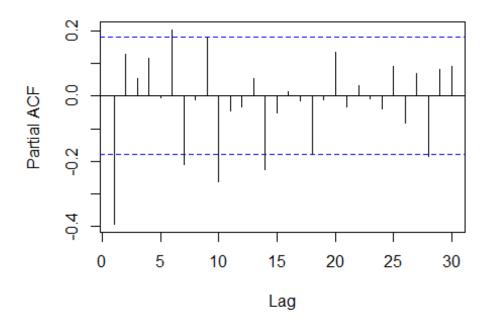
#starting with an ARIMA model with both a first and first weekly difference
#preliminary analysis
transcase <- diff(diff(newcase),7)
acf(as.vector(transcase),main="ACF of transformed series",lag.max=30)</pre>

ACF of transformed series



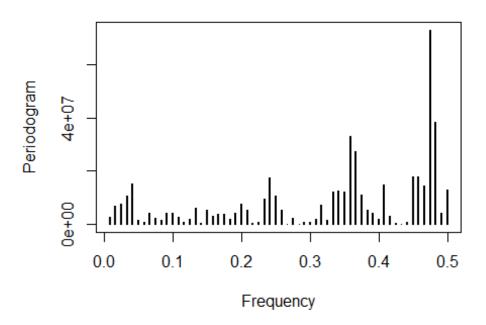
pacf(as.vector(transcase), main="PACF of transformed series", lag.max=30)

PACF of transformed series



periodogram(transcase, main="Periodgram of transformed series")

Periodgram of transformed series



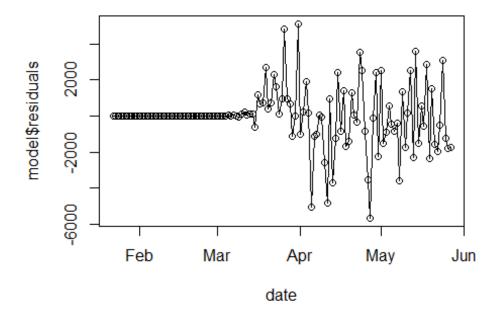
```
#model fitting:
#looking at the periodograms, it appears a ARIMA(1,1,0)x(1,1,0)_{-}7 is
justified to start
tsmodel <- function(ar,ma,ars,mas){</pre>
  mod <-
arima(newcase, order=c(ar, 1, ma), seasonal=list(order=c(ars, 1, mas), period=7))
  return(mod)
}
tsmodel(1,0,1,0)
##
## Call:
## arima(x = newcase, order = c(ar, 1, ma), seasonal = list(order = c(ars, 1, ma))
mas),
       period = 7))
##
##
## Coefficients:
##
              ar1
                      sar1
##
         -0.3344
                   -0.2568
## s.e.
          0.0904
                    0.0953
## sigma^2 estimated as 3188580: log likelihood = -1060.17, aic = 2124.34
tsmodel(2,0,1,0)
##
## Call:
```

```
## arima(x = newcase, order = c(ar, 1, ma), seasonal = list(order = c(ars, 1, ma))
mas),
##
       period = 7)
##
## Coefficients:
##
            ar1
                    ar2
                            sar1
##
         -0.259 0.1927
                         -0.2972
## s.e.
          0.094 0.0912
                          0.0934
##
## sigma^2 estimated as 3067794: log likelihood = -1058, aic = 2121.99
tsmodel(2,0,2,0)
##
## Call:
## arima(x = newcase, order = c(ar, 1, ma), seasonal = list(order = c(ars, 1, ma))
mas),
##
       period = 7)
##
## Coefficients:
##
                     ar2
                             sar1
                                       sar2
             ar1
         -0.2424
                  0.1793
                          -0.3636
                                   -0.2169
##
## s.e.
          0.0968 0.0934
                           0.0991
                                    0.0936
##
## sigma^2 estimated as 2920166: log likelihood = -1055.39, aic = 2118.78
tsmodel(3,0,2,0) #not significant
##
## arima(x = newcase, order = c(ar, 1, ma), seasonal = list(order = c(ars, 1, ma))
mas),
##
       period = 7)
##
## Coefficients:
                     ar2
##
                             ar3
                                               sar2
             ar1
                                      sar1
         -0.2503
                  0.1866 0.0356
                                   -0.3584
                                           -0.2227
##
## s.e.
          0.0988 0.0953 0.0948
                                   0.1000
                                             0.0950
##
## sigma^2 estimated as 2916556: log likelihood = -1055.32, aic = 2120.64
tsmodel(2,0,3,0) #not significant
##
## Call:
## arima(x = newcase, order = c(ar, 1, ma), seasonal = list(order = c(ars, 1, ma))
mas),
##
       period = 7)
##
## Coefficients:
##
                     ar2
                             sar1 sar2
                                                sar3
             ar1
```

```
-0.2408 0.1834 -0.3789 -0.2390
                                            -0.0602
## s.e.
          0.0968 0.0934
                           0.1021
                                    0.1003
                                             0.0980
## sigma^2 estimated as 2908774: log likelihood = -1055.2, aic = 2120.4
tsmodel(2,1,2,0)
##
## Call:
## arima(x = newcase, order = c(ar, 1, ma), seasonal = list(order = c(ars, 1, ma))
       period = 7))
##
##
## Coefficients:
##
            ar1
                    ar2
                             ma1
                                     sar1
                                              sar2
##
         0.4163
                 0.3484
                        -0.6987
                                  -0.3566
                                           -0.2261
## s.e. 0.1863 0.0882
                          0.1781
                                   0.0976
                                            0.0952
##
## sigma^2 estimated as 2892421: log likelihood = -1054.78, aic = 2119.55
tsmodel(2,1,2,1)
##
## Call:
## arima(x = newcase, order = c(ar, 1, ma), seasonal = list(order = c(ars, 1, ma))
##
       period = 7)
##
## Coefficients:
##
             ar1
                      ar2
                              ma1
                                     sar1
                                             sar2
                                                      sma1
                                           0.1189
##
         -0.8498
                 -0.0243 0.6236 0.5177
                                                   -0.9300
## s.e.
          0.2995
                   0.1561 0.2723 0.2988
                                           0.1828
                                                    0.3759
##
## sigma^2 estimated as 2766731: log likelihood = -1053.9, aic = 2119.8
tsmodel(2,2,2,1) #not significant
##
## Call:
## arima(x = newcase, order = c(ar, 1, ma), seasonal = list(order = c(ars, 1, ma))
mas),
##
       period = 7)
##
## Coefficients:
##
                    ar2
                             ma1
                                      ma2
                                             sar1
                                                     sar2
            ar1
                                                               sma1
##
         0.1066 0.6321
                        -0.3125
                                  -0.3817
                                           0.4227
                                                   0.1037
                                                          -0.8495
## s.e. 0.2633 0.2231
                          0.3131
                                   0.2779 0.3304 0.2050
                                                            0.3139
## sigma^2 estimated as 2791097: log likelihood = -1053.48, aic = 2120.95
tsmodel(2,1,2,2) #R did not like this
```

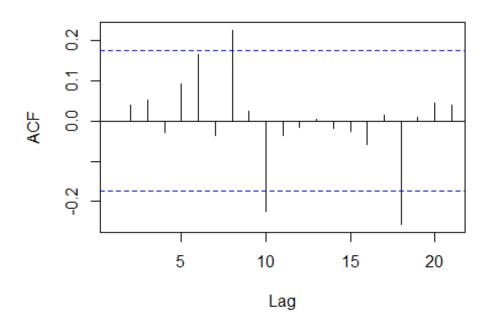
```
##
## Call:
## arima(x = newcase, order = c(ar, 1, ma), seasonal = list(order = c(ars, 1, ma))
       period = 7))
##
##
## Coefficients:
## Warning in sqrt(diag(x$var.coef)): NaNs produced
##
             ar1
                       ar2
                               ma1
                                        sar1
                                               sar2
                                                         sma1
                                                                 sma2
##
         -0.8647
                   -0.0320
                           0.6393
                                     -0.1223
                                              0.251
                                                     -0.2674
                                                               -0.426
## s.e.
          0.3931
                    0.1945
                            0.3479
                                         NaN
                                              0.185
                                                          NaN
                                                                  NaN
##
## sigma^2 estimated as 2821964: log likelihood = -1054.1, aic = 2122.2
#the final model is an ARIMA(2,1,2)X(2,1,1)_7
#diagnostics:
model<-tsmodel(2,1,2,2)</pre>
plot(date, model$residuals, main="model residuals", type="o")
```

model residuals



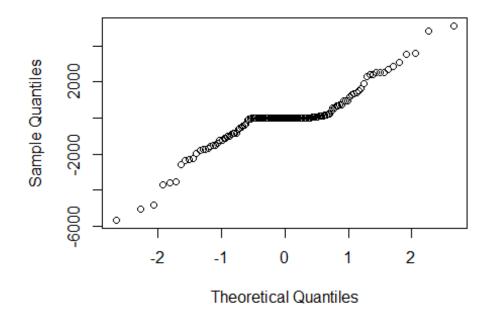
acf(as.vector(model\$residuals),main="ACF of model residuals")

ACF of model residuals



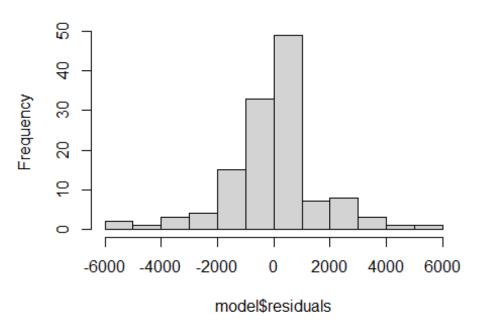
qqnorm(model\$residuals,main="QQ plot of model residuals")

QQ plot of model residuals



hist(model\$residuals,main="histogram of model residuals")

histogram of model residuals



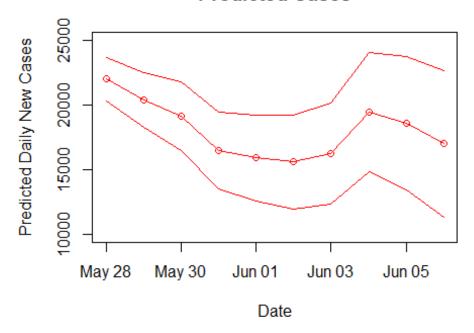
```
#predictions
predictions <- predict(model,n.ahead=10)
dateahead<- seq(from=(n+1),to=(n+10))
dateahead <- as.Date(dateahead,origin = "2020-01-21")
format(dateahead,format = "%b %d %y")

## [1] "May 28 20" "May 29 20" "May 30 20" "May 31 20" "Jun 01 20" "Jun 02 20"

## [7] "Jun 03 20" "Jun 04 20" "Jun 05 20" "Jun 06 20"

plot(dateahead,predictions$pred,main="Predicted
Cases",type="o",ylim=c(10000,25000),ylab="Predicted Daily New
Cases",xlab="Date",col="red")
lines(dateahead,(predictions$pred - predictions$se),type="l",col="red")
lines(dateahead,(predictions$pred + predictions$se),type="l",col="red")</pre>
```

Predicted Cases



```
datenew <- c(date,dateahead)
total <- c(newcase,predictions$pred)
plot(datenew,total,col=c(rep("black",n),rep("red",10)),main="Predicted
Cases",type="o",ylab="Daily New Cases",xlab="Date")
lines(dateahead,(predictions$pred - predictions$se),type="l",col="red")
lines(dateahead,(predictions$pred + predictions$se),type="l",col="red")</pre>
```

Predicted Cases

