

# The effects of varying depth in cosmic shear surveys

Sven Heydenreich<sup>1</sup>, Peter Schneider<sup>1</sup>, Hendrik Hildebrandt<sup>2,1</sup>, Marika Asgari<sup>3</sup>, Catherine Heymans<sup>3,2</sup>, Benjamin Joachimi<sup>4</sup>, Chieh-An Lin<sup>3</sup>, Tilman Tröster<sup>3</sup>, and Jan Luca van den Busch<sup>2,1</sup>

<sup>1</sup> Argelander-Institut für Astronomie, Auf dem Hügel 71, 53121 Bonn, Germany

<sup>2</sup> Astronomisches Institut, Ruhr-Universität Bochum, Universitätsstr. 150, 44801 Bochum, Germany

<sup>3</sup> Institute for Astronomy, University of Edinburgh, Royal Observatory, Blackford Hill, Edinburgh EH9 3HJ, UK

<sup>4</sup> Department of Physics and Astronomy, University College London, Gower Street, London WC1E 6BT, UK  
e-mail: sven@astro.uni-bonn.de, peter@astro.uni-bonn.de

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## ABSTRACT

Cosmic shear proves to be a powerful tool to study the properties of the Universe. The discrepancy in the parameter  $S_8 = \sigma_8 \sqrt{\Omega_m/0.3}$  between measurements in the local Universe and the cosmic microwave background motivates further investigation of yet unaccounted systematic biases. Ground-based surveys are subject to a variation in depth caused by varying atmospheric conditions; we investigate and quantify the resulting effects. In particular, we check whether they introduce a bias to the resulting cosmological parameters and if they can be responsible for the occurrence of B-modes. We construct a semi-analytic model to estimate the impact on the shear correlation functions and analyse the implications for cosmological parameters. Furthermore, we construct COSEBIs from the correlation functions to quantify the occurring B-modes. For the Kilo-Degree Survey this effect introduces an error in  $\xi_{\pm}$  of the order of a few percent on small scales. We find that the resulting bias in  $\Omega_m$ ,  $\sigma_8$  and  $S_8$  will be significant in next-generation cosmic shear surveys. We find that the dependence of this effect on the underlying cosmology is not negligible. We also report the occurrence of B-modes, although at a not yet significant level. We conclude that the effects of varying depth for current cosmic shear surveys on cosmological parameters are not yet significant, but should be accounted for in next-generation experiments. [\[Link to the current google doc\]](#)

**Key words.** gravitational lensing – weak lensing – cosmic shear

## 1. Introduction

The discovery of cosmic shear has provided us with a new and powerful cosmological tool to empirically test the standard model of cosmology and to determine its parameters. Contrary to the analysis of the cosmic microwave background (CMB, e.g. by Planck Collaboration et al. 2018), cosmic shear is more sensitive to the properties of the local Universe and thus provides an excellent consistency check for the standard model. Current cosmic shear surveys are particularly sensitive to the parameter  $S_8 = \sigma_8(\Omega_m/0.3)^\alpha$ , where  $\sigma_8$  characterizes the normalization of the matter power spectrum and  $\Omega_m$  is the matter density parameter. The parameter  $\alpha \approx 0.5$  depends on the exact survey properties; in this paper we will fix it to be  $\alpha = 0.5$ . It is interesting to note that all three current major cosmic shear results report a lower  $S_8$  than inferred from the CMB analysis by Planck Collaboration et al. (2018). While their analysis determined a value of  $S_8 = 0.830 \pm 0.013$ , Hikage et al. (2019) report  $S_8 = 0.800^{+0.029}_{-0.028}$  from an analysis of the Subaru Hyper Suprime-Cam survey, Hildebrandt et al. (2018, hereafter H18) obtained  $0.737^{+0.040}_{-0.036}$  from KiDS+VIKING data, and the Dark Energy Survey (DES, Troxel et al. 2018) arrived at  $S_8 = 0.782 \pm 0.027$ . Also, Heymans et al. (2013) report  $S_8 = 0.759 \pm 0.020$  from their analysis of CFHTLenS data. Reweighting the obtained redshifts of data from DES and combining this with KiDS data (Joudaki et al. 2019, Asgari et al. in prep.), yields even higher tension with the value determined for  $S_8$  by the Planck Collaboration. This discrepancy has received a lot of attention (Joudaki et al. 2017; Spurio Mancini et al. 2019; Tröster et al. 2019). It could

be interpreted as a statistical coincidence, a sign of new physics like massive neutrinos (Battye & Moss 2014), time-varying dark energy or modified gravity (Planck Collaboration et al. 2016); or as the manifestation of a systematic effect, either in the cosmic shear surveys or in the Planck mission (Addison et al. 2016), that is not yet accounted for.

For current cosmic shear surveys, the estimated systematic error is of comparable size to the statistical error, implying that for next-generation surveys, a significant reduction of systematic errors is necessary (Hildebrandt et al. 2017, hereafter H17). With surveys like the Large Synoptic Survey Telescope (LSST, Ivezić et al. 2008) and Euclid (Laureijs et al. 2011) soon to start, systematic effects in gravitational lensing have received a large amount of attention (Asgari et al. 2019; Blake 2019; Shirasaki et al. 2019).

To check for remaining systematics, a weak lensing signal can be divided into two components, the so-called E- and B-modes (Crittenden et al. 2002; Schneider et al. 2002b). To leading order, B-modes can not be created by astrophysical phenomena and are thus an excellent test for remaining systematics. The most useful E- and B-mode decomposition for cosmic shear surveys is provided by Complete Orthogonal Sets of E- and B-mode Integrals (COSEBIs, Schneider et al. 2010, hereafter S10), as it can easily be applied to real data. Note that the non-existence of B-modes does not necessarily imply that the sample is free of remaining systematics.

One systematic effect is the variation of depth in a survey. While effects like Galactic extinction or dithering strategies do play a role in every survey, this work focuses on the ef-

fects caused by varying atmospheric conditions that are found in ground-based surveys. To first order, this variation can be modelled by a piece-wise constant depth function, which varies from pointing to pointing. In this work we assume the specifications of the Kilo-Degree Survey (KiDS, Kuijken et al. 2015), namely an assembly of 1 deg<sup>2</sup> square fields. To quantify the depth, we chose the limiting magnitude of the  $r$ -band, as defined in de Jong et al. (2017), since it serves as the detection band and is thus most important for determining source galaxies.

In Sect. 2 we will introduce two simple toy models to understand this effect and analyze the impact on the cosmic shear power spectrum. In Sect. 3 we will estimate the effect on the shear correlation functions  $\xi_{\pm}$  using a semi-analytic model. We will present our results in Sect. 4. In Sect. 5 we will discuss our results and comment on the impact of our used simplifications. App. A is reserved for detailed calculations that can not be done in the main paper, in App. B we introduce way to apply our model to a given survey footprint. App. C is reserved for figures and tables that can not be displayed in the main body. We will assume the standard weak gravitational lensing formalism, a summary of which can be found in Bartelmann & Schneider (2001).

## 2. Simple, analytic toy models

For our first analysis we assume that all the matter between sources and observer is concentrated in a single lens plane of distance  $D_d$  from the observer. If we now distribute sources at varying distances  $D_s$ , two effects become apparent: Firstly, the lensing efficiency  $D_{ds}/D_s$  varies, where  $D_{ds}$  is the distance between the lens plane and the respective source. Secondly, and more importantly, for a more distant source *more* matter is concentrated between the source and the observer, leading to a stronger shear signal.

Assuming that the depth, and thus the source redshift population, only varies between pointings of the camera, an observer will measure a shear signal that is modified by a step-like depth-function,  $\gamma^{\text{obs}}(\theta) = W(\theta)\gamma(\theta)$ , where  $W$  is proportional to the mean of the lensing efficiency  $D_{ds}/D_s$  of one pointing and  $\gamma$  denotes the shear that this pointing would read if it were of the average depth. We can parametrize  $W$  as  $W(\theta) = 1 + w(\theta)$ . This implies that  $\langle w(\theta) \rangle = 0$  holds, where  $\langle \cdot \rangle$  denotes the average over all pointings.

### 2.1. Modelling the power spectrum

In our first model we describe the impact of varying depth on the power spectrum, following the simplifications described above. In accordance with the definition of the shear power spectrum

$$\langle \hat{\gamma}(\ell) \hat{\gamma}^*(\ell') \rangle = (2\pi)^2 \delta(\ell - \ell') P(|\ell|), \quad (1)$$

where  $\hat{\gamma}$  denotes the Fourier transform of  $\gamma$ , we define the observed power spectrum via

$$P^{\text{obs}}(\ell) \equiv \frac{1}{(2\pi)^2} \int d^2\ell' \langle \hat{\gamma}^{\text{obs}}(\ell) \hat{\gamma}^{\text{obs}*}(\ell') \rangle. \quad (2)$$

Note that due to the depth-function, both the assumptions of homogeneity and isotropy break down, which means that we can neither assume isotropy in the power spectrum, nor can we assume that  $\langle \hat{\gamma}^{\text{obs}}(\ell) \hat{\gamma}^{\text{obs}*}(\ell') \rangle$  vanishes for  $\ell \neq \ell'$ . To model a constant depth on each individual pointing,  $\alpha$ , we can choose random variables,  $w_{\alpha}$ , that only need to satisfy  $\langle w_{\alpha} \rangle = 0$ . As

we assume an infinite number of pointings,  $\alpha$  can assume any two-dimensional integer value  $\mathbb{Z}^2$  and we can parametrize  $w(\theta)$  as

$$w(\theta) = \sum_{\alpha \in \mathbb{Z}^2} w_{\alpha} \Xi(\theta - L\alpha), \quad (3)$$

with the box-function

$$\Xi(\theta) = \begin{cases} 1 & \theta \in \left[-\frac{L}{2}, \frac{L}{2}\right]^2 \\ 0 & \text{else} \end{cases}, \quad (4)$$

where  $L$  is the sidelength of one pointing. Following the calculations in App. A.1, we derive

$$P^{\text{obs}}(\ell) = P(\ell) + \langle w^2 \rangle \int \frac{d^2\ell'}{(2\pi)^2} \hat{\Xi}(\ell - \ell') P(\ell'). \quad (5)$$

Here we have denoted  $\langle w^2 \rangle \equiv \langle w_{\alpha}^2 \rangle$  as the dispersion of the depth-function, since the statistical properties of this function do not depend on the pointing  $\alpha$ . The Fourier transform of the box function,  $\hat{\Xi}$ , is a 2-dimensional sinc-function (see A.1). The observed power spectrum,  $P^{\text{obs}}$ , is thus composed of the original power spectrum  $P(\ell)$  from Eq. (1), plus a convolution of the power spectrum with a sinc-function, scaling with the variance of the function  $w(\theta)$ .

### 2.2. Modelling the shear correlation functions

More convenient measures to infer cosmological information from observational data are the shear correlation functions  $\xi_{\pm}$ , which are defined as

$$\xi_{\pm}(\theta) = \langle \gamma_t \gamma_t \rangle(\theta) \pm \langle \gamma_{\times} \gamma_{\times} \rangle(\theta). \quad (6)$$

Here,  $\gamma_t$  and  $\gamma_{\times}$  denote the tangential- and cross-component of the shear for a galaxy pair with respect to their relative orientation (see Schneider et al. 2002a). The shear correlation functions are the prime estimators to quantify a cosmic-shear signal, since it is simple to include a weighting of the shear measurements into the correlation functions and, contrary to the power spectrum, one does not have to worry about the shape of the survey footprint or masked regions, or model the noise contribution. For this analysis we will follow the assumption that a deeper pointing shows a stronger shear signal  $\gamma^{\text{obs}}(\theta) = W(\theta)\gamma(\theta)$  as described above. While this is not true for a 3-dimensional lensing matter distribution, it should be a reasonable first approximation for small variations in mean source redshift. Additionally, we assume that a greater depth does not only lead to a stronger average shear, but also to a higher galaxy number density, implying a correlation between those two quantities.

Let  $N^i(\theta)$ ,  $N^j(\theta)$  be the average weighted number of galaxies<sup>1</sup> per pointing in redshift bins  $i$  and  $j$  and let  $W^i(\theta)$ ,  $W^j(\theta)$  be the weighting of average shear. The observed correlation func-

<sup>1</sup> Instead of using the actual number of galaxies, we take the sum of their lensing weights, following H17. Due to this we account for different weighting of galaxies in the shear correlation functions as well as in the average redshift distribution.



Fig. 1: Probability  $E(\theta)$  that a random pair of galaxies of distance  $\theta$  lie in the same  $1 \text{ deg}^2$  pointing.

tions  $\xi_{\pm}^{ij, \text{obs}}(\theta)$  now change from uniform depth,  $\xi_{\pm}^{ij, \text{uni}}(\theta)$ , via

$$\begin{aligned} \xi_{\pm}^{ij, \text{obs}}(\theta) &= \frac{\langle N^i(\theta') N^j(\theta' + \theta) \gamma_{\text{t}}^{i, \text{obs}}(\theta') \gamma_{\text{t}}^{j, \text{obs}}(\theta' + \theta) \rangle}{\langle N^i(\theta') N^j(\theta' + \theta) \rangle} \\ &\quad \pm \frac{\langle N^i(\theta') N^j(\theta' + \theta) \gamma_{\text{x}}^{i, \text{obs}}(\theta') \gamma_{\text{x}}^{j, \text{obs}}(\theta' + \theta) \rangle}{\langle N^i(\theta') N^j(\theta' + \theta) \rangle} \\ &= \frac{\langle N^i(\theta') N^j(\theta' + \theta) W^i(\theta') W^j(\theta' + \theta) \rangle}{\langle N^i(\theta') N^j(\theta' + \theta) \rangle} \xi_{\pm}^{ij, \text{uni}}(\theta), \end{aligned} \quad (7)$$

where the average  $\langle \cdot \rangle$  represents both an ensemble average as well as an average over the position  $\theta'$ . Assuming that the depth of different pointings is uncorrelated, the only important property of a galaxy pair is whether or not they lie in the same pointing. We want to denote the probability that a random galaxy pair of separation  $\theta$  lies in the same pointing by  $E(\theta)$ . This function is depicted in Fig. 1, and an analytic expression is derived in App. A.2.

To compute the modified shear correlation functions, we parametrize the number densities  $N^i(\theta) = \langle N^i \rangle [1 + n^i(\theta)]$  and the weight  $W^i(\theta) = 1 + w^i(\theta)$  and, as in Eq. (4), interpret  $n^i(\theta)$  as a function with average  $\langle n^i \rangle = 0$  that is constant on each pointing. We can see that  $\langle n^i(\theta') n^j(\theta' + \theta) \rangle = E(\theta) \langle n^i(\theta') n^j(\theta') \rangle = E(\theta) \langle n^i n^j \rangle$  holds and compute:

$$\begin{aligned} &\frac{\langle N^i(\theta') N^j(\theta' + \theta) W^i(\theta') W^j(\theta' + \theta) \rangle}{\langle N^i \rangle \langle N^j \rangle} \\ &= 1 + \langle n^i w^i \rangle + \langle n^j w^j \rangle + E(\theta) [\langle n^i n^j \rangle + \langle n^i w^j \rangle + \langle n^j w^i \rangle \\ &\quad + \langle w^i w^j \rangle + \langle n^i n^j w^i \rangle + \langle n^i n^j w^j \rangle + \langle n^i w^j w^j \rangle + \langle n^j w^i w^i \rangle \\ &\quad + \langle n^i n^j w^i w^j \rangle]. \end{aligned} \quad (9)$$

Ignoring correlations higher than second order in  $n^i$  and  $w^i$ ,<sup>2</sup> and performing the same calculation for the denominator of Eq. (8),

<sup>2</sup> It is not inherently obvious that this is a valid assumption. However, after performing calculations with and without higher-order correlations, the largest relative difference between the outcomes of both equations was less than  $5 \times 10^{-4}$ .

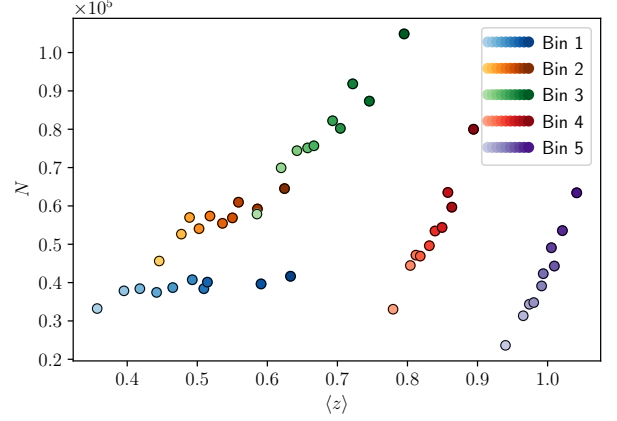


Fig. 2: Weighted number of galaxies  $N$  and average redshift  $\langle z \rangle$  in the KiDS+VIKING-450 survey (KV450, Wright et al. 2018) in pointings of different depth for each of the five tomographic bins used in H18. Each colour corresponds to one redshift bin of H18. A single point represents one percentile of the respective redshift bin, where the fainter points denote pointings of shallower depth.

we get

$$\begin{aligned} \xi_{\pm}^{ij, \text{obs}}(\theta) &= \left[ 1 + \langle n^i w^i \rangle + \langle n^j w^j \rangle + E(\theta) (\langle n^i n^j \rangle + \langle n^i w^j \rangle \right. \\ &\quad \left. + \langle n^j w^i \rangle + \langle w^i w^j \rangle) \right] \left[ 1 + E(\theta) \langle n^i n^j \rangle \right]^{-1} \xi_{\pm}^{ij, \text{uni}}(\theta). \end{aligned} \quad (10)$$

A model correlation function for a cosmic shear survey is usually calculated by taking the average redshift distribution of a redshift bin, weighted by the number density. Ignoring that the depth is correlated on scales of one pointing (here at  $\theta \leq \sqrt{2}^\circ$ ) is equivalent to setting  $E(\theta) \equiv 0$ . Note that there is still a correlation between  $N$  and  $W$  for the same galaxy. Performing the same calculations as above, this yields a relation between the correlation function of uniform depth,  $\xi_{\pm}^{ij, \text{uni}}$ , and the one that is usually modelled,  $\xi_{\pm}^{ij}$ :

$$\xi_{\pm}^{ij}(\theta) = \left( 1 + \langle n^i w^i \rangle + \langle n^j w^j \rangle \right) \xi_{\pm}^{ij, \text{uni}}(\theta). \quad (11)$$

When an observer now calculates the model correlation functions  $\xi_{\pm}^{ij}$  without accounting for varying depth between pointings, the ratio between modelled and observed correlation functions becomes:

$$\begin{aligned} \frac{\xi_{\pm}^{ij}(\theta)}{\xi_{\pm}^{ij, \text{obs}}(\theta)} &\approx \left[ 1 + \langle n^i w^i \rangle + \langle n^j w^j \rangle + E(\theta) \langle n^i n^j \rangle \right] \\ &\quad \times \left[ 1 + \langle n^i w^i \rangle + \langle n^j w^j \rangle + E(\theta) (\langle n^i n^j \rangle + \langle n^i w^j \rangle \right. \\ &\quad \left. + \langle n^j w^i \rangle + \langle w^i w^j \rangle) \right]^{-1}. \end{aligned} \quad (12)$$

It is interesting to note that  $\xi_{\pm}^{ij} = \xi_{\pm}^{ij, \text{obs}}$  holds wherever  $E(\theta) = 0$ , so we expect the observed and the modelled correlation functions to be equivalent on scales where the depth is uncorrelated.

### 3. A semi-analytic model

The previously derived analytic model describes how varying depth between pointings modifies the correlation function due

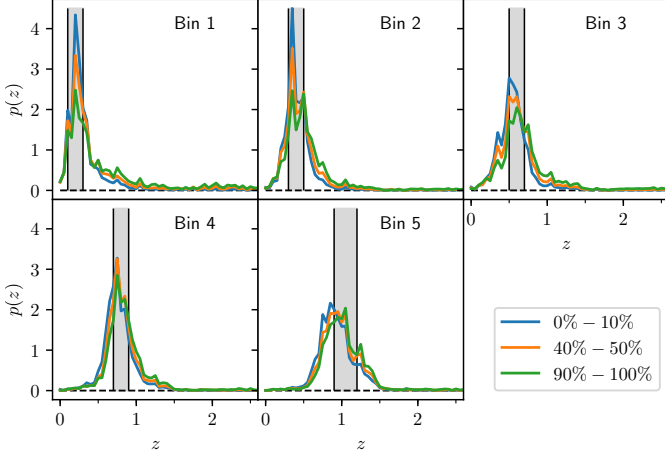


Fig. 3: The source redshift distributions  $p_m^i(z)$  for a selection of very shallow pointings (blue), average pointings (yellow) and very deep pointings (green). The percentage points in the legend denote to which percentile a pointing belongs, when all are ordered by their depth.

to the correlation between number density and average redshift of source galaxies. While this model serves as an intuitive first approximation, it completely ignores any effects from the large scale structure (LSS) between the closest and the most distant galaxy. Therefore, we do not expect this model to yield accurate, quantitative results for cosmic shear surveys.

Below we derive a more sophisticated model that includes the effects of the LSS. While it is computationally more expensive, it yields accurate results for cosmic shear surveys, which are sensitive to the exact redshift distributions of sources as well as the underlying cosmology.

An inspection of KiDS-data showed that the redshift distribution of sources is highly correlated with the limiting magnitude in the  $r$ -band. We thus chose to separate the survey into 10 percentiles, sorted by  $r$ -band depth, i.e. if a pointing had a shallower depth than 90% of the other pointings, it would belong to the first percentile, and so on. For each percentile  $m$  and each tomographic redshift bin  $i$  we can extract a weighted number of galaxies  $N_m^i$  and a source redshift distribution  $p_m^i(z)$  following the direct spectroscopic calibration method of H18. In Fig. 2 the average redshift and weighted number of galaxies are plotted for each percentile of each redshift bin, whereas a selection of source redshift distributions is depicted in Fig. 3. A table of the limiting magnitudes for each percentile can be found in Tab. C.1.

Given two comoving distance probability distributions of sources,  $\mathcal{L}_m^i(\chi)$  and  $\mathcal{L}_n^j(\chi)$ , we can compute the shear correlation functions from the underlying matter power spectrum,  $P_\delta(k, \chi)$ , via (Kaiser 1992)

$$\xi_{\pm, mn}^{ij}(\theta) = \int_0^\infty \frac{d\ell}{2\pi} J_{0,4}(\ell\theta) P_{\kappa, mn}^{ij}(\ell), \quad (13)$$

$$P_{\kappa, mn}^{ij}(\ell) = \frac{9H_0^4 \Omega_m^2}{4c^4} \int_0^{\chi_H} d\chi \frac{g_m^i(\chi) g_n^j(\chi)}{a^2(\chi)} P_\delta\left(\frac{\ell}{f_K(\chi)}, \chi\right), \quad (14)$$

$$g_m^i(\chi) = \int_\chi^{\chi_H} d\chi' \mathcal{L}_m^i(\chi') \frac{f_K(\chi' - \chi)}{f_K(\chi')}. \quad (15)$$

Here,  $J_n$  denote the  $n$ -th order Bessel Functions,  $f_K(\chi)$  is the comoving angular diameter distance and  $\chi_H$  is the comoving distance to the horizon. The parameters  $H_0$  and  $c$  denote the Hubble constant and the speed of light.

Using Eq. (13), we can compute the model correlation functions,  $\xi_{\pm, mn}^{ij}(\theta)$ , for each pair of percentiles  $m, n$  and redshift bins  $i, j$ .<sup>3</sup> When measuring the shear correlation functions of a survey, we take the weighted average of tangential and cross shears of all pairs of galaxies (see H17). If, for a single pair of galaxies, one galaxy lies in the  $m$ -th percentile of redshift bin  $i$  and the second one lies in the  $n$ -th percentile of redshift bin  $j$ , then their contribution to the observed correlation functions is, on average,  $\xi_{\pm, mn}^{ij}(\theta)$ . This means that if we know each of those single correlation functions, we can reconstruct the total correlation functions via a weighted average of the single functions. Formally, we define

$$\xi_{\pm}^{ij, \text{obs}}(\theta) = \frac{\sum_{m,n} \mathcal{P}_{mn}^{ij}(\theta) \xi_{\pm, mn}^{ij}(\theta)}{\sum_{m,n} \mathcal{P}_{mn}^{ij}(\theta)}, \quad (16)$$

where  $\mathcal{P}_{mn}^{ij}$  is a weighting of the correlation functions, which has to be proportional to the probability that a galaxy pair of separation  $\theta$  comes from percentiles  $m$  and  $n$ . In this analysis, we will assume an uncorrelated distribution of depth and neglect boundary effects as well as the sample variance of the depth-distribution between pointings. We will later discuss the validity of these assumptions as well as possible mitigation strategies.

To calculate  $\mathcal{P}_{mn}^{ij}(\theta)$  we imagine two arbitrary (infinitesimally small) surface elements  $d^2\theta_1$  and  $d^2\theta_2$  of separation  $\theta$  on the sky. For the case  $m \neq n$  we know that the two galaxies contributing to  $\mathcal{P}_{mn}^{ij}(\theta)$  have to lie in different pointings, else they would automatically be in the same percentile. The probability that the surface elements are within different pointings is  $[1 - E(\theta)]$ . Furthermore, the first element  $d^2\theta_1$  has to lie in percentile  $m$ , the probability of which is  $1/10$ . The pointing of the second element  $d^2\theta_2$  has to be of percentile  $n$ ; the probability of that is also equal to  $1/10$ . The probability that a galaxy pair populates those surface elements is proportional to the weighted number of galaxies  $N_m^i$  and  $N_n^j$ . We get for  $n \neq m$ :

$$\mathcal{P}_{mn}^{ij}(\theta) = [1 - E(\theta)] \frac{1}{100} N_m^i N_n^j. \quad (17)$$

For the calculation of  $\mathcal{P}_{mn}^{ij}(\theta)$  we have to account for a different possibility: In case that the galaxies lie in the same pointing, they automatically are in the same percentile. We therefore obtain

$$\mathcal{P}_{mn}^{ij}(\theta) = E(\theta) \frac{1}{10} N_m^i N_m^j \delta_{mn} + [1 - E(\theta)] \frac{1}{100} N_m^i N_n^j, \quad (18)$$

where  $\delta_{mn}$  denotes the Kronecker delta. Inserting this into Eq. (16), we compute

$$\xi_{\pm, mn}^{ij, \text{obs}}(\theta) = \frac{1}{C} \sum_{m=1}^{10} N_m^i \left\{ E(\theta) N_m^j \xi_{\pm, mn}^{ij}(\theta) + \frac{[1 - E(\theta)]}{10} \sum_{n=1}^{10} N_n^j \xi_{\pm, mn}^{ij}(\theta) \right\}, \quad (19)$$

<sup>3</sup> For the calculation of the shear correlation functions we use NICAIA (Kilbinger et al. 2009). For the power spectrum on nonlinear scales, we use the method of Takahashi et al. (2012).

with the normalization

$$C = \sum_{m=1}^{10} N_m^i \left[ E(\theta) N_m^j + \frac{[1 - E(\theta)]}{10} \sum_{n=1}^{10} N_n^j \right]. \quad (20)$$

A mathematically more rigorous derivation of this function can be found in App. A.3.

Computing this for all 5 redshift bins of the KV450-survey, forces us to calculate and coadd 1275 correlation functions<sup>4</sup>. Since the variation in depth is a relatively small effect, even tiny numerical errors can add up, skewing the calculations. Additionally, calculating  $10^3$  correlation functions is computationally expensive. However, if we examine Eq. (15), we see that the comoving distance distribution of sources enters linearly. This in turn implies that in Eqs. (14) and (13), both source distance distributions enter linearly, meaning that, instead of adding correlation functions, we can add their respective redshift distributions and compute the correlation functions of that. In particular, we can define the *combined number of galaxies*  $N^i$  and *average comoving distance probability distribution*,  $\mathcal{L}^i(\chi)$ , of tomographic bin  $i$  as

$$N^i \equiv \sum_m N_m^i, \quad \mathcal{L}^i(\chi) = \frac{\sum_m N_m^i \mathcal{L}_m^i(\chi)}{\sum_m N_m^i}. \quad (21)$$

Defining  $\xi_{\pm}^{ij}$  as the correlation functions between the average comoving distance distributions  $\mathcal{L}^i(\chi)$  and  $\mathcal{L}^j(\chi)$ , we find:

$$\begin{aligned} \sum_{m,n} N_m^i N_n^j \xi_{\pm, mn}^{ij}(\theta) &= \frac{9H_0^4 \Omega_m^2}{4c^4} \sum_{m,n} N_m^i N_n^j \int_0^\infty \frac{d\ell}{2\pi} J_{0,4}(\ell\theta) \\ &\quad \times \int_0^{\chi_H} \frac{d\chi}{a^2(\chi)} P_\delta \left( \frac{\ell}{f_K(\chi)}, \chi \right) \int_\chi^{\chi_H} d\chi' \mathcal{L}_m^i(\chi') \frac{f_K(\chi' - \chi)}{f_K(\chi')} \\ &\quad \times \int_\chi^{\chi_H} d\chi'' \mathcal{L}_n^j(\chi'') \frac{f_K(\chi'' - \chi)}{f_K(\chi'')} \\ &= N^i N^j \frac{9H_0^4 \Omega_m^2}{4c^4} \int_0^\infty \frac{d\ell}{2\pi} J_{0,4}(\ell\theta) \int_0^{\chi_H} \frac{d\chi}{a^2(\chi)} P_\delta \left( \frac{\ell}{f_K(\chi)}, \chi \right) \\ &\quad \times \int_\chi^{\chi_H} d\chi' \frac{\sum_m N_m^i \mathcal{L}_m^i(\chi')}{N^i} \frac{f_K(\chi' - \chi)}{f_K(\chi')} \\ &\quad \times \int_\chi^{\chi_H} d\chi'' \frac{\sum_n N_n^j \mathcal{L}_n^j(\chi'')}{N^j} \frac{f_K(\chi'' - \chi)}{f_K(\chi'')} \\ &= N^i N^j \xi_{\pm}^{ij}(\theta). \end{aligned} \quad (22)$$

Consequently, we can apply this to (19), yielding

$$\begin{aligned} \xi_{\pm}^{ij, \text{obs}}(\theta) &= \frac{1}{C} \left\{ E(\theta) \left[ \sum_{m=1}^{10} N_m^i N_m^j \xi_{\pm, mm}^{ij}(\theta) \right] \right. \\ &\quad \left. + \frac{[1 - E(\theta)]}{10} \xi_{\pm}^{ij}(\theta) N^i N^j \right\}. \end{aligned} \quad (23)$$

For each pair of redshift bins we thus only have to compute eleven correlation functions, which reduces the number of functions to compute from 1275 to 165.

<sup>4</sup> For each of the 15 pairs of redshift bins we need to calculate 100 correlation functions, except for the pairs of bins with the same redshift, where only 55 correlation functions need to be calculated due to symmetry.

## 4. Results

Here we apply both the analytic and the semi-analytic method to model the data from the KiDS+VIKING-450 survey (KV450, Wright et al. 2018). While the application of the semi-analytic method is straightforward, for the analytic method we need to decide how to estimate the weight function  $W$  from the given redshift data. Following the separation of a survey into percentiles as in Sect. 3, we define  $W(\theta) \equiv W_n$  whenever  $\theta$  is in a pointing of percentile  $n$ . For the determination of  $W_n$  we test two approaches: As a first method, following Van Waerbeke et al. (2006); Bernardeau et al. (1997), we estimate

$$W_n \propto \langle z \rangle_n^{0.85}, \quad (24)$$

where  $\langle z \rangle_n$  is the average redshift of percentile  $n$ . As a second method we define

$$W_n \propto \sqrt{\langle \gamma_{\times} \gamma_{\times} \rangle(\theta_{\text{ref}}) + \langle \gamma_{\times} \gamma_{\times} \rangle(\theta_{\text{ref}})} = \sqrt{\xi_{+,nn}^{ij}(\theta_{\text{ref}})}, \quad (25)$$

where the  $\xi_{+,nn}^{ij}(\theta_{\text{ref}})$  denotes the model correlation function defined in Sect. 3, evaluated at a characteristic scale  $\theta_{\text{ref}}$ , that needs to be chosen.

While the first method suffers from the fact that the power-law index only holds for sources of redshifts  $1 \lesssim z \lesssim 2$ , the second method is sensitive to the angular range  $\theta_{\text{ref}}$ , at which the shear correlation functions are evaluated, which is fairly arbitrary. In our case, we chose  $\theta_{\text{ref}} \approx 11'$ , which is roughly in the logarithmic middle between the range of the correlation functions,  $[0.5, 300']$ . The choice of other values for  $\theta_{\text{ref}}$  leads to a different amplitude of the change  $\xi_{\pm}/\xi_{\pm}^{\text{obs}}$ , but does not affect its shape. In particular, the highest amplitude of the change is at  $\theta_{\text{ref}} = 0.5'$ .

We applied both analytic methods and the semianalytic one to data from KV450, following the separation into tomographic bins as in H18, and computed the ratio between our model for the observed correlation functions,  $\xi_{\pm}^{\text{obs}}$ , and the model correlation functions,  $\xi_{\pm}$ , ignoring variations in depth.

We compare our models to the results measured from numerical simulations. Using a modified version (Joachimi, Lin, et al. in prep.) of Full-sky Lognormal Astro-fields Simulation Kit (FLASK, Xavier et al. 2016), we generate galaxy mocks with coherent clustering and lensing signals from lognormal fields. For each lognormal field, one mock with uniform depth and another one with variable depth is generated. In the variable case, the depth of KiDS-1000 data (Kuijken et al. 2019) is binned by magnitude into roughly 20 bins. Afterwards, a linear relation between depth and effective number density is extracted. The KiDS-1000 survey is put on a Healpix grid, and for each pixel the limiting magnitude is calculated. According to this limiting magnitude, an effective number density can be assigned, using the linear relation extracted above. For each pixel and each tomographic redshift bin we use the same limiting magnitude to assign an average source redshift distribution from the ones extracted in this work. In the uniform case, redshifts and number densities are sampled from the average of these tomographic sets. Finally, the ratio of the average lensing signals from the two mocks is computed. The number of realizations is 2000. Shape noise is omitted.

The results can be seen in Fig. 4. We observe that for high-redshift bins, both analytic methods as well as the semi-analytic one yield consistent results. Due to the redshift-dependent index in the power law of the first analytic method, it is not able to accurately describe the effect for low redshift bins. The second analytic method, however, traces the semi-analytic one pretty well



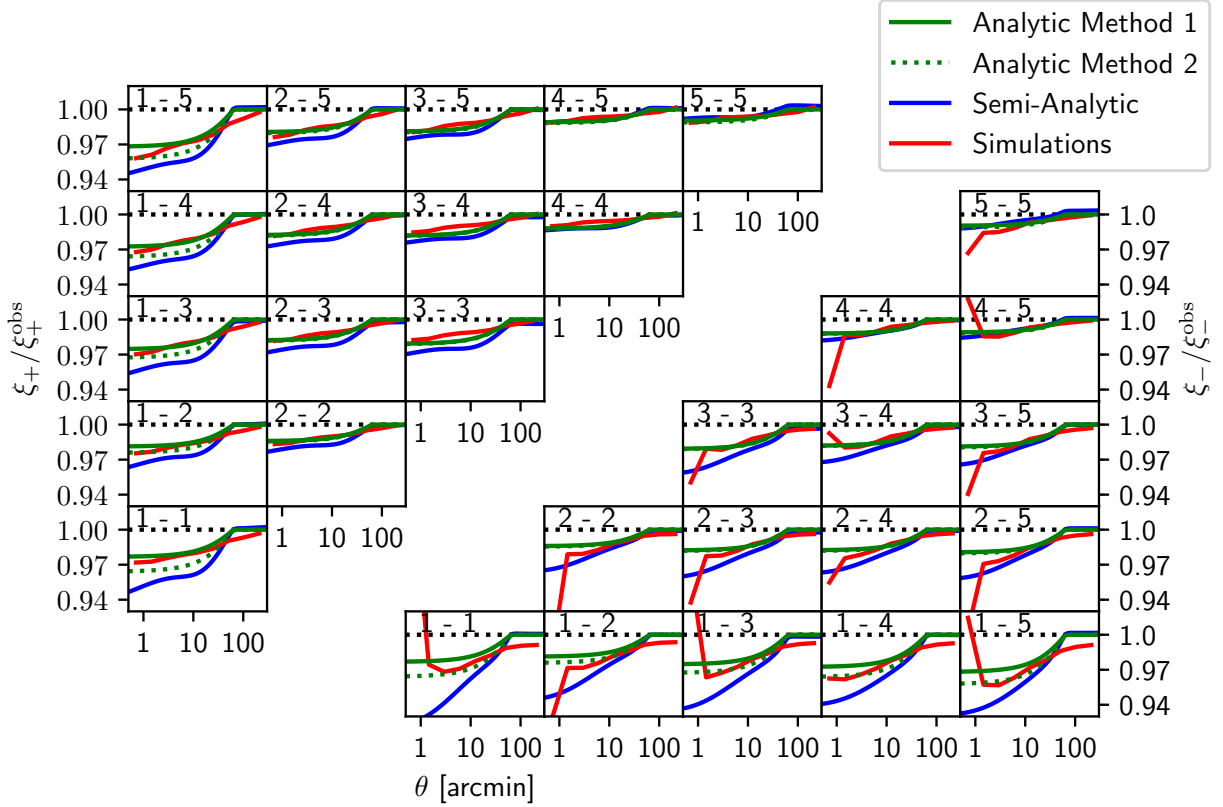


Fig. 4: The ratio of modelled to observed correlation functions for the analytic methods (green), the semi-analytic method (blue) and the numerical simulations (red) for a cross-correlation of all redshift bins. The numbers in the upper left corners correspond to the respective redshift bins, the upper left triangle depicts the ratios of  $\xi_+$ , whereas the lower right triangle depicts the ratios of  $\xi_-$ . The semi-analytic model was computed for the best-fit cosmology of H18. For the characteristic scale  $\theta_{\text{ref}}$  of the second analytic method we chose  $\theta_{\text{ref}} \approx 11'$ .

for  $\xi_+$ . As  $\xi_-$  is affected much stronger by this effect, the analytic method is not able to trace this change<sup>5</sup>. Furthermore we note that the effect seems to be strongest in the first redshift bin, which is not surprising, as there the average redshift between pointings varies the most (compare Fig. 2).

The simulations and the models seem to be in relatively good agreement, but there are some differences. It is noticeable that in the simulations, the value  $\xi_{\pm}/\xi_{\pm}^{\text{obs}}$  consistently stays below unity at large scales, which can be attributed to the fact that the depth of different pointings is not completely uncorrelated, as was assumed in the models. Furthermore, we notice some strong features in the simulations at lower values of  $\theta$ , which arise due to the resolution limit of the simulations. In general, the semi-analytic model seems to over-estimate the effect compared to the simulations, which take the full distribution of depth into account. This slight discrepancy could be attributed to the fact that the simulations follow a finer magnitude-binning for the number densities of galaxies. Due to the fact that the discrepancies arise predominantly on small scales, the most likely reason for

the discrepancy is that the simulations take the full variations in depth into account, which include scales smaller than one pointing (especially chip positions and dithering strategies). Several tests suggest that both small-scale effects and a finer magnitude binning partly negate the varying depth between pointings.

An additional difference between the models and simulations is that in the models we neglect boundary effects and the sample-variance of the depth-distribution between pointings, whereas the simulations were performed with the KiDS-1000 footprint. In App. B we develop a model to extract the correction  $\xi_{\pm}^{ij}/\xi_{\pm}^{ij,\text{obs}}$  for a specific survey footprint. With this model we can estimate the impact of a correlated distribution of depth, the sample variance of the depth-distribution and boundary effects. We find that for a square footprint of  $450 \text{ deg}^2$  or  $1000 \text{ deg}^2$  with an uncorrelated depth-distribution, finite field effects are negligible.

As the next step we want to assess how the observational depth variations propagate to cosmological parameters inferred from  $\xi_{\pm}^{ij,\text{obs}}$  compared to  $\xi_{\pm}^{ij}$ . For this test we choose a fiducial cosmology,  $\Phi$ , and determine the relative change in  $\Omega_m$  and  $\sigma_8$  compared to a reference setup with uniform depth. All other cosmological parameters are kept fixed. First, we compute the reference correlation functions,  $\xi_{\pm}^{ij}(\theta, \Phi)$ , for each pair of redshift bins  $i, j$  using NICAFA as described in Sec. 3. Then we derive the observed correlation functions,  $\xi_{\pm}^{ij,\text{obs}}(\theta, \Phi)$ , from Eq. (23). Using the Markov-Chain Monte Carlo sampler EMCEE, we sample correlation functions  $\xi_{\pm}^{ij}(\theta, \Phi')$  for different cosmologies  $\Phi'$  and find the likelihood distribution, given the data vector  $\xi_{\pm}^{ij,\text{obs}}(\theta, \Phi)$

<sup>5</sup> The effect on  $\xi_-$  is much stronger due to the fact that in Equation (13),  $\xi_+$  is computed by filtering the power spectrum with the 0-th order Bessel function. This function peaks at  $\ell\theta = 0$ , meaning that for all values of  $\theta$ , the correlation function  $\xi_+$  is sensitive to small values of  $\ell$ , corresponding to large separations  $\theta$ . However,  $\xi_-$  is obtained by filtering with the 4-th order Bessel function, which peaks at approximately  $\ell\theta \approx 5$ , so for different  $\theta$  this function is sensitive to varying parts of the convergence power spectrum. A more detailed analysis of this can be found in the Appendix of Köhlinger et al. (2017).

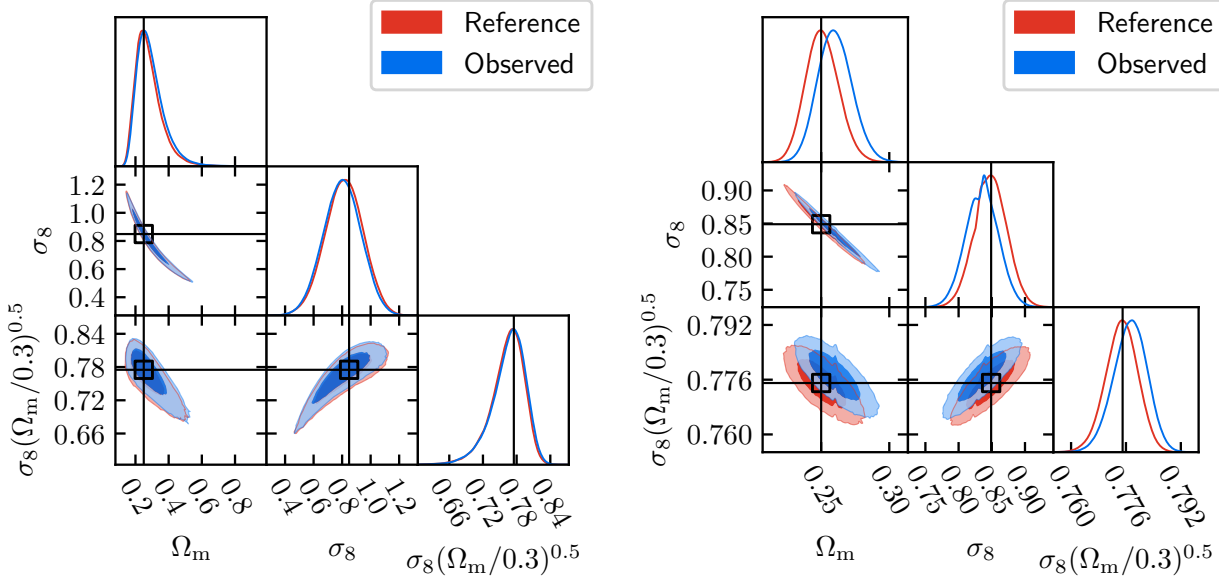


Fig. 5: Results of the MCMC simulation to estimate the bias caused by a variation of depth in a cosmic shear survey for a KiDS-like (left) and ‘Euclid-like’ survey (right). The left simulation was computed using the covariance matrix of H18. As Euclid will survey approx. 15 000 deg<sup>2</sup>, the covariance matrix of the ‘Euclid-like’ survey is the one of H18 divided by 30. Both simulations were computed using a fiducial cosmology of  $\Omega_m = 0.25$  and  $\sigma_8 = 0.85$ .

and the covariance-matrix computed in H18. This yields an estimate of the shift in  $\Omega_m$  and  $\sigma_8$  introduced by varying depth.

As can be seen in Fig. 5, the impact of varying depth is insignificant compared to the uncertainties. To get a rough estimate for the impact on future surveys, we divide our covariance-matrix by a factor of 30, to approximately account for the increased survey area of LSST and Euclid with respect to KV450. Here, the impact on both  $\Omega_m$  and  $\sigma_8$  is significant at the level of approximately  $1\sigma$ . Conveniently the parameter  $\sigma_8$  is considerably more robust against this effect.

Calculating the correction  $\xi_{\pm}^{ij}/\xi_{\pm}^{ij,obs}$  for varying values of  $\Omega_m$  and  $\sigma_8$  reveals a nontrivial dependence on the cosmology, which can be seen in Figure C.1. For various combinations of  $\Omega_m$  and  $\sigma_8$  within the 95% confidence limit of KV450, we report a variation in  $\xi_{\pm}/\xi_{\pm}^{obs}$  of a few percentage points on small scales.

To estimate the B-modes created by this effect, we extract the COSEBIs from the correlation functions,  $\xi_{\pm}^{obs}$ , that have been modified under the semi-analytic model, and from a reference set of correlation functions  $\xi_{\pm}$ . To be most sensitive to the effect of varying depth, we chose logarithmic COSEBIs with an angular range of  $\theta_{min} = 0'.5$  to  $\theta_{max} = 72'$ . As the B-modes of the reference correlation functions are zero, they are a good test for numerical errors in the calculations. Motivated by the discussion in Asgari et al. (2017), we calculated the COSEBIs from correlation functions binned in 400 000 linear bins, which yielded negligible numerical errors. We report a consistent B-mode behaviour across all redshift-bins, which can be seen in Figure 6. However, we compare the B-Modes to the ones measured by Asgari et al. (in prep.) in KV450, which were consistent with zero. Since the B-modes created by varying depth are smaller than these by a factor of 50, we conclude that this effect can not create measurable B-modes in the KV450 survey. It should be noted that the difference in E-modes is as large as the B-modes, which suggests that any significant change in the cosmological parameters due to a varying depth will also yield a significant detection of B-modes.

## 5. Discussion

With our semi-analytic model we describe the impact of varying depth in ground-based cosmic shear surveys. During our analysis we have made several simplifications, which we discuss below.

1. In the most general terms, we are analysing the effects of a position-dependent selection function on cosmic shear surveys. In our analysis, this selection function was governed by the KiDS  $r$ -band depth of a pointing. This neglects a number of other effects: The depth in different bands and the seeing of a pointing will also modify the number densities and redshift distributions on the scale of a pointing (although those variations are also correlated with  $r$ -band depth and thus at least partly accounted for), whereas dithering strategies as well as imperfections in the telescope and CCD cause modifications on sub-pointing scales. However, several tests showed that these effects are subdominant compared to the variations caused by the  $r$ -band depth.
2. We have assumed an uncorrelated distribution of the depth-function and neglected boundary effects as well as the sample variance of the depth-distribution between pointings. While the boundary effects arising from a finite survey footprint have a small impact on the shape of the function  $E(\theta)$ <sup>6</sup>, the governing factor is the sample variance of the depth-distribution. We have assumed that the probability for any pointing to be in percentile  $n$  is exactly the expectation value, namely  $1/10$ . While this would be true for an infinitely large survey with an uncorrelated distribution of the depth-function, it does not necessarily hold for a real survey. However, our analysis in App. B suggests that these effects are not significant for the KV450 survey. In the models, we have also assumed an uncorrelated distribution of the depth-function.

<sup>6</sup> This would be due to the fact that a pointing next to a boundary has fewer neighbours, therefore making it more likely that a galaxy pair is in the same pointing.



Fig. 6: Difference in the E-modes (top left) and B-modes (bottom right) between the reference and the observed correlation functions. For comparison: Scaled total E-modes of the reference correlation function  $E_n$  and scaled B-modes measured in the KV450 survey  $B_n^{KV450}$ . All E- and B-modes were calculated using the logarithmic COSEBIs in S10 for an angular range of  $\theta_{\min} = 0.5$ ,  $\theta_{\max} = 72'$ .

As can be seen in Fig 4, this approximation introduces a small error when compared to the simulations.

3. In our MCMC runs we did not account for degeneracies with other cosmological parameters or observational effects. Especially intrinsic alignments and baryon feedback also modify the correlation functions primarily on small scales, so they are likely to be degenerate with the effect of varying depth (Troxel & Ishak 2015). In an MCMC run that includes these nuisance parameters, we suspect that the parameters for intrinsic alignments and baryon feedback change to mitigate this effect, so that the impact on cosmological parameters will be smaller than in our results.

Despite these repercussions, we are confident to say that the effects of varying depth are not significant for the KV450 survey. In particular this means that a varying depth can not explain the discrepancy between observations of the local Universe and results from analysis of the CMB.

We have shown that this effect can create B-modes. However, Asgari et al. (in prep.) measured the B-modes of the KV450 survey in the same  $\theta$ -range. Those B-modes are larger than the ones created by varying depth by a factor of approx. 50 and show a completely different pattern, yet they are consistent with zero. Thus it is safe to say that varying depth does not create any measurable B-modes in the KV450 survey. An interesting observation is that the change in E-modes is as large as the created B-modes (compare Fig. 6). This means that as soon as this effect causes a significant bias in the cosmological parameters, it will also create significant B-modes. Additionally, the created pat-

tern is very characteristic, which makes it easy to recognize in a B-mode analysis of an actual survey (see Asgari et al. 2019).

For next-generation surveys like Euclid, this effect will be significant. Although Euclid is a space-based telescope, the photometric redshift determination will still be done using ground-based data and therefore suffer from the same effects. Considering our quite rough assumptions regarding the variation in depth and the covariance matrix of the Euclid-survey, a study using a realistic variation of depth and covariance matrix should be conducted.

While the cosmology dependence (Fig. C.1) is not significant for the KV450 survey, it will be relevant for the Euclid survey. In that case, a calculation of the correction for this effect is necessary for various cosmologies.

Additionally, it is interesting to note that  $E(\theta)$  is the azimuthal average of the function  $E(\theta)$  derived in Sect. A.2, which is not isotropic. Therefore, it would be possible to observe a direction-dependent correlation function  $\xi_{\pm}^{i,j,obs}(\theta)$  in future surveys. An anisotropy in the observed correlation function could be a sign for the influence of varying depth.

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*Author contributions:* All authors contributed to the development and writing of this paper. The authorship list is given in two groups: the lead authors (SH, PS, HHi) followed by key contributors to either the scientific analysis or the data products in alphabetical order.

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## Appendix A: Detailed Calculations

### Appendix A.1: Calculation of the power spectrum

Here we will perform the calculation for the observed power spectrum  $P^{\text{obs}}(\ell)$ . For this, we assume an infinitely large field in order to perform our integration over  $\mathbb{R}^2$ . In reality, finite field effects would play a role. We begin with the calculation of the correlation for the Fourier transformed shear:

$$\begin{aligned}
 \langle \hat{\gamma}^{\text{obs}}(\ell) \hat{\gamma}^{\text{obs}*}(\ell') \rangle &= \left\langle \int d^2\theta \int d^2\theta' W(\theta) W(\theta') \gamma(\theta) \gamma^*(\theta') \exp(i\ell\theta - i\ell'\theta') \right\rangle \\
 &= \left\langle \int d^2\theta \int d^2\theta' W(\theta) W(\theta') \exp(i\ell\theta - i\ell'\theta') \int \frac{d^2k}{(2\pi)^2} \int \frac{d^2\ell}{(2\pi)^2} \hat{\gamma}(\mathbf{k}) \hat{\gamma}^*(\ell) \exp(-i\mathbf{k}\theta + i\ell\theta') \right\rangle \\
 &= \left\langle \int d^2\theta \int d^2\theta' \int \frac{d^2k}{(2\pi)^2} \int \frac{d^2\ell}{(2\pi)^2} P(\mathbf{k}) (2\pi)^2 \delta(\mathbf{k} - \ell) \exp[i(\ell\theta - \ell'\theta' - \mathbf{k}\theta + \ell\theta')] W(\theta) W(\theta') \right\rangle \\
 &= \left\langle \int \frac{d^2k}{(2\pi)^2} P(\mathbf{k}) \int d^2\theta W(\theta) \exp[i\theta(\ell - \mathbf{k})] \int d^2\theta' W(\theta') \exp[-i\theta'(\ell' - \mathbf{k})] \right\rangle \\
 &= \left\langle \int \frac{d^2k}{(2\pi)^2} P(\mathbf{k}) \widehat{W}(\ell - \mathbf{k}) \widehat{W}^*(\ell' - \mathbf{k}) \right\rangle
 \end{aligned} \tag{A.1}$$

It is important to keep in mind that the ensemble averages of the weight function are independent of the ensemble averages of the shear values, meaning  $\langle W(\theta) \gamma(\theta) \rangle = \langle W(\theta) \rangle \langle \gamma(\theta) \rangle$ . We can define  $W(\theta) = 1 + w(\theta)$  with  $\langle w(\theta) \rangle = 0$ , which leads to the expression

$$\begin{aligned}
 \langle \hat{\gamma}^{\text{obs}}(\ell) \hat{\gamma}^{\text{obs}*}(\ell') \rangle &= \left\langle \int \frac{d^2k}{(2\pi)^2} P(\mathbf{k}) \left\{ (2\pi)^4 \delta(\ell - \mathbf{k}) \delta(\ell' - \mathbf{k}) + (2\pi)^2 [\hat{w}(\ell - \mathbf{k}) \delta(\ell' - \mathbf{k}) + \hat{w}^*(\ell' - \mathbf{k}) \delta(\ell - \mathbf{k})] + \hat{w}(\ell - \mathbf{k}) \hat{w}^*(\ell' - \mathbf{k}) \right\} \right\rangle \\
 &= (2\pi)^2 \delta(\ell - \ell') P(\ell) + [\langle \hat{w}(\ell - \ell') \rangle P(\ell') + \langle \hat{w}^*(\ell' - \ell) \rangle P(\ell)] + \left\langle \int \frac{d^2k}{(2\pi)^2} \hat{w}(\ell - \mathbf{k}) \hat{w}^*(\ell' - \mathbf{k}) P(\mathbf{k}) \right\rangle \\
 &= (2\pi)^2 \delta(\ell - \ell') P(\ell) + \left\langle \int \frac{d^2k}{(2\pi)^2} \hat{w}(\ell - \mathbf{k}) \hat{w}^*(\ell' - \mathbf{k}) P(\mathbf{k}) \right\rangle,
 \end{aligned} \tag{A.2}$$

where in the final step we have used that the average  $\langle \hat{w}(\ell) \rangle$  vanishes. Up until now, we have not specified our weight-function  $w$ . We parametrize it as

$$w(\theta) = \sum_{\alpha \in \mathbb{Z}^2} w_{\alpha} \Xi(\theta - L\alpha), \text{ with the box-function } \Xi(\theta) = \begin{cases} 1 & \theta \in \left[-\frac{L}{2}, \frac{L}{2}\right]^2 \\ 0 & \text{else} \end{cases}. \tag{A.3}$$

Here, the  $w_{\alpha}$  are random variables, drawn from the random distribution describing the survey depths. For the Fourier transform we compute:

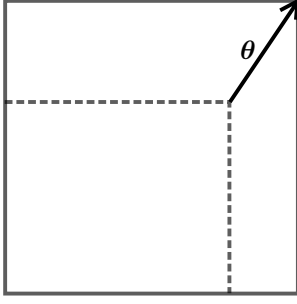
$$\hat{w}(\ell) = \sum_{\alpha \in \mathbb{Z}^2} w_{\alpha} \exp(-iL\ell \cdot \alpha) \widehat{\Xi}(\ell), \tag{A.4}$$

where

$$\widehat{\Xi}(\ell) = \frac{4 \sin\left(\frac{L\ell_1}{2}\right) \sin\left(\frac{L\ell_2}{2}\right)}{\ell_1 \ell_2}, \tag{A.5}$$

is a 2-dimensional sinc function. Assuming an uncorrelated weight-distribution ( $\langle w_{\alpha} w_{\beta} \rangle = 0$  for  $\alpha \neq \beta$ ) and setting  $\langle w^2 \rangle \equiv \langle w_{\alpha}^2 \rangle$  for each  $\alpha$ , we get

$$\begin{aligned}
 &\left\langle \int \frac{d^2k}{(2\pi)^2} \hat{w}(\ell - \mathbf{k}) \hat{w}^*(\ell' - \mathbf{k}) P(\mathbf{k}) \right\rangle \\
 &= \left\langle \int \frac{d^2k}{(2\pi)^2} \sum_{\alpha, \beta} w_{\alpha} w_{\beta} \exp[-iL(\ell - \mathbf{k}) \cdot \alpha] \widehat{\Xi}(\ell - \mathbf{k}) \exp[iL(\ell' - \mathbf{k}) \cdot \beta] \widehat{\Xi}^*(\ell' - \mathbf{k}) P(\mathbf{k}) \right\rangle \\
 &= \int \frac{d^2k}{(2\pi)^2} \sum_{\alpha} \langle w^2 \rangle \exp[-iL(\ell - \mathbf{k}) \cdot \alpha + iL(\ell' - \mathbf{k}) \cdot \alpha] \widehat{\Xi}(\ell - \mathbf{k}) \widehat{\Xi}^*(\ell' - \mathbf{k}) P(\mathbf{k}).
 \end{aligned} \tag{A.6}$$



**Fig. A.1.** Graphic representation on how to obtain the function  $E(\theta)$ . For a separation vector  $\theta$ , the dashed square represents the area of galaxies that have their partner in the same pointing.

Using this result, we can obtain the observed power spectrum

$$P^{\text{obs}}(\ell) = \frac{1}{(2\pi)^2} \int d^2\ell' \langle \hat{\gamma}^{\text{obs}}(\ell) \hat{\gamma}^{\text{obs}*}(\ell') \rangle, \quad (\text{A.7})$$

by performing the  $\ell'$ -integration in (A.2):

$$\begin{aligned} P^{\text{obs}}(\ell) &= P(\ell) + \int \frac{d^2\ell'}{(2\pi)^2} \int \frac{d^2\mathbf{k}}{(2\pi)^2} \sum_{\alpha} \langle w^2 \rangle \exp[-iL(\ell - \mathbf{k}) \cdot \alpha + iL(\ell' - \mathbf{k}) \cdot \alpha] \widehat{\Xi}(\ell - \mathbf{k}) \widehat{\Xi}(\ell' - \mathbf{k}) P(\mathbf{k}) \\ &= P(\ell) + \int \frac{d^2\mathbf{k}}{(2\pi)^2} \sum_{\alpha} \langle w^2 \rangle \exp[-iL(\ell - \mathbf{k}) \cdot \alpha] \widehat{\Xi}(\ell - \mathbf{k}) P(\mathbf{k}) \int \frac{d^2\ell'}{(2\pi)^2} \widehat{\Xi}^*(\ell' - \mathbf{k}) \exp[iL(\ell' - \mathbf{k}) \cdot \alpha] \\ &= P(\ell) + \langle w^2 \rangle \int \frac{d^2\mathbf{k}}{(2\pi)^2} \widehat{\Xi}(\ell - \mathbf{k}) P(\mathbf{k}) \sum_{\alpha} \exp[-iL(\ell - \mathbf{k}) \cdot \alpha] \Xi(L\alpha) \\ &= P(\ell) + \langle w^2 \rangle \int \frac{d^2\mathbf{k}}{(2\pi)^2} \widehat{\Xi}(\ell - \mathbf{k}) P(\mathbf{k}), \end{aligned} \quad (\text{A.8})$$

which is a convolution of the power spectrum and the 2-dimensional sinc function (A.5).

#### Appendix A.2: The function $E(\theta)$

When computing the shear correlation between a pair of galaxies, it is of central importance whether those two galaxies lie in the same pointing or not. We want to model the probability that a pair of galaxies with separation  $\theta$  lie in the same pointing by the function  $E(\theta)$ , which we will derive here:

Given one square field of length  $L$  (in our case  $L = 60'$ ) and a separation vector  $\theta = (\theta_1, \theta_2)$ , without loss of generality we can assume  $\theta_1, \theta_2 \geq 0$ . The dashed square in Fig. A.1 represents all possible positions that the first galaxy can take, such that the second galaxy is still within the same pointing. The volume of this square equals

$$V(|\theta|, \phi) = [L - |\theta| \cos(\phi)] [L - |\theta| \sin(\phi)], \quad (\text{A.9})$$

where  $\phi$  represents the polar angle of the vector  $\theta$ . The function  $E(\theta)$  then simply equals  $V(|\theta|, \phi)/L^2$ . To exclude negative volumes (which could occur when  $|\theta| > 1$  holds), we need to add the Heaviside step function  $\mathcal{H}$ :

$$E(\theta) = \left[ 1 - \frac{|\theta|}{L} \cos(\phi) \right] \left[ 1 - \frac{|\theta|}{L} \sin(\phi) \right] \mathcal{H} \left[ 1 - \frac{|\theta|}{L} \cos(\phi) \right] \mathcal{H} \left[ 1 - \frac{|\theta|}{L} \sin(\phi) \right]. \quad (\text{A.10})$$

As  $E(\theta)$  is not isotropic, in order to obtain the function  $E(\theta) = E(|\theta|)$ , we need to calculate the azimuthal average of Eq. (A.10) over all angles  $\phi$ . While the case  $\theta_1, \theta_2 \geq 0$  certainly does not hold for all angles  $\phi$ , we can omit the other cases by making use of the symmetry of the problem.

$$\begin{aligned} E(\theta) &= \frac{4}{2\pi} \int_0^{\frac{\pi}{2}} d\phi E(\theta) = \frac{2}{\pi} \begin{cases} \int_0^{\frac{\pi}{2}} d\phi \left[ 1 - \frac{|\theta|}{L} \cos(\phi) \right] \left[ 1 - \frac{|\theta|}{L} \sin(\phi) \right], & |\theta| \leq L \\ \int_{\arccos(L/|\theta|)}^{\arcsin(L/|\theta|)} d\phi \left[ 1 - \frac{|\theta|}{L} \cos(\phi) \right] \left[ 1 - \frac{|\theta|}{L} \sin(\phi) \right], & L \leq |\theta| \leq \sqrt{2}L \\ 0, & \sqrt{2}L \leq \theta \end{cases} \\ &= \begin{cases} \frac{1}{L^2\pi} [L^2\pi - (4L - \theta)\theta], & \theta \leq L \\ \frac{2}{\pi} \left[ 4 \sqrt{\frac{\theta^2}{L^2} - 1} - 1 - \frac{\theta^2}{2L^2} - \arccos\left(\frac{L}{\theta}\right) + \arcsin\left(\frac{L}{\theta}\right) \right], & L \leq \theta \leq \sqrt{2}L \\ 0, & \sqrt{2}L \leq \theta \end{cases} \end{aligned} \quad (\text{A.11})$$

### Appendix A.3: Calculation of the shear correlation functions

Following H17, given a set of galaxies we calculate the shear correlation function  $\xi_+^{ij}$  via

$$\xi_+^{ij}(\theta) = \frac{\sum_{a,b} w_a^i w_b^j \epsilon_a^i \epsilon_b^{j*} \Delta(|\theta_a^i - \theta_b^i|)}{\sum_{a,b} w_a^i w_b^j \Delta(|\theta_a^i - \theta_b^i|)}. \quad (\text{A.12})$$

Here,  $w$  represents the lensing weight of the galaxy, whereas  $\epsilon$  is its (complex) ellipticity and  $\theta$  its position on the sky. We have defined the function  $\Delta$  as

$$\Delta(|\theta_a^i - \theta_b^i|) = \begin{cases} 1, & |\theta_a^i - \theta_b^i| \in [\theta, \theta + d\theta] \\ 0, & \text{else} \end{cases}, \quad (\text{A.13})$$

where we assume  $d\theta \ll \theta$ . We define  $N$  as the number of pointings in the survey and  $F_k^i$  as the set of galaxies in pointing  $k$  and tomographic redshift bin  $i$ . The numerator in Eq. (A.12) then transforms to:

$$\begin{aligned} & \sum_{k,\ell=1}^N \sum_{a \in F_k^i} \sum_{b \in F_\ell^j} w_a^i w_b^j \epsilon_a^i \epsilon_b^{j*} \Delta(|\theta_a^i - \theta_b^i|) \\ &= \sum_{k=1}^N \sum_{a \in F_k^i} w_a^i \sum_{\ell=1}^N \sum_{b \in F_\ell^j} w_b^j \Delta(|\theta_a^i - \theta_b^i|) \epsilon_a^i \epsilon_b^{j*} \\ &= \sum_{k=1}^N \sum_{a \in F_k^i} w_a^i \left[ \sum_{b \in F_k^j} w_b^j \Delta(|\theta_a^i - \theta_b^i|) \epsilon_a^i \epsilon_b^{j*} + \sum_{\ell \neq k} \sum_{b \in F_\ell^j} w_b^j \Delta(|\theta_a^i - \theta_b^i|) \epsilon_a^i \epsilon_b^{j*} \right]. \end{aligned} \quad (\text{A.14})$$

When we denote the probability that pointing  $k$  is of percentile  $m$  by  $\mathcal{P}_m^k$  and assume that the product  $\epsilon_a^i \epsilon_b^{j*}$  always equals its expectation value, we can set the numerator as

$$\sum_{k=1}^N \sum_{a \in F_k^i} w_a^i \sum_m \mathcal{P}_m^k \left[ \overbrace{\sum_{b \in F_k^j} w_b^j \Delta(|\theta_a^i - \theta_b^i|) \xi_{+,mm}^{ij}(\theta)}^{(\text{A.15.a})} + \overbrace{\sum_{\ell \neq k} \sum_{b \in F_\ell^j} w_b^j \Delta(|\theta_a^i - \theta_b^i|) \sum_n \mathcal{P}_n^\ell \xi_{+,mn}^{ij}(\theta)}^{(\text{A.15.b})} \right]. \quad (\text{A.15})$$

The term (A.15.a) denotes all galaxies that lie within distance interval  $[\theta, \theta + d\theta]$  of galaxy  $a$ , and are in the same pointing as galaxy  $a$ . This term is equal to the (weighted) number density of galaxies in the pointing multiplied by  $2\pi\theta d\theta E(\theta)$ .

The term (A.15.b) denotes all galaxies within distance interval  $[\theta, \theta + d\theta]$  of galaxy  $a$ , that are *not* in the same pointing as galaxy  $a$ . This is equal to the number density of galaxies in the respective pointings multiplied by  $2\pi\theta d\theta [1 - E(\theta)]$ .

If we assume that said number density in a pointing is equal to the number density in the percentile it belongs to,  $\hat{n}_n^j$ , and set  $\mathcal{P}_n^\ell = 1/10$ , the numerator becomes

$$\sum_{k=1}^N \sum_{a \in F_k^i} w_a^i \sum_m \mathcal{P}_m^k \left[ 2\pi\theta d\theta E(\theta) \hat{n}_m^j \xi_{+,mm}^{ij}(\theta) + 2\pi\theta d\theta \frac{1 - E(\theta)}{10} \sum_n \hat{n}_n^j \xi_{+,mn}^{ij}(\theta) \right]. \quad (\text{A.16})$$

The term  $\sum_{a \in F_k^i} w_a^i$  denotes the number of galaxies in pointing  $k$ , which we set as the number density of galaxies in the respective percentile multiplied with the area  $A$  of the pointing. Applying this and setting  $\mathcal{P}_m^k = 1/10$ , the numerator reads

$$\begin{aligned} & \frac{2\pi\theta d\theta}{10} \sum_{k=1}^N \sum_m \hat{n}_m^i A \left[ E(\theta) N_m^j \xi_{+,mm}^{ij}(\theta) + \frac{1 - E(\theta)}{10} \sum_n \hat{n}_n^j \xi_{+,mn}^{ij}(\theta) \right] \\ &= \frac{2\pi\theta d\theta N A}{10} \sum_m \hat{n}_m^i \left[ E(\theta) \hat{n}_m^j \xi_{+,mm}^{ij}(\theta) + \frac{1 - E(\theta)}{10} \sum_n \hat{n}_n^j \xi_{+,mn}^{ij}(\theta) \right]. \end{aligned} \quad (\text{A.17})$$

The same line of argumentation can be applied to the denominator, which then reads:

$$\frac{2\pi\theta d\theta N A}{10} \sum_m \hat{n}_m^i \left[ E(\theta) \hat{n}_m^j + \frac{1 - E(\theta)}{10} \sum_n \hat{n}_n^j \right]. \quad (\text{A.18})$$

Taking the ratio of the two quantities, and setting  $N_n^i = A \hat{n}_n^i$  we see that Equations (A.12) and (19) are the same.

$E_{02}(\theta)$	$E_{12}(\theta)$	$E_{22}(\theta)$
$E_{01}(\theta)$	$E_{11}(\theta)$	
$E_{00}(\theta)$		

**Fig. B.1.** Graphic representation of the definitions of  $E_{ab}(\theta)$ . When the first galaxy is in the bottom left pointing, the probability to find the second galaxy in a pointing of distance  $(a, b)$  is  $E_{ab}(\theta)$ .

## Appendix B: Finite field effects

In this chapter we will outline how to calculate the correction of the correlation functions for a finite survey with a potentially correlated distribution of depth between pointings. Essentially, this boils down to the calculation of  $\mathcal{P}_{mn}^{ij}(\theta)$  from Eq. (16). We calculate this weighting by the geometrical probability that a pair of galaxies of separation  $\theta$  is of percentiles  $m$  and  $n$ ,  $\mathcal{P}(m, n|\theta)$ , weighted by the respective number of galaxies in the percentiles  $N_m^i, N_n^j$ :

$$\mathcal{P}_{mn}^{ij}(\theta) = N_m^i N_n^j \mathcal{P}(m, n|\theta). \quad (\text{B.1})$$

At first we define functions  $E_{ab}(\theta)$  as the probability that a galaxy pair of separation  $\theta$  is in pointings of distance  $(a, b)$ . This situation is depicted in Fig. B.1. Due to symmetry, for the azimuthal average of the functions,  $E_{ab}(\theta) = E_{-ab}(\theta) = E_{ba}(\theta)$  holds for all combinations of  $a$  and  $b$ . Note that  $E_{00}(\theta) = E(\theta)$  and  $\sum_{a,b} E_{ab}(\theta) \equiv 1$ .

Let  $\mathcal{P}^*(m, n|a, b)$  denote the probability that two pointings of distance  $(a, b)$  are of percentile  $m$  and  $n$  (which is directly calculable from a given survey footprint). Then the following equation holds:

$$\mathcal{P}(m, n|\theta) = \sum_{a,b} E_{ab}(\theta) \mathcal{P}^*(m, n|a, b). \quad (\text{B.2})$$

Note that the expectation value of  $\mathcal{P}^*(m, n|a, b)$  for uncorrelated distributions is

$$\langle \mathcal{P}^*(m, n|a, b) \rangle = \begin{cases} 0.1 \delta_{mn}, & \text{for } (a, b) = (0, 0) \\ 0.01, & \text{else} \end{cases}, \quad (\text{B.3})$$

where  $\delta_{mn}$  denotes the Kronecker delta. Keeping in mind that

$$\sum_{(a,b) \neq (0,0)} E_{ab}(\theta) = 1 - E(\theta), \quad (\text{B.4})$$

we can use the expectation value (B.3) to calculate (B.2) as a consistency check. In that case, we receive the same value for the coefficients in (B.1) as we have in Eq. (18) in Sec. 3 for the case of an infinite footprint and uncorrelated distribution of depth.

The  $E_{ab}$  can all be calculated analytically, similar to our method in Sec. A.2. We again assume a selection of square fields with side length  $L$ , and later set  $L = 60'$  to adapt to the KV450 survey. As an example, for  $E_{01}$  we have several possible situations, depicted in Fig. B.3. Setting  $E_{ab}(\theta) = V(\theta, \phi)/L^2$ , we define

$$\begin{aligned} E_{01}^{(a)}(\theta) &\equiv \frac{\theta}{L} \sin(\phi) \left[ 1 - \frac{\theta}{L} \cos(\phi) \right] \\ E_{01}^{(b)}(\theta) &\equiv \left[ 2 - \frac{\theta}{L} \sin(\phi) \right] \left[ 1 - \frac{\theta}{L} \cos(\phi) \right] \end{aligned} \quad (\text{B.5})$$





**Fig. B.3.** Representation of how to calculate  $E_{01}(\theta)$  for different values of  $\theta$ . For  $\theta \sin(\phi) < L$ , as depicted in the left part, the volume of the dashed rectangle is  $V(\theta, \phi) = \theta \sin(\phi)[L - \theta \cos(\phi)]$ . For  $\theta \sin(\phi) > L$ , as depicted in the right part, the volume of the dashed rectangle is  $V(\theta, \phi) = [2L - \theta \sin(\phi)][L - \theta \cos(\phi)]$ .



**Fig. B.4.** Visualisation of the numerical computation for  $E_{01}(\theta)$ . For a circle of radius  $\theta$ , the length of the red arc divided by  $2\pi$  represents the fraction of galaxies within the respective pointing. This value needs to be integrated for all possible centers of the circle in the pointing. That procedure is straightforward to expand for other  $E_{ab}(\theta)$ .

With some geometric considerations, we compute:

$$\begin{aligned}
 E_{01}(\theta) &= \begin{cases} \frac{1}{\pi} \int_0^{\frac{\pi}{2}} d\phi E_{01}^{(a)}(\theta), & \frac{\theta}{L} < 1 \\ \frac{1}{\pi} \left[ \int_{\arccos(L/\theta)}^{\arcsin(L/\theta)} d\phi E_{01}^{(a)}(\theta) + \int_{\arcsin(L/\theta)}^{\frac{\pi}{2}} d\phi E_{01}^{(b)}(\theta) \right], & 1 < \frac{\theta}{L} < \sqrt{2} \\ \frac{1}{\pi} \int_{\arccos(L/\theta)}^{\frac{\pi}{2}} d\phi E_{01}^{(b)}(\theta), & \sqrt{2} < \frac{\theta}{L} < 2 \\ \frac{1}{\pi} \int_{\arccos(2L/\theta)}^{\arcsin(2L/\theta)} d\phi E_{01}^{(b)}(\theta), & 2 < \frac{\theta}{L} < \sqrt{5} \\ 0, & \sqrt{5} < \frac{\theta}{L} \end{cases} \\
 &= \begin{cases} \frac{(2L-\theta)\theta}{2\pi L^2}, & \frac{\theta}{L} < 1 \\ \frac{1}{\pi} \left[ \frac{3}{2} - 2\frac{\theta}{L} + \frac{\theta^2}{L^2} + 2\sqrt{\frac{\theta^2}{L^2} - 1} + 2\arcsin\left(\frac{L}{\theta}\right) \right], & 1 < \frac{\theta}{L} < \sqrt{2} \\ \frac{1}{2\pi} \left[ -1 - 4\frac{\theta}{L} + 4\sqrt{\frac{\theta^2}{L^2} - 1} + 4\arccos\left(\frac{L}{\theta}\right) \right], & \sqrt{2} < \frac{\theta}{L} < 2 \\ \frac{1}{2\pi} \left[ -5 - \frac{\theta^2}{L^2} + 2\sqrt{\frac{\theta^2}{L^2} - 4} + 4\sqrt{\frac{\theta^2}{L^2} - 1} - 4\arcsin\left(\frac{L}{\theta}\right) + 4\arcsin\left(\frac{2L}{\theta}\right) \right], & 2 < \frac{\theta}{L} < \sqrt{5} \\ 0, & \sqrt{5} < \frac{\theta}{L} \end{cases} \quad (\text{B.6})
 \end{aligned}$$



**Fig. B.5.** The functions  $E_{ab}(\theta)$  for the first few possible combinations.



**Fig. B.6:**  $2\sigma$ -contours of the corrections for the correlation functions for a  $100 \text{ deg}^2$  field (blue), a  $450 \text{ deg}^2$  field (red) and a  $1000 \text{ deg}^2$  field (green). As can be seen, the variance of the variation is small for a  $450 \text{ deg}^2$  field and barely noticeable for a  $1000 \text{ deg}^2$  field.

Naturally, to calculate those functions for all possible combinations would be rather tedious, however they are simple to determine numerically (compare Fig. B.4). A plot of these functions can be found in Fig. B.5.

We sample several realizations of a random depth-distribution for a  $100 \text{ deg}^2$ -field, a  $450 \text{ deg}^2$ -field and a  $1000 \text{ deg}^2$ -field. For each realization we extract the Function  $\mathcal{P}^*(m, n|a, b)$  and, using Eq. (B.2), calculate the ratio  $\xi_{\pm}^{\text{obs}}/\xi_{\pm}$ . Afterwards, we compute the variance of these ratios. As can be seen from Fig. B.6, the effect is quite significant for a  $100 \text{ deg}^2$ -field, but almost negligible for a  $1000 \text{ deg}^2$ -field. This leads to the assumption that both for the KV450 survey as well as for all next-generation cosmic shear surveys, finite field effects do not need to be accounted for. However, if the distribution of depth is correlated in the surveys, that might have a noticeable impact on the results.

## Appendix C: Additional Figures and Tables

Table C.1: Limiting magnitudes for the ten percentiles

Percentile	$r$ -band depth
0	25.76
10	26.06
20	26.15
30	26.19
40	26.23
50	26.27
60	26.31
70	26.34
80	26.39
90	26.44
100	26.60

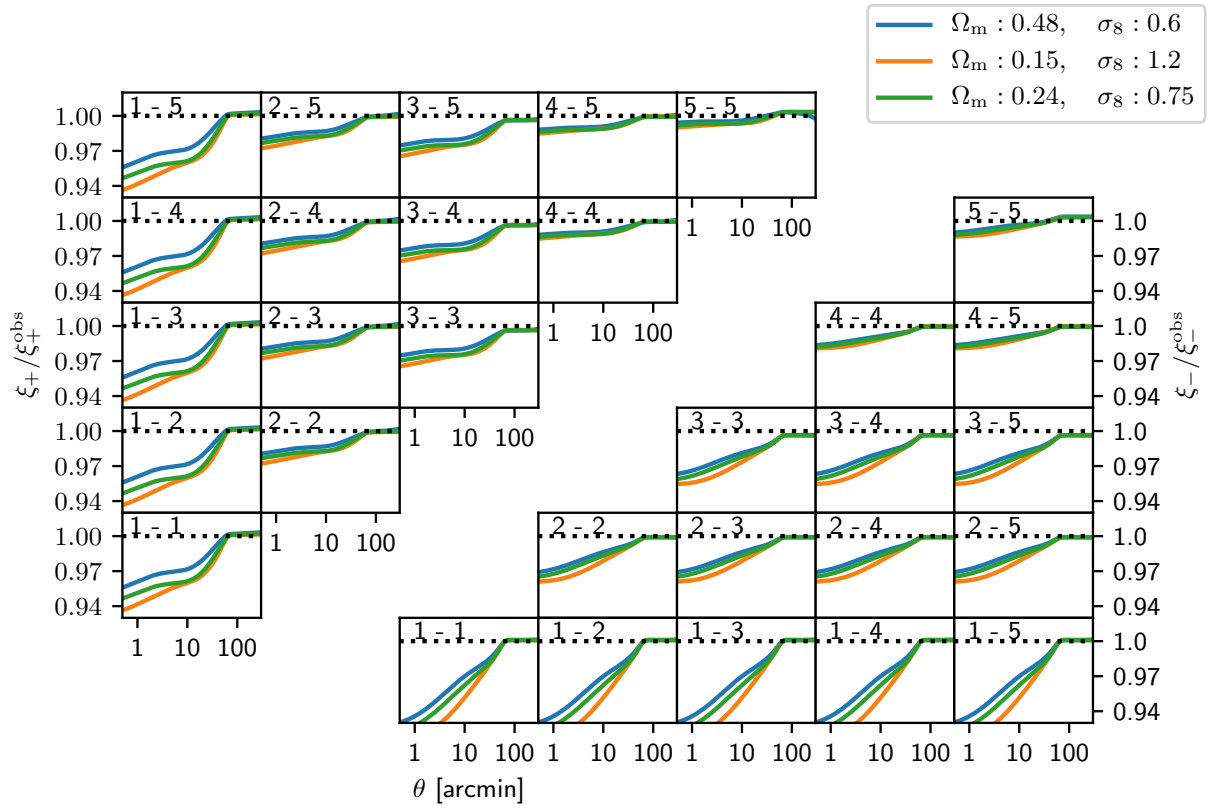


Fig. C.1: Correction to the correlation functions in varying cosmologies. Depicted here are three flat sample cosmologies, where values within the 98% CL of the KV450 survey were sampled.