Assignment–2

Title: Learning Probability Density Functions using data only

Dataset: Consider NO_2 concentration as the feature (x).
Dataset link: https://www.kaggle.com/datasets/shrutibhargava94/india-air-quality-data

Objective
To learn an unknown probability density function of a transformed random variable using a Generative Adversarial Network (GAN).

Tasks to be Performed

Step-1: Transform each value of x into z using the transformation function given below.

$$z = T_r(x) = x + a_r*\sin(b_r*x) \tag{1}$$

where $a_r = 0.5 * (r \bmod 7)$, $b_r = 0.3 * (r \bmod 5 + 1)$

where, mod returns remainder and r is your UNIVERSITY ROLL NUMBER.

Step-2: PDF Estimation using GAN (Core Task)
In this assignment, no analytical form of the probability density function is given.

You are required to:

1. Assume that the transformed variable (z) is sampled from an unknown distribution.
2. Design and train a Generative Adversarial Network (GAN) to learn this distribution.
3. Use the generator network to implicitly model the probability density of (z).

Important Notes
- The GAN must learn the distribution only from samples of (z).
- No parametric PDF (Gaussian, exponential, etc.) should be assumed.
- The discriminator should distinguish between:
    - Real samples: (z)
    - Fake samples: ($z_f = G(error)$), where error follows N(0,1).

Step-3: PDF Approximation from Generator Samples
After training the GAN:
1. Generate a large number of samples (z_f) from the generator
2. Estimate the probability density (p_h (z)) using:
    - Histogram density estimation or Kernel Density Estimation (KDE)

What to Submit
- Transformation parameters (a_r, b_r)
- GAN architecture description
- PDF plot obtained from GAN samples
- Observations on:
  - Mode coverage
  - Training stability
  - Quality of generated distribution

Important Instructions
- Deadline: 11 Feb 2026
- Late submissions will receive zero marks.
- Technical issues must be reported before the deadline.
- Use of AI-based tools is strictly prohibited.
- Submissions exhibiting AI-generated patterns will be treated as academic misconduct.
- If AI usage is detected → Marks = 0