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# Nonparametric Analysis of **US Dairy Production and Consumption**

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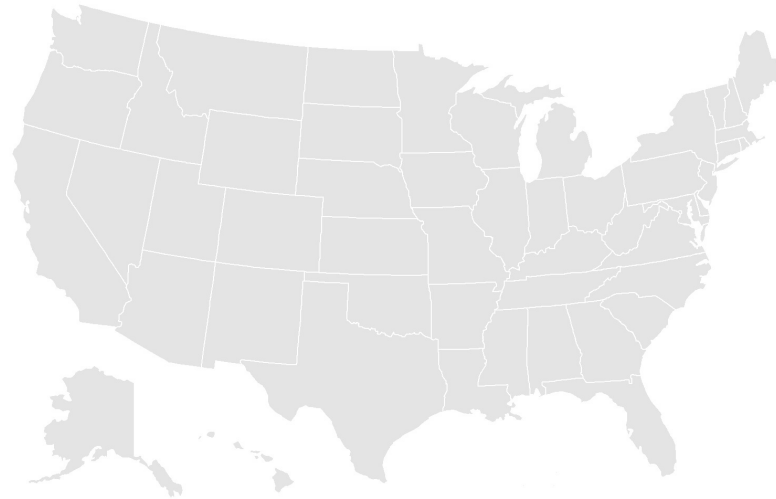
December 13th, 2022  
Work in Progress Presentation #2



# Dataset presentation

The data consists of **yearly** measurements of production and consumptions of **US dairy** products.

Although there are many variables available, we are **focusing** on:



1980



2014

+

2015



2021

Data  
provided by  
tidytuesday

Production

**Milk price [\$]**

Milk production [lbs]

Hay price [\$] etc.

Consumption  
[lbs/person]

Milk (milk, yogurt, cottage, ...)

Cheese (mozzarella, cheddar, swiss, ...)

We retrieved  
data to fill the  
observations  
up to the past  
year

# Goals

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We identified our main stakeholders in **cheese factories** with one of the following **needs**:

## Improvements to the production chain



**Identify** which dairy products have seen their **consumption increase** and which **decline** over time, and the reasons behind



The aim is to **understand potential improvements** to production chain and **marketing strategy** of declining goods

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## Optimal price strategy of a new competitor



A **new potential competitor** wants to decide whether to **join the market** or not, the problem is to identify the **potential of its resources**



It's therefore important to have a clear idea of the **pricing** of goods and make **predictions** about it

# Data Pipeline



Adjust prices for **inflation**:<sup>1</sup>

$$2022 \text{ USD value} = \frac{\text{CPI in 2022}}{\text{CPI in 1980}} \cdot 1980 \text{ USD value}$$

Embed **import/export** data

**Import volume** as price regressor, index of competition with domestic production  
**Export volume** as indicator of drive for production demand

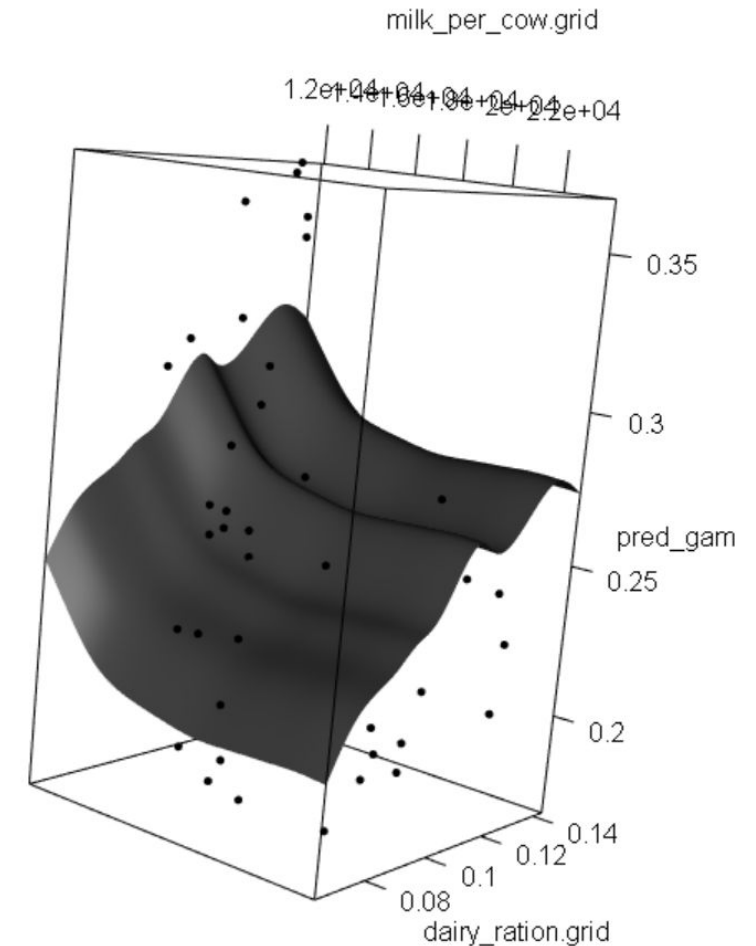
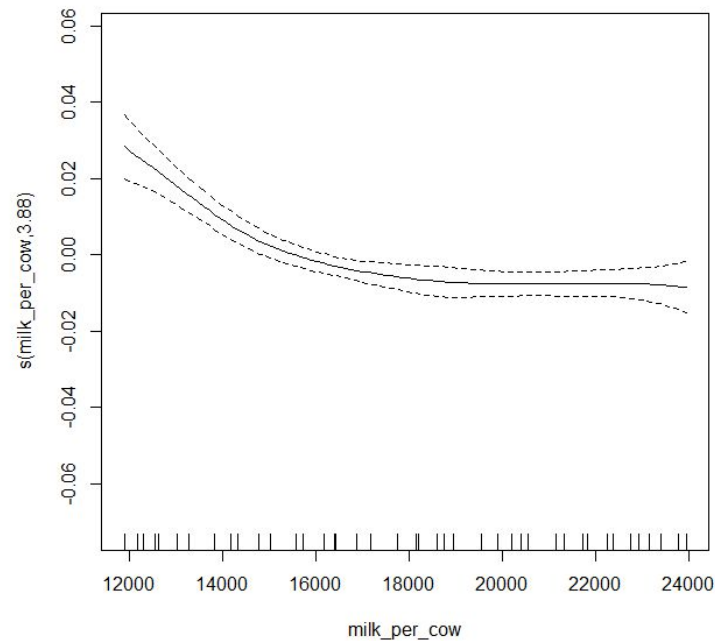
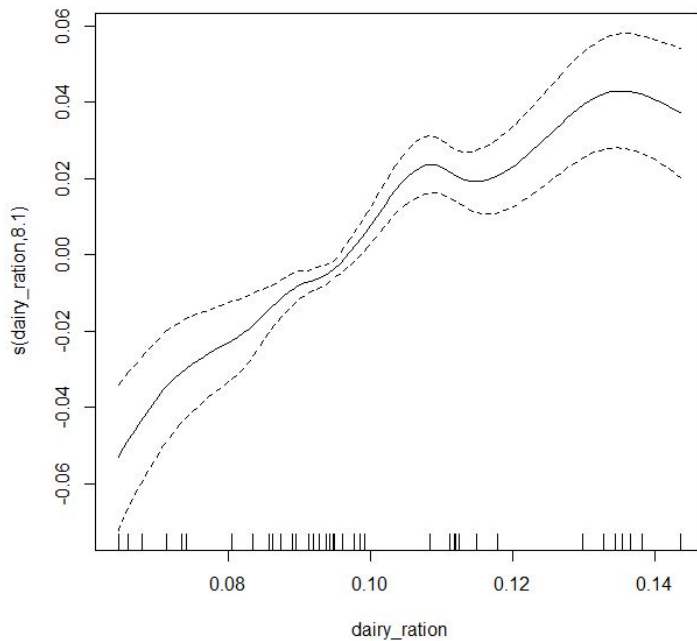
<sup>1</sup>CPI: Consumer Price Index

# GAM



$$\begin{aligned}\text{avg\_price\_milk} = & \beta_0 + \beta_1 \text{milk\_cow\_cost\_per\_animal}_i \\ & + \beta_2 \text{milk\_volume\_to\_buy\_cow\_in\_lbs}_i \\ & + \beta_3 \text{milk\_feed\_price\_ratio}_i \\ & + f_1(\text{dairy\_ration}_i) + f_2(\text{milk\_per\_cow}_i) + \epsilon_i\end{aligned}$$

We performed multiple **Permutation Tests** to assess the significance of each covariate.



# GAM

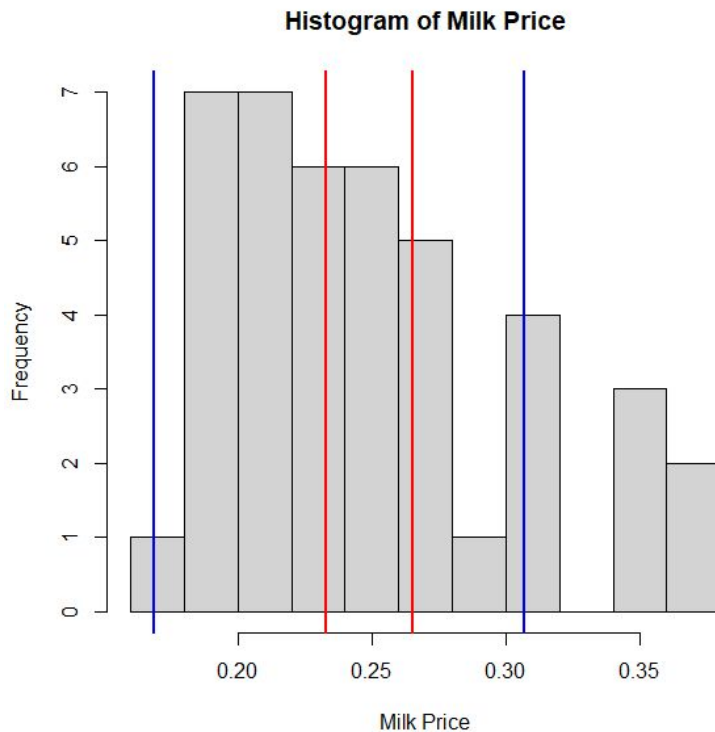


## Conformal Prediction

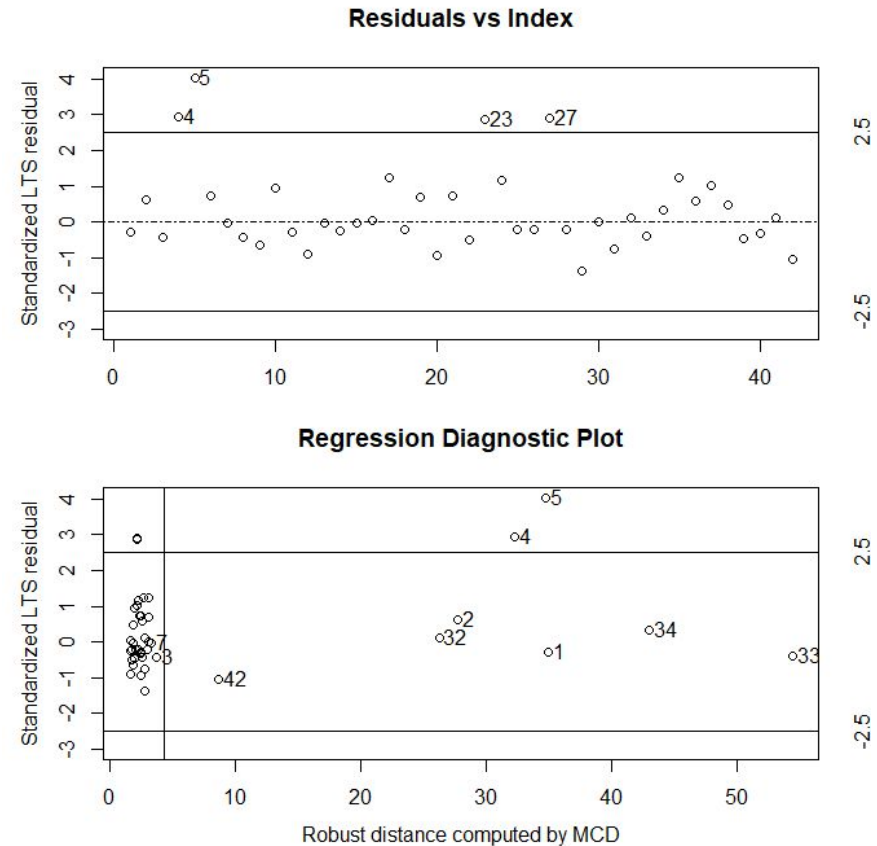
The two conformal interval are respectively:

**Red:** Based on the aforementioned **GAM**.

**Blue:** Created using the **KNN** distance.



## Robust Regression



We can note four outliers, corresponding to the years **1983, 1984, 2002, and 2006**.

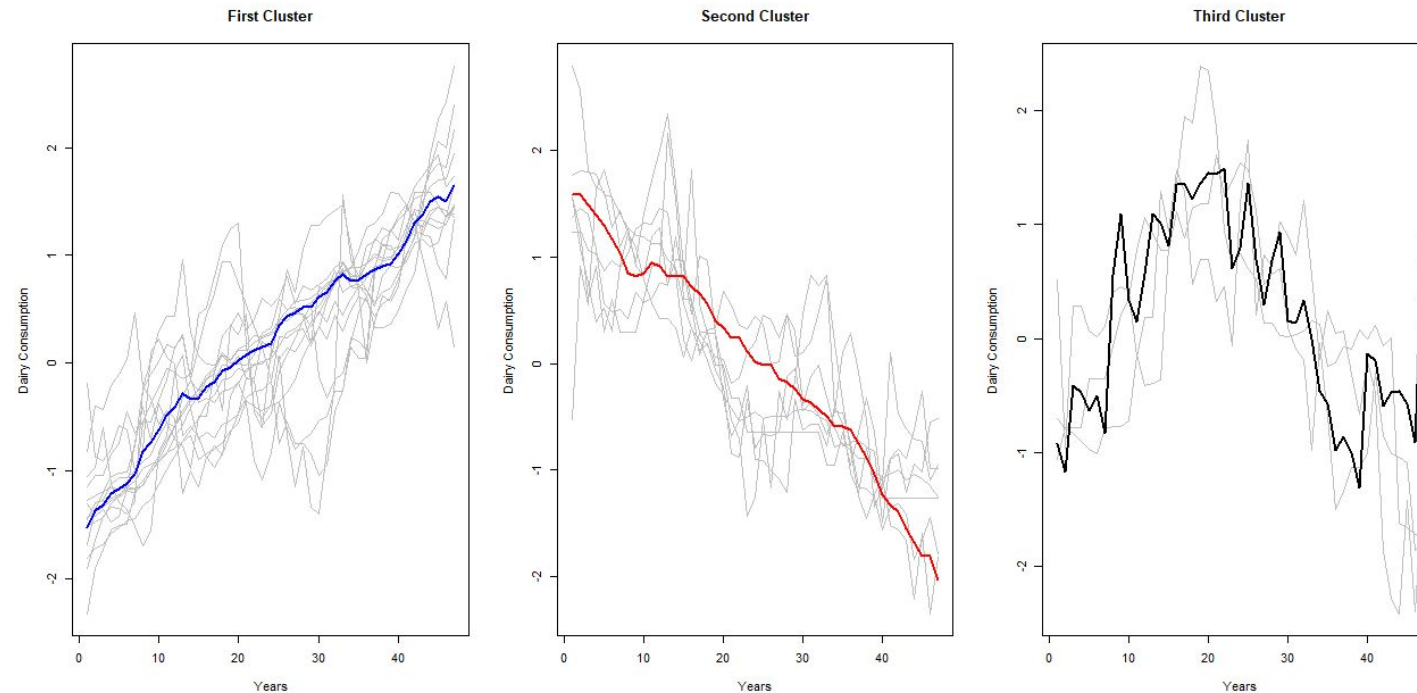
# Bayesian Clustering



$$\mathbf{y}_i = \mathbf{Z}\boldsymbol{\alpha}_i + \mathbf{X}\boldsymbol{\beta}_i + \boldsymbol{\theta}_i + \boldsymbol{\epsilon}_i, \quad i = 1, 2, \dots, n$$

$$\theta_{it} = \rho\theta_{i,t-1} + \nu_{it}$$

$$\boldsymbol{\gamma}_i = (\boldsymbol{\beta}_i, \boldsymbol{\theta}_i) \quad \boldsymbol{\gamma}_i | G \stackrel{\text{iid}}{\sim} G, \text{ for } i = 1, \dots, n \text{ with } G \sim \mathcal{PD}(a, b, G_0)$$



Through an **outlier detection**, we verified that there were no outliers in the three clusters.



# Future Developments



- Perform a **Stakeholder Analysis** to categorize our stakeholders by using the Power-Interest matrix
- Since the single state's information is available, we may consider **adding a spatial component** by grouping the states on East Coast, Central States, and West Coast and understand their differences
- Consider possible ways of embedding the **import/export** data in our current model
- Explore more **distances** for the conformal prediction
- Perform **prediction** using our models using fictitious (or real? 🤖) cheese factories
- We would like to explain why the years 1983, 1984, 2002, and 2006 have been detected as **outliers** in the Robust Regression and find some actual events related to this anomalies



# Thank you for the attention!

## References

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- Nieto-Barajas, L. E., & Contreras-Cristán, A. (2014). **A Bayesian nonparametric approach for time series clustering.** *Bayesian Analysis*, 9(1), 147-170.

