

## CHAPTER 18

# Signal Generators and Waveform-Shaping Circuits

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## IN THIS CHAPTER YOU WILL LEARN

1. That an oscillator circuit that generates sine waves can be implemented by connecting a frequency-selective network in the positive-feedback path of an amplifier.
2. The conditions under which sustained oscillations are obtained and the frequency of the oscillations.
3. How to design nonlinear circuits to control the amplitude of the sine wave obtained in a linear oscillator.
4. A variety of circuits for implementing a linear sine-wave oscillator.
5. How op amps can be combined with resistors and capacitors to implement precision multivibrator circuits.
6. How a bistable circuit can be connected in a feedback loop with an op-amp integrator to implement a generator of square and triangular waveforms.
7. The application of one of the most popular IC chips of all time, the 555 timer, in the design of generators of pulse and square waveforms.
8. How a triangular waveform can be shaped by a nonlinear circuit to provide a sine waveform.

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## Introduction

In the design of electronic systems, the need frequently arises for signals having prescribed standard waveforms, for example, sinusoidal, square, triangular, or pulse. Systems in which standard signals are required include computer and control systems where clock pulses are needed for, among other things, timing; communication systems where signals of a variety of waveforms are utilized as information carriers; and test and measurement systems where signals, again of a variety of waveforms, are employed for testing and characterizing electronic devices and circuits. In this chapter we study signal-generator circuits.

The signal-generator or oscillator circuits studied in this chapter are collectively capable of providing signals with frequencies in the range of hertz to hundreds of gigahertz. While some can be fabricated on chip, others utilize discrete components. Examples of commonly encountered oscillators include the microprocessor clock generator (fabricated on chip utilizing the ring oscillator studied in Section 16.4.4 with frequencies in the several-gigahertz range); the carrier-waveform generator in wireless transceivers (on chip, up to the hundreds-of-gigahertz range); the oscillator in an electronic watch (utilizing a quartz

crystal with a frequency of  $2^{15}$  Hz); and the variable-frequency function generator in the electronics lab (utilizing a discrete circuit with frequency in the hertz to megahertz range).

There are two distinctly different approaches for the generation of sinusoids, perhaps the most commonly used of the standard waveforms. The first approach, studied in Sections 18.1 to 18.3, employs a **positive-feedback loop** consisting of an amplifier and an RC or LC **frequency-selective network**. While the frequency of the generated sine wave is determined by the frequency-selective network, the amplitude is set using a nonlinear mechanism, implemented either with a separate circuit or using the nonlinearities of the amplifying device itself. In spite of this, these circuits, which generate sine waves utilizing resonance phenomena, are known as **linear oscillators**. The name clearly distinguishes them from the circuits that generate sinusoids by way of the second approach. In these circuits, a sine wave is obtained by appropriately shaping a triangular waveform. We study waveform-shaping circuits in Section 18.8, following the study of triangular-waveform generators.

Circuits that generate square, triangular, pulse (etc.) waveforms, called **nonlinear oscillators** or **function generators**, employ circuit building blocks known as **multivibrators**. There are three types of multivibrator: the **bistable** (Section 18.4), the **astable** (Section 18.5), and the **monostable** (Section 18.6). The multivibrator circuits presented in this chapter employ op amps and are intended for precision analog applications. Bistable and monostable multivibrator circuits using digital logic gates were studied in Chapter 16.

A general and versatile scheme for the generation of square and triangular waveforms is obtained by connecting a bistable multivibrator and an op-amp integrator in a feedback loop (Section 18.5). Similar results can be obtained using a commercially available versatile IC chip, the 555 timer (Section 18.7).

## 18.1 Basic Principles of Sinusoidal Oscillators

In this section, we study the basic principles of the design of linear sine-wave oscillators. In spite of the name *linear oscillator*, some form of nonlinearity has to be employed to provide control of the amplitude of the output sine wave. In fact, all oscillators are essentially nonlinear circuits. This complicates the task of analysis and design of oscillators: No longer is one able to apply transform (*s*-plane) methods directly. Nevertheless, techniques have been developed by which the design of sinusoidal oscillators can be performed in two steps: The first step is a linear one, and frequency-domain methods of feedback circuit analysis can be readily employed. Subsequently, in step 2, a nonlinear mechanism for amplitude control can be provided.

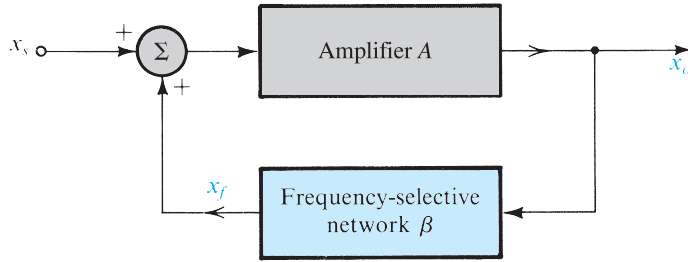
### 18.1.1 The Oscillator Feedback Loop

The basic structure of a sinusoidal oscillator consists of an amplifier and a frequency-selective network connected in a **positive-feedback loop**, such as that shown in block diagram form in Fig. 18.1. Although no input signal will be present in an actual oscillator circuit, we include an input signal here to help explain the principle of operation. It is important to note that unlike the negative-feedback loop of Fig. 11.1, here the feedback signal  $x_f$  is summed with a *positive* sign. Thus the gain-with-feedback is given by

$$A_f(s) = \frac{A(s)}{1 - A(s)\beta(s)} \quad (18.1)$$

where we note the negative sign in the denominator. The loop gain  $L(s)$  is given by

$$L(s) \equiv A(s)\beta(s) \quad (18.2)$$



**Figure 18.1** The basic structure of a sinusoidal oscillator. A positive-feedback loop is formed by an amplifier and a frequency-selective network. In an actual oscillator circuit, no input signal will be present; here an input signal  $x_s$  is employed to help explain the principle of operation.

and the characteristic equation is

$$1 - L(s) = 0 \quad (18.3)$$

### 18.1.2 The Oscillation Criterion

If at a specific frequency  $f_0$  the loop gain  $A\beta$  is equal to unity, it follows from Eq. (18.1) that  $A_f$  will be infinite. That is, at this frequency the circuit will have a finite output for zero input signal. Such a circuit is by definition an oscillator. Thus the condition for the feedback loop of Fig. 18.1 to provide sinusoidal oscillations of frequency  $\omega_0$  is

$$L(j\omega_0) \equiv A(j\omega_0)\beta(j\omega_0) = 1 \quad (18.4)$$

That is, at  $\omega_0$  the phase of the loop gain should be zero and the magnitude of the loop gain should be unity. This is known as the **Barkhausen criterion**. Note that for the circuit to oscillate at one frequency, the oscillation criterion should be satisfied only at one frequency (i.e.,  $\omega_0$ ); otherwise the resulting waveform will not be a simple sinusoid.

An intuitive feeling for the Barkhausen criterion can be gained by considering once more the feedback loop of Fig. 18.1. For this loop to *produce* and *sustain* an output  $x_o$  with no input applied ( $x_s = 0$ ), the feedback signal  $x_f$ ,

$$x_f = \beta x_o$$

should be sufficiently large that when multiplied by  $A$  it produces  $x_o$ , that is,

$$Ax_f = x_o$$

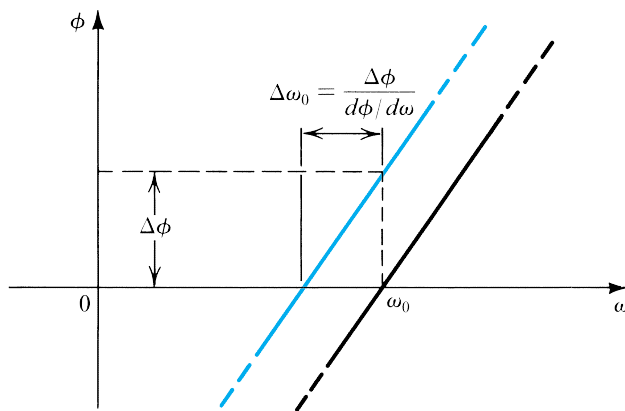
that is,

$$A\beta x_o = x_o$$

which results in

$$A\beta = 1$$

It should be noted that the *frequency of oscillation*  $\omega_0$  is determined solely by the phase characteristics of the feedback loop; the loop oscillates at the frequency for which the phase is zero (or, equivalently,  $360^\circ$ ). It follows that the stability of the frequency of oscillation will be determined by the manner in which the phase  $\phi(\omega)$  of the feedback loop varies with frequency. A “steep” function  $\phi(\omega)$  will result in a more stable frequency. This can be seen if one imagines a change in phase  $\Delta\phi$  due to a change in one of the circuit components. If  $d\phi/d\omega$  is large, the resulting change in  $\omega_0$  will be small, as illustrated in Fig. 18.2.



**Figure 18.2** Dependence of the oscillator-frequency stability on the slope of the phase response. A steep phase response (i.e., large  $d\phi/d\omega$ ) results in a small  $\Delta\omega_0$  for a given change in phase  $\Delta\phi$  [resulting from a change (due, for example, to temperature) in a circuit component].

An alternative approach to the study of oscillator circuits consists of examining the circuit poles, which are the roots of the **characteristic equation** (Eq. 18.3). For the circuit to produce **sustained oscillations** at a frequency  $\omega_0$  the characteristic equation has to have roots at  $s = \pm j\omega_0$ . Thus  $1 - A(s)\beta(s)$  should have a factor of the form  $s^2 + \omega_0^2$ .

### EXERCISE

- 18.1** Consider a sinusoidal oscillator formed by connecting an amplifier with a gain of 2 and a second-order bandpass filter in a feedback loop. Find the pole frequency and the center-frequency gain of the filter needed to produce sustained oscillations at 1 kHz.

**Ans.** 1 kHz; 0.5

### 18.1.3 Analysis of Oscillator Circuits

Analysis of a given oscillator circuit to determine the frequency of oscillation and the condition for the oscillations to start proceeds in three steps:

1. Break the feedback loop to determine the loop gain  $A(s)\beta(s)$ . This step is similar to that utilized in Section 11.2 in the analysis of negative-feedback amplifiers.
2. The oscillation frequency  $\omega_0$  is found as the frequency for which the phase angle of  $A(j\omega)\beta(j\omega)$  is zero or, equivalently,  $360^\circ$ .
3. The condition for the oscillations to start is found from

$$|A(j\omega_0)\beta(j\omega_0)| \geq 1$$

Note that making the magnitude of the loop gain slightly greater than unity ensures that oscillations will start.