1 Introduction

Artificial Intelligence

- broad concept
- different interpretations
 we do not have a definition of inteligence

Statistical machine learning

· Algorithms and applications where computer learn from data AGI

- Artificial General Intelligence
 Hypothetical computer program that can perform intellectual tasks as well as, or better than a human.

Turing Test

- Also called imitation game
 Tests of a machine's ability to exhibit intelligent behaviour equivalent to, or indistinguishable from that of a human
 Has some philosophical problems (Complex problems, humans cant solve / AI must learn to lie)

Examples of application (today)

- Personalization of news feeds
 Product searching and recommendation s on eCommerce plat-
- forms Voice-to-text
- · Predictive maintenance Bias

 The inability for a machine learning method (like linear regression) to capture the true relationship, eg. Straight Line can't be curved like the true relationship

Variance

- The difference in fits between training and testing set (different
- data sets in general)

 Low variance Sum of Squares are very similar for different datasets

The ideal ML algorithm has low bias and can accurately model the true relationship and it has low variability by producing consistent predictions across different datasets.

1.1 Tasks and Algorithms of Machine Learning



1.2 Dialogflow

Intents An intent categorizes an end-user's intention for one conversation turn.

- Recognizes the need of a user
- Require training to match to user inputs
 Follow up Intents (on Success)
- Fallback Intents (on Failure)

Entities Each intent parameter has a type, called the entity type, which dictates exactly how data from an end-user expression is extracted.

- Extract information from user inputs
- Help to identify required intent
 System Entities Date and time / Numbers / Amounts / Units /
- Developer Entities defined by list of words (@pizza-type / @drink
- / etc.)

 User Entities transient, temporary Information based on Conversation (@previous-orders)

Dialog

• Linear Gather a list of information

• Non Linear Using Contexts

Context

• Each Intent can have Input & Output Context

Intents are active based on active Context
 Expire automatically

Fulfillment

- Action triggered on fullfilled Intents
 e.g. Webhook

1.3 7 Steps of Machine Learning

- 1. Gathering data Collect quantity/quality data for training/tes-
- ting
 2. Preparing that data Cleanup data (remove duplicates, correct errors, deal with missing values, normalize data, convert data
- Choosing a model Select the right algorithm(s)
- Training Train the model, each iteration of process is a training step
 5. Evaluation Use metrics to measure objective performance of the
- model, test model against previously unseen data, good train/e-val split is 80/29, 70/30

 Hyperparameter tuning Try to improve upon the positive results achieved during the evaluation through gamble with stepNumber
- of training steps, learning rate, initialization values and distri-
- 7. Prediction Model should be ready for practical applications

2 Natural Language Processing (NLP)

- Automated processing of human language (written & spoken)
 Aims to understand and generis thuman (natural) language
 Understanding spoken text still difficult
- Understanding written text became BIG business (search-
- Generating human-like conversations is still very hard

2.1 4 Ingredients of Machine Learning

1. Data

- Dataset
 Pre-Processing Pipeline including cleansing, feature-engineering, data augmentation etc.

2. Cost-Function (Loss)

- Formal mathematical expression for good / bad
- Commonly Mean Squared Error (MSE)
- 3. Model
- From linear model: $\hat{y}_i = ax_i + b$
- To complicated million parameter neural networks
- Different tasks require different models (regression / decision
- 4. Optimization Procedure
- Algorithm that changes the parameters of the model that the • E.g. Stochastic Gradient Descent (SGD), ADAM, RMSProp...
- For successful ML, there are many more ingredients ...

5. Performance optimization

- Building of efficient pipelines
- Followwing tool specific recommendations
- 6. Visualization and evaluation of the learning Process
- Learning curves
- Performance measures
- Tensorboard

7. Cross-Validation & Regularization

- · Train models that generalize well to unseen data
- Estimate the generalization error

2.2 Representation of Words

Vectors can be used to represent words based on their meaning.

2.2.1 One-hot representation

- Vector with a single 1-Value
 All other Values are set to 0
 Count the Number of different Words, Define one unique vector per word

Dini Mom isch fett

	[1]		[O]		[O]		[0]		[0]	
	0		1		0		0		0	
Dini:	0	Mom:	0	isch:	1	fett:	0	7.7:	0	
	o		0		0		1		0	
	lol		l o l		0		0		111	

Disadvantages

- Very high dimensional vector space (1 Dimension / unique Word)
 Sparse Representation: Each vector has a single 1 and N Zeroes.
- (Memory Inefficient)

 No Generalization: All words are unrelated to each other.
- Does not capture any aspect of the meaning of a word

Make a list of words (optionally alphabetically). Use the index to represent each word.

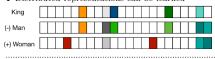
Example: Dini Mom isch fett.

Dini: 0, Mom: 1, isch: 2, fett: 3, '.': 4

- Dense Equivalent of one-hot encoding
 Indexes are not more useful that one-hot vectors
- Often used as preprocessing step
 Indices / One-Hot Vectors are fed into a network which learns more useful representations

2.2.3 Distributed Representation

- vectors that capture (at least partially) the semantics of a word Words that occur in similar contexts (neighboring words) tend
- to have similar meanings Similar words share similar representations
- Distributed representations can be learned



Words to Vectors

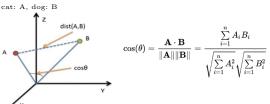
Queen

- Mathematical function maps word to high dimensional Vector
 In neural networks, this function is implemented in the Embedding Laver

Advantage (of vectors)

 Good embedding maps similar/related words to similar regions of the vector space (nearby words have a semantic similarity)
 Dot-Product (Skalarprodukt) is a measure of similarity
 Possible to add/subtract vectors Calculate Similarities between words Dot-Product (Skalarprodukt) of 2 Vectors is

- maximal when parallel (0°), both vectors with norm 1 results in max value 1 • zero when orthogonal (90°) • minimal (negative) when opposite directions (180°) both vectors
- with norm 1 results in max value -1 Cosine Distance
- Way to calculate how similar two words (vectors) are



Example A: (3, 6, 2, 1), B: (2, 7, 2, 0) $A \cdot B = 6 + 42 + 4 + 0 = 52$ $||A||||B|| = \sqrt{(9+36+4+1)} * \sqrt{(4+49+4+0)} = 53.38539$ A * B/(||A||||B||) = 0.9740high value equals high similarity (to be an animal)

3 Probability

3.1 Random Variable

- Values depend on outcomes of a random phenomenon
- Random variable X is a variable that takes a numerical value x, which depends on a random experiment
- Discrete X takes any of a finite set of values 1.5, 2.123, 6.2, 10
- Continous X takes any value of an uncountable range e.g. real numbers from an interval

Best we can know

- All possible values
- Probability of each value

E.g. The discrete random variable X is the number observed when rolling a fair dice. P(X = x) / P(x): 1/6 for each possible value

Joint Probability

- Joint Properties of two random variables
- Defined by the Joint Probability Mass Function

E.g. Dice1 = 5 AND Dice2 = 4
$$P_{XY}(5,4) = P_X(5) * P_Y(4) = 1/6 * 1/6 = 1/36$$

	X=1	X=2	X=3	X=4	X=5	X=6	
Y=1	1/36	1/36	1/36	1/36	1/36	1/36	
Y=2	1/36	1/36	1/36	1/36	1/36	1/36	
Y=3	1/36	1/36	1/36	1/36	1/36	1/36	
Y=4	1/36	1/36	1/36	1/36	1/36	1/36	
Y=5	1/36	1/36	1/36	1/36	1/36	1/36	
Y=6	1/36	1/36	1/36	1/36	1/36	1/36	

Independent random Variables

· Joint Probability is the product of the individual probabilities

P(X,Y)=P(X)*P(Y) (only if independant) P(X,Y,Z)=P(X)*P(Y)*P(Z) (only if independant) Correlated random Variables

- There are events that are not independent
 Such random variables are correlated
 X: observe clouds (0=no, 1=small, 2=big)
- Y: observe rain (0=no, 1=light, 2=moderate, 3=heavy)

Conditional Probability

- One variable is no longer random X is observed, its value is fixed

• Calculate the probabilities of Y given X: P(Y|X)

$$\begin{split} &P(X,Y) = P(X|Y) * P(Y) \\ &P(X,Y) = P(Y|X) * P(X) \\ &P(Y|X) = \frac{P(X,Y)}{P(X)} \\ &\textbf{Bayes Rule} \\ &P(X|Y) * P(Y) = P(Y|X) * P(X) \\ &\text{Therefore} \end{split}$$

 $P(Y|X) = \frac{P(X|Y) * P(Y)}{P(X)}$

3.2 Probability mass function (PMF)

Wahrscheinlichkeitsfunktion, a function f(x) that provides the probability for each value x of a discrete random variable X

Graph of a PMF



See trends, clusters and local patterns in data

Difficult to see in raw data

Detect outliers and unusual groups
 Validate Hypothesis/Conjecture/Theory

Important in a Plot

X-Axis labels which data is represented and its units
 Y-Axis labels which data is represented and its labels

• Scale linear, logarithmic

• Dimensionality of the data 2D / 3D

Dataframe a two-dimensional labelled data structure with columns of different types

4.0.1 Data Analysis Libraries

NumPv

• Package for scientific computing in Python

Multidimensional array object

• Routines for fast array operations (sorting, selecting, FFT, line-

pandas

• Built on top of NumPy • Routines for accessing tabular data from files (.csv, xls, etc.) • Supports 2-dimensional data (dataframe and series)

Dataframes are something like database tables

MatPlotLib

Library for visualizing data
Provides bargraphs, histograms, piecharts, scatter plots, lines, boxplots, heatmaps, ...

Seaborn

· Extension of MatPlotLib, NumPy and pandas

More user friendly
 Plots are aesthetically better

4.0.2 Line Plots

• Bivariate, Continuous

• Recognizes trend (pattern of change) (over time)

4.0.3 Bar Chart

Used for categorical dataCounting based on each category

4.0.4 Histogram

Represents the empirical distribution of a variable

Automatically creates bins (interval) along the range of values
Shows vertical bars to indicate the number of observations per

4.0.5 Descriptive Statisics: Box Plots and Violin Plots



4.0.6 Scatter Plot

Relationship between (two) continuous variables
Helps to get an idea of the degree of correlation between varia-

5 Linear Regression

a simple method to analyse data

• Only consideres a linear relationship between input and output

Only consideres a linear relationship between input and output.
 In the simplest case, x and y are scalars and the linear model therefore has only two free parameters.
 The goal is to identify a (slope) and b (intercept) for which the linear model best explains the data.

$$\hat{y}_i = ax_i + b$$

Applications

• Interpretation has some input an effect on the output, eg. Is there a relationship between smoking cigaretts and the risk of lung

• Prediction Given some sensor data like oil pressure, temperature ..., eg. a model could predict (and thereby hopefully prevent) an

5.1 Model

In ML, we use the term model for any mathematical function that explains the data

$$\begin{aligned} y_i &\approx f(x_i) \\ y_i &= f(x_i) + \epsilon_i \end{aligned}$$

where ϵ_i is unexplained noise. It is often assumed that ϵ_i follows a normal distribution. Instead of approximating y_i , we calculate an estimate $\hat{y_i}$ (y hat) of the usually unknown y_i :

$$\hat{y_i} = f(x)$$

5.2 Mean Squared Error (MSE)

Loss we want to minimize
Usually divided by 2

$$\begin{split} \hat{y_i} &= ax_i + b \\ e_i &= y_i - \hat{y_i} \\ \text{The difference } e_i \text{, called residual} \\ E &= \frac{1}{2N} * \sum_{i=1}^N e_i^2 \\ E &= \frac{1}{2N} * \sum_{i=1}^N (\hat{y_i} - (a * x_i + b))^2 \end{split}$$

5.3 Correlation and Causality

· Correlation is not causality

Correlation refers to the degree to which a pair of variables are

• Linear regression is a tool to detect correlations between two or more variables

• Correlation can be quantified using the Pearson correlation co-

6 Optimization

• Training or learning in AI often suggests an algorithm performing some sort of optimization

It is the problem of finding a set of inputs to an objective func-tion that results in a maximum or minimum function evaluation

• In our examples the objective is to minimize the loss function

6.1 Gradient Descent

At any location [a,b] we look at the error-gradient in the neighbourhood of [a,b] and move a (small) step in the direction where the error shrinks the most. By repeating this procedure, we will eventually arrive at the location where the error is smallest.

Iterative Method/Procedure

• Each iteration, the model parameters are updated such as that the Loss (MSE) is reduced

Move along a trajectory which includes fewer points
At each point of the trajectory we evaluate the gradient of the

error function • At each iteration, we would have to iterate over all N = 1'000

points to calculate the gradient of the loss function.

Calculate Gradient

Gradient of E =
$$\begin{bmatrix} \frac{\partial B}{\partial E} \\ \frac{\partial B}{\partial E} \end{bmatrix}$$

Calculate these two partial derivatives

$$\frac{\partial E}{\partial a} = \frac{1}{N} \; \Sigma_{i=1}^{N} \left(y_{i} - (a \cdot x_{i} + b) \right) \cdot - x_{i}$$

$$\frac{\partial E}{\partial b} = \frac{1}{N} \sum_{i=1}^{N} (y_i - (a \cdot x_i + b)) \cdot -1$$

$$\text{Gradient of E} = \begin{bmatrix} \frac{\partial E}{\partial a} \\ \frac{\partial E}{\partial b} \end{bmatrix} = \begin{bmatrix} \frac{1}{N} \sum_{i=1}^{N} (y_i - (a \cdot x_i + b))(-x_i) \\ \frac{1}{N} \sum_{i=1}^{N} (y_i - (a \cdot x_i + b))(-1) \end{bmatrix}$$

6.2 Stochastic Gradient Descent (SGD)

we do not need the exact gradient to find a trajectory toward the minimum. Instead, at each iteration we can randomly pick a few datapoints and use them to calculate an approximation of the gradient

• At each iteration, the gradient is calculated on a (randomly selected) subset of the data

• For a fixed learning rate, SGD does not converge

Mini-batches

• 1 < n < N

• Increasing the batch-size will reduce the variance of the gradient estimation

batch-size n = 1 yields a very noisy gradient
batch-size n = N is expensive to calculate

• often mini-batches of size n = 32 or n = 64 are used

Annealed SGD

• The learning rate alpha is reduced over time

This is called (simulated) annealing
 There are different options (called schedules) how to reduce al-

pha over time
• A fixed learning rate α does not converge. The algorithm keeps fluctuating around the minimum. Annealed SGD solves this appearent contradiction by adapting the learning rate. It starts with a large α and reduces it over time

6.2.1 General remarks on SGD

• Gradient-based methods only work if we can express a Loss function as a differentiable function

 SGD is dealing with only a single datum at each iteration. This is very inefficient and rarely used. Batch- or mini-batch gradient-descent is usually used

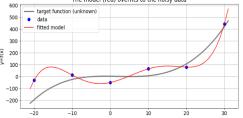
7 Generalization & Regularization

7.1 Overfitting

• A model that perfectly fits the data does not have to be perfect • In-Sample Error (Trainig error) was minimized (MSE = 0) • Out-of-sample Error (Generalization Error, Test Error) is the MSE of new Data

A good model has a low Generalization Error
Overfitting happens if the MSE of Training Error is small thanks

to a complex model but the Generalization Error is large The model (red) overfits to the noisy data



7.2 Underfitting

· Using a too simple model

• In-Sample Error is large

Generalization Error is large



7.3 Training-Set, Test-Set, Model Evaluation

• The Generalization Error can't be calculated

But Estimated
 Split the data into 2 sets

- Training-Set (80% of data) - Test-Set (20% of data)

Training:

• Fit the model to the training set

This minimizes the in-sample error

Evaluating

Using the Test-Set
Produces the Test-Error

• This is an estimate of the Generalization Error

7.4 Bias-Variance Trade-off

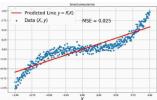
Variance: Difference of fits between data sets. Bias: Results that are systematically prejudiced due to faulty assumptions.

High Bias

• A too simple model for the given data Low Variance

· The model is relatively stable

· Very simular model if trained with new data



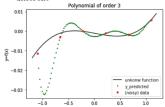
Low Bias

• A more complex model can better explain the data

High Variance

Given a new datapoint, the MSE can be very large

• For a different set with more datapoints, the model may be very different



7.4.1 Trade-off

- · Higher bias implies lower variance
- Lower bias implies higher variance
- In practice, all we want is low variance
 The model can only be as complex as the data permits
- You have to find an optimal balance between bias and variance

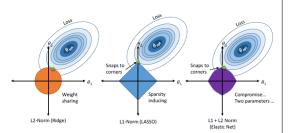


7.5 Regularization

- · Technique to control the model complexity
- Add a penalty term to the Loss More complex models get a higher penalty

- Add a constrain to the optimization process regularized loss = $MSE + \lambda$ model-complexity

$$\sum_{i=1}^{n} (y_i - \sum_{j=1}^{p} x_{ij} \beta_j)^2 + \lambda \sum_{j=1}^{p} \beta_j^2$$



8 Cross-Validation

Problem with 80/20 Data Separation

- Test Error depends on random set
 For different Set, the test error would be different

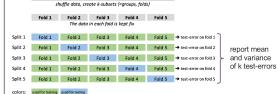
With Cross-Validation we can obtain a better estimate of the generalization error

8.1 k-fold Cross-Validation

Without cross-validation:



1 training phases and is used once for testing: All Data



8.1.1 Some Comments

- Typical Values for k are 5,10 or N
- The data of a fold does not change during procedure
 Do not preprocess the whole dataset
- Apply the preprocessing pipe-line to each split

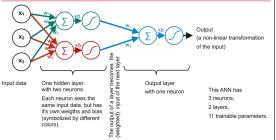
9 Artificial Neural Networks (ANN)

9.1 Artificial Neurons

- ullet Receives an input vector $[x_1, x_2, \ldots]$
- Each neuron has its own input weights $[w_1, w_2, ...]$ and bias b
- Calculates the sum of the weighted input (dot product $\vec{x} * \vec{w}$), adds a bias b, and passes it through a nonlinear activiation func-



9.2 Simple ANN



9.3 Traning an ANN

Supervised learning

- Data with label For each input \vec{x} we are given the output \vec{y}
- ANN is initialized with random weights
- An optimizer reduces a cost-function (e.g. MSE)
 At every iteration, and for every single weight w and bias b, the partial derivative needs to be calculated. (Backpropagation)

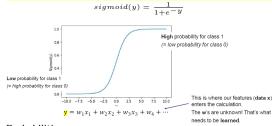


10 Classification & Logistic Regression

10.1 Binary Classification

- · Decision with 2 possible outcomes Hail in Lausanne (yes/no)
 Master admission (admission / no admission)
- Based on different data / entity
- 10.1.1 Decision using Linear Regression • Train the model with gradient descent
- Models the response (y) and post process the response to compute the probability

10.1.2 The sigmoid function



Probabilities

- We can write the estimated probability
 For a prediction we can write

$$P(x) = \frac{1}{1 + e^{-(W^T x)}}$$

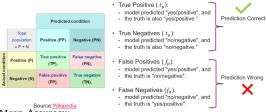
- . Given all the data points (X,Y) we want to maximize the probability that all the predictions are correct.

 • For each of the training data, we want to maximize the likelihood
- of correct prediction

 We can use Gradient Descent to find W

11 Classifier Evaluation

11.1 Confusion Matrix



Mean Accuracy:

- How often is the classifier correct?
- $\bullet \ A = (t_p + t_n)/n$
- Mean Error:
- How often is the classifier wrong?
 E = (fp + fn)/n
- Precision:
- When the prediction is 1, how often is it correct? $\bullet \ P = t_p/(t_p + f_p)$
- Sensitivity, Recall, True Positive Rate (TPR):

- How often the prediction is 1 when it's actually 1 $\bullet \ R = t_p/(t_p + \hat{f}_n)$

Miss Rate, False Negative Rate (FNR)

• MR = 1 - TPR

11.2 Why Accuracy is not enough?

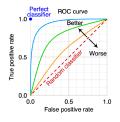
• If the prediction is constant the accuracy may still look decent

- E.g. allways predict false
 90% of the data is false
- Accuracy = 90% (decent) Precision = 0
- Recall = 0

- Increasing precision reduces Recall and vice versa
 Threshold is a business decision (depending on goals)

11.4 Receiver Operating Characteristics

- Defined by FPR and TPR as x and y axes
 Visualizes tradeoff between TP (benefits) and FP (cost)



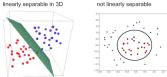
Area under the curve

- Area under the ROC curve
- Shows how well the TPR and FPR is looking in the aggregate
 The greater the area under the curve, the higher the quality of the model
- The greater the area, the higher the ratio of TP to FP

12 KNN

12.1 Linear Seperability

linearly separable in 2D



- Based on logistic regression model, you can draw a line
- This is the Linear decision boundary
 If a simple line perfectly seperates the classes, then the classes are said to be linearely seperable

12.3 k-Neares Neighbors (KNN)





12.3.1 Distance Metric

- Easy and simple ML model
- Few hyperparameters to tune

12.3.3 Disadvantages

- Large computation cost during runtime if sample size is large

12.3.4 Hyperparameters

Distance Function: Euclidean distance is most used

13 Clustering

13.1 Unsupervised Learning

- We are given Data (features, x) without labels (y)
 Can we still learn something from the data?
 Yes! Often the data has some structure

- The goal of unsupervised learning is to self-discover patterns from the data

- Astronomical Data

13.3 Naive K-means

- 2. Initialize the value of k cluster centres (aka, means, centroids) $(C_1, C_2, \dots, C_{k_c})$

- Find the squared Euclidean distance between the centres and all the data points.
- 2. Assign each data point to the cluster of the nearest centre.
- 4. Update: Each cluster now potentially has a new centre (mean). Update the centre for each
- 5. If some stopping criterion met, Done
- 6. Else, go to Assignment step 3

13.3.1 Stopping Criterion

- When centres don't change (time consuming)
- The datapoints assigned to specific cluster remains the same (takes too much time)
- Fixed number of iterations have reached (choose wisely)

12.2 Non-Linear decision boundary

• When classes are not linearly seperable · Resort to polynomial terms

- A datapoint is know by the company it keeps
- Computes k nearest neighbours
 Returns the most frequent class of the k neighbours





• Cosine Distance

- Manhattan Distance
 Euclidean Distance (most used) Minkowski Distance

- k should be wisely selected
- Not efficient for high dimensional datasets

 Proper scaling should be provided for fair treatment among fea-

• K Value: how many neighbours to participate in the KNN algo

- Data points which have shared properties
 Fall into one cluster or one alike group

· Similar Data Points are close together

- 13.2.1 Applications
- Social Network Analysis
- Marked segmentation
 Recommendation systems
- Let us assume we know the number of clusters k.
- 1. New Centres $((C'_1, C'_2, \dots, C'_{k_c}) = \text{Average of all the data points in the cluster}(1, 2, \dots, k_c)$

- The distance of datapoints from their centres >= treshold we

13.3.2 Initialization

- Performance depends on the random initialization
- Some seeds can result in a poor convergence rate
 Some seeds can converge to suboptimal clustering
- If centres are very close, it takes a lot of iterations to converge
 Initialize randomly, run multiple times

13.3.3 Standardization of data

- Features with large values may dominate the distance value
 Features over small values will have no impact
- · Normalize values!

13.3.4 Sklean k-means

Initialization

- Init = K-means++
 Only initialization of the centroids will change
 Chosen centroids should be far from each other max iter:
- Number of iterations before stopping

n init:

 $\buildrel \bullet$ Number of time the k-means algorithm will be run with different centroid seeds

13.3.5 Evaluating Cluster Quality

- Make clusters so that for each cluster the distance of each cluster member from its center is minimizes
 Inertia or within-cluster sum-of-squares (WCSS)
 Sum of squared distances to center
- As small as possible

Silhouette Score

- How far the datapoints in one cluster are from the datapoints in another cluster
- SS of a point: $\frac{b-a}{max(a,b)}$
- a: average intra-cluster distance (distance between each point
- within)

 b: average inter-cluster distance (distance between a cluster and its nearest neighbour)

14 Ensamble Methods

14.1 Wisdom of Crowd

- Suppose you have a difficult question
 Ask many people and aggregate the answer
 This might work very well instead of finding the best suited per-

14.2 Ensamble

- Wisdom of Crowd can be applied to ML
- Instead of finding the best model, aggregate the results of weak
- Aggregate predictions of regressors or classifiers
 Might get better accuracy than the best predictor
 Ensamble: group of predictors

14.3 Ensamble Method

- Suppose we have many different weak models (better than ran-
- dom)

 Get prediction from all of them and take a vote
- Class with most votes is the predicted class
 Commonly used towards the end of a project
 Requirement: enough models / diverse models
- 14.4 Bagging and Pasting

- Bagging (Bootstrap Aggregating)

 Sampling with replacement

 Allows data points to be used several times
- Allows data point
 Pasting
 Sampling without replacement

14.5 No free lunch theorem

No single machine learning algorithm is universally the best-performing algorithm for all problems

14.5.1 Out of Bag (oob) Evaluation

- Using BaggingSome Data Points may not be used at all
- Use them for evaluation