5.domača naloga – rešitve

Naloga 1:

a)
$$f(x_1, x_2, x_3, x_4) = \&^4(15, 11, 7, 4, 3, 0), \underline{\mathsf{MNO}} = \underline{\mathsf{MKNO}}$$

a) $f(x_1, x_2, x_3, x_4) = \overline{x_1}. \ x_3 \vee \overline{x_3}. x_4 \vee x_3. \overline{x_4}$, $\underline{\mathsf{MDNO}} : [4, 9]$
b) $f(x_1, x_2, x_3, x_4) = \overline{x_1}. \ x_4 \vee \overline{x_3}. x_4 \vee x_3. \overline{x_4}$, $\underline{\mathsf{MDNO}} : [4, 9]$
 $f(x_1, x_2, x_3, x_4) = (\overline{x_1} \vee \overline{x_3} \vee \overline{x_4}). (x_3 \vee x_4)$, $\underline{\mathsf{MKNO}} : [3, 7]$

b)
$$f(x_1, x_2, x_3, x_4) = \&^4(15, 12, 11, 10, 8, 7, 5, 3, 1), \underline{\mathsf{MNO}} = \underline{\mathsf{MDNO}}$$

$$f(x_1, x_2, x_3, x_4) = x_1. \ x_4 \lor \overline{x_2}. \overline{x_3}. x_4 \lor \overline{x_1}. x_3. \overline{x_4}, \underline{\mathsf{MDNO}}: \texttt{[4, 11]}$$
 a) $f(x_1, x_2, x_3, x_4) = (\overline{x_1} \lor x_4). (x_3 \lor x_4). (x_1 \lor \overline{x_3} \lor \overline{x_4}). (x_1 \lor \overline{x_2} \lor x_3), \underline{\mathsf{MKNO}}: \texttt{[5, 14]}$ b) $f(x_1, x_2, x_3, x_4) = (\overline{x_1} \lor x_4). (x_3 \lor x_4). (x_1 \lor \overline{x_3} \lor \overline{x_4}). (x_1 \lor \overline{x_2} \lor \overline{x_4}), \underline{\mathsf{MKNO}}: \texttt{[5, 14]}$

c)
$$f(x_1, x_2, x_3, x_4) = \&^4(15, 14, 11, 7, 6, 5, 4, 3)$$
, MNO = MDNO = MKNO
$$f(x_1, x_2, x_3, x_4) = x_2. \ x_4 \lor x_2. \ x_3 \lor \overline{x_1}.x_3$$
, MDNO: [4, 9]
$$f(x_1, x_2, x_3, x_4) = (\overline{x_1} \lor x_2). (x_3 \lor x_4). (x_2 \lor x_3)$$
, MKNO: [4, 9]

d)
$$f(x_1, x_2, x_3, x_4) = \&^4(15, 14, 10, 8, 6, 3, 2, 1, 0), \underline{\text{MNO} = MDNO}$$

$$f(x_1, x_2, x_3, x_4) = \overline{x_2}. \ x_3 \lor x_1. \overline{x_2}. \overline{x_4} \lor \overline{x_1}. x_2. \overline{x_4}, \underline{\text{MDNO}}: \texttt{[4, 11]}$$

$$f(x_1, x_2, x_3, x_4) = (\overline{x_2} \lor \overline{x_4}). (\overline{x_1} \lor \overline{x_2}). (x_3 \lor \overline{x_4}). (x_1 \lor x_2 \lor x_3), \underline{\text{MKNO}}: \texttt{[5, 13]}$$

Naloga 2:

a)
$$f(x_1, x_2, x_3, x_4, x_5) =$$
 $\lor^5 (2, 3, 4, 5, 10, 11, 12, 13, 16, 18, 19, 20, 21, 26, 27, 28) \lor^5_? (6, 7, 14, 15, 29), \underline{\mathsf{MNO}} = \underline{\mathsf{MDNO}}$ a) $f(x_1, x_2, x_3, x_4, x_5) = x_1.\overline{x_2}.\overline{x_3}.\overline{x_5} \lor \overline{x_3}.x_4 \lor x_3.\overline{x_4}$, $\underline{\mathsf{MDNO}}$: [4, 11] b) $f(x_1, x_2, x_3, x_4, x_5) = x_1.\overline{x_2}.\overline{x_4}.\overline{x_5} \lor \overline{x_3}.x_4 \lor x_3\overline{x_4}$, $\underline{\mathsf{MDNO}}$: [4, 11] $f(x_1, x_2, x_3, x_4, x_5) = (\overline{x_3} \lor \overline{x_4}).(x_3 \lor x_4 \lor \overline{x_5}).(\overline{x_2} \lor x_3 \lor x_4).(x_1 \lor x_3 \lor x_4)$, $\underline{\mathsf{MKNO}}$: [5, 15]

b)
$$f(x_1, x_2, x_3, x_4, x_5) =$$

 $V^{5}(0, 1, 3, 8, 10, 11, 17, 20, 21, 25, 26, 27, 28, 30, 31)$ $V_{?}^{5}(2, 6, 9, 29)$, MNO = MKNO

$$f(x_1, x_2, x_3, x_4, x_5) = \overline{x_1}.\overline{x_3} \vee x_1.x_2.x_4 \vee x_1.x_3.\overline{x_4} \vee x_1.\overline{x_4}.x_5$$
, MDNO: [5, 15]

$$f(x_1, x_2, x_3, x_4, x_5) == (x_1 \vee \overline{x_3}). (\overline{x_1} \vee x_2 \vee \overline{x_4}). (\overline{x_1} \vee x_3 \vee x_4 \vee x_5), \text{MKNO: [4, 12]}$$

c)
$$f(x_1, x_2, x_3, x_4, x_5) =$$

 \vee^{5} (0, 1, 5, 7, 8, 9, 10, 13, 22, 23, 26, 30, 31) \vee^{5} (2, 18, 19, 27, 28), MNO = MDNO = MKNO

a)
$$f(x_1, x_2, x_3, x_4, x_5) = \overline{x_1} \cdot \overline{x_3} \cdot \overline{x_5} \vee x_1 \cdot x_4 \vee \overline{x_1} \cdot \overline{x_4} \cdot x_5 \vee \overline{x_2} \cdot x_3 \cdot x_4 \cdot x_5$$
, MDNO: [5, 16]

b)
$$f(x_1, x_2, x_3, x_4, x_5) = \overline{x_1}.\overline{x_3}.\overline{x_5} \lor x_1.x_4 \lor \overline{x_1}.\overline{x_4}.x_5 \lor \overline{x_1}.\overline{x_2}.x_3.x_5$$
, MDNO: [5, 16]

MKNO: [5, 16]

a)
$$f(x_1, x_2, x_3, x_4, x_5) = (x_1 \lor \overline{x_3} \lor x_5). (\overline{x_1} \lor x_4). (x_1 \lor \overline{x_2} \lor \overline{x_4} \lor \overline{x_5}). (x_2 \lor x_3 \lor \overline{x_4})$$

$$\mathbf{b)}\,f(x_1,x_2,x_3,x_4,x_5)=(x_1\vee\overline{x_3}\vee x_5).\,(\overline{x_1}\vee x_4).\,(x_1\vee\overline{x_2}\vee\overline{x_4}\vee\overline{x_5}).\,(x_3\vee\overline{x_4}\vee\overline{x_5})$$

c)
$$f(x_1, x_2, x_3, x_4, x_5) = (x_1 \lor \overline{x_3} \lor x_5).(\overline{x_1} \lor x_4).(x_1 \lor \overline{x_2} \lor \overline{x_3} \lor \overline{x_4}).(x_3 \lor \overline{x_4} \lor \overline{x_5})$$