$$\langle \tilde{\theta}, QR \rangle_{\mathrm{F}} = \begin{bmatrix} \tilde{\theta} \\ Q^* & R^* \end{bmatrix}$$