$$Q R = Q A \tilde{S} \tilde{Y}^* = \tilde{X} \tilde{S} \tilde{Y}^*$$