

Exercise 5.2

$$\begin{aligned}
 \text{a.) } P(\text{Cancer} | \text{Test1} \wedge \text{Test2}) &= \alpha \sum P(\text{Cancer}, \text{Test1}, \text{Test2}) \\
 &= \alpha \sum P(\text{Cancer}) \cdot P(\text{Test1} | \text{Cancer}) \cdot P(\text{Test2} | \text{Cancer}) \\
 &= \alpha \langle (0.01 \cdot 0.9 \cdot 0.9), (0.99 \cdot 0.2 \cdot 0.2) \rangle \\
 &= \alpha \langle \frac{0.0081}{0.0477}, \frac{0.0396}{0.0477} \rangle \\
 &\approx \langle 0.17, 0.83 \rangle
 \end{aligned}$$

$$\begin{array}{r}
 + 0.0396 \\
 + 0.0081 \\
 \hline
 0.0477
 \end{array}$$

$$\begin{aligned}
 \text{b.) } P(\text{Cancer} | \text{Test1} \wedge \neg \text{Test2}) &= \alpha \sum P(\text{Cancer}, \text{Test1}, \neg \text{Test2}) \\
 &= \alpha \sum P(\text{Cancer}) \cdot P(\text{Test1} | \text{Cancer}) \cdot P(\neg \text{Test2} | \text{Cancer}) \\
 &= \alpha \langle (0.01 \cdot 0.9 \cdot 0.1), (0.99 \cdot 0.2 \cdot 0.8) \rangle \\
 &= \alpha \langle \frac{0.0009}{0.1593}, \frac{0.1584}{0.1593} \rangle \\
 &\approx \langle 0.00565, 0.99435 \rangle
 \end{aligned}$$

Exercise 5.3

$$\text{a.i.) } P(\text{Raise} | \text{Sunny}) = P(\text{Raise}) = \langle 0.01, 0.99 \rangle$$

$$\begin{aligned}
 \text{a.ii.) } P(\text{Raise} | \text{Happy} \wedge \text{Sunny}) &= \alpha \sum P(\text{Raise}, \text{Happy}, \text{Sunny}) \\
 &= \alpha \sum P(\text{Raise}) \cdot P(\text{Happy} \wedge \text{Sunny} | \text{Raise}) \\
 &= \alpha \langle (0.01 \cdot 1.0), (0.99 \cdot 0.7) \rangle \\
 &= \alpha \langle \frac{0.01}{0.703}, \frac{0.693}{0.703} \rangle \\
 &\approx \langle 0.0142, 0.98578 \rangle
 \end{aligned}$$