Miles Benjamin CS 6140 Homework 1 ¶

Just start at the top and start running in order. If you want to go back start at the beginning of the section to make sure that the variables are initialized properly. Hope this works well for you!

```
In [1]: import numpy as np
import math
import scipy as sp
import matplotlib.pyplot as plt
import scipy.io as scio
%matplotlib inline
```

Importing all the libraries

10 part 1

going to start by generating a dataset for which I know an approximate regression

```
In [89]:
         X_{trn} = []
          for i in range (20):
              X trn.append([1,i])
              # Making a data set of approx y = 1.5x to test the algorithm
          sp.random.seed(123)
          Y trn = []
          for i in range(len(X_trn)):
              Y_{trn.append}(X_{trn[i][1]} * (sp.rand(1) + 1))
         X tst = []
          for i in range(100):
              X \text{ tst.append}([1,i - 50])
         Y tst = []
          for i in range(len(X_tst)):
              Y_{tst.append}(X_{tst[i][1]} * (sp.rand(1) + 1))
          plt.subplot(2,1,1)
         plt.title('Y = 1.5X training')
          plt.plot(X_trn, Y_trn)
         plt.subplot(2,1,2)
          plt.title('Y = 1.5X testing')
         plt.plot(X_tst, Y_tst)
          plt.tight layout(pad=0.4, w pad=0.5, h pad=1.0)
```



```
In [90]: def calcCFTheta(X,Y):
             inver = np.dot(X.T, X)
             xy = np.dot(X.T, Y)
             theta = np.dot(np.linalg.inv(inver), xy)
             return theta
In [91]: def computeCost(X, Y, theta):
             cost = np.power(np.linalg.norm((X*theta - Y), 2))
             #print("cost: ", cost)
             return cost
In [92]: def gradientDescent(X, Y, theta, lrnRate, ittr, batch):
             #print(X, Y, theta, lrnRate)
             m = len(Y)
             for i in range(ittr):
                 miniX = []
                 miniY = []
                 for j in range(batch):
                      batchIdx = math.floor((sp.rand(1) * m)[0])
                     miniX.append(X.A[batchIdx])
                     miniY.append(Y.A[batchIdx])
                 miniX = np.mat(miniX)
                 miniY = np.mat(miniY)
                 theta = theta - (lrnRate/m) * (miniX.T * (miniX * theta - miniY)
                 #print(theta)
             return theta
```

In [96]: def outputRegression(theta1, theta2, X tst, Y tst, n):

```
print('GD Theta: ', theta1, '\n CF Theta: ', theta2)
             plt.figure(figsize=(12, 3*n))
             for i in range(n):
                 if (i != 0):
                     # Get the right X feature column
                     c = (i-1) *4
                     X test Col = np.mat([np.array(X tst)[:, i]])
                     X test_Col = X_test_Col.T
                     # Plot Stochastic Gradient Descent
                     plt.subplot(n,4,c+1)
                     title = 'LG w/ SGD ', i
                     plt.title(title)
                     plt.plot(X_test_Col, X_test_Col * theta1[i], linewidth = 2)
                     plt.plot(X_test Col, Y tst, '.')
                     # Plot error for SGD
                     plt.subplot(n,4,c+2)
                     title = 'LG w/ SGD Error ', i
                     plt.title(title)
                     plt.plot(X test Col, abs(Y tst - (X test Col * theta1[i])),
                     # Plot Closed Form Solution
                     plt.subplot(n,4,c+3)
                     title = 'LG w/ CFS ', i
                     plt.title(title)
                     plt.plot(X_test_Col, X_test_Col * theta2[i], linewidth = 2)
                     plt.plot(X_test_Col, Y_tst, '.')
                     # Plot CFS Error
                     plt.subplot(n,4,c+4)
                     title = 'LG w/ CFS Error ', i
                     plt.title(title)
                     plt.plot(X test Col, abs(Y tst - (X test Col * theta2[i])),
                     plt.tight_layout(pad=0.4, w_pad=0.5, h_pad=1.0)
In [97]: def linRegress(X_trn, Y_trn, X_tst, Y_tst, ittr, lrnRate, batch, n):
             m = len(X trn) # number of training samples (should be 20)
             X = np.mat(X trn)
             Y = np.mat(Y trn)
             theta1 = [0] * n
```

theta1 = gradientDescent(X, Y, theta1, lrnRate, ittr, batch)

outputRegression(thetal, theta2, X tst, Y tst, n)

theta1 = np.mat(theta1).T

theta2 = calcCFTheta(X,Y)

In [143]: def nFeatureizeData(X, n):

```
X_{out} = []
                for i in range(len(X)):
                     temp = []
                     for j in range(n + 1):
                           temp.append(np.power(X[i][0],j))
                     X out.append(temp)
                return X_out;
In [98]:
           batch = 4
           ittr = 2000
            lrnRate = 0.01
            n = 2
            linRegress(X_trn, Y_trn, X_tst, Y_tst, ittr, lrnRate, batch, n)
           GD Theta: [[ 0.46088082]
             [ 1.39017333]]
            CF Theta: [[ 0.65462812]
             [ 1.37924891]]
                    ('LG w/ SGD ', 1)
                                        ('LG w/ SGD Error ', 1)
                                                                ('LG w/ CFS', 1)
                                                                                     ('LG w/ CFS Error ', 1)
                                    30
             100
                                                         100
              75
                                                          75
                                    25
                                                                                25
              50
                                                          50
                                    20
              25
                                                          25
                                    15
                                                          -25
             -25
                                    10
             -50
             -75
            -100
                                                         -100
```

10 part 2

```
In [144]: mat = scio.loadmat('HW1_Data/dataset1.mat')

X_trn = mat['X_trn']
    Y_trn = mat['Y_trn']
    X_tst = mat['X_tst']
    Y_tst = mat['Y_tst']
    data = [X_trn,Y_trn,X_tst,Y_tst]

In [100]: print('shape of the X data is [%d, %d]' % X_trn.shape)
    print('shape of the Y data is [%d, %d]' % Y_trn.shape)

shape of the X data is [120, 1]
    shape of the Y data is [120, 1]
```

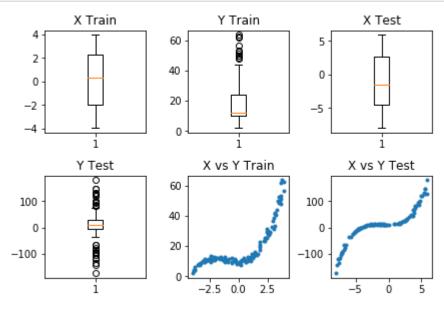
```
In [101]: data_labels = ['X Train', 'Y Train', 'X Test', 'Y Test']

for x in range(4):
    plt.subplot(2,3,x +1)
    plt.boxplot(data[x])
    plt.title(data_labels[x])

plt.subplot(2,3,5)
    plt.plot(X_trn, Y_trn, '.')
    plt.title("X vs Y Train")

plt.subplot(2,3,6)
    plt.plot(X_tst, Y_tst, '.')
    plt.title("X vs Y Test")

plt.tight_layout(pad=0.4, w_pad=0.5, h_pad=1.0)
```



N = 1

I know I don't have to do this, but I was curious

```
In [145]: n = 1
             batch = 4
             ittr = 2000
             lrnRate = 0.01
             features = n + 1
             linRegress(nFeatureizeData(X_trn, n), Y_trn, nFeatureizeData(X_tst, n),
             GD Theta: [[ 8.76170969]
               [ 5.12283991]]
              CF Theta: [[ 17.81209242]
                 4.8607913 ]]
                      ('LG w/ SGD ', 1)
                                           ('LG w/ SGD Error ', 1)
                                                                    ('LG w/ CFS ', 1)
                                                                                         ('LG w/ CFS Error ', 1)
                                      140
                                                                                    140
               150
                                                             150
                                      120
                                                                                    120
               100
                                                             100
                                      100
                                                                                    100
                                                              50
                50
                                       80
                                                              0
                                       60
                                                                                     60
                                                             -50
               -50
                                       40
              -100
                                                            -100
                                       20
                                                                                     20
              -150
                                                            -150
```

For N = 2

```
In [146]: n = 2
               batch = 4
               ittr = 2000
               lrnRate = 0.01
               features = n + 1
               linRegress(nFeatureizeData(X_trn, n), Y_trn, nFeatureizeData(X_tst, n),
                               [[ 2.60594924]
               GD Theta:
                 [ 4.70017367]
                 [ 2.22991393]]
                CF Theta: [[ 9.49203678]
                 [ 4.79191663]
                 [ 1.52906587]]
                         ('LG w/ SGD ', 1)
                                                 ('LG w/ SGD Error ', 1)
                                                                             ('LG w/ CFS ', 1)
                                                                                                     ('LG w/ CFS Error ', 1)
                                                                                               150
                                           150
                 150
                                                                     150
                                           125
                                                                                               125
                                                                     100
                 100
                                                                                                100
                                           100
                  50
                                                                      50
                                                                       0
                                                                                                75
                  0
                                            75
                 -50
                                                                     -50
                                            50
                                                                                                50
                -100
                                                                     -100
                                            25
                                                                                                25
                                                                    -150
                -150
                         ('LG w/ SGD ', 2)
                                                 ('LG w/ SGD Error ', 2)
                                                                             ('LG w/ CFS ', 2)
                                                                                                     ('LG w/ CFS Error ', 2)
                                           300
                 150
                                                                     150
                                                                                               250
                                           250
                                                                     100
                 100
                                                                                               200
                                           200
                                                                      50
                                                                                               150
                  0
                                           150
                                                                       0
                                                                                                100
                 -50
                                                                     -50
                                           100
                -100
                                                                    -100
                                            50
                                                                    -150
                -150
                                                                60
                                                                                                                     60
                                      60
                                                                                           60
```

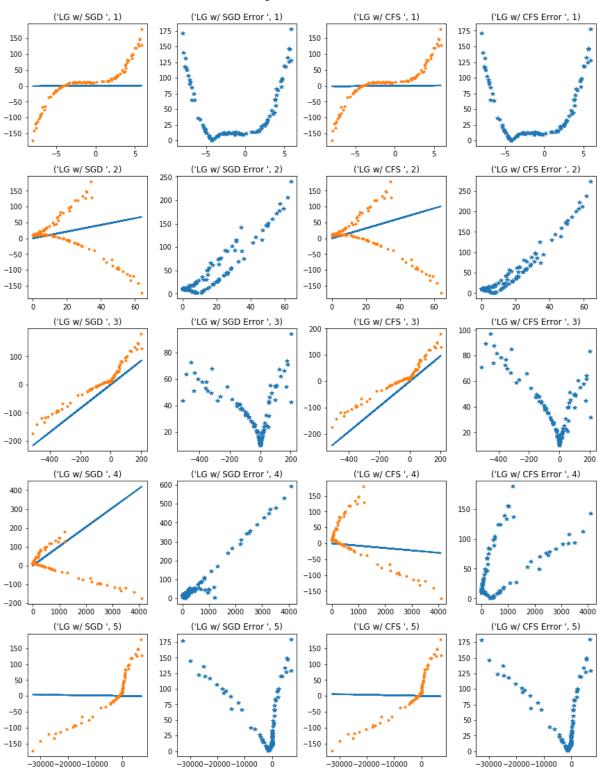
For N = 3

```
In [147]: n = 3
                batch = 4
                ittr = 2000
                lrnRate = 0.01
                features = n + 1
                linRegress(nFeatureizeData(X_trn, n), Y_trn, nFeatureizeData(X_tst, n),
                                 [[ 2.70779825]
                GD Theta:
                  [ 0.30743738]
                  [ 2.25590356]
                  [ 0.39081937]]
                 CF Theta: [[ 10.00815033]
                      0.20418927]
                      1.47413164]
                      0.47320168]]
                          ('LG w/ SGD ', 1)
                                                                                  ('LG w/ CFS ', 1)
                                                                                                            ('LG w/ CFS Error ', 1)
                                                    ('LG w/ SGD Error ', 1)
                                              175
                                                                                                      175
                  150
                                                                          150
                                              150
                                                                                                      150
                  100
                                                                          100
                                              125
                                                                                                      125
                   50
                                                                           50
                                              100
                                               75
                  -50
                                                                          -50
                                               50
                                                                                                       50
                 -100
                                                                         -100
                                               25
                                                                                                      25
                 -150
                                                                         -150
                          ('LG w/ SGD ', 2)
                                                    ('LG w/ SGD Error ', 2)
                                                                                  ('LG w/ CFS ', 2)
                                                                                                            ('LG w/ CFS Error ', 2)
                                              300
                                                                                                      250
                  150
                                                                          150
                                              250
                                                                          100
                  100
                                                                                                      200
                   50
                                                                           50
                                              200
                                                                                                      150
                                              150
                                                                                                      100
                                                                          -50
                  -50
                                              100
                 -100
                                                                         -100
                                               50
                 -150
                                                                         -150
                                                0
                          ('LG w/ SGD ', 3)
                                                    ('LG w/ SGD Error ', 3)
                                                                                  ('LG w/ CFS ', 3)
                                                                                                            ('LG w/ CFS Error ', 3)
                                                                          200
                                                                                                      100
                                              100
                                                                          100
                  100
                                               80
                                                                            0
                                                                                                      60
                                               60
                    0
                                                                                                      40
                                                                         -100
                                               40
                 -100
                                                                                                      20
                                               20
                                                                         -200
                 -200
                                         200
                                                    -400
                                                         -200
                                                                     200
                                                                                                 200
                                                                                                                             200
                        -400
                             -200
                                                                                -400
                                                                                     -200
                                                                                                            -400
                                                                                                                 -200
```

For N = 5

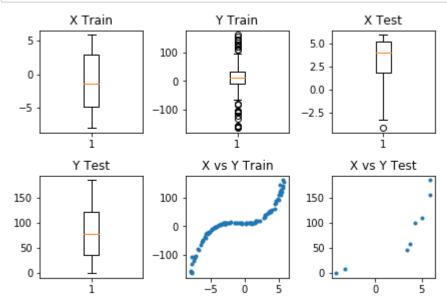
```
In [148]: n = 5
   batch = 4
   ittr = 20000
   lrnRate = 0.0001
   features = n + 1
   linRegress(nFeatureizeData(X_trn, n), Y_trn, nFeatureizeData(X_tst, n), Y
# I had to really tone down the learning rate and turn up the itteration.
# it appears that there is a direct correlation between the size of n and
```

```
GD Theta: [[ 4.85328498e-01]
  [ 1.35269865e-01]
  [ 1.05553575e+00]
  [ 4.21730646e-01]
  [ 1.02181622e-01]
  [ -1.24677512e-04]]
  CF Theta: [[ 9.84545670e+00]
  [ 2.03644970e-01]
  [ 1.57564738e+00]
  [ 4.75176601e-01]
  [ -7.40094164e-03]
  [ -1.77139419e-04]]
```



10.3

```
In [149]: mat = scio.loadmat('HW1 Data/dataset2.mat')
          X trn = mat['X trn']
          Y_trn = mat['Y_trn']
          X_tst = mat['X_tst']
          Y_{tst} = mat['Y_{tst}']
          data = [X trn,Y trn,X tst,Y tst]
In [150]:
          print('shape of the X data is [%d, %d]' % X_trn.shape)
          print('shape of the Y data is [%d, %d]' % Y trn.shape)
          shape of the X data is [100, 1]
          shape of the Y data is [100, 1]
In [157]: data_labels = ['X Train', 'Y Train', 'X Test', 'Y Test']
          for x in range(4):
               plt.subplot(2,3,x +1)
               plt.boxplot(data[x])
               plt.title(data labels[x])
          plt.subplot(2,3,5)
          plt.plot(X_trn, Y_trn, '.')
          plt.title("X vs Y Train")
          plt.subplot(2,3,6)
          plt.plot(X_tst, Y_tst, '.')
          plt.title("X vs Y Test")
          plt.tight_layout(pad=0.4, w_pad=0.5, h_pad=1.0)
```



```
In [208]: def calcCFRidge(X,Y,lam):
    #print(lam, X, Y)
    inver = np.dot(X.T, X) + (lam * np.identity(len(X[0])))
    xy = np.dot(X.T, Y)
    theta = np.dot(np.linalg.inv(inver), xy)
    return theta
```

```
In [292]: def kCrossValid(X,Y,lams,c):
               # I just did K=N cross validation. I didn't have time to generalize
               thetas = []
               holdOuts = []
               for i in range(len(lams)):
                   X_{test} = []
                   Y \text{ test} = []
                   for j in range(len(X)):
                        if (j != i):
                            X test.append(X[j])
                            Y test.append(Y[j])
                   X \text{ test} = \text{np.mat}(X \text{ test})
                   Y test = np.mat(Y test)
                   if (c == 1):
                        thetas.append(calcCFRidge(X_test,Y_test,lams[i]))
                   if (c == 0):
                        dummytheta = [0] * len(X[0])
                        dummytheta = np.mat(dummytheta).T
                        #print(dummytheta)
                        thetas.append(gradDescentRidge(X test,Y test,dummytheta, 0.0
                   holdOuts.append(abs(Y[i] - X[i]*thetas[i]))
               holdOuts = np.asarray(holdOuts)
               #print(np.argmin(holdOuts))
               return lams[np.argmin(holdOuts)]
```

```
In [293]: def gradDescentRidge(X, Y, theta, lrnRate, lams, ittr, batch):
    #print(X, Y, theta, lrnRate)
    m = len(Y)

for i in range(ittr):
    miniX = []
    miniY = []
    for j in range(batch):
        batchIdx = math.floor((sp.rand(1) * m)[0])

        miniX.append(X.A[batchIdx])
        miniY.append(Y.A[batchIdx])

    miniX = np.mat(miniX)
    miniY = np.mat(miniY)

#print("\ntheta: ", theta, "\nminiX: ", miniX, "\nminiY: ", minitheta = theta - (lrnRate/m) * ((miniX.T * (miniX * theta - miniY))

return theta
```

```
In [297]: N = [2]
          for k in range(len(N)):
              X temp = nFeatureizeData(X trn, N[k])
              sp.random.seed(123)
              lams = []
              for i in range(len(X temp)):
                  lams.append(sp.rand(1) * 10)
              lam2 = kCrossValid(X_temp, Y_trn, np.asarray(lams), 1)[0]
              lam1 = kCrossValid(X temp, Y trn, np.asarray(lams), 0)[0]
              X = nFeatureizeData(X tst, N[k])
              theta1 = [0] * (N[k] +1)
              theta1 = np.mat(theta1).T
              theta1 = gradDescentRidge(np.mat(X), np.mat(Y tst), np.mat(theta1),
              print("Stocastic Grad Descent")
              print("lambda: ", lam1, " theta: ", theta1)
              theta2 = calcCFRidge(np.mat(X), np.mat(Y tst), lam1)
              print("Closed Form Solution")
              print("lambda: ", lam2, " theta: ", theta2)
              outputRegression(theta1, theta2, X, Y_tst, N[k] + 1)
          Stocastic Grad Descent
          lambda: 42.6351306963 theta: [[-2.83651949]
```

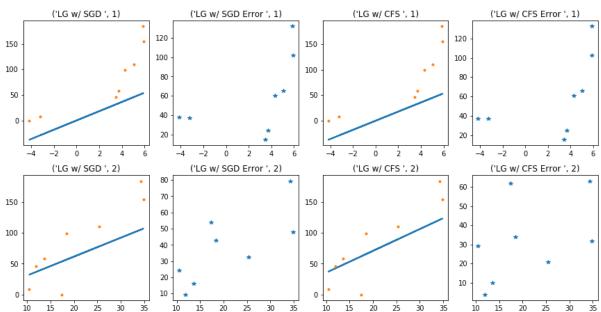
```
lambda: 42.6351306963 theta: [[-2.83651949]
  [ 9.07501993]
  [ 3.07809323]]

Closed Form Solution

lambda: 1.6129206695 theta: [[-12.76880157]
  [ 8.932615 ]
  [ 3.55154316]]

GD Theta: [[-2.83651949]
  [ 9.07501993]
  [ 3.07809323]]

CF Theta: [[-12.76880157]
  [ 8.932615 ]
  [ 3.55154316]]
```



```
In [295]: N = [3]
          for k in range(len(N)):
              X temp = nFeatureizeData(X trn, N[k])
              sp.random.seed(123)
              lams = []
              for i in range(len(X temp)):
                   lams.append(sp.rand(1) * 10)
              lam2 = kCrossValid(X_temp, Y_trn, np.asarray(lams), 1)[0]
              lam1 = kCrossValid(X temp, Y trn, np.asarray(lams), 0)[0]
              X = nFeatureizeData(X tst, N[k])
              theta1 = [0] * (N[k] +1)
              theta1 = np.mat(theta1).T
              theta1 = gradDescentRidge(np.mat(X), np.mat(Y tst), np.mat(theta1),
              print("Stocastic Grad Descent")
              print("lambda: ", lam1, " theta: ", theta1)
              theta2 = calcCFRidge(np.mat(X), np.mat(Y tst), lam1)
              print("Closed Form Solution")
              print("lambda: ", lam2, " theta: ", theta2)
              outputRegression(theta1, theta2, X, Y_tst, N[k] + 1)
          Stocastic Grad Descent
          lambda: 5.94431879445 theta: [[ 0.23262323]
           [ 0.48047131]
           [ 2.18935039]
           [ 0.41686872]]
```

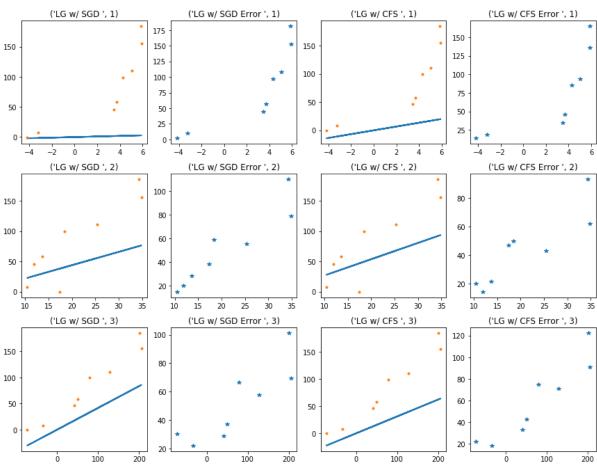
```
lambda: 5.94431879445 theta: [[ 0.23262323]
  [ 0.48047131]
  [ 2.18935039]
  [ 0.41686872]]

Closed Form Solution

lambda: 2.8613933495 theta: [[-5.53988052]
  [ 3.36237553]
  [ 2.67880489]
  [ 0.31145214]]

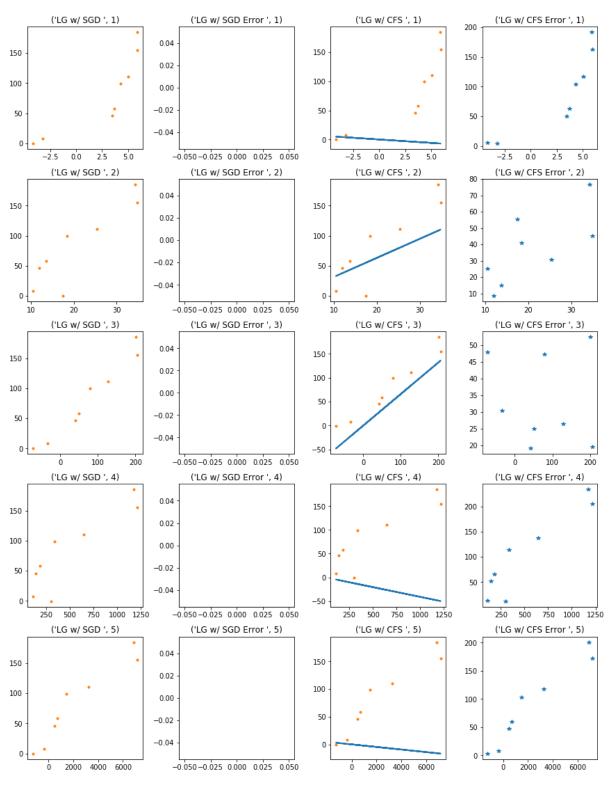
GD Theta: [[ 0.23262323]
  [ 0.48047131]
  [ 2.18935039]
  [ 0.41686872]]

CF Theta: [[-5.53988052]
  [ 3.36237553]
  [ 2.67880489]
  [ 0.31145214]]
```



```
In [296]: # This one won't run, I think it's too much for the kernel to handle!
          N = [5]
          for k in range(len(N)):
              X temp = nFeatureizeData(X trn, N[k])
              sp.random.seed(123)
              lams = []
              for i in range(len(X temp)):
                   lams.append(sp.rand(1) * 10)
              lam2 = kCrossValid(X temp, Y trn, np.asarray(lams), 1)[0]
              lam1 = kCrossValid(X_temp, Y_trn, np.asarray(lams), 0)[0]
              X = nFeatureizeData(X tst, N[k])
              theta1 = [0] * (N[k] +1)
              theta1 = np.mat(theta1).T
              thetal = gradDescentRidge(np.mat(X), np.mat(Y tst), np.mat(thetal),
              print("Stocastic Grad Descent")
              print("lambda: ", lam1, " theta: ", theta1)
              theta2 = calcCFRidge(np.mat(X), np.mat(Y tst), lam1)
              print("Closed Form Solution")
              print("lambda: ", lam2, " theta: ", theta2)
              outputRegression(theta1, theta2, X, Y tst, N[k] + 1)
          /usr/local/lib/python3.5/dist-packages/ipykernel_launcher.py:19: Runtim
          eWarning: invalid value encountered in subtract
          Stocastic Grad Descent
          lambda: 6.96469185598 theta: [[ nan]
           [ nan]
           [ nan]
           [ nan]
           [ nan]
           [ nan]]
          Closed Form Solution
          lambda: 0.957125166124 theta: [[ -2.69428026e+00]
           [ -1.17375436e+00]
           [ 3.16040989e+00]
             6.60069335e-01]
           [ -4.10876507e-02]
           [ -2.32212241e-03]]
          GD Theta: [[ nan]
           [ nan]
           [ nan]
           [ nan]
```

```
[ nan]
[ nan]]
CF Theta: [[ -2.69428026e+00]
[ -1.17375436e+00]
[ 3.16040989e+00]
[ 6.60069335e-01]
[ -4.10876507e-02]
[ -2.32212241e-03]]
```



In []: