

You are given a **0-indexed** 2D integer array `questions` where `questions[i] = [pointsi, brainpoweri]`.

The array describes the questions of an exam, where you have to process the questions **in order** (i.e., starting from question `0`) and make a decision whether to **solve** or **skip** each question. Solving question `i` will **earn** you `pointsi` points but you will be **unable** to solve each of the next `brainpoweri` questions. If you skip question `i`, you get to make the decision on the next question.

- For example, given `questions = [[3, 2], [4, 3], [4, 4], [2, 5]]`:
 - If question `0` is solved, you will earn `3` points but you will be unable to solve questions `1` and `2`.
 - If instead, question `0` is skipped and question `1` is solved, you will earn `4` points but you will be unable to solve questions `2` and `3`.

Return the **maximum** points you can earn for the exam.

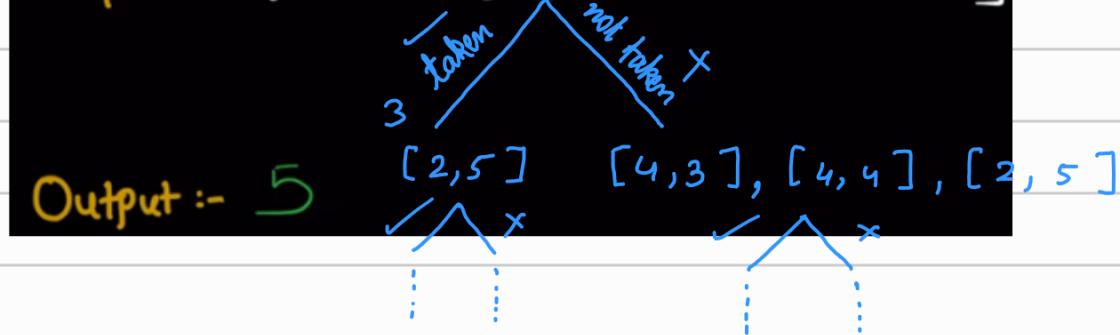
Input :- `questions = [[3, 2], [4, 3], [4, 4], [2, 5]]`

meaning of above is that let's say we solved first ques `[3, 2]` so we will get 3 points but we won't be able to solve next 2 questions since brainpower is 2 of the first question.

Output :- 5

dp question → taken / not taken .

Input :- questions = $\begin{bmatrix} [3,2] & [4,3] & [4,4] & [2,5] \end{bmatrix}$



if taken grab that el's ht
& go to BrainPower of the element
i + 2 + 1 element

if not taken, go to next element.

[since we have to skip
brainpower no of next
elements].

Recursion + Memoization

```

7 //Approach-1 (Using Simple Recursion + Memo) - Knapsack variant
8 class Solution {
9 public:
10     int n;
11     long long solve(int i, vector<vector<int>>& questions, vector<long long> &t) {
12
13         if(i >= n)
14             return 0;
15
16         if(t[i] != -1)
17             return t[i];
18
19         long long taken = questions[i][0] + solve(i+questions[i][1]+1, questions, t);
20
21         long long not_taken = solve(i+1, questions, t);
22
23         return t[i] = max(taken, not_taken);
24
25     }
26
27
28     long long mostPoints(vector<vector<int>>& questions) {
29         n = questions.size();
30         vector<long long> t(n+1, -1);
31         return solve(0, questions, t);
32     }
33 }
34 
```

Ex: $\begin{bmatrix} 3, 2 \end{bmatrix} \rightarrow \text{points}$.
 $\begin{bmatrix} 4, 3 \end{bmatrix} \rightarrow \text{brain power}$
 gotoneel .

BOTTOM UP APPROACH

during recursion + memo only index was changing solve(i, quo)
(i)

∴ we can solve it using 1D array.

vector <int> t

// t[i]

State definition:

In bottom up what we do is to find answer of $t[i]$
we try to find answer by relating from the past ex: $t[i-1]$,
 $t[i-2]$, $t[i-3]$

$\swarrow t[i]$

But the problem here in this question is ↴

i	0	1	2	3	4
	(1, 2)	(2, 2)	(1, 5)	(3, 5)	(4, 6)

↑ ↴

let's say i is here its impacting future 2 tasks [Brainpower]
so how to solve using bottom up [where it dependnt on the past]
but here its diff ↴ (any task is impacting future task)

Let's say i was here, so index 2 & 3 will be skipped
↓
(discarded)

0	1	2	3	4
(1, 2)	(2, 2)	(1, 5) (1, 5)	(3, 5) (3, 5)	(4, 6)

now i comes here

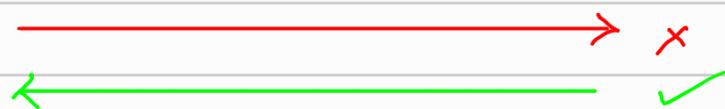
0	1	2	3	4
(1, 2)	(2, 2)	(1, 5) (1, 5)	(3, 5) (3, 5)	(4, 6)

now how would we know if its been discarded or not . where in the past it has been discarded from (either index 0 or 1) we do not know .

\therefore we can not go from left to right (as any task is impacting future tasks) .

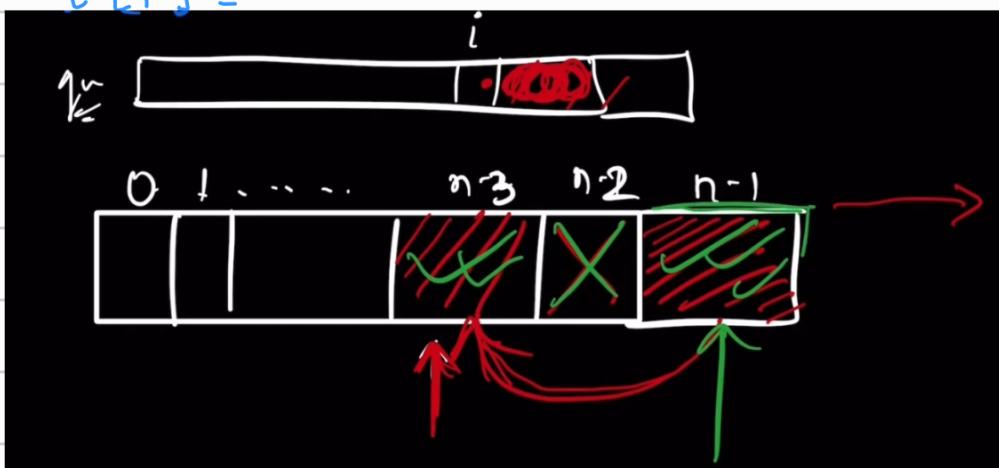
\therefore we will move from right to left .

0	1	2	3	4
(1, 2)	(2, 2)	(1, 5)	(3, 5)	(4, 6)



Right to left :-

$t[i] =$



Let's say we are at i & brainpower is 1 \therefore we will skip one element

now in bottom up array we are solving from right to left \therefore to solve $n-3$ (i 's equivalent) we can take help of $n-1$ & after (i 's future elements) but here it's fast since we are solving from R to L & skip $n-2$ (due to brainpower)

$t[i] = \max \text{ points gained by Qns from } [i \rightarrow n-1]$

given in question 0 to $n-1$
& $t[i] = i \text{ to } n-1$

$\therefore \text{result} = t[0] \rightarrow \begin{matrix} \text{max pts gained by Qns from} \\ (0 \rightarrow n-1) \end{matrix}$

hence we need to return $t[0]$.

DRY RUN...

q	0	1	2	3	4
$q =$	$(1, 2)$	$(2, 2)$	$(1, 5)$	$(3, 5)$	$(4, 6)$
t					

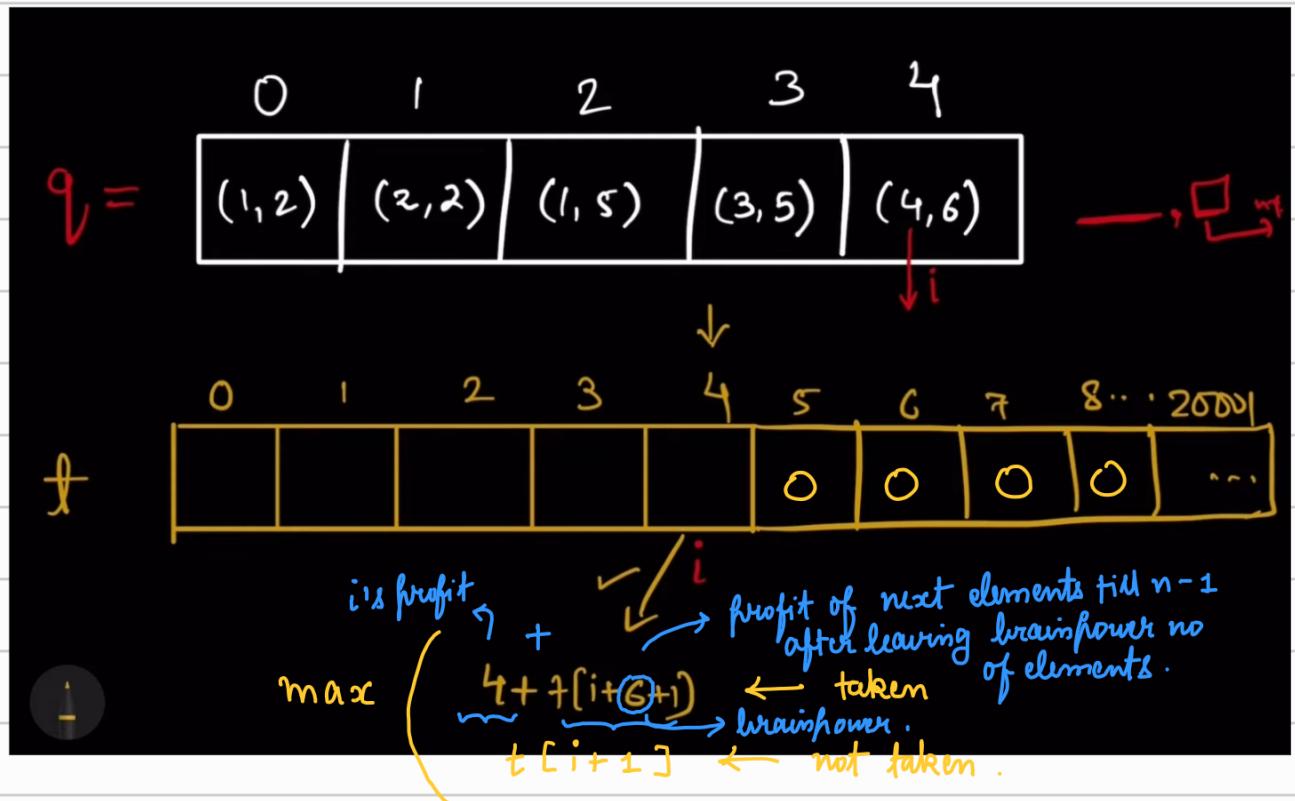
i

$4 + t[i+6+1]$

\square $n-1$

leaving 6 elements, any elements after till $n-1$, profit will be added.

But it will get out of bounds.
 \therefore take a big array & put 0.
[So out of bound issue is resolved].



in not taken case since we are not taking $i \therefore$ we won't get any profit \therefore whatever profit we got from right side we will put the same profit here only (since not taken) .

$$t[i] = \max \left(\underbrace{t[i+1]}_{\text{not taken}}, \underbrace{t[i+1] + q[i+1][0] + t[i+q[i+1]+1]}_{\text{taken}} \right);$$

0	1	2	3	4
(1,2)	(2,2)	(1,5)	(3,5)	(4,6)

t	0	1	2	3	4	5	6	7	8 ... 2000
t					4	0	0	0	0

t	0	1	2	3	4	5	6	7	8 ... 2000
t				4	4	0	0	0	0

$$\max (\underline{3} + t[i+5+1], \underline{4})$$

taken

not taken.

(∵ take previous point)

(discussed earlier)

t	0	1	2	3	4	5	6	7	8 ... 2000
t			4	4	4	0	0	0	0

$$\max (\underline{1} + 0 = 1,$$

taken
not taken

t	0	1	2	3	4	5	6	7	8 ... 2000
t		6	4	4	4	0	0	0	0

$$(\underline{2} + 4 = 6, \underline{4})$$

t	0	1	2	3	4	5	6	7	8 ... 2000
t	6	6	4	4	4	0	0	0	0

$$(\underline{1} + 4 = 5, \underline{6})$$

$$\therefore \text{Answer} \rightarrow \underline{\underline{t[0] = 6}}$$

```
1 class Solution {
2 public:
3     long long mostPoints(vector<vector<int>>& q) {
4         int n = q.size();
5
6         if (n == 1)
7             return q[0][0];
8
9         vector<long long> t(200001, 0);
10        //t[i] = max points gained by Qns from i to n-1
11        //return t[0] -> 0 to n-1
12
13        for(int i = n-1; i>=0; i--) {
14            t[i] = max(q[i][0] + t[i + q[i][1] + 1], t[i+1]);
15        }
16
17        return t[0];
18    }
19}
```

t[i] taken not taken