

Data Science & AI



Machine Learning



Supervised Learning

Lecture No.- 04



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Recap of Previous Lecture



Topic

Ridge

Topic

lasso

Topic

Regression

Topic

Topic

Topics to be Covered



Topic

Decision Tree

Topic

Decision Tree Regressor

Topic

Decision Tree Classifier

Topic

Topic

Decision Tree Classifier And Regressor

Agenda

① Decision Tree Classifier [classification]

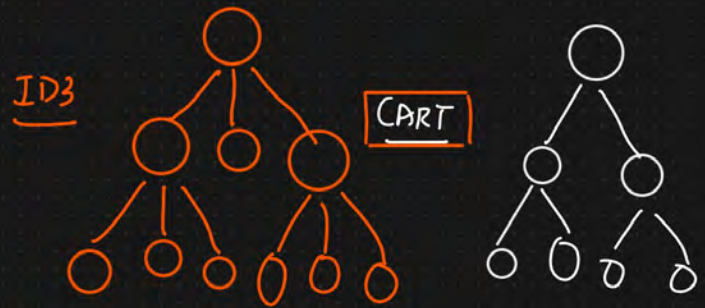
② Decision Tree Regressor [Regression]

① Decision Tree Classifier

Two Types

① ID3 [Iterative Dichotomiser 3]

② CART [Classification And Regression Trees]



Age = 14

if (age ≤ 15):

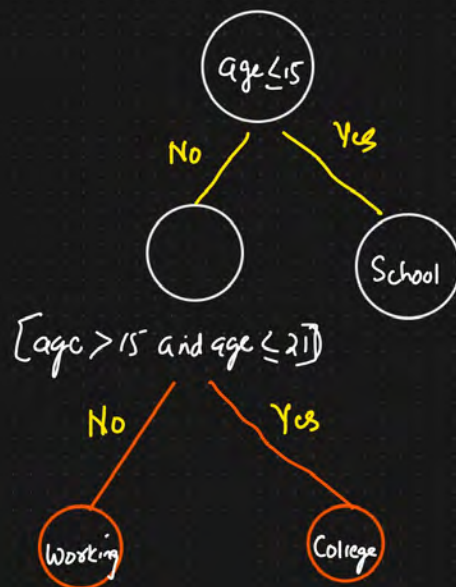
Print("School")

elif (age > 15 and age ≤ 21):

Print("College")

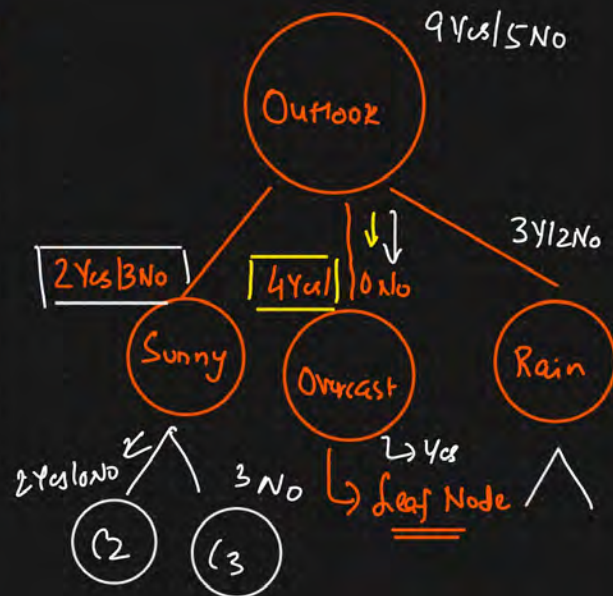
else (age > 21):

Print("Working")

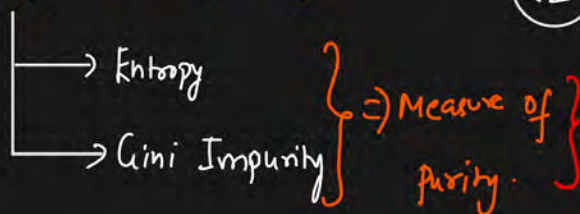


Dataset: Predict Play Tennis or Not

Day	Outlook	Temperature	Humidity	Wind	Play Tennis
1	Sunny	Hot	High	Weak	No
2	Sunny	Hot	High	Strong	No
3	Overcast	Hot	High	Weak	Yes
4	Rain	Mild	High	Weak	Yes
5	Rain	Cool	Normal	Weak	Yes
6	Rain	Cool	Normal	Strong	No
7	Overcast	Cool	Normal	Strong	Yes
8	Sunny	Mild	High	Weak	No
9	Sunny	Cool	Normal	Weak	Yes
10	Rain	Mild	Normal	Weak	Yes
11	Sunny	Mild	Normal	Strong	Yes
12	Overcast	Mild	High	Strong	Yes
13	Overcast	Hot	Normal	Weak	Yes
14	Rain	Mild	High	Strong	No



① Purity check: Pure split or Impure Split



② What feature you need to select to start the split? → Information Gain.

$$2 \text{ Yes} / 2 \text{ No}$$

$$P_+ = \frac{2}{4} = 0.5$$

① Entropy

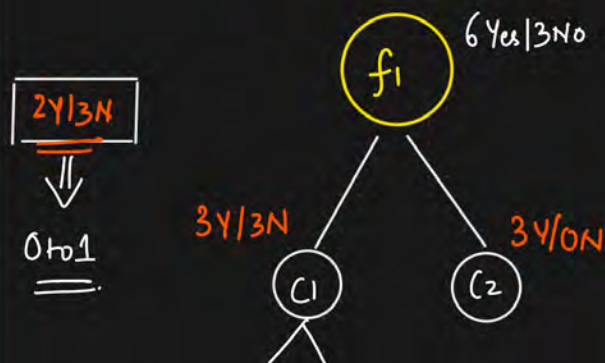
ii) Gini Impurity

$$H(s) = -P_+ \log_2 P_+ - P_- \log_2 P_-$$

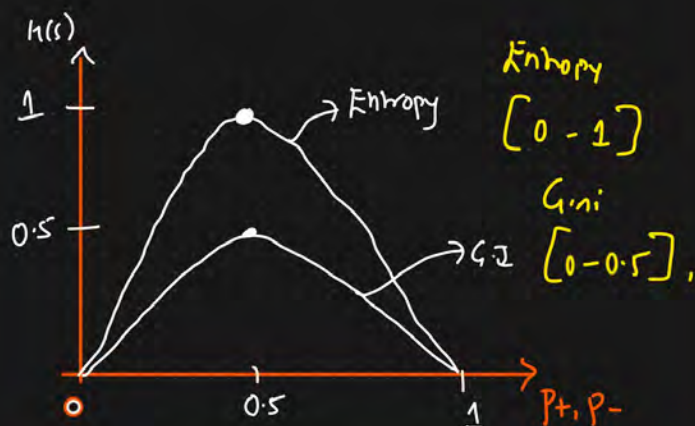
P_+ = probability of +ve category

P_- = probability of negative category

$$G.I = 1 - \sum_{i=1}^n (P_i)^2$$



$$H(C_1) = -P_+ \log_2 P_+ - P_- \log_2 P_-$$



$$= -\frac{1}{2} \log_2\left(\frac{1}{2}\right) - \frac{1}{2} \log_2\left(\frac{1}{2}\right)$$

$= 1 \Rightarrow$ Impure Split

Multiclass classification $[c_1, c_2, c_3]$

$$H(S) = -p_{c_1} \log_2 p_{c_1} - p_{c_2} \log_2 p_{c_2} - p_{c_3} \log_2 p_{c_3}$$

$$H(c_2) = -\frac{3}{3} \log_2\left(\frac{3}{3}\right) - \frac{0}{3} \log_2\left(\frac{0}{3}\right)$$

$= 0 \Rightarrow$ Pure Split

② Gini Impurity

$$G.I = 1 - \sum_{i=1}^n (p_i)^2$$

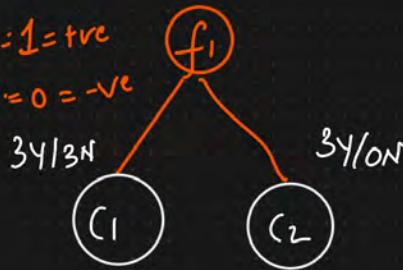
$$= 1 - \left[(p_+)^2 + (p_-)^2 \right]$$

$$= 1 - \left[\left(\frac{3}{6}\right)^2 + \left(\frac{3}{6}\right)^2 \right]$$

$$= 1 - \left[\frac{1}{4} + \frac{1}{4} \right] = 0.5$$

\Downarrow
Impure Split.

Yes: 1 = true
No: 0 = false



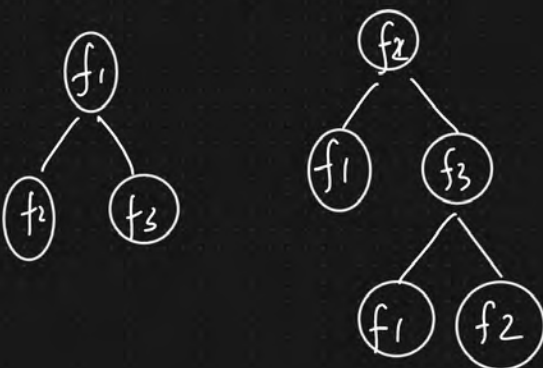
$$G.I(c_2) = 1 - \left[(1)^2 + (0)^2 \right]$$

$$= 1 - 1$$

$= 0 \Rightarrow$ Pure Split.

② What feature you need to select to start the split? \rightarrow Information Gain

$f_1 \quad f_2 \quad f_3 \quad \text{o/p}$



Information Gain

Entropy of the root Node

$$\text{Gain}(S, f) = H(S) - \sum_{v \in \text{val}(S)} \frac{|S_v|}{|S|} H(S_v)$$

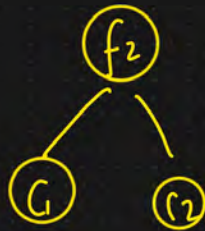
$$H(S) = -p_+ \log_2 p_+ - p_- \log_2 p_-$$

$$= -\frac{9}{14} \log_2 \frac{9}{14} - \frac{5}{14} \log_2 \left(\frac{5}{14} \right)$$

$$H(S) \approx 0.94$$

$$H(C_1) = -\frac{6}{8} \log_2 \frac{6}{8} - \frac{2}{8} \log_2 \frac{2}{8} \approx 0.81$$

$$H(C_2) = 1$$



$$\text{Gain}(S, f_2) = 0.051$$

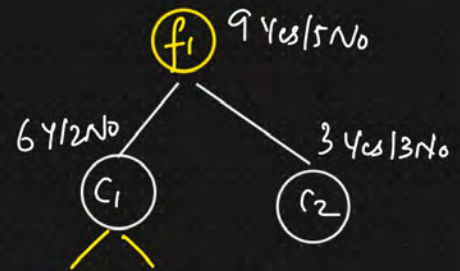
$$\text{Gain}(S, f_2) = 0.051 > \text{Gain}(S, f_1) = 0.049$$

Higher the IG ↑

Entropy Vs Gini Impurity

Whenever dataset is small → Entropy
dataset is huge → Gini Impurity

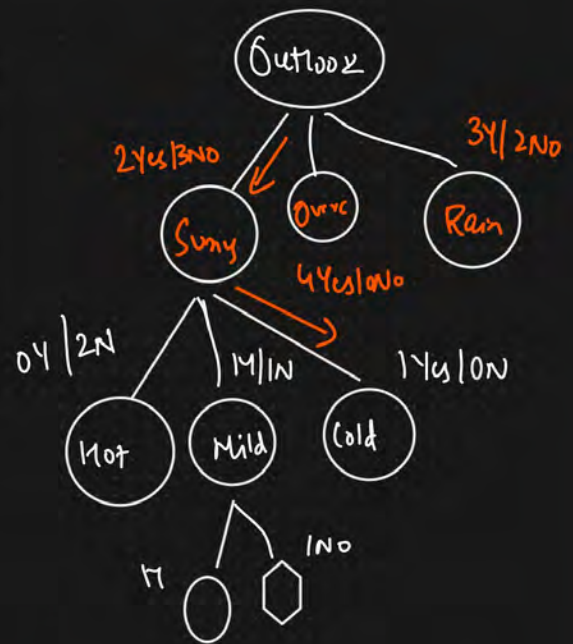
f1 f2 f3 O/P



$$\text{Gain}(S, f_1) = 0.94 - \left[\frac{8}{14} \times 0.81 + \frac{6}{14} \times 1 \right]$$

$$\text{Gain}(S, f_1) = 0.049$$

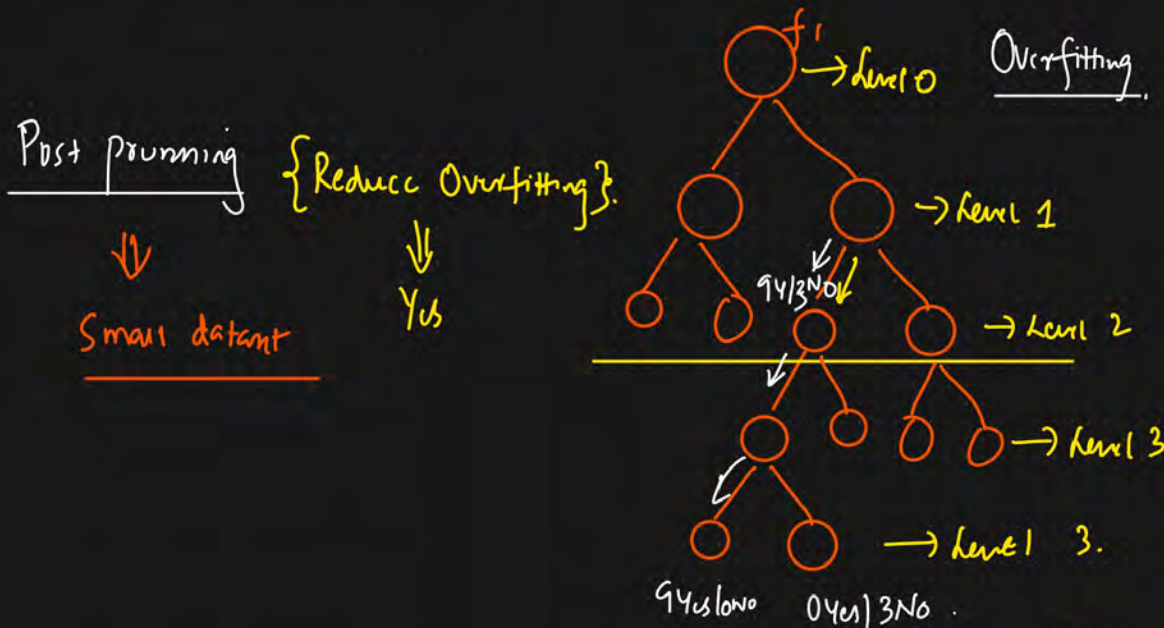
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→ Outlook Temperature
Sunny Cold

Play
Yes

Decision Tree Post Pruning And Pre pruning [Post Pruning And Pre pruning]

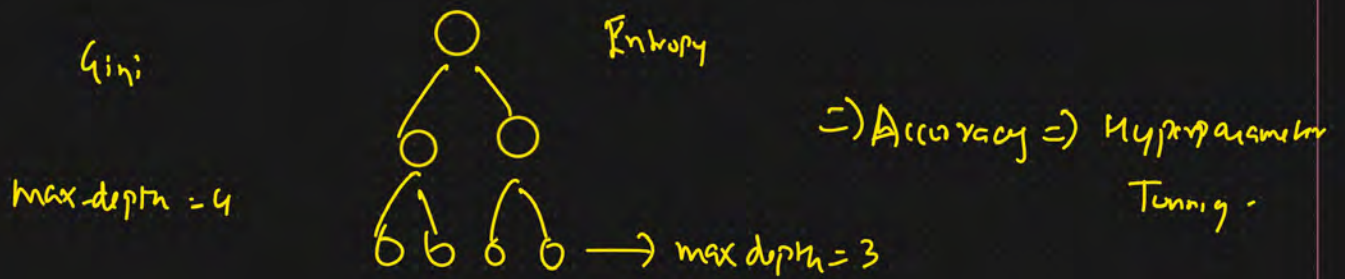


Post pruning → Small dataset → Yes

Pre Pruning → DATASET → Suitable parameter ⇒ Hyperparameter Tuning.

Max depth, Split, Criterion

Select the best parameters

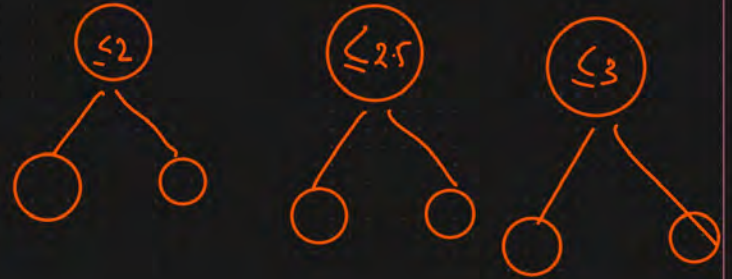
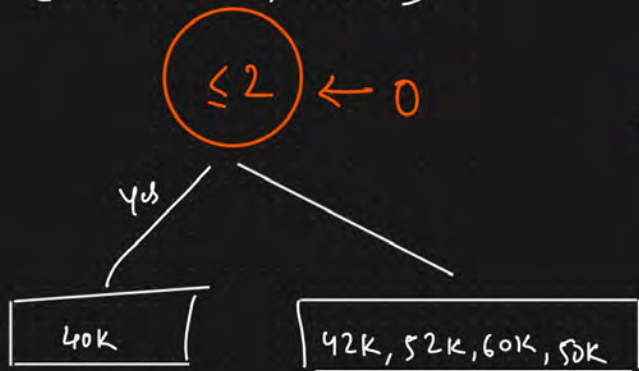


④ Decision Tree Regressor

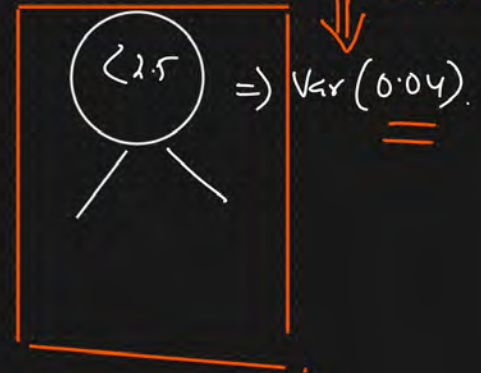
DATASET

Exp	Career Gap	Salary
2	Yes	40K
2.5	Yes	42K
3	No	52K
4	No	60K
4.5	Yes	56K
		$\bar{y} = 50K$

[40K, 42K, 52K, 60K, 56K]



Split \Rightarrow Variance Reduction



Variance Reduction

$$\text{Variance (Root)} = \frac{1}{n} \sum_{i=1}^n (y_i - \bar{y})^2 \quad [\text{MSE}]$$

Mean of y

$$= \frac{1}{5} [(10)^2 + (8)^2 + (2)^2 + 10^2 + 6^2]$$

Variance Reduction :

$$\text{Var(Root)} - \sum w_i \text{Var(child)}$$

$$60.8 - \left[\frac{1}{5} * 100 + \frac{4}{5} * 51 \right]$$

$$\text{Variance}(\text{Root}) = 60.8$$

$$\text{Var}(\text{Right}) = \underline{\underline{51}} = \underline{\underline{0}}$$

$$\text{Var}(\text{Left}) = \frac{1}{1} [(40-50)^2]$$

$$\text{Var}(\text{Left}) = 100$$

THANK - YOU