GATE BM 2023 Quetion 9

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Question :
Out of 1000 individuals in a town, 100 unidentified individuals are covid positive. Due to lack of adequate covid-testing kits, the health authorities of the town devised a strategy to identify these covid-positive individuals. The strategy is to:

1) Collect saliva samples from all 1000 individuals and randomly group them into sets of 5.
2) Mix the samples within each set and test the mixed sample for covid.
3) If the test done in (ii) gives a negative result, then declare all the 5 individuals to be covid negative.
4) If the test done in (ii) gives a positive result, then all the 5 individuals are separately tested for covid.

Given this strategy, no more than testing kits will be required to identify all the 100 covid positive individuals irrespective of how they are grouped

1) 700
2) 600
3) 800
4) 1000

Solution :
Given :

Parameter	Value
Number of individuals	1000
Strenght of each group	5
Number of groups	200
Number of Covid positive individuals	100

$$Number of tests initially to examine each group = a \quad (1)$$
$$= 200 \quad (2)$$

Worst case Scenario

There will be 100 groups who will test positive(one positive in each group).
Now, for these 100 groups: We will test the 5 individuals in that group separately.

$$Number of tests in each positive group = 5 \quad (3)$$
$$(4)$$

$$Number of more tests = b \quad (5)$$
$$= 5 * 100 \quad (6)$$
$$= 500 \quad (7)$$

$$\therefore Total tests = a+b \quad (8)$$
$$= 200 + 500 \quad (9)$$
$$= 700 \quad (10)$$

So, the correct answer is option A 700.