



We know that,

$$R_{ij}^{(k)} = R_{ij}^{(k-1)} + R_{ik}^{(k-1)} \cdot (R_{kk}^{(k-1)})^* \cdot R_{kj}^{(k-1)}$$

Since $k=3$

$$R_{ij}^3 = R_{ij}^2 + R_{ik}^{(2)} (R_{kk}^{(2)})^* R_{kj}^2$$

~~Now, $\Rightarrow R_{13}^3 = R_{13}^2 + R_{12}^2 (R_{22}^2)^*$~~

~~$\Rightarrow R_{13}^3 = R_{13}^2 + R_{13}^2 (R_{33}^2)^* R_{33}^2$~~

$k=0 \Rightarrow R_{ii}^0 = \epsilon + 1 = 1^*$

$R_{12}^{(0)} = 0$

$R_{13}^0 = \phi$

$R_{21} = \phi$

$R_{22} = \epsilon$

$R_{23} = 1$

$R_{31}^0 = \phi$

$R_{32}^0 = 1$

$R_{33}^0 = \epsilon + 0 = 0^*$

$$K=1 \Rightarrow$$

$$R_{11}^1 = R_{11}^0 + R_{11}^0 (R_{11}^0)^* R_{11}^{(0)}$$

$$= (\Sigma+1) + (\Sigma+1)(\Sigma+1)^*(\Sigma+1)$$

$$= (\Sigma+1)^* = 1^*$$

$$R_{12}^1 = R_{12}^0 + R_{11}^0 (R_{11}^0)^* R_{12}^{(0)}$$

$$= 0 + (\Sigma+1)(\Sigma+1)^* \cdot 0$$

$$= (\Sigma+1)^* \cdot 0 = 1^* \cdot 0$$

$$R_{13}^1 = R_{13}^0 + R_{11}^0 (R_{11}^0)^* R_{13}^0$$

$$= \phi + (\Sigma+1)(\Sigma+1)^* \phi$$

$$= \phi + \phi$$

$$= \phi$$

$$R_{21} = R_{21}^0 + R_{21}^0 (R_{11}^0)^* R_{11}^0$$

$$= \phi + \phi (\Sigma+1)^* (\Sigma+1)$$

$$= \phi$$

$$R_{22}^1 = R_{22}^0 + R_{21}^0 (R_{11}^0)^* R_{12}^{(0)}$$

$$= \cancel{\Sigma} + \phi (\Sigma+1)^* \cdot 0$$

$$= \Sigma + \phi = \Sigma$$

$$R_{23}^1 = R_{23}^0 + R_{21}^0 (R_{11}^0)^* R_{13}^0$$

$$= 1 + \phi (\Sigma + 1)^* \phi$$

$$= 1 + \phi = 1$$

$$R_{33}^1 = R_{33}^0 + R_{31}^0 (R_{11}^0)^* R_{13}^0$$

$$= (\Sigma + 0) + \phi (\Sigma + 1)^* \phi$$

$$= \Sigma + 0 + \phi$$

$$= \Sigma + 0 = 0^*$$

$$K=2 \Rightarrow$$

$$R_{13}^2 = R_{13}^1 + R_{12}^1 (R_{22}^1)^* R_{23}^1$$

$$= \phi + (1^* \cdot 0) (\Sigma)^* \cdot 1$$

$$= \phi + 1^* \cdot 0 \cdot 1$$

$$= 1^* \cdot 0 \cdot 1$$

$$\Rightarrow R_{33}^2 = R_{33}^1 + R_{32}^1 (R_{22}^1)^* R_{23}^1$$

$$= 0^* + 1 \cdot \Sigma^* \cdot 1$$

$$= (0^* + 1 \cdot 1)$$



$$\begin{aligned} \therefore R_{13}^3 &= R_{13}^2 + R_{13}^2 (R_{33}^2)^* R_{33}^2 \\ &= (1^* \cdot 0.1) + (1^* \cdot 0) (0^* + 1.1)^* (0^* + 1.1) \\ &= (1^* \cdot 0.1) + (1^* \cdot 0) (0^* + 1.1)^* \\ &= (1^* \cdot 0.1) (0^* + 1.1)^* \\ &= (1^* \cdot 0.1) (0 + 1.1)^* \end{aligned}$$