$$M_1 = (1,0)$$
 $M_3 = (2,-2)$

$$\sum_{z} = \begin{pmatrix} z & 0 \\ 0 & 1 \end{pmatrix}$$

decisión

$$\begin{vmatrix} 5 & -1 & 0 \\ 0 & .56 \end{vmatrix} \begin{bmatrix} (1,0) - (2,2) \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & \frac{25}{14} \end{bmatrix} \begin{pmatrix} -1 \\ 2 \end{pmatrix} = \begin{pmatrix} -1 \\ \frac{25}{5} \end{pmatrix}$$

$$\begin{vmatrix} 6 & -1 \\ 0 & \frac{25}{14} \end{vmatrix} \begin{pmatrix} 1 & 0 \\ 0 & \frac{25}{14} \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} - \begin{pmatrix} 2 & -2 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ 0 & \frac{25}{14} \end{pmatrix} \begin{pmatrix} -2 \\ -2 \end{pmatrix}$$

+ 1, (==)

 $\beta_0 = \frac{1}{7} \left(1 - \frac{78}{7} \right) + 0$

501:

$$A_{5}$$
: $\lambda = -8$ $\lambda_{2} = 0$

1 S: formos
$$\hat{\Sigma}_{k} = \hat{\Sigma}$$

$$\hat{\Sigma} = \frac{k!}{\sum_{k=0}^{k-1} (X_{k} - \mathcal{A}_{k})(X_{k} - \mathcal{A}_{k})^{T}} = \frac{\sum_{k=0}^{k-1} (n_{k} - 1) \hat{\Sigma}_{k}}{n - k}$$

3
$$\log \left(\frac{f_1(x) \pi_1}{f_k(x) \pi_k} \right) = \log \left(f_1(x) \pi_1 \right) - \log \left(f_k(x) \pi_k \right)$$

$$S_{h} = -\frac{1}{2} \log (2_{1}) - \frac{1}{2} (x-n_{1})^{T} 2_{1}^{T} (x-n_{1}) + \log (\pi_{1}) + \frac{1}{2} \log (2_{h})$$

$$\left(\frac{L^{k}}{L^{1}}\right) = 106$$

+ 1 (x-Mr) (x-Mr)- log (Tr)

=- 1 ((x-n,) [2] (x-m,) - (x-n,) [2] (x-n,)

= - \frac{1}{2} \log \left(\frac{\z_1}{\z_h} \right) - \frac{1}{2} \left(\x - \mu_1 \right)^T \zeta_1^{-1} \left(\x - \mu_1 \right) - \left(\x - \mu_1 \right)^T \zeta_1^{-1} \left(\x - \mu_1 \right) + \log \left(\frac{\pi_1}{\pi_1 h} \right)



Ejercicios

$$\Sigma = \begin{pmatrix} 1 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \qquad \vdots \qquad \times \sim N_{orn} (0, \Sigma)$$

$$= 7 - \lambda - 7\lambda + \lambda^{2} - 4\lambda$$

$$= \lambda^{2} - 8\lambda + 3 = 0$$

$$= 7 - \lambda - 7\lambda + \lambda^{2} - 4$$

$$= \lambda^{2} - 8\lambda + 3 = 0$$

$$\lambda = 7.6 \qquad \lambda z = .39$$

 $\sum_{1}^{-1} = \frac{1}{3} \begin{pmatrix} 1 & -2 \\ -2 & 7 \end{pmatrix} = \begin{pmatrix} \frac{1}{2} & -\frac{2}{3} \\ -\frac{2}{3} & \frac{7}{3} \end{pmatrix}$

 $\begin{cases} \frac{1}{2} = \frac{1}{3} \begin{pmatrix} 3 & 0 \\ 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 3 \end{pmatrix}$

$$\therefore \ \): \ existe \ \ on \ \ vector$$

$$b) \ \ Sea \ \ x = (x_1, x_2)$$

 $L(x) = log \left(\frac{f_1(x) \pi_1}{f_2(x) \pi_2} \right) = log + l$

$$b = \sum_{1}^{1} (\Lambda_{1} - \Lambda_{2}) = \begin{pmatrix} \Lambda_{2} & -\frac{1}{3} \\ -\frac{1}{3} & \frac{1}{2} \end{pmatrix} \begin{pmatrix} 3 \\ -2 \end{pmatrix} = \begin{pmatrix} 1 + \frac{1}{3} \\ -2 - \frac{1}{3} \end{pmatrix} = \begin{pmatrix} \frac{7}{3} \\ -2 - \frac{1}{3} \end{pmatrix}$$

$$bo = -\frac{1}{2} \left(M_{1} \sum_{1}^{7} M_{1} - M_{2}^{7} M_{2} \right) + \log \left(\frac{\Pi_{2}^{2}}{\Pi_{1}^{2}} \right)$$

$$= -\frac{1}{2} \left(\begin{pmatrix} 1 \\ 0 \end{pmatrix} \begin{pmatrix} \Lambda_{2} & -\frac{1}{3} \\ -\frac{1}{3} & \frac{3}{3} \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} - \begin{pmatrix} -2 \\ 2 \end{pmatrix} \begin{pmatrix} \Lambda_{3} & -\frac{1}{3} \\ -\frac{1}{3} & \frac{7}{3} \end{pmatrix} \begin{pmatrix} -2 \\ 2 \end{pmatrix} \right) + \log \left(1 \right)$$

$$= \frac{47}{6}$$

(1)
$$(x, -2, x, z) = \frac{47}{6} + \frac{7}{3} = \frac{20}{3}$$
 (1) $(x, -2, x, z) = \frac{35}{6} > 0$ = 7 (2,1) se osigno o TT.

$$\begin{array}{lll} & & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ \end{array} \begin{array}{ll} & & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ & \\ & \\ \end{array} \begin{array}{ll} & \\ & \\ &$$

$$\Omega = -\frac{1}{2} \left(\begin{array}{ccc} 2 & 3 \\ 3 & 3 \end{array} \right) \left(\begin{array}{ccc} x_2 \\ x_2 \end{array} \right) = -\frac{1}{2} \left(\begin{array}{ccc} -\frac{1}{2} & -\frac{1}{3} \\ -\frac{1}{2} & 2 \end{array} \right) = \left(\begin{array}{ccc} \frac{1}{3} & \frac{1}{3} \\ \frac{1}{3} & -1 \end{array} \right)$$

$$\beta = \sum_{i=1}^{2} \Lambda_{i} - \sum_{i=1}^{2} \Lambda_{i} = \begin{pmatrix} \frac{1}{3} & -\frac{1}{3} \\ -\frac{1}{3} & \frac{3}{3} \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} - \begin{pmatrix} 1 & 0 \\ 0 & \frac{1}{3} \end{pmatrix} \begin{pmatrix} -2 \\ 2 \end{pmatrix} - \begin{pmatrix} \frac{7}{3} \\ -\frac{1}{3} \end{pmatrix}$$

$$= \sum_{1}^{3} \Lambda_{1} - \sum_{2}^{3} \Lambda_{2} = \begin{pmatrix} \frac{1}{3} & -\frac{2}{3} \\ -\frac{1}{3} & \frac{3}{3} \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} - \begin{pmatrix} 1 & 0 \\ 0 & \frac{1}{3} \end{pmatrix} \begin{pmatrix} -2 \\ 2 \end{pmatrix} - \begin{pmatrix} \frac{1}{3} & \frac{1}{3} \\ -\frac{1}{3} & \frac{3}{3} \end{pmatrix}$$

$$= \frac{1}{2} \begin{pmatrix} \log (1) + (10) + 10 & \begin{pmatrix} \frac{1}{3} & -\frac{2}{3} \\ -\frac{2}{3} & \frac{3}{3} \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} - (-2 & 2) & \begin{pmatrix} 1 & 0 \\ 0 & \frac{1}{3} \end{pmatrix} \begin{pmatrix} -2 \\ 2 \end{pmatrix} \end{pmatrix}$$

$$= \frac{1}{2} \left(\log (1) + (10) + 10 \left(\frac{1}{3} - \frac{2}{3} \right) \begin{pmatrix} 1 \\ 0 \end{pmatrix} - (-2 \ z) \left(\frac{1}{3} - \frac{2}{3} \right) \right)$$

$$= \frac{5}{2}$$

$$\beta_0 = \frac{1}{Z} \left(\log (1) + (10) + 10 \left(\frac{1}{3} - \frac{2}{3} \right) / (1) - (-2 z) / (1 0) / (2) \right) - \log (1)$$

$$= \frac{5}{Z}$$

$$C) Q(X_1 = 2, X_2 = 1)$$

$$\beta_{0} = \frac{1}{Z} \left(\log (1) + (10) + 10 \left(\frac{1}{3} - \frac{2}{3} \right) \left(\frac{1}{3} \right) - (-2 z) \left(\frac{1}{3} - \frac{2}{3} \right) \right) - \log z$$

$$= \frac{5}{Z}$$

$$C) Q(X_{1}=2, X_{2}=1)$$

$$= \frac{5}{2}$$
c) $Q(x_1=2, x_2=1)$

$$= \frac{1}{2}$$
c) $Q(x_{1}=2, x_{2}=1)$

$$= \frac{5}{2} + (\frac{7}{3} - \frac{1}{3}) / (\frac{2}{3}) + (\frac{1}{3}) / (\frac{1}$$

e)
$$Q(x_1=2, x_2=1)$$

= $\frac{5}{2} + (\frac{7}{3} - \frac{4}{3})(\frac{7}{1}) + (\frac{7}{3} - \frac{7}{3})(\frac{7}{1})$

e)
$$Q(x_{1}=2, x_{2}=1)$$

= $\frac{5}{2} + (\frac{7}{3} - \frac{4}{3})(\frac{7}{1}) + (\frac{1}{3} - \frac{1}{3})(\frac{7}{1})$

e)
$$Q(x_{1}=2, x_{2}=1)$$

$$= \frac{5}{2} + (\frac{7}{3} - \frac{1}{3})(\frac{2}{1}) + (\frac{1}{3} - \frac{1}{3})(\frac{2}{1})$$

$$= \frac{15}{2} + (\frac{7}{3} - \frac{1}{3})(\frac{2}{1}) + (\frac{1}{3} - \frac{1}{3})(\frac{2}{1})$$

$$= \frac{5}{2} + \left(\frac{7}{3} - \frac{1}{3}\right) \begin{pmatrix} 2 \\ 1 \end{pmatrix} + \left(2 + 1\right) \begin{pmatrix} \frac{1}{3} & \frac{1}{3} \\ \frac{1}{3} & -1 \end{pmatrix} \begin{pmatrix} 2 \\ 1 \end{pmatrix}$$

$$= 15$$

$$= \frac{15}{2} > 0$$

$$= \frac{15}{2} > 0$$

$$\therefore \text{ Se assigna } (2, 1) \text{ a } \Pi_1$$

$$z^{-1} = \frac{1}{49} \begin{pmatrix} 5 & -1 \\ -1 & 10 \end{pmatrix}$$
 def $|z| = 49$

$$\tilde{z}_{i} = \begin{pmatrix} 1 \\ 3 \\ 0 \end{pmatrix} \qquad def \left[\tilde{z}_{i} \right] = 12$$

$$\Sigma_{3}^{-1} = \frac{1}{21.75} \begin{pmatrix} u & -1.5 \\ -1.5 & 6 \end{pmatrix}$$
 $\Delta_{c} + |\Sigma_{3}| = 21.75$

$$\sum_{3} = \frac{1}{21.75} \left(-1.5 \quad 6 \right) \quad det \quad \left(\sum_{3} | = 21.75 \right)$$

$$b_0 = -\frac{1}{2} \left(\log \left(\frac{u_1 q}{12} \right) + (-u_1 u_1) \frac{1}{u_1 q} \left(\frac{5}{-1} \right) (-u_1 u_1) - (3, -3) \left(\frac{1}{3} \frac{0}{0} \right) (3, -3) \right)$$

- lag ((3,-3)

$$\frac{1}{1.75}\begin{pmatrix} u & -1.5 \\ -1.5 & 6 \end{pmatrix} \qquad d_{c} + |\mathcal{E}_{3}| = 21.$$

$$\frac{2}{3} = \frac{1}{21.75} \left(-1.5 + 6 \right)$$
 det $\left(\frac{2}{3} \right) = 21.7$

	5-6	-	
2			