

**Definition 0.1.** *If  $f_1 : \Sigma_1^* \rightarrow L$  and  $f_2 : \Sigma_2^* \rightarrow L$  are proof systems for  $L$ , then  $f_2$  p-simulates  $f_1$  provided there is a function  $g : \Sigma_1^* \rightarrow \Sigma_2^*$  such that  $f_2(g(x)) = f_1(x)$  for all  $x$ .*

It's easy to show that p-simulation is a transitive reflexive relation, so that its symmetric closure is an equivalence relation. If we require the function  $g$  is bounded in length by a polynomial in the length of its argument and a proof system  $f_2$  for  $L$  p-simulates a polynomially bounded proof system  $f_1$  for  $L$ , then  $f_2$  is also polynomially bounded.