

Automata on Infinite Structure
Fall 2018

Exercice Sheet 11

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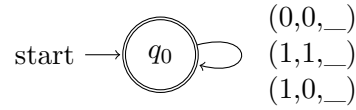
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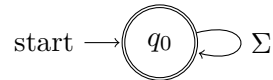
Exercise 1

$$\begin{aligned} \exists x.(x \in Q_a \wedge x + 1 \in Q_b) &= \\ \exists x.(x \in X_0 \wedge \neg(x + 1 \in X_0)) &= \\ \exists X_1.(\text{sing}(X_1) \wedge X_1 \subseteq X_0 \wedge \exists X_2.(\text{sing}(X_2) \wedge \text{succ}(X_1, X_2) \wedge \neg(X_2 \subseteq X_0))) &= \\ \exists X_1.\exists X_2.(X_1 \subseteq X_0 \wedge \neg(X_2 \subseteq X_0) \wedge \text{succ}(X_1, X_2)) \end{aligned}$$

Automata for $X_1 \subseteq X_0$



Automata for $\neg(X_2 \subseteq X_0)$



Automata for $\text{succ}(X_1, X_2)$

