

ML

* Example with Data:

House Size (x)	Rent (y)
800	1.5
1200	2.0
1500	2.5
1800	3.0

Ans:

Step-1 : Min-Max Normalization:

formula:

$$x' = \frac{x - \min(x)}{\max(x) - \min(x)}$$

$$y' = \frac{y - \min(y)}{\max(y) - \min(y)}$$

∴ Applying Normalization:

Original x	Normalized x'
800	$\frac{800-800}{1800-800} = 0$
1200	$\frac{1200-800}{1800-800} = 0.4$
1500	$\frac{1500-800}{1800-800} = 0.7$
1800	$\frac{1800-800}{1800-800} = 1$

Original y	Normalized y'
1.5	$\frac{1.5-1.5}{3.0-1.5} = 0$
2.0	$\frac{2.0-1.5}{3.0-1.5} = 0.3333$
2.5	$\frac{2.5-1.5}{3.0-1.5} = 0.6667$
3.0	$\frac{3.0-1.5}{3.0-1.5} = 1$

Step 2:* Initialize Parameters:We start with: $w=0, b=0, \alpha=0.3$ Step 3: Compute Predictions:

$$\hat{y} = w\vec{x} + b$$

Initially all predictions are,

$$\hat{y} = 0\vec{x} + 0 = 0$$

Step 4: Compute Loss (MSE) :- mean Squared Error

$$J = \frac{1}{n} \sum_{i=1}^n (\hat{y}_i - y_i)^2$$

$$= \frac{1}{4} [(0-0)^2 + (0-0.3333)^2 + (0-0.6667)^2 + (0-1)^2]$$

$$= 0.3889$$

Step 5: Compute Gradients:

$$\frac{\partial J}{\partial w} = -\frac{2}{n} \sum_{i=1}^n (x_i'(y_i - \hat{y}_i))$$

$$\frac{\partial J}{\partial b} = -\frac{2}{n} \sum_{i=1}^n (y_i - \hat{y}_i)$$

Evaluating the gradient with respect to w:

$$\frac{\partial J}{\partial w} = -\frac{2}{4} [0(0-0) + 0.4(0.3333-0) + 0.7(0.6667-0) + 1(1-0)]$$

$$= -0.8$$

$$= -0.8$$

Evaluating the gradient with respect to b:

$$\frac{\partial J}{\partial b} = -\frac{2}{4} [0(0-0) + (0.3333-0) + (0.6667-0) + (1-0)]$$

$$= -1$$

Step-6: Update Parameters

(cont)

$$w = w - \alpha \frac{\partial J}{\partial w}$$

$$= 0 - (0.3x - 0.8) = 0.24$$

$$b = b - \alpha \frac{\partial J}{\partial b}$$

$$= 0 - (0.3x - 1) = 0.3$$

Step-7: Compute New Predictions

The new predictions are:

$$\hat{y} = 0.24x + 0.3$$

\hat{x}	\hat{y}
0	0.3
0.4	0.396
0.7	0.468
1.0	0.54

Actual Data
Predicted Data
 \hat{y} value

Step-8:

The new loss is:

$$J = \frac{1}{n} \sum_{i=1}^n (\hat{y}_i - y_i)^2$$

$$= \frac{1}{4} [(0.3 - 0)^2 + (0.396 - 0.333)^2 + (0.468 - 0.6667)^2 + (0.54 - 1)^2]$$

$$= 0.0863$$

Lecture 5

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Assessing Model Performance

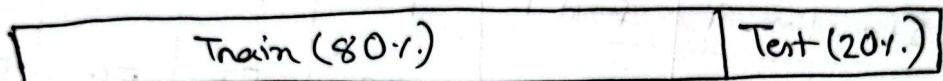
Holdout Validation

* Split the Dataset into two parts - Training set & a test set

■ Training Data: Data the model was trained on.

■ Test Data : Data the model has not seen before.

Typically, with a split ratio of 70:30 or 80:20



K-Fold Cross Validation

K-Fold cross Validation is a method to check how well a machine performs. Instead of using just one train test split, it divides the dataset into K parts (folds).

How it works:

1. The dataset is split into equal K parts (folds).
2. The model is trained K times, each time using K-1 fold for training and 1 fold for testing.
3. Each fold gets a chance to be the test set once.
4. The final performance is the average of all K test results.

5 Fold Cross Validation

Iteration 1	Fold 1	F2	F3	F4	F5
Iteration 2	Fold 1	F2	F3	F4	F5
Iteration 3	Fold 1	F2	F3	F4	F5
Iteration 4	Fold 1	F2	F3	F4	F5
Iteration 5	Fold 1	F2	F3	F4	F5

Confusion Matrix

TP (True Positive): Correctly Predicted positive case.

TN (True Negative): n n Negative Case.

FP (False Positive): Incorrectly n Positive Case

FN (False Negative): n n Negative n .

Negative \rightarrow 0

Positive \rightarrow 1

1 - Positive
0 - Negative

Date:

Instance	1	2	3	4	5	6	7	8	9	10	11	12
Actual Classification	1	1	1	1	1	1	1	1	0	0	0	0
Predicted Classification	0	0	1	1	1	1	1	1	1	0	0	0
Result	FN	FN	TP	TP	TP	TP	TP	TP	FP	TN	TN	TN

True
False
True/
False
Positive/
Negative

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Q
S A N
C B O M
T F Y - m

Fit
Unfit
Y ~ 3
X

		Predicted Condition	
		Positive (P)	Negative (PN)
Actual Condition	Total Population P+N	True Positive	FN
	Negative (N)	FP	TN

		Prediction Condition	
		Fit = 4	Unfit = 5
Actual Condition	Total Fit = 8 = 12	6	2
	Unfit = 4	1	3

$$\text{Accuracy} = \frac{TP + TN}{TP + TN + FP + FN} = \frac{6+3}{6+3+1+2} = 0.75 = 75\%$$

$$\text{Precision} = \frac{TP}{TP + FP} = \frac{6}{6+1} = \frac{0.857}{0.857} = 85.7\%$$

$$\text{Sensitivity/Recall} = \frac{TP}{TP + FN} = \frac{6}{6+2} = 0.75 = 75\%$$

$$\text{Specificity} = \frac{TN}{TN + FP} = \frac{3}{3+1} = 0.75 = 75\%$$

∴ F-measure/F-score,

$$F_1 = \frac{2 \times (\text{Precision} \times \text{Recall})}{(\text{Precision} + \text{Recall})}$$

$$= \frac{2(0.857 \times 0.75)}{(0.857 + 0.75)} = 0.80 = 80\%$$

Supervised Learning

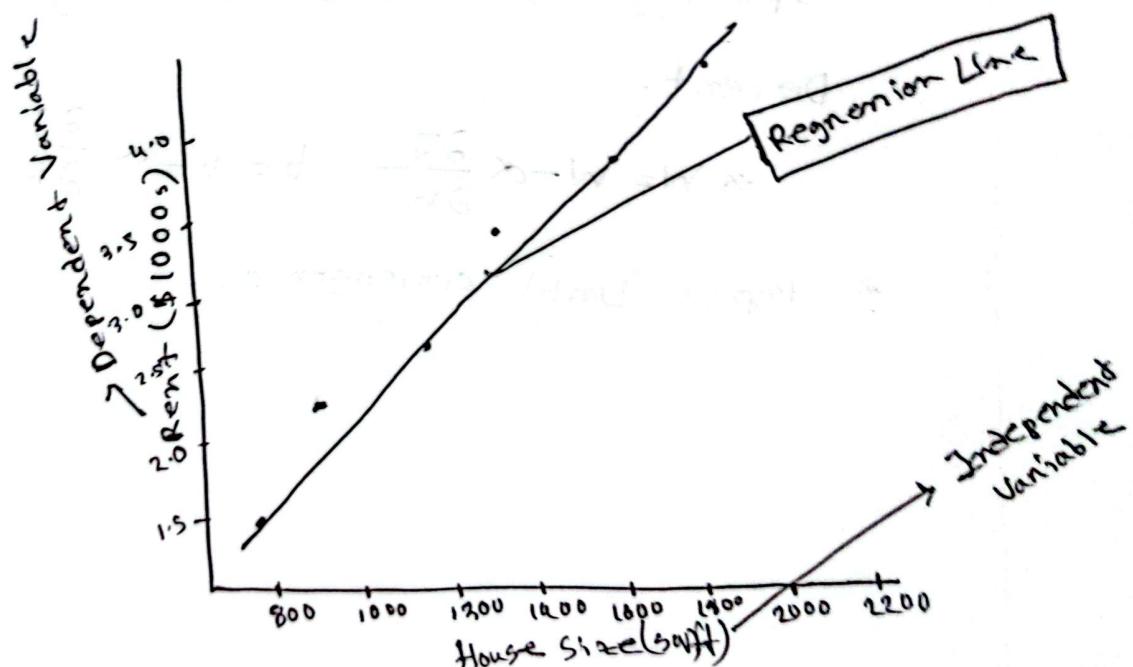
Linear Regression

Linear Regression is a basic technique in machine learning used for predicting continuous values. (price, temperature or sales).

~~How it~~ It helps understand the relationship between input and output variables using straight line.

Dependent Variable (Label): The value we want to predict (e.g., house rent)

Independent Variable (Feature): The Input used for prediction.



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Mathematics Behind Linear Regression

■ Hypothesis function: $\hat{y} = WX + b$

■ Cost function: Mean Squared Error $J(w, b) = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$

Linear Regression Algorithm

- * Initialize weight (w), bias (b), and learning rate (α)
- * Compute the predicted values \hat{y}
- * Compute the loss using Mean Squared Error (MSE).
- * Update weight and bias using Gradient Descent.

$$w = w - \alpha \frac{\partial J}{\partial w}, b = b - \alpha \frac{\partial J}{\partial b}$$

- * Repeat Until convergence.

Multiple Linear Regression

It uses two or more independent variables (predicting rent based on house size and location).

* The formulation: $\hat{y} = w_0 + w_1x_1 + w_2x_2 + \dots + w_px_p + b$

* Gradient Descent for Multiple Linear Regression

$$w_i = w_i - \alpha \frac{\partial J}{\partial w_i}, \quad b = b - \alpha \frac{\partial J}{\partial b}$$

Pros:

- * Simple model
- * Computationally efficient
- * Interpretability of the Output

Cons:

- * Overly-Simplistic
- * Linearity Assumption
- * Severely affected by Outliers.

Polynomial Regression

Polynomial Regression is used when the relationship between variables is not a straight line but a curve.

- It fits an nth-degree polynomial equation to the data.

Example: Instead of a straight line, we fit a curve to better match the data points.

Types of Polynomial Regression:

- * Linear (degree = 1) → straight line
- Quadratic (degree = 2) → U-shaped curve
- Cubic (degree = 3) → S-shaped curve

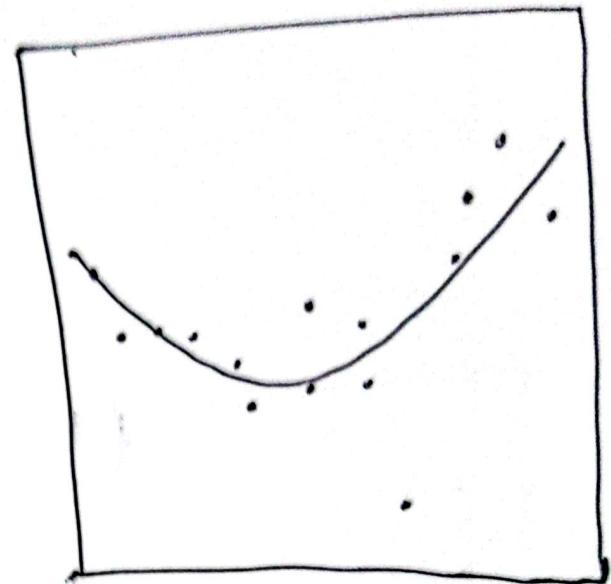
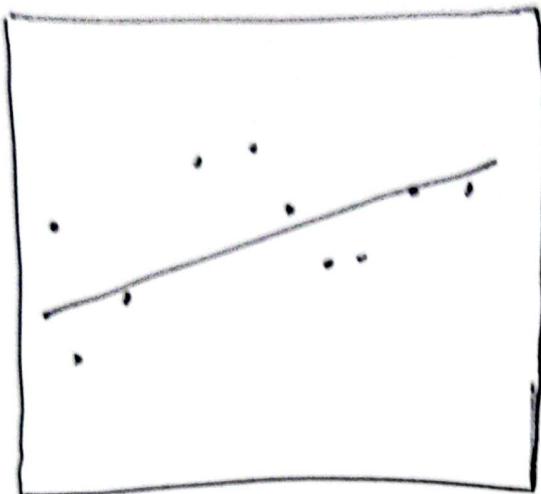
Pros:

- can model more complex relationships.
- Works well when a straight line doesn't fit.

Cons:

- Very sensitive to Outliers (one bad value can affect the curve)

Why Polynomial Regression



Linear Regression

- * Continuous Values, $f(x)$, $x \in \mathbb{R}$, $y \in \mathbb{R}$.
- * n independent (x) dependent variable (y) $\xrightarrow{\text{(label)}}$ y from x .
- * It can be multivariate linear regression.
- * Mathematic Behind Linear Regression

linear equation $y = mx + c$

ML \rightarrow ML \rightarrow Hypothesis function.

x	y
1	2
3	4
2	

True
value
 \rightarrow data
set
already come

Suppose, $y = 2x + 4$

to find,

$$y = 2x + 4$$

$$= 8$$

$\therefore y = 8 \rightarrow$ value \hat{y} = Predicted Value

\therefore Mean Squared Error (MSE) $= J(W, b) = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$

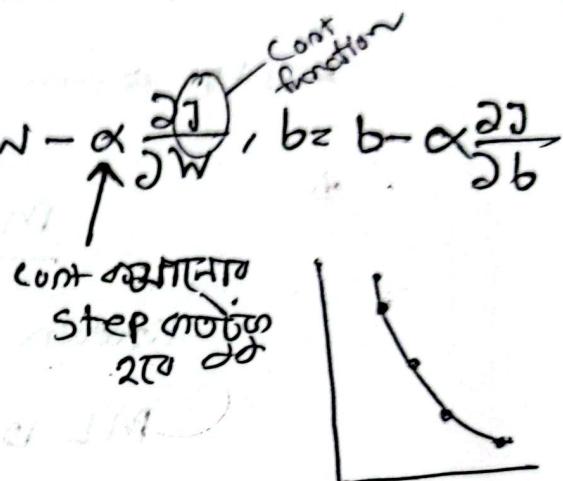
$(\text{real value} - \text{predicted value})^2$

Linear Regression Algorithm

Hence, $y = Wx + b$

- * Gradient Descent ප්‍රාග්ධනයෙන් සාර්ථක, Cont ගෘහනය රාජ්‍යී ගුණ තුළ,
 - * Cont ගෘහනය Step: $w = w - \alpha \frac{\partial J}{\partial w}$, $b = b - \alpha \frac{\partial J}{\partial b}$

ഉള്ളട പര്യന്ത Gradient
 Descent പു; സാധിക്കും Cont
 കമ്മാന്നു പുതെ ചുരുക്ക + പര്യന്ത
 convergence രീതി



Multiple linear Regression

formula: $\hat{y} = w_0 + w_1 x_1 + w_2 x_2 + \dots + w_p x_p + b$

- Gradient descent for multiple L.R:

$$w_i = w_i - \alpha \frac{\partial J}{\partial w}, \quad b = b - \alpha \frac{\partial J}{\partial b}$$

Pros and Cons of Linear Regression

Pros:

- ▢ Simple model.
- ▢ Computationally efficient
- ▢ Interpretability of the Output

Cons

- ▢ Only-Simplistic
- ▢ Linearity Assumption
- ▢ Severely affected by Outliers.

Gradient vector

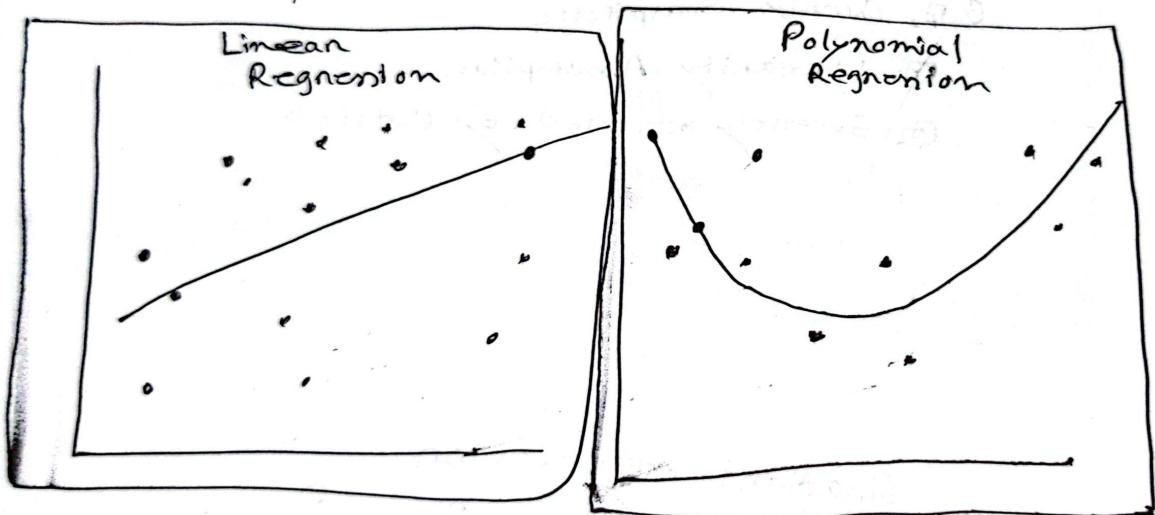
$$\vec{\nabla} f(x) = \vec{g} = g_1^{\hat{i}} + g_2^{\hat{j}}$$

$$\|g\| = \sqrt{g_1^2 + g_2^2}$$

Polynomial Regression

(ii) It describes the relationship between the independent variable x and the dependent variable y using an n th degree polynomial in x .

Hence, polynomial equation is: $a_0 + a_1x + a_2x^2 + a_3x^3$



Why Polynomial Regression:
not enough or too much