

Generate the Gaussian distributed datasets

Assignment requirement:

https://docs.wixstatic.com/ugd/33750e_84919aa1813c45fb89a4250e17edd18f.pdf

1. Define mean vector, we set all the mean=0

```
1 def zero_mean(dim):
2     mean = np.zeros([dim])
3     return mean
```

2. Generate the covariance matrix

- p: unit variance
- dim: dimensionality

```
1 def covariance_matrix(p, dim):
2     cov = np.zeros([dim, dim])
3     for i in range(dim):      #first, generate the upper triangular matrix
4
5         cnt = 0
6         for j in range(i, dim):
7             if(i==j):
8                 cov[i][j] = 1
9             else:
10                cov[i][j] = pow(p, cnt+1)
11                cnt = cnt + 1
12
13     cov = cov + cov.T - np.diag(cov.diagonal()) #upper triangular to symmetric matrix
14     return cov
```

3. Generate gaussian distribution based on the zero mean vector and covariance matrix we created.

- mean: mean vector
- cov: covariance matrix
- sampleNo: #samples
- dim: dimensionality

```
1 def gauss_distribution(mean, cov, sampleNo, dim):
2     [eigenvalues, eigenvectors] = np.linalg.eig(cov)
3     # l = np.matrix(np.diag(np.sqrt(eigenvalues)))
4     # print(l)
```

```

5     R = cholesky(cov)
6     s = np.dot(np.random.randn(sampleNo, dim), R) + mean
7     return s

```

4. plot the result of the gaussian distribution

```

1 def node_plot(s):
2     plt.plot()
3     plt.plot(s[:,0],s[:,1],'+')
4     plt.show()
5
6 def histogram(s):
7     plt.plot()
8     plt.hist(s[:,1], bins='auto') # arguments are passed to np.histogram
9     plt.show()

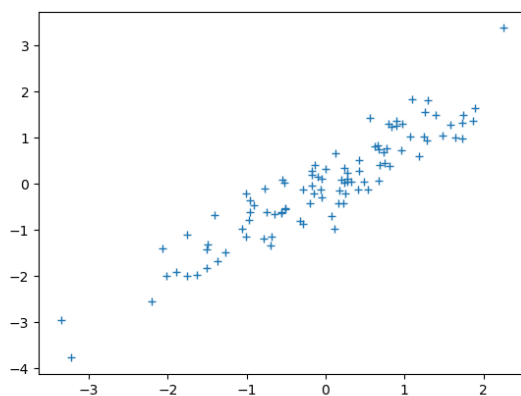
```

Output:

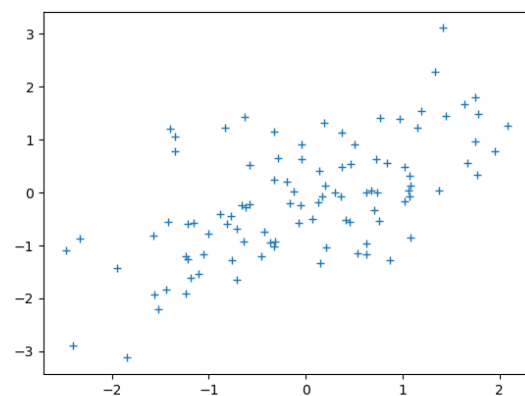
Two Gaussian distributed classes in which the dimensionality is $n = 20$ and each class has 100 samples.

Class 1 : unit variance = 0.9

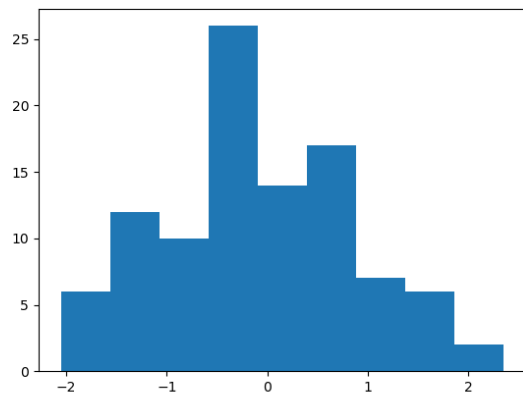
Class 2 : unit variance = 0.5



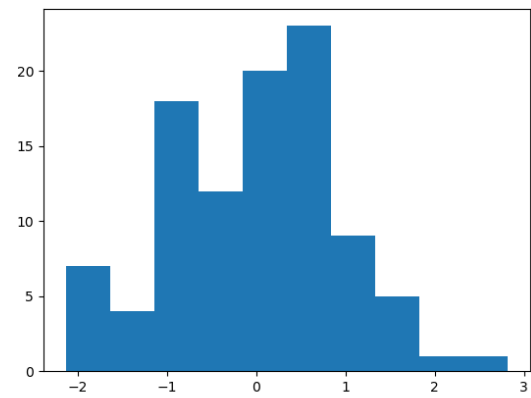
Class 1



Class 2



Class 1



Class 2

The code is on: https://github.com/SnoopyKnight/gaussian_disturbition

Reference:

- https://en.wikipedia.org/wiki/Normal_distribution
- <https://docs.scipy.org/>
- <https://matplotlib.org/>