

# Data Analytics Application Series I: Wind Energy Part II

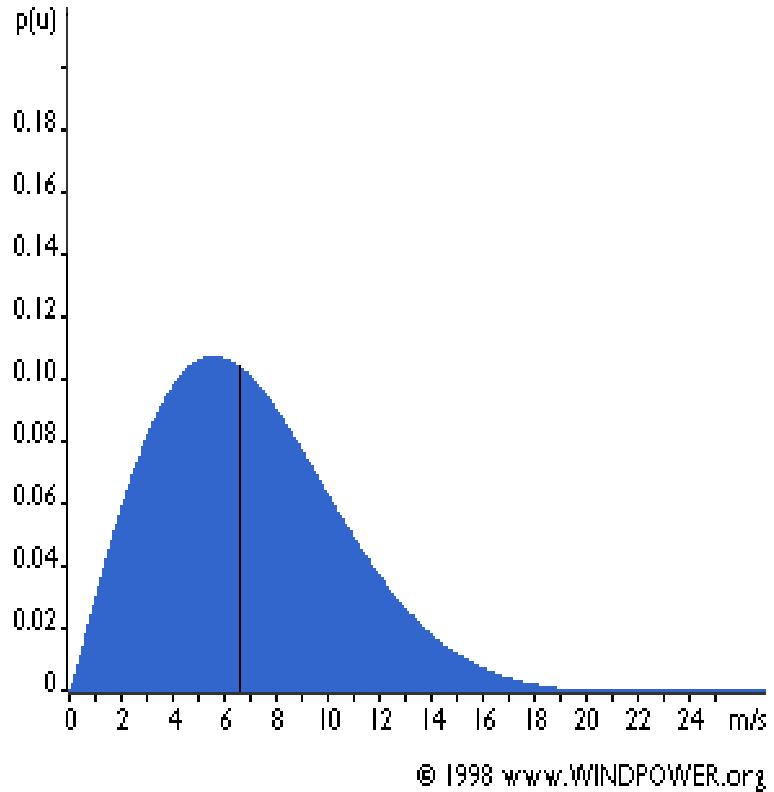
Zijun Zhang

Parts of contents from Prof. Andrew Kusiak's wind power course

# Characterizing Wind Variations

- ✓ Characterization of the **variation of wind speed** of importance to the wind industry
- ✓ **Designers** use it to optimize the design of the turbines, e.g., by **minimizing the energy generation cost**
- ✓ **Wind farm designers** use it to locate wind farms and select turbines
- ✓ **Investors** use it to estimate the income from electricity generation

# Wind Variations: Weibull Distribution



## The General Pattern of Wind Speed Variations

- ✓ Weibull distribution describes the wind variation for a typical site
- ✓ The site has the mean wind speed of 7 m/s
- ✓ The shape parameter of the function is  $k = 2$
- ✓ The data has been collected over a year period

# Weibull Distribution

$$f(x; k, \lambda) = \frac{k}{\lambda} \left(\frac{x}{\lambda}\right)^{k-1} e^{-(x/\lambda)^k}$$

where:

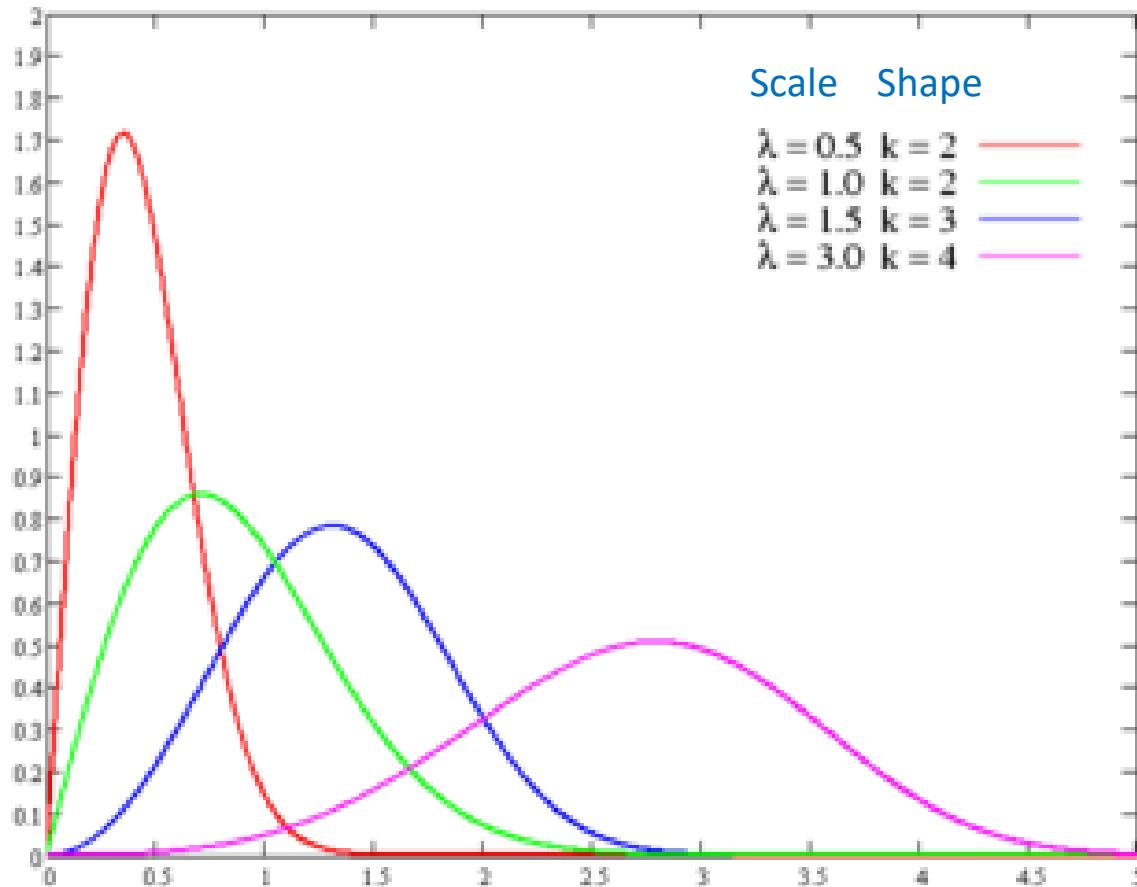
$\lambda > 0$  is the **scale** parameter

$k > 0$  is the **shape** parameter of the distribution

For  $k = 3.4$ , the Weibull distribution appears similar to the normal distribution

For  $k = 1$ , the Weibull distribution becomes the exponential distribution

# Weibull Distribution



$$f(x; k, \lambda) = \frac{k}{\lambda} \left(\frac{x}{\lambda}\right)^{k-1} e^{-(x/\lambda)^k}$$

Median

$$\lambda \ln(2)^{1/k}$$

Mode

$$\lambda \left(\frac{k-1}{k}\right)^{\frac{1}{k}}$$

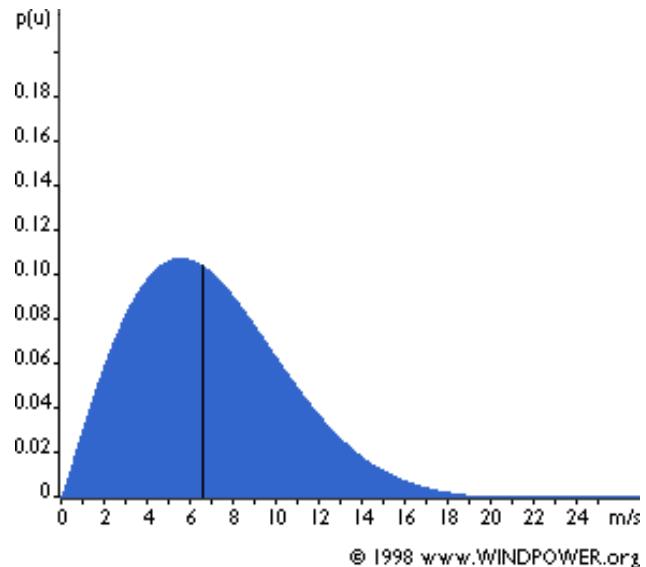
Mean

$$\lambda \Gamma\left(1 + \frac{1}{k}\right)$$

where the gamma function is

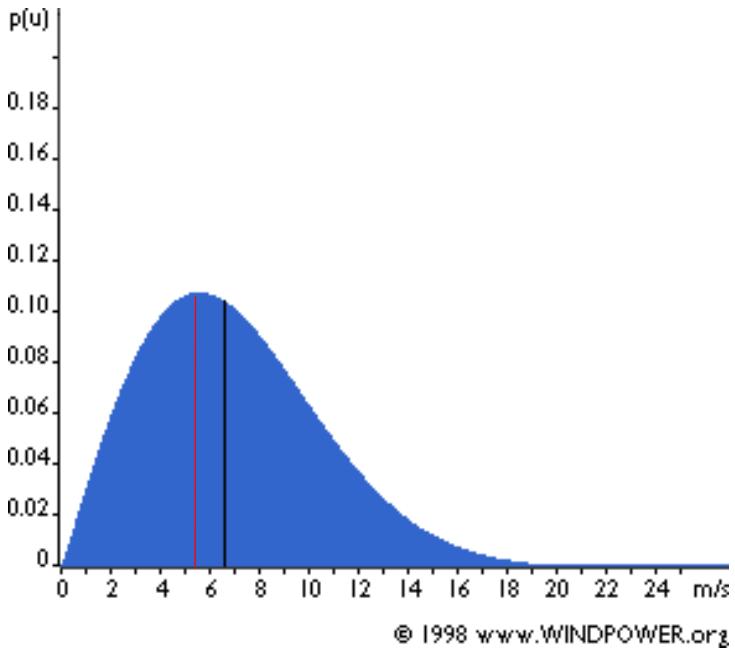
$$\Gamma(z) = \int_0^\infty t^{z-1} e^{-t} dt$$

# Description of Wind Speeds

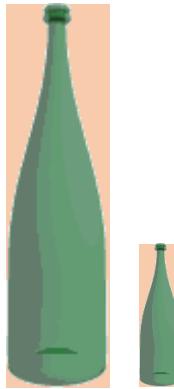


- ✓ The area under the pdf curve is always exactly 1 (the **probability** that the wind is blowing at some wind speed including 0 is 100 %)
- ✓ Median = 6.6 m/s (Half of the blue area is to the left)
- ✓ This means that 50% of the time the wind speed is less than 6.6 m/s, the other 50% of the time it is greater than 6.6 m/s
- ✓ Note: The median 6.6 m/s is not equal the mean 7m/s due to asymmetry of the pdf

# Description of Wind Speeds



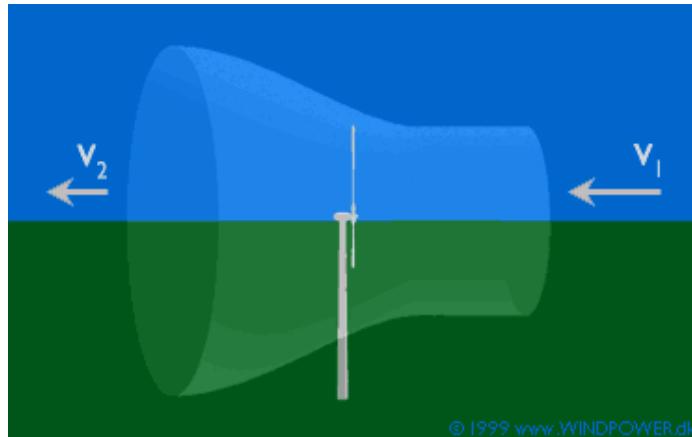
- ✓ Mode = 5.5 m/s (The **most common wind speed**)
- ✓ The statistical distribution of wind speeds depends on location climate conditions, the landscape, and its surface
- ✓ The Weibull distribution may thus vary in its shape, determined by the pdf parameters



# The Average Bottle Fallacy

- ✓ The **average energy content** of the wind at a turbine site **can not** be determined from the **average wind speed**, rather the **Weibull distribution** is needed
- ✓ How large (in volume) is the average bottle, one is 0.24m and the other is 0.76m tall and both are of same shape?
- ✓ Though one is only only 3.17 taller than the other, its volume is actually  $3.17^3 = 32$  times larger than the small bottle (bottle V = cube of its size)

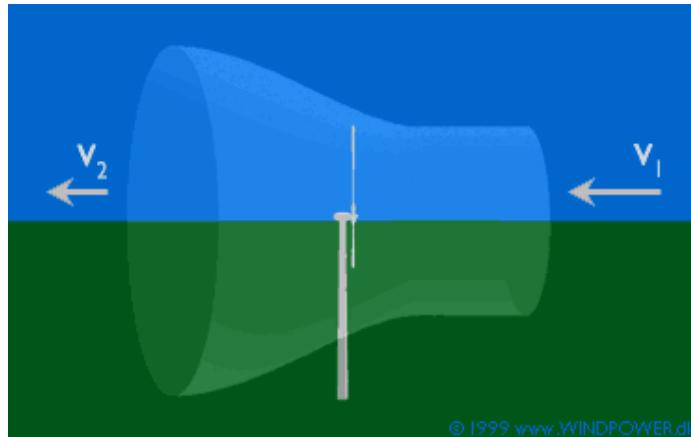
# Betz' Law



## The Ideal Braking of the Wind

- ✓ The **more kinetic energy** a wind turbine extracts from the **wind**, the **more the wind will be slowed down** (as it leaves the left side of the turbine in the tunnel)

- ✓ An attempt to extract **all the energy from the wind**, would reduce the **speed to zero**, i.e., the air could not leave the turbine
- ✓ In that case we would not extract any energy at all, as the **new air** would obviously **be prevented from entering the rotor** of the turbine
- ✓ Passing air without speed change would lead to zero extracted energy



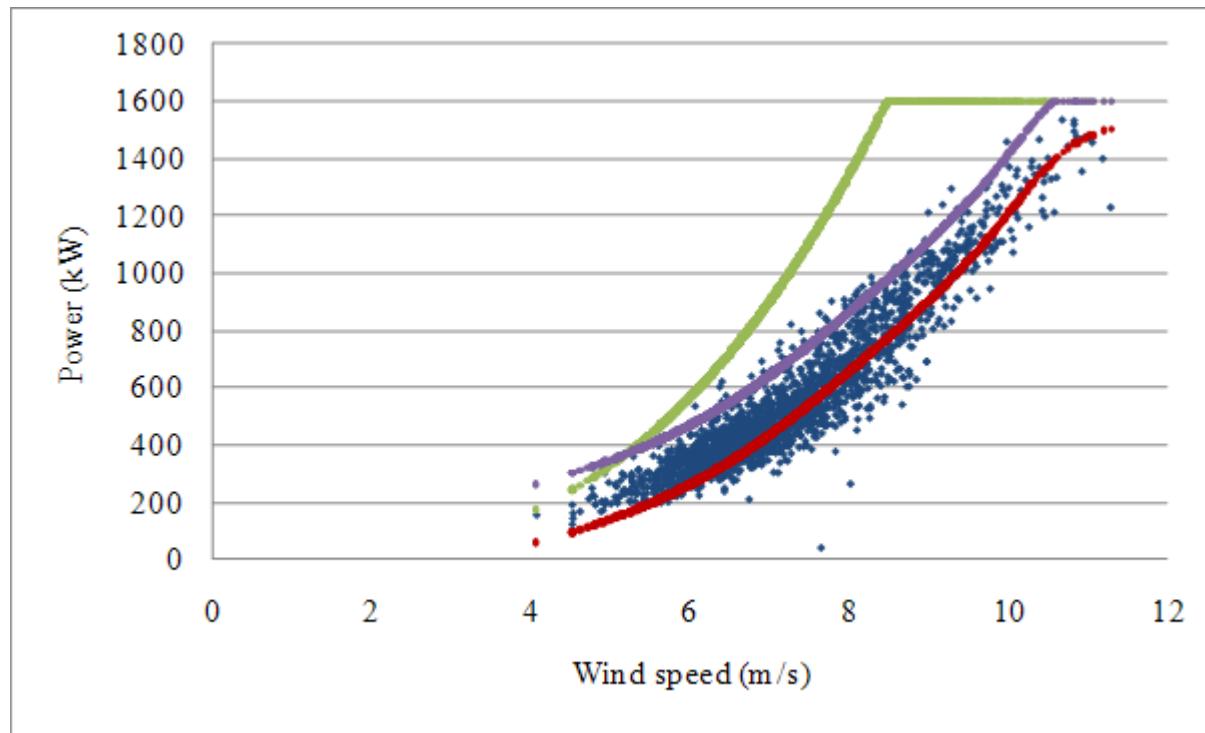
# Betz' Law

- ✓ The optimal point is: An ideal wind turbine slows down the wind by 2/3 of its original speed ( $v_2 = 1/3v_1$ )

- ✓ Betz' law (Year 1919) says that one can only convert not more than  $16/27$  (or 59%) of the kinetic energy in the wind to mechanical energy using a wind turbine.  
(Albert Betz, German Physicist)

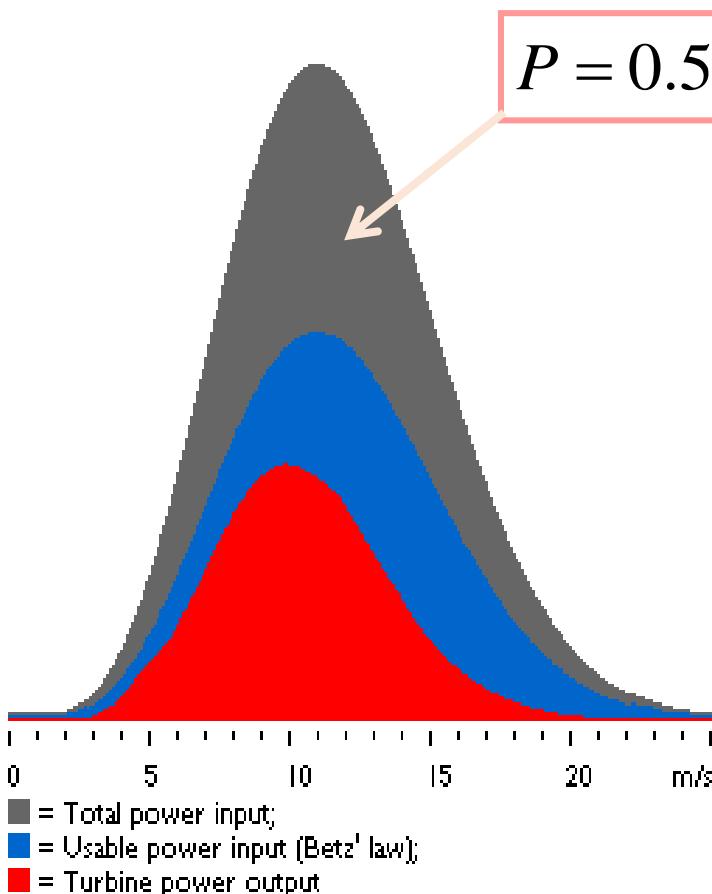
Modern rotors achieve values of the coefficient of performance  $C_p = 0.4 - 0.5$ , which is 70% to 80% of the theoretically possible value of  $C_{p\max} = 0.59$

# Drawback of Betz' Law



The green line is the power optimization boundary estimated based on Betz' Law

# Power Density Function



$$P = 0.5 \times \rho \times A \times v^3$$

The Power of the Wind

- ✓ The area under the **blue curve** shows theoretical power that can be extracted (Betz' law says, **16/27 of the total power** in the wind)
- ✓ The total area under the **red curve** represents the electrical power a certain **wind turbine could produce**
- ✓ Turbine's **power curve** determines the actual power produced

$$E = E_{rot} \times E_{ger} \times E_{gen} \times E_{p-conv}$$

where:  $E$  = Wind Turbine System Efficiency  
=  $E_{Rotor} \times E_{Gearbox} \times E_{Generator} \times E_{PowerConverter}$

# Wind Turbine Modeling

Majorly talk about modeling wind power conversion process.

There are a number of ways for modeling the wind power conversion process:

- Computational Fluid Dynamics (More for design stage)
- Power Curve Model (Easy to compute)
- Data-driven Model (For tracking real dynamics in operations)

# Computational Fluid Dynamics Model



Aerodynamics Model

$$P_a = \frac{1}{2} \rho \pi R^2 C_p(\lambda, \beta) v^3$$

$$\lambda = \frac{\omega_r R}{v}$$

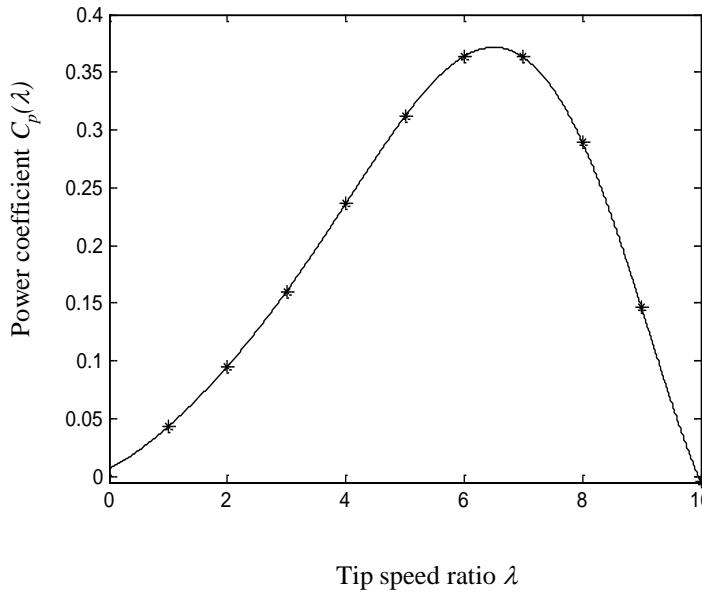
Tip-speed ratio

# Mechanical Power: Summary 1

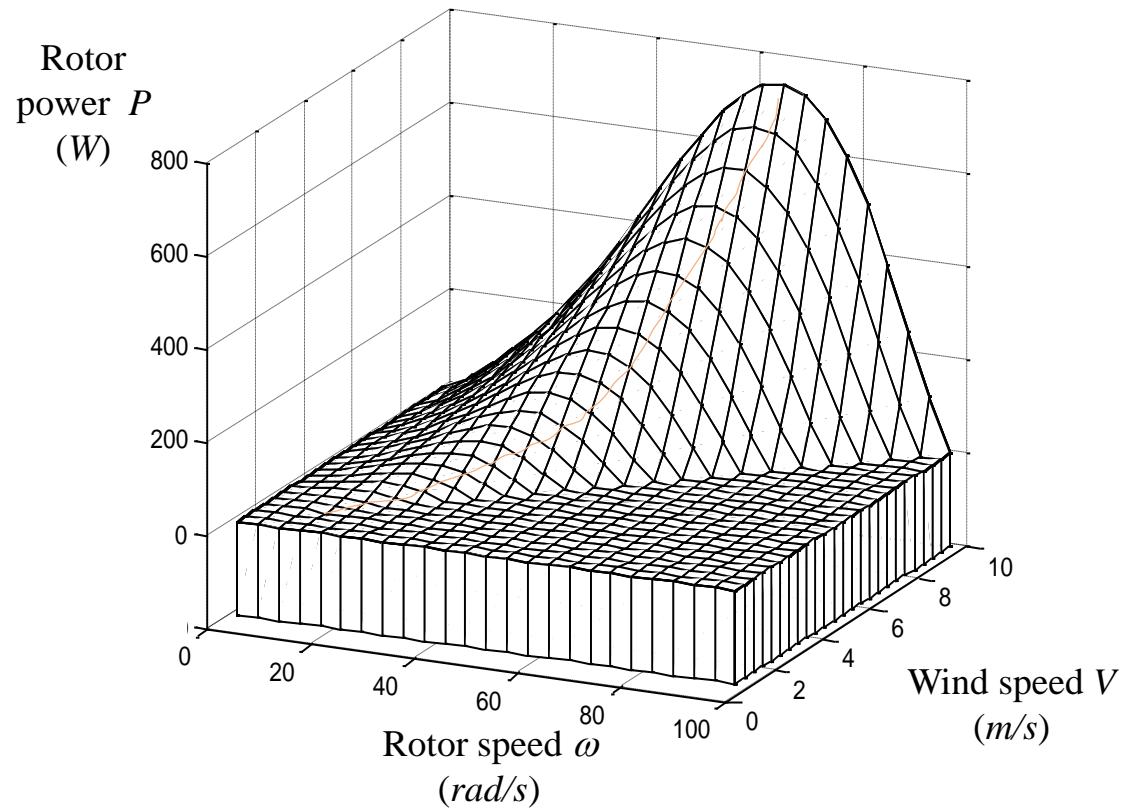
$$P = \frac{1}{2} \rho A C_p(\lambda) V^3$$

$$\lambda = \frac{r \omega}{V}$$

- $P$  Mechanical power produced by the rotor  
 $\rho$  Air density  
 $A$  Rotor swept area  
 $V$  Wind speed  
 $\lambda$  Tip speed ratio  
 $C_p$  Power coefficient  
 $r$  Rotor radius  
 $\omega$  Rotor speed



# Mechanical Power: Summary 2



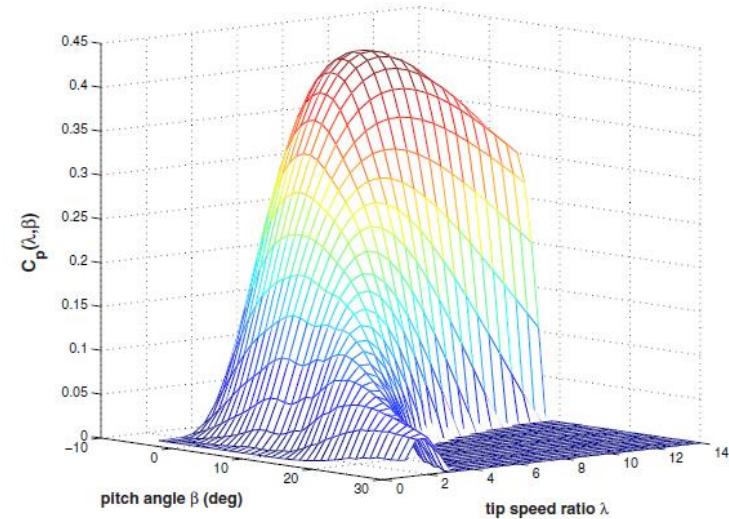
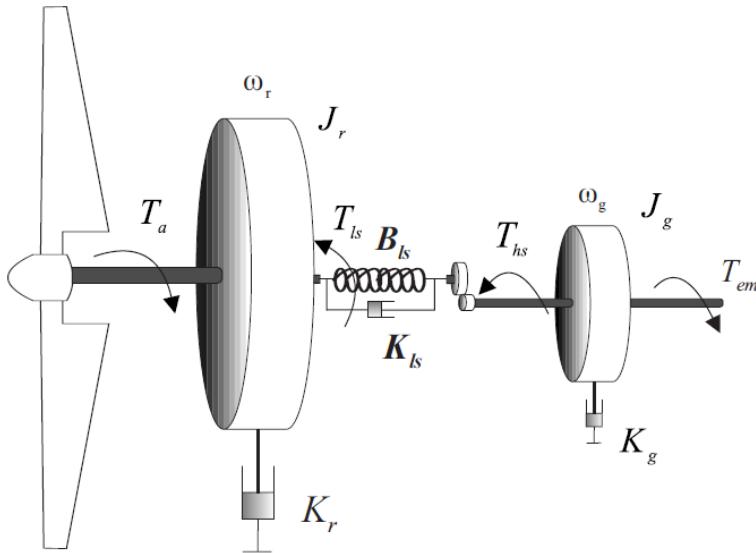
# Summary 3

- ✓ It is important to notice is that the bulk of wind energy is extracted at wind speeds above the average wind speed
- ✓ This is due to the fact that the energy content of high wind speeds is much higher than energy content of low wind speeds
- ✓ Basically, the non-linear (cube) relationship between the power and wind speed

$$P = 0.5 \times \rho \times A \times v^3$$

# Computational Fluid Dynamics Model

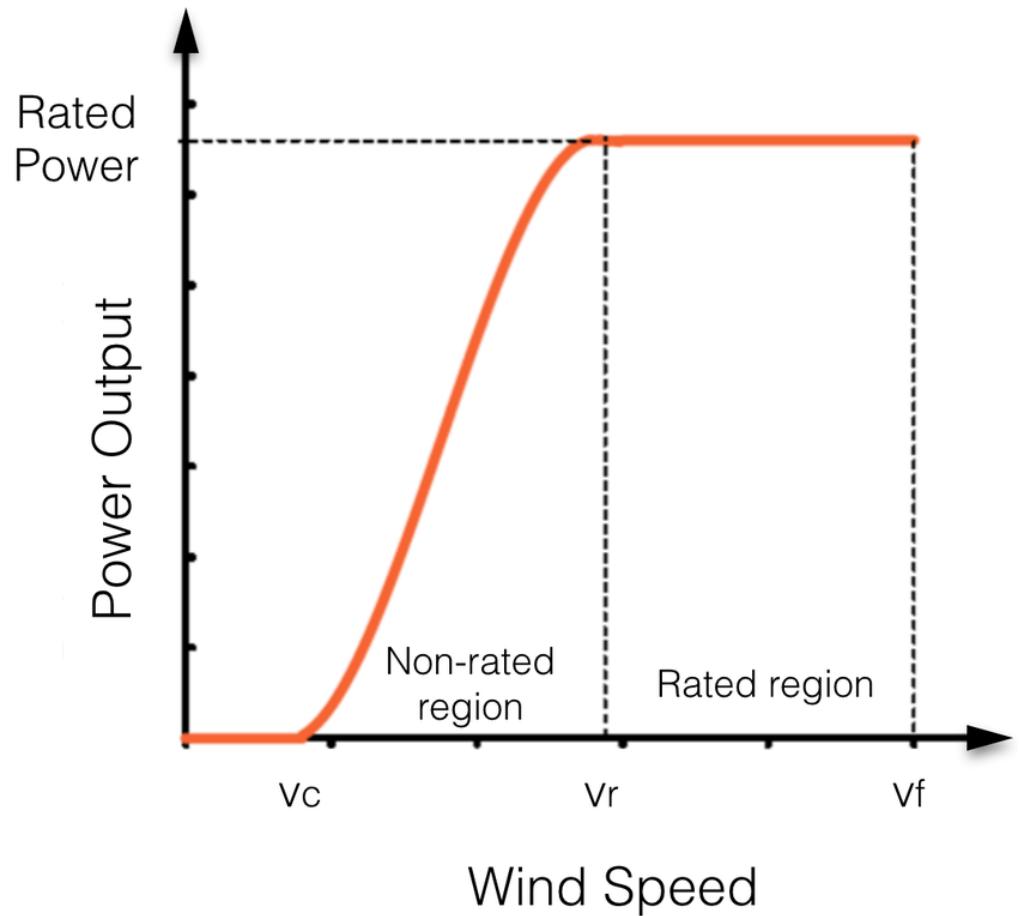
- The challenging point -  $C_p(\cdot)$  in the aerodynamics model is highly nonlinear and does not have exact form.



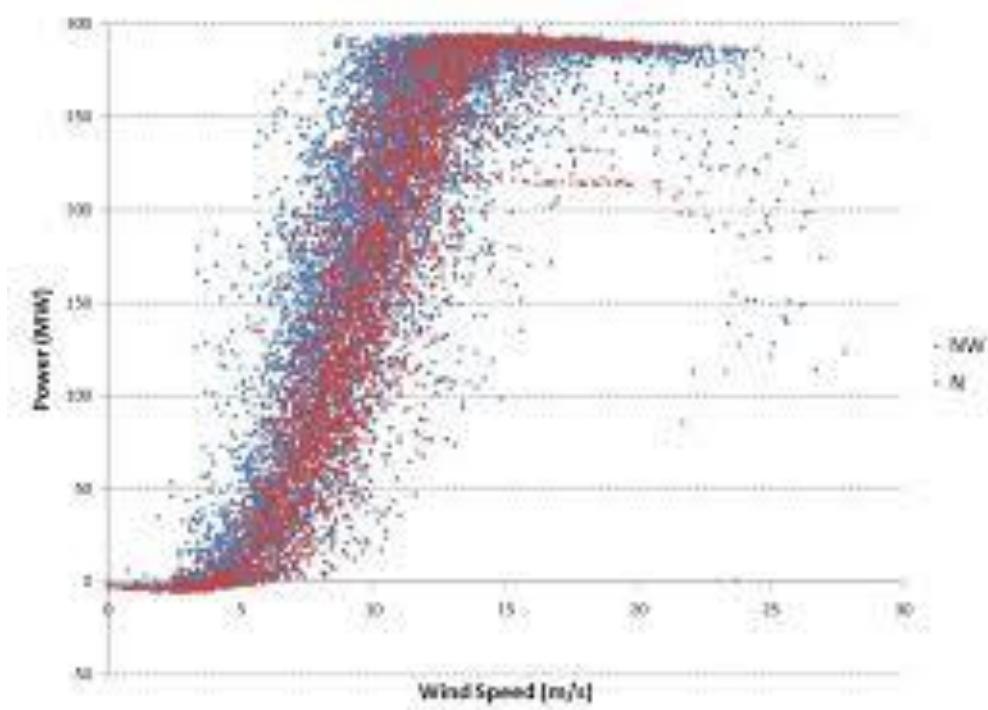
# Computational Fluid Dynamics Model

- $C_p(\cdot)$ , the power coefficient, needs to be estimated
- Estimation based on data
- Estimation based on control theory
- Estimation based on stochastic process

# Power Curve Model

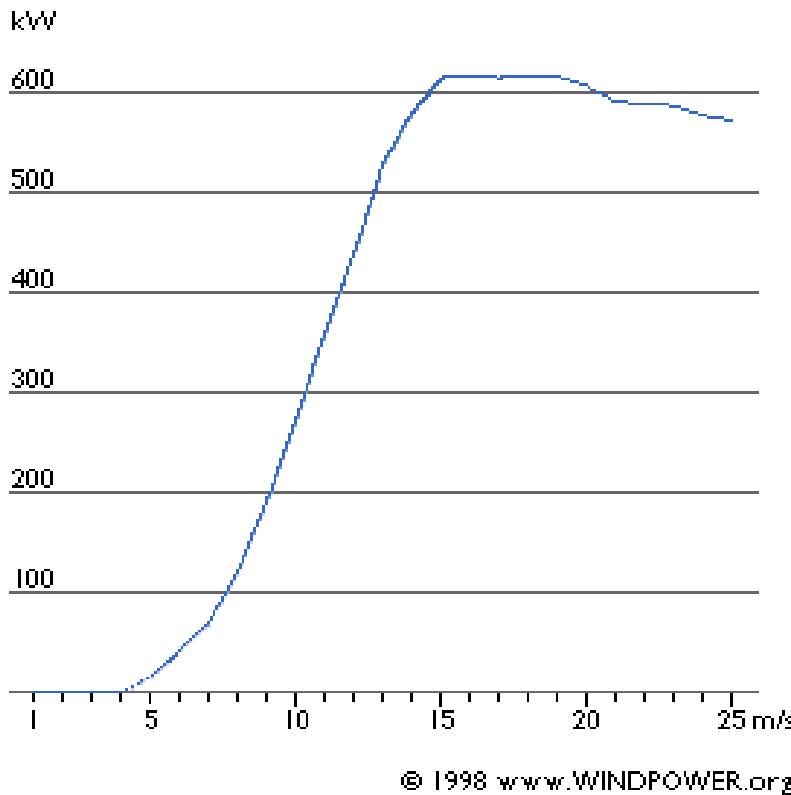


Ideal Power Curve Model



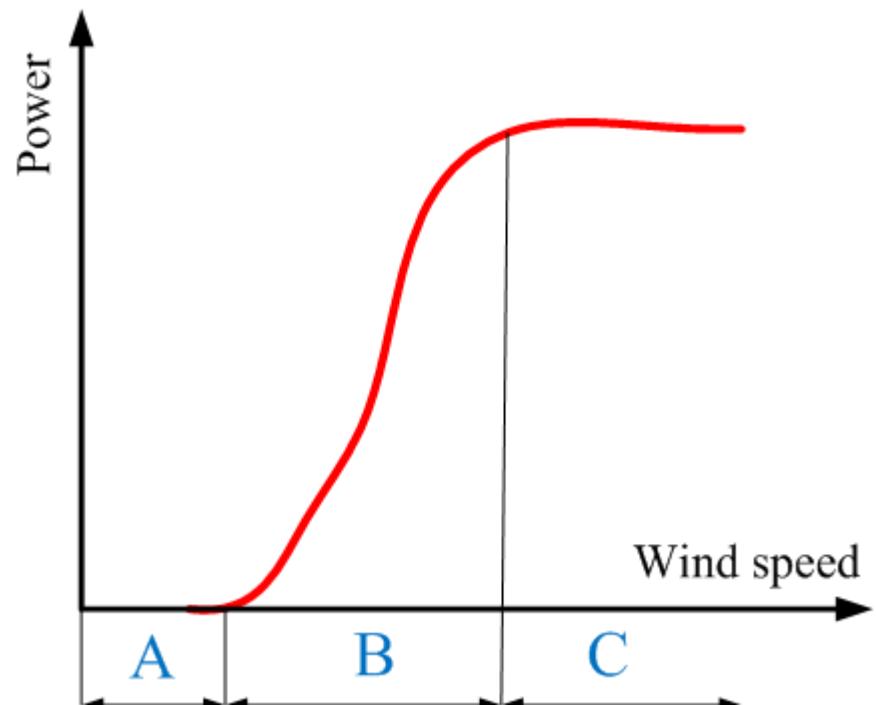
Real Power Curve Model

# The Power Curve of a Wind Turbine



- ✓ The power curve of a wind turbine plots large the electrical power output at different wind speeds
- ✓ The **cut-in wind speed**: Turbines are designed to start running at wind speeds, e.g., 3 to 5 m/s
- ✓ The **cut-out wind speed**: Turbines are programmed to stop at high wind speeds, e.g., above 25 m/s to avoid damaging the turbine

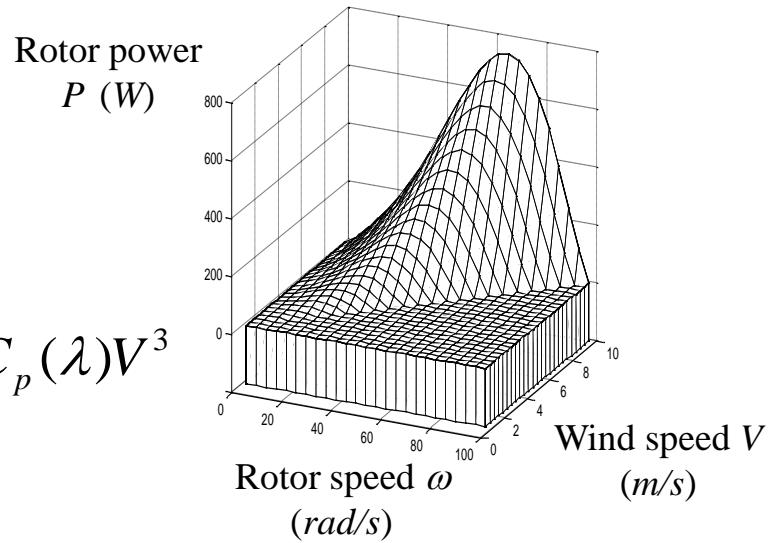
# Power Curve



$$P = \frac{1}{2} \rho A C_p(\lambda) V^3$$

$$\lambda = \frac{r \omega}{V}$$

- A: Insufficient power to overcome friction and initial torque
- B: Turbine operates to maximize efficiency
- C: Fixed (rated) power operation



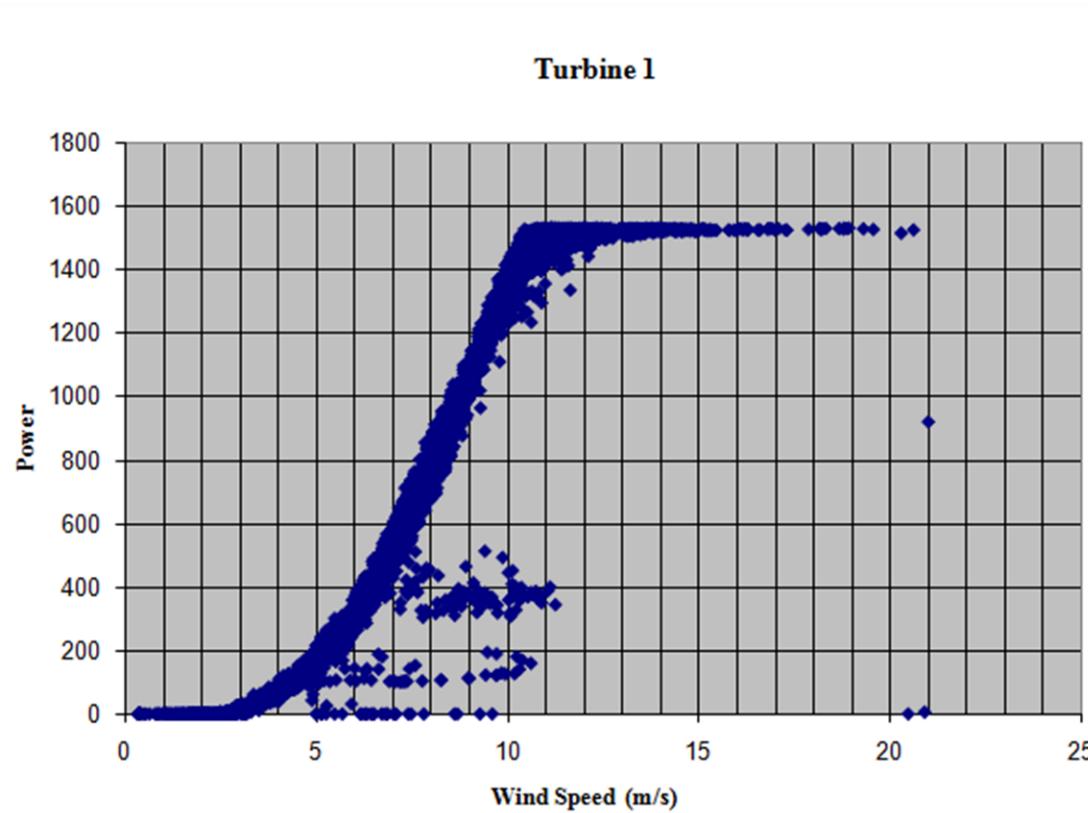
# Plotting Power Curves

- ✓ If the wind speed is not fluctuating too rapidly, then one may use the wind speed measurements from the anemometer and read the electrical power output from the wind turbine and plot the two values in the form of the power curve
- ✓ In practice the wind speed always fluctuates, one cannot measure exactly the column of wind passing and therefore one will see a swarm of points dispersed around
- ✓ Furthermore, the actual anemometer error can be 3% , thus leading to 9% (or even 10%) error of the certified power curves

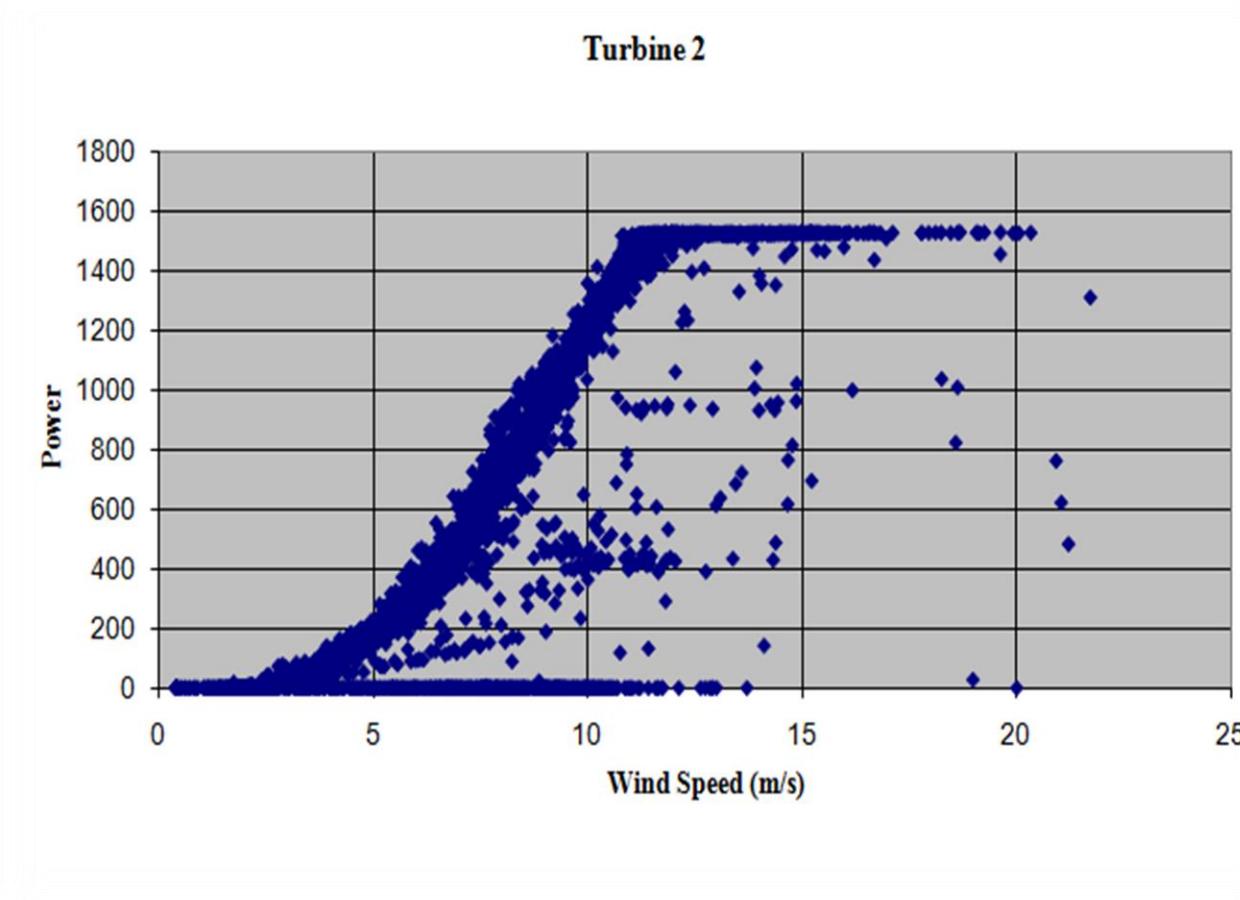
?

$$P = 0.5 \times \rho \times A \times v^3$$

# Actual Power Curve



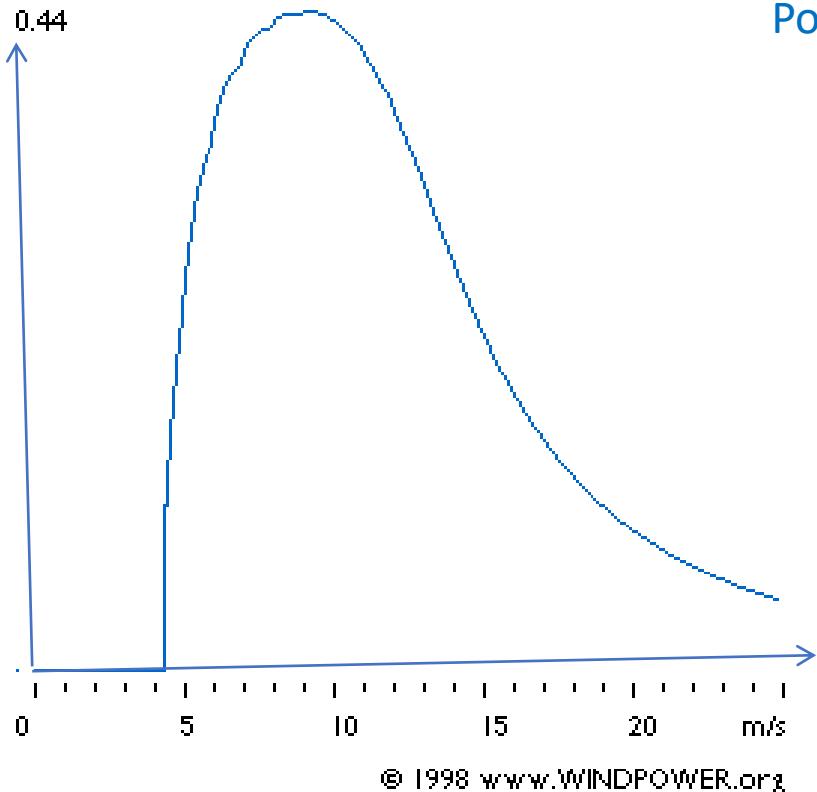
# Actual Power Curve



# Verifying Power Curves

- ✓ Power curves are constructed using measurements in areas with low turbulence intensity, and with the wind coming directly towards the front of the turbine
- ✓ Local turbulence and complex terrain (e.g., turbines placed on a rugged slope) may mean that wind gusts hit the rotor from varying directions
- ✓ It may therefore be difficult to reproduce the power curve exactly at any given location

# The Power Coefficient



Illustrative power efficiency curve

Power coefficient = Turbine efficiency

- ✓ The **power coefficient** indicates how **efficiently** a turbine converts the wind energy into electricity

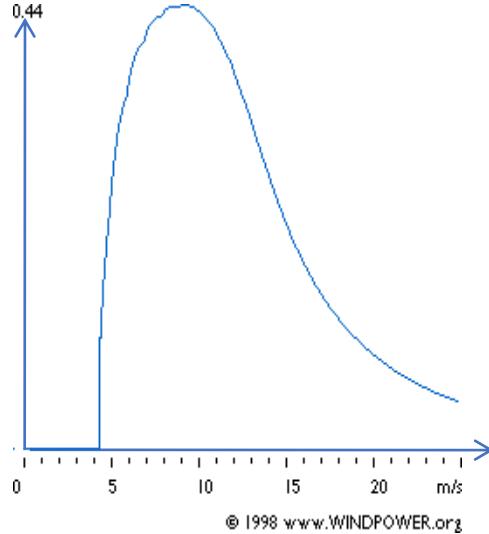
$$E = E_{rot} \times E_{ger} \times E_{gen} \times E_{p-conv}$$

- ✓ **Power coefficient =**  
$$\frac{\text{The electrical power output}}{\text{The wind energy input (From the power equation)}}$$

- ✓ The efficiency varies with the wind speed

$$P = 0.5 \times \rho \times A \times v^3$$

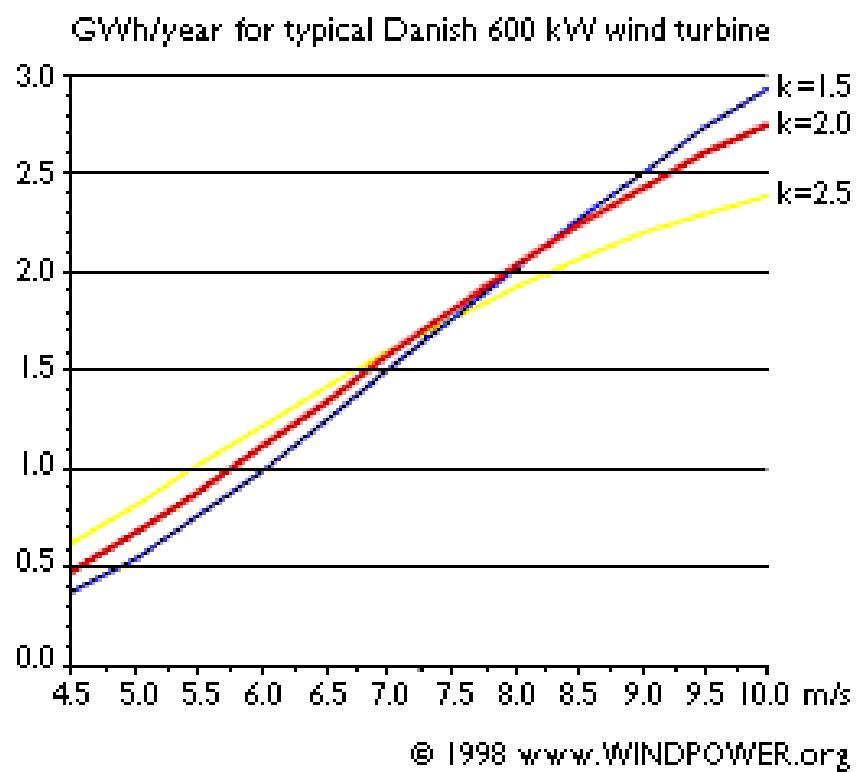
# The Power Coefficient



Power coefficient = Turbine efficiency

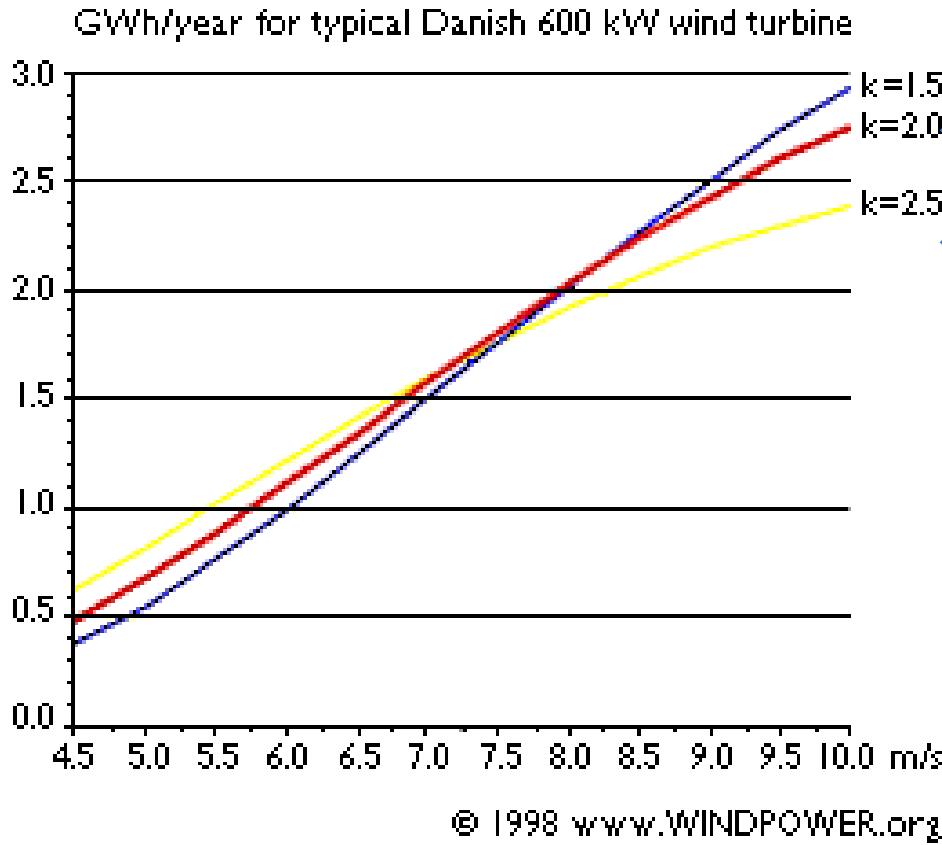
- ✓ Example: A turbine was designed for the max efficiency of 44% at a wind speed of about 9 m/s
- ✓ The efficiency is not as important at low wind speeds as there is not much energy to harvest
- ✓ At high wind speeds the turbine wastes the excess energy above the cut out speed
- ✓ **Efficiency therefore matters most** in the regions of wind speeds (i.e., high) where the most of energy is to be found

# Annual Energy Output from a Wind Turbine

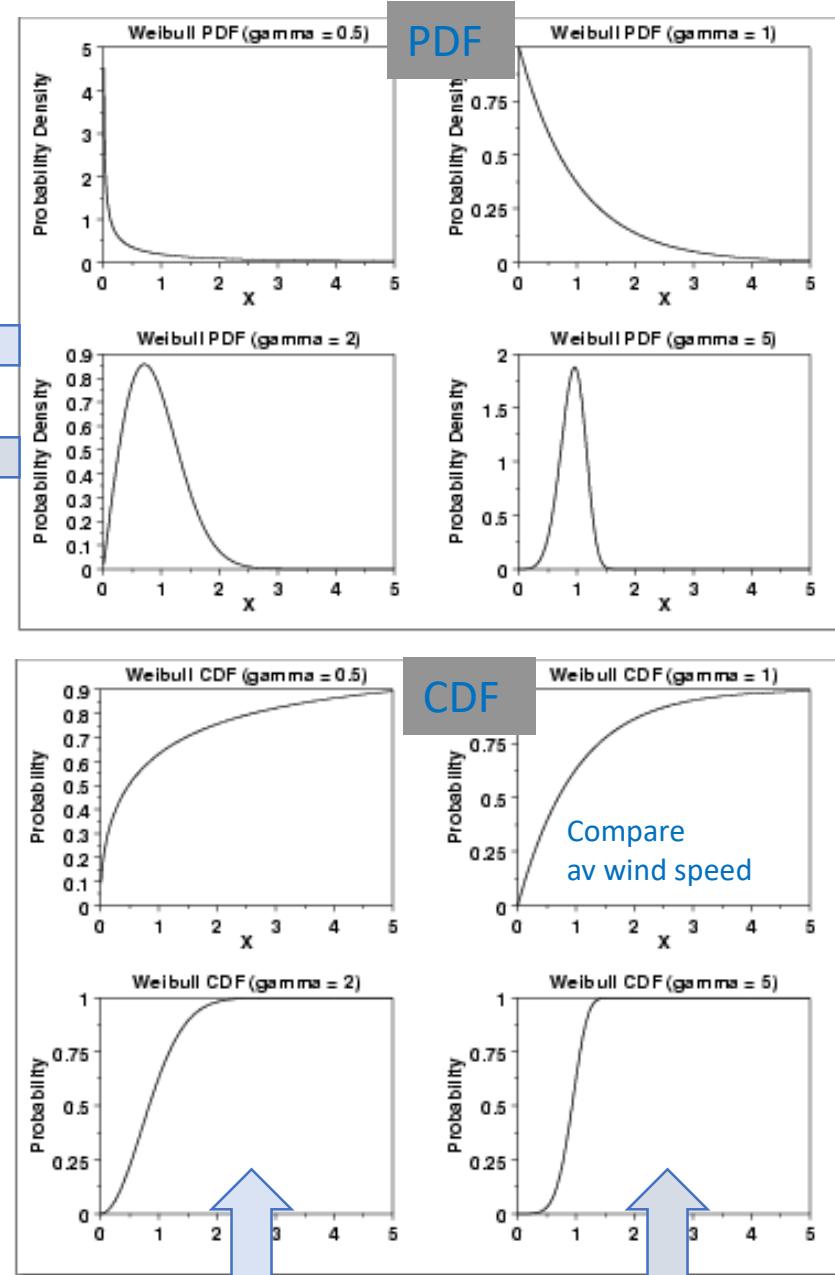


- ✓ The relationship between the average wind speed and the annual energy output from a wind turbine
- ✓ Standard atmosphere with air density of 1.225 kg/m<sup>3</sup>
- ✓ For each of the Weibull **shape parameters  $k = 1.5, 2.0$ , and  $2.5$** , the annual energy output is computed at different average wind speeds at the turbine hub height

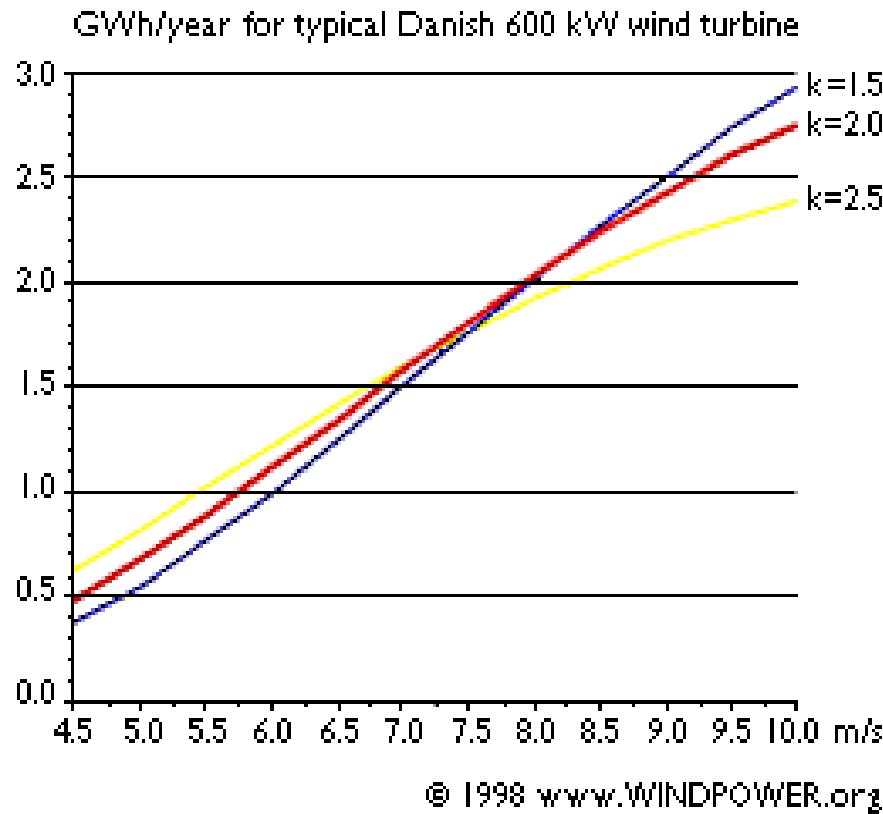
# The Impact of $k$



Shape parameter  $\gamma = k$   
Scale parameter  $\lambda = 1$   
(Location parameter = 0)

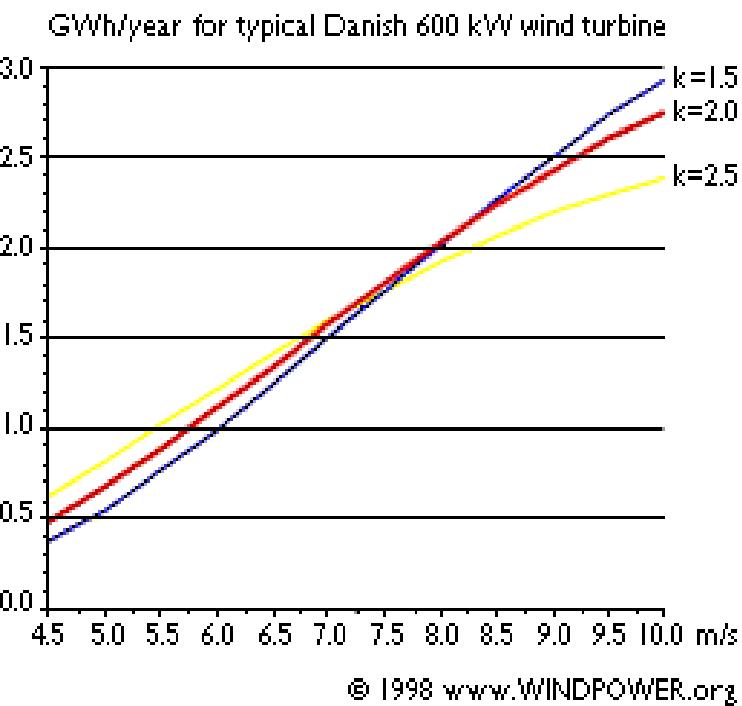


# Annual Energy Output from a Wind Turbine



- ✓ Depending on the value of shape parameter  $k$  the energy output may vary up to 50% at a low average wind speed of 4.5 m/s, and some 30% at a higher average wind speed of 10m/s

# Output Varies with the Average Wind Speed



- ✓ Consider the red curve with the shape parameter  $k = 2$ , normally shown by manufacturers
- ✓ For an average wind speed of 4.5 m/s the turbine generates about 0.5 GWh per year
- ✓ For an average wind speed to 9 m/s 2.4 GWh/year it generated
- ✓ Thus, doubling the average wind the energy output increased 4.8 times

# Output Varies with the Wind Speed

- ✓ For the average speeds **5 and 10 m/s** (the same speed ratio of **2**), energy output would differ by the factor of **4** (rather than **4.8**)
- ✓ The reason for the difference, is that the **efficiency of the wind turbine** varies with the wind speed (**the power curve**)
- ✓ Note, that the uncertainty that applies to the power curve also applies to the above result
- ✓ The calculations can be refined by considering that, e.g., in temperate climates the wind tends to be stronger in winter than in summer, and stronger during the daytime than at night

# The Capacity Factor

✓ Turbine capacity factor =

The actual annual energy output

—————  
The theoretical maximum output

Theoretical maximum output = if the turbine was running at its maximum rated power for 8766 hours of the year (=24h\*365.25days)

✓ Example: For a 600 kW turbine producing 1.5 million kWh per year, its capacity factor is

$$= 1,500,000 / (365.25 * 24 * 600) = 1,500,000 / 5,259,600$$

$$= 0.285 = 28.5\%$$

✓ The capacity factor may theoretically vary from 0 to 100%, but in practice it usually is 20% to 70%

# Turbine/Wind Plant Availability Factor

The time turbine/wind plant is available

✓ Availability factor =

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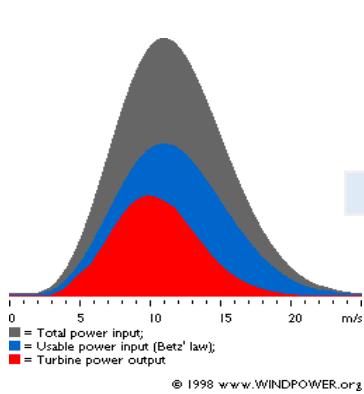
The total time (in a year)

- ✓ Different specific definitions of the availability factor
- ✓ Has improved in recent years
- ✓ Equipment reliability
- ✓ Warranty terms

# Comparison

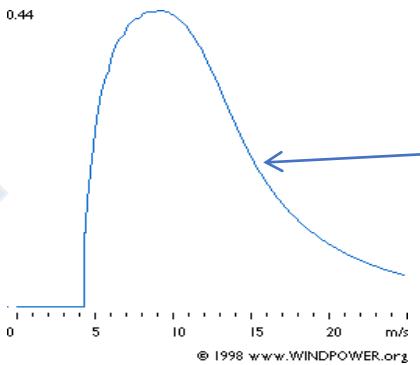
The electrical power output [KW]

✓ Turbine power coefficient =



The wind energy input [KW]

Aerodynamic  
break



The actual annual energy output [kWh]

✓ Turbine capacity factor =

The theoretical maximum output [kWh]

The time turbine/wind plant is available

✓ Availability factor =

The total time (in a year)

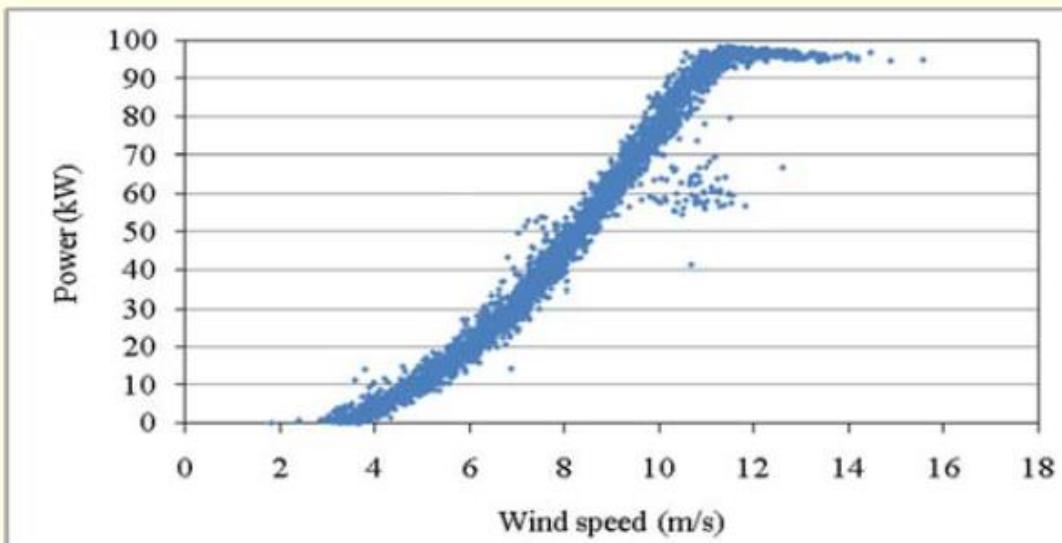
# Power Curve – 10-min Data

GE 1.5 MW wind turbine (10 minutes average)

Time Stamp	Wind speed	Electric Power
10:00 AM	7.08	352.18
10:10 AM	8.79	552.14
10:20 AM	9.36	784.91
10:30 AM	9.65	805.39
10:40 AM	9.86	940.64
10:50 AM	9.84	965.74
11:00 AM	11.03	1203.76
11:10 AM	10.28	1023.21
11:20 AM	9.96	974.13
11:30 AM	9.71	853.73
11:40 AM	10.84	1204.88

# Power Curve - Plotted

GE 1.5 MW wind turbine (10 minute average)



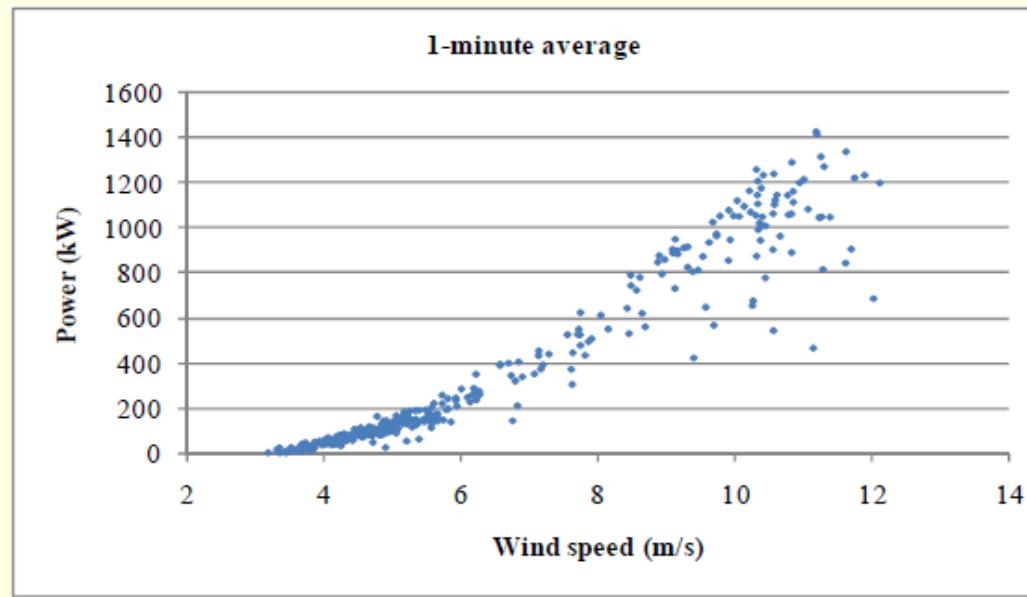
# Power Curve – 1-min Data

GE 1.5 MW wind turbine (1 minute average)

Time Stamp	Wind speed	Electric Power
1:00 PM	6.58	390.58
1:01 PM	6.23	351.57
1:02 PM	6.01	285.90
1:03 PM	6.20	288.90
1:04 PM	5.73	258.35
1:05 PM	5.74	220.68
1:06 PM	5.61	221.45
1:07 PM	5.27	187.55
1:08 PM	5.25	154.75
1:09 PM	5.48	154.25
1:10 PM	5.65	168.08
1:11 PM	5.65	174.10
1:12 PM	5.82	198.13

# Power Curve - Plotted

GE 1.5 MW wind turbine (1 minute average)



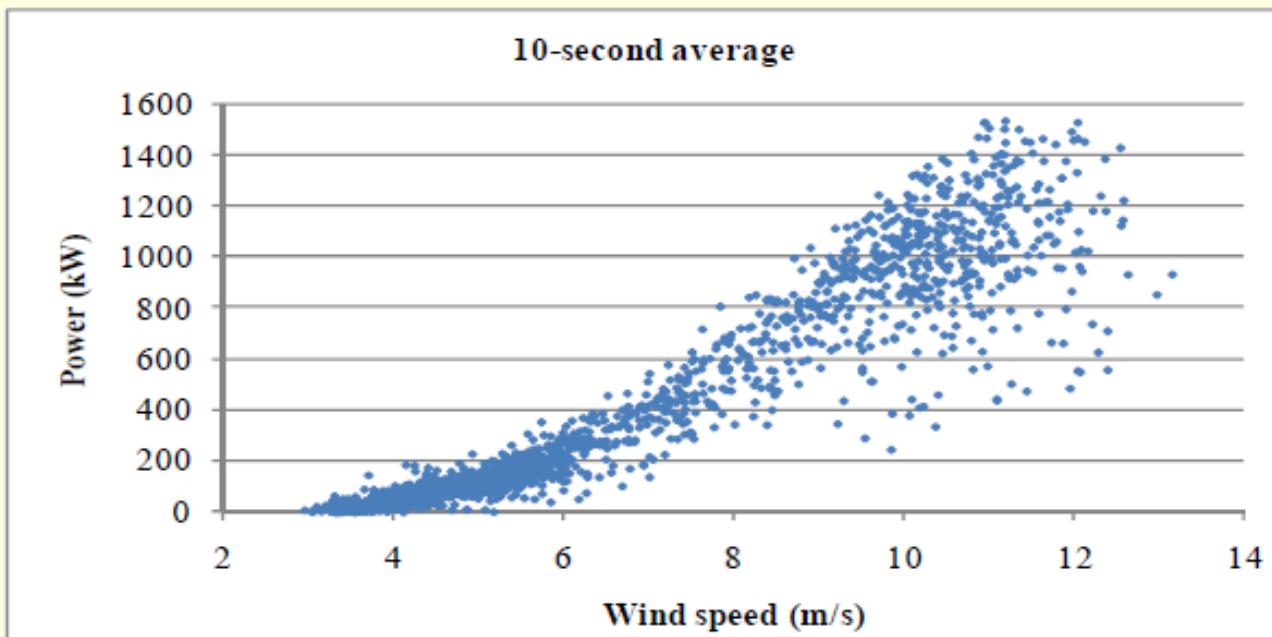
# Power Curve – 10-sec Data

GE 1.5 MW wind turbine (10 second average)

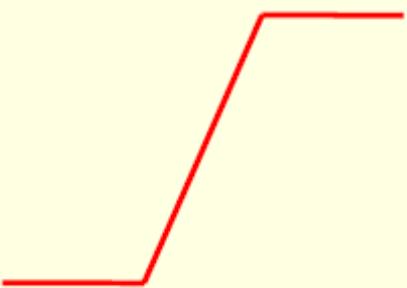
Time Stamp	Wind speed	Electric Power
4:35:20	6.74	371.60
4:35:30	6.77	417.90
4:35:40	6.47	389.40
4:35:50	6.32	369.60
4:36:00	6.24	372.60
4:36:10	6.93	422.40
4:36:20	6.70	403.30
4:36:30	6.38	381.80
4:36:40	6.11	361.20
4:36:50	6.04	339.20
4:37:00	6.00	313.00
4:37:10	6.13	310.89
4:37:20	5.86	300.20
4:37:30	5.65	286.80

# Power Curve - Plotted

GE 1.5 MW wind turbine (10 second average)



# Power Curve Model 1



$$y = f(v) = \begin{cases} 0, & v < v_{cut-in} \\ \lambda v + \eta, & v_{cut-in} \leq v \leq v_{rated} \\ P_{rated}, & v_{cut-out} > v > v_{rated} \end{cases}$$

Linear power  
curve function

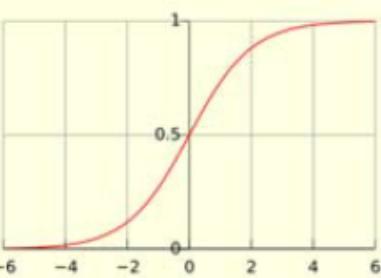
$y$  power output

$v$  wind speed

$\lambda$  slope,  $\eta$  intercept

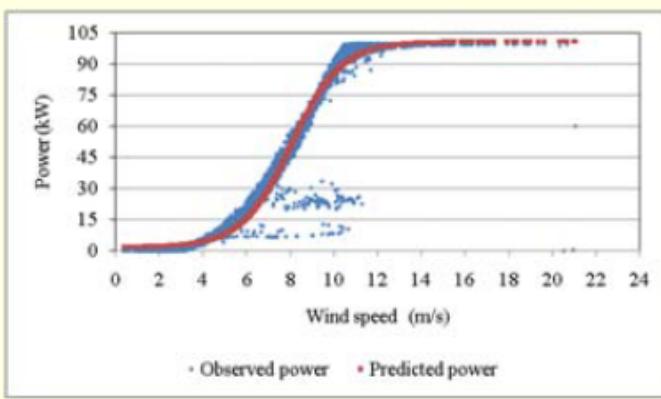
$P_{rated}$  rated power

# Power Curve Model 2

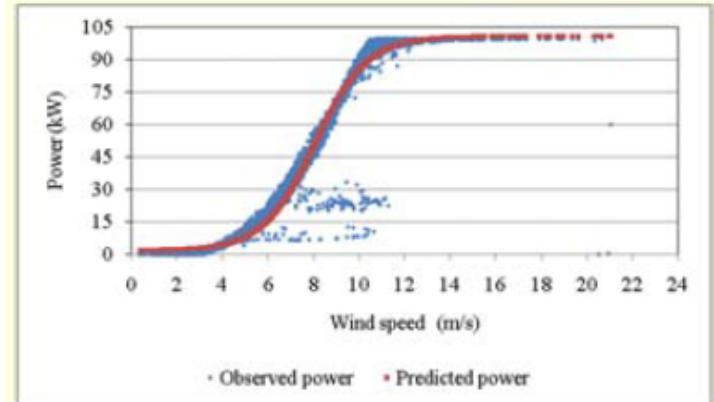


Logistic  
function  
power  
curve

$$y = f(v, \theta) = a \frac{1 + me^{-v/\tau}}{1 + ne^{-v/\tau}}$$
$$\theta = (a, m, n, \tau)$$



# Power Curve Model 2



Least square estimation of the power curve

$$\min_{\theta} \sum_{i=1}^N (f(v_i, \theta) - y_i)^2$$

Change Theta to minimize the squared error

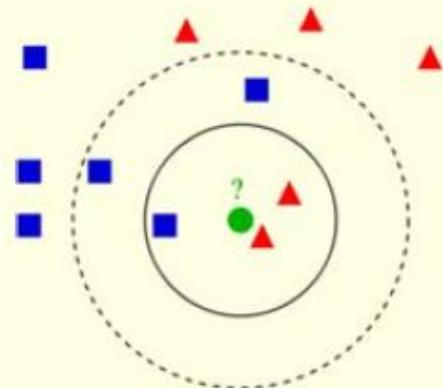
Number of field data points

Power curve function predicting power output

Actual measured power output

# Power Curve Model 3

k-NN (k nearest neighbors) algorithm



# Power Curve Model 3

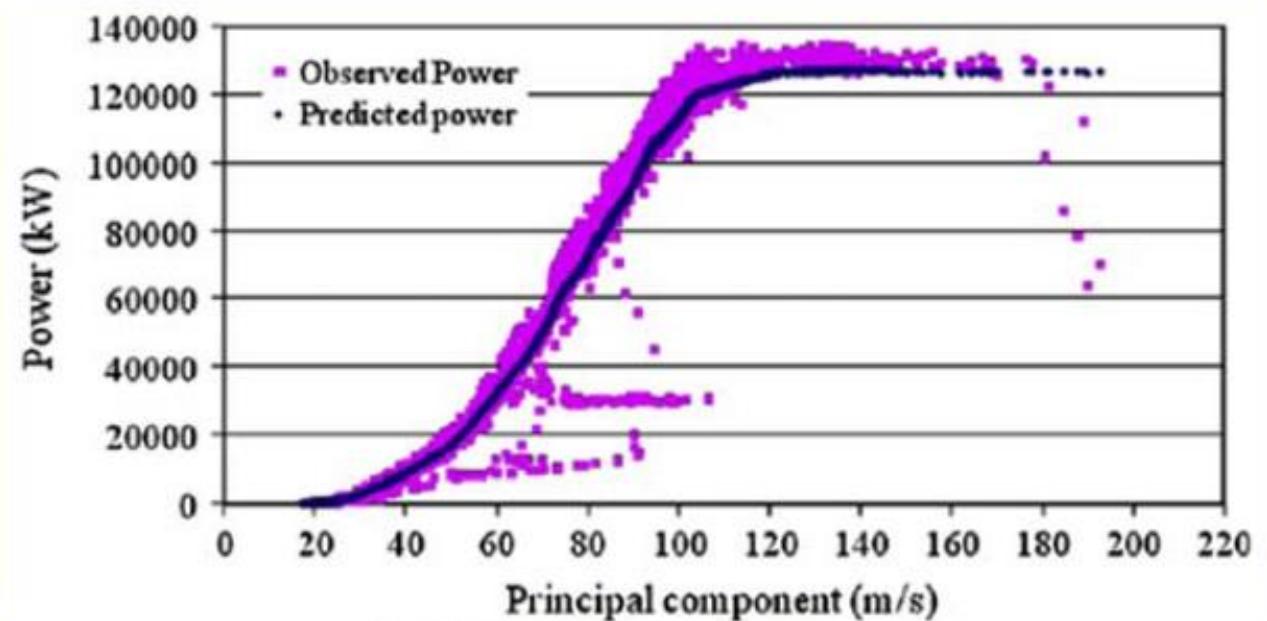
Remove bad data points

- Turbine down time
- Sensor errors

Principal component analysis

- Reduce dimensions
- Reduce noises in the data

$$PCA = \alpha_1 v_{turbine1} + \dots + \alpha_N v_{turbineN}$$



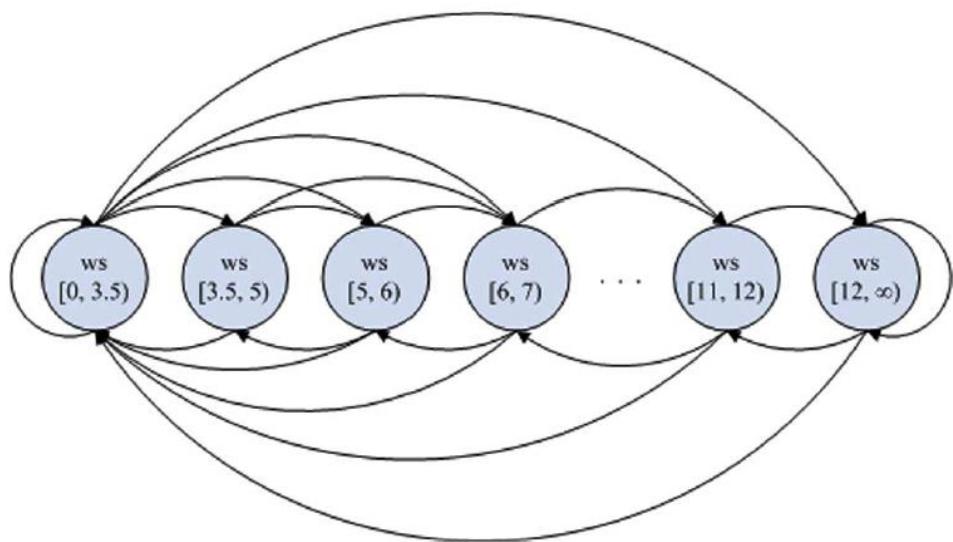
# Data-driven Model 1

- A Gray-box Model Extended From Aerodynamic Model

$$P_a = \frac{1}{2} \rho \pi R^2 C_p(\lambda, \beta) v^3 \quad \xrightarrow{\hspace{1cm}} \quad P_{a(t)} = \frac{1}{2} \rho \pi R^2 f_A \\ \times (\omega_{r(t)}, \omega_{r(t-T)}, v_t, v_{t-T}, \beta_t, \beta_{t-T}, C_{p(t-T)}) v_t^3$$


$$C_{p(t)} = f_A(\omega_{r(t)}, \omega_{r(t-T)}, v_t, v_{t-T}, \beta_t, \beta_{t-T}, C_{p(t-T)}).$$

# Data-driven Model 1



TRANSITION MATRIX OF WIND SPEED CHANGES IN 60 s

WS Interval	[0, 3.5)	[3.5, 5)	[5, 6)	[6, 7)	[7, 8)	[8, 9)	[9, 10)	[10, 11)	[11, 12)	[12, $\infty$ )
[0, 3.5)	0.8922	0.1015	0.0052	0.0007	0.0001	0.0001	0.0001	0.0000	0.0000	0.0000
[3.5, 5)	0.1618	0.6397	0.1550	0.0345	0.0075	0.0014	0.0001	0.0000	0.0000	0.0000
[5, 6)	0.0049	0.1213	0.6718	0.1574	0.0343	0.0084	0.0013	0.0005	0.0000	0.0000
[6, 7)	0.0002	0.0147	0.1058	0.7075	0.1294	0.0327	0.0071	0.0021	0.0003	0.0002
[7, 8)	0.0000	0.0026	0.0313	0.1949	0.4660	0.2276	0.0581	0.0146	0.0037	0.0013
[8, 9)	0.0000	0.0001	0.0047	0.0446	0.2288	0.4392	0.2027	0.0568	0.0176	0.0053
[9, 10)	0.0001	0.0000	0.0007	0.0101	0.0822	0.2766	0.3581	0.1775	0.0709	0.0238
[10, 11)	0.0001	0.0000	0.0000	0.0027	0.0214	0.1066	0.2606	0.3227	0.1986	0.0874
[11, 12)	0.0000	0.0000	0.0001	0.0005	0.0038	0.0347	0.1239	0.2637	0.3217	0.2516
[12, $\infty$ )	0.0000	0.0000	0.0000	0.0000	0.0007	0.0040	0.0201	0.0622	0.1448	0.7682

# Data-driven Model 2

- A direct data-driven model with process engineering

$$P_{a(t)} = f_A(\tau_t, v_t, v_{t-T}, \beta_t)$$

# Data-driven Model 3

- A data-driven considering system dynamics

$$P_a(t) = f(P_a(t-T), v_t, \omega_{r(t)}, \beta_t)$$

# Data-driven Modeling Process

- Feature selection
- Modeling method selection

PERFORMANCE OF FIVE ALGORITHMS FOR MODEL TWO

Algorithm	MAE	SD of MAE	MAPE	SD of MAPE
Neural network	7.3416	5.8452	0.0260	0.3762
Boosting tree	48.0019	58.3010	0.1277	3.3080
Random forest	96.1827	106.6014	0.1834	2.3494
Support vector machine	27.5409	14.5258	0.1440	5.6230
$k$ -nearest neighbor	9.9953	8.8141	0.0342	0.6884

PERFORMANCE OF FIVE ALGORITHMS FOR MODEL ONE

Algorithm	MAE	SD of MAE	MAPE	SD of MAPE
Neural network	1.2877	1.6810	0.0344	0.2230
Boosting tree	5.6543	5.6819	0.1298	0.2920
Random forest	6.9763	6.9643	0.1569	0.3536
Support vector machine	5.8793	3.6885	0.1454	0.2202
$k$ -nearest neighbor	2.9935	3.4315	0.0723	0.2763

PERFORMANCE OF FIVE ALGORITHMS FOR MODEL THREE

Algorithm	MAE	SD of MAE	MAPE	SD of MAPE
Neural network	20.5270	29.8117	0.0442	0.3440
Boosting tree	59.8376	60.5458	0.1507	3.6392
Random forest	94.4690	103.2844	0.1851	3.0446
Support vector machine	45.2412	46.8501	0.1920	5.5457
$k$ -nearest neighbor	28.1062	43.5211	0.0610	0.9422

# Data-driven Modeling Process

SUMMARY OF PREDICTION ACCURACY OF THREE MODELS

Model	MAE	SD of MAE	MAPE	SD of MAPE
Model-One	18.3454	28.9566	0.0344	0.2230
Model-Two	7.3416	5.8452	0.0260	0.3762
Model-Three	20.5270	29.8117	0.0442	0.3440

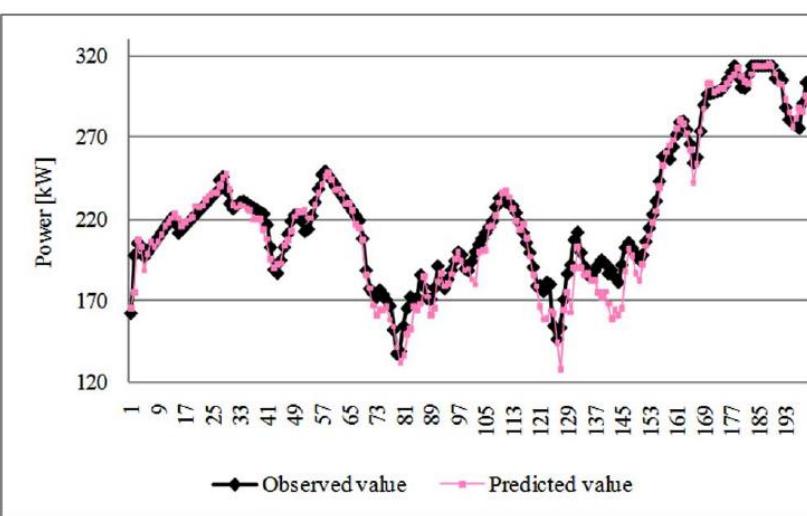


Fig. 10. First 200 test points in predicting power by model one.

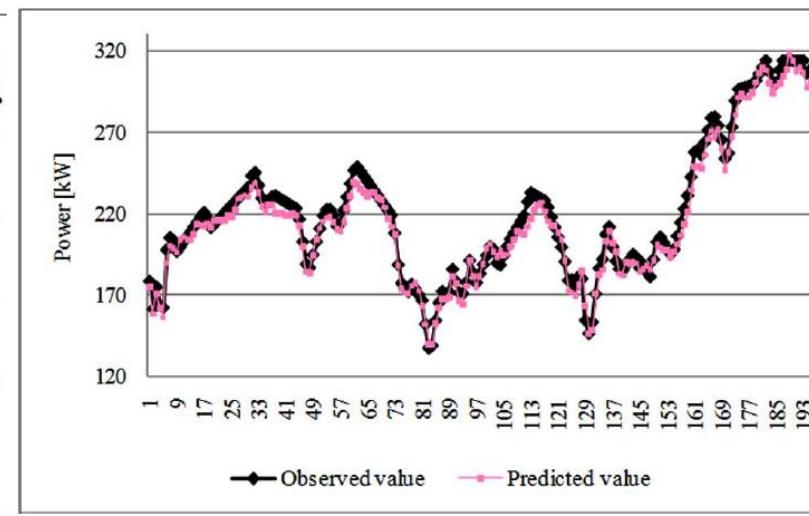


Fig. 11. First 200 test points in predicting power by model two.

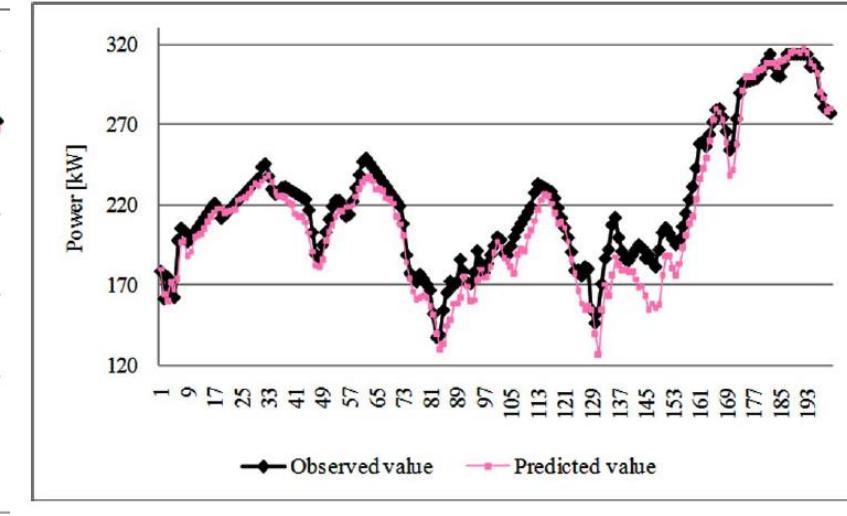


Fig. 12. First 200 test points in predicting power by model three.

# Multi-period Prediction

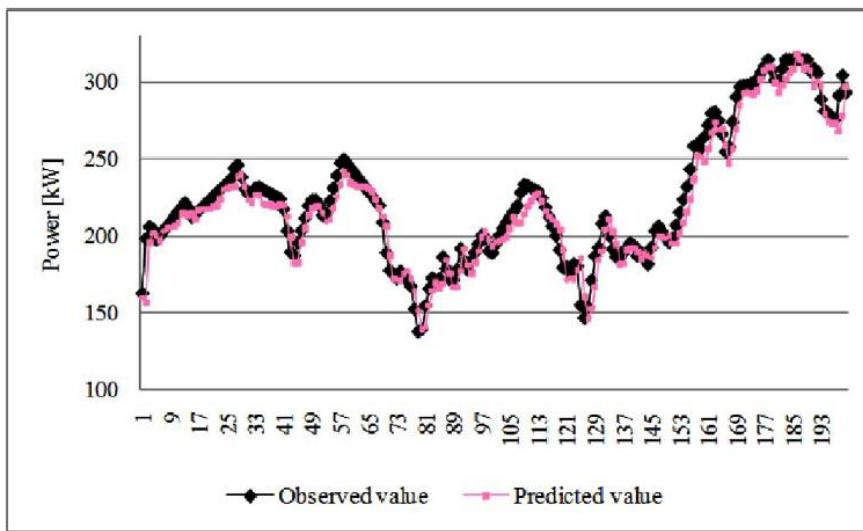


Fig. 13. First 200 points of  $t + 10$  s predictions by model two based on dataset 1.

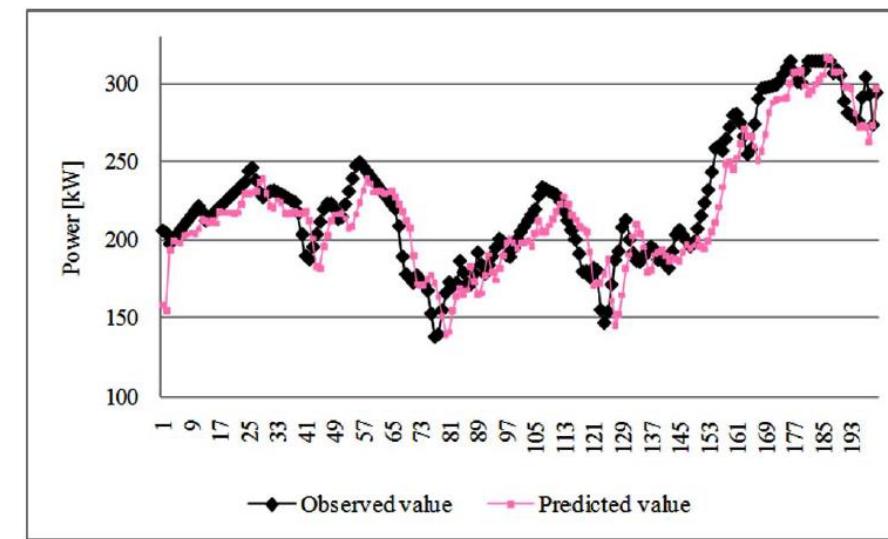


Fig. 15. First 200 points of  $t + 30$  s prediction by model two based on dataset 1.

# In-Class Practice

- Use weka to conduct the wind speed prediction
- Datasets have been available in Canvas
- Let us do it together...